

- Using Figure 2.2 as a model? illustrate the operation of Insertion-Sort on the array A = (31,41,59,26,41,58).



- Rewrite the Insertion-Sort procedure to sort into nonincreasing instead of non-decreasing order.

```
def sort(array):
    for i in range(1, len(array), 1):
```

```

tempValue = array[i];
j = i-1;
while j >= 0 and array[j] < tempValue:
    array[j+1] = array[j];
    j = j - 1;
array[j+1] = tempValue;

array = [1,2,3,4,5,6];
sort(array)
print(array);

```

```

array = [6,5,4,3,2,1];
sort(array)
print(array);

```

```

array = [1];
sort(array)
print(array);

```

### 3 Consider the searching problem

Input: A sequence of  $n$  numbers =  $A = (a_1, a_2, \dots, a_n)$  and a value  $v$ .

Output: An index  $i$  such that  $v = A[i]$  or the special value NIL if  $v$  does not appear in  $A$ .

Write pseudocode for linear search? which scans through the sequence? looking for  $v$ / Using a loop invariant, prove that your algorithm is correct. Make sure that your loop invariant fulfills the three necessary properties.

```

def search(array, v):
    for i in range(0, len(array), 1):
        if array[i] == v:
            return i;
    return None;

print(search([1,2,3,4,5,6], 6));
print(search([1,2,3,4,5,6], 1));
print(search([1,2,3,4,5,6], 7));

```

Loop Invariant:

For an array length of  $n$ , if value  $v$  exists in array it located at  $A[i..n-1]$ .

Initialization: for  $i = 0$ , value  $v$  can be located in whole array  $A[0..n-1]$

Maintenance: for  $i = k$ , value  $v$  can be located at the part of array  $A[k..n-1]$ , so if value  $v$  exists at  $A[k]$  we find it, if not, at the next iteration  $i = k+1$ , value  $v$  can be located at the part of array  $A[k+1..n-1]$ . Invariant holds.

Termination: If loop terminates at  $i=n-1$ , we find the value at  $A[i,n-1]$ . If loop terminates at  $i = n$ , we didn't find value, return none.

**4 Consider the problem of adding two n-bit binary integers? stored in two n-element arrays A and B. The sum of the two integers should be stored in binary form in an (n+1)-element array C. State the problem formally and write pseudocode for adding the two integers.**

Input: 2 arrays A and B of length n. Each element of array contains only numbers 0 or 1. Output: array C of length n+1, calculated as  $C[i+1]=A[i]+B[i]$ . If  $C[i+1] \geq 2$  then  $C[i] = A[i-1]+B[i-1] + 1$  and  $C[i+1]=C[i+1] \bmod 2$ .

```
def add(array1 , array2 , length):
    resultArray = [0] * (length + 1);
    for i in range(length-1, -1, -1):
        resultArray[i+1] = resultArray[i+1] + array1[i] + array2[i];
        if resultArray[i+1] > 1:
            resultArray[i] = 1;
            resultArray[i + 1] = resultArray[i+1] % 2;
    return resultArray;

print(add([1],[1], 1)); #10
print(add([1,0,1,0],[0,1,0,1], 4)); #01111
print(add([1,1,1,1],[1,1,1,1], 4)); #11110
```