

## Bubble Sort Performance Analysis

In this project, I tested four versions of the bubble sort algorithm to see how fast they can sort arrays of different sizes and types. I worked with three kinds of arrays:

- **Random elements:** Numbers in no particular order.
- **Already sorted elements:** Numbers already arranged in ascending order.
- **Reverse-sorted elements:** Numbers arranged in descending order.

I tested the algorithms with arrays ranging from 5,000 to 60,000 elements and measured how long it took to sort them. I recorded my outputs and filled in the tables below.

### Classic Bubble Sort

| Number of Elements | Random Elements | Already Sorted | Reverse Sorted |
|--------------------|-----------------|----------------|----------------|
| 5000               | 0.226486        | 0.123599       | 0.255183       |
| 10000              | 0.905823        | 0.512495       | 1.024800       |
| 20000              | 3.598270        | 2.008290       | 4.142300       |
| 30000              | 8.223190        | 4.576100       | 9.441760       |
| 40000              | 14.890800       | 8.402280       | 18.086800      |
| 50000              | 29.065700       | 13.485200      | 26.792300      |
| 60000              | 34.200600       | 19.134600      | 39.491300      |

### Reduced Bubble Sort

| Number of Elements | Random Elements | Already Sorted | Reverse Sorted |
|--------------------|-----------------|----------------|----------------|
| 5000               | 0.098231        | 0.099605       | 0.100824       |
| 10000              | 0.396547        | 0.397634       | 0.392999       |
| 20000              | 1.611050        | 1.586400       | 1.588650       |
| 30000              | 3.710500        | 3.904310       | 3.703710       |
| 40000              | 6.797520        | 7.255650       | 6.619870       |
| 50000              | 10.318500       | 10.484600      | 10.791900      |

|       |           |           |           |
|-------|-----------|-----------|-----------|
| 60000 | 15.193500 | 15.276800 | 14.998700 |
|-------|-----------|-----------|-----------|

### Bubble Sort With Flag

| Number of Elements | Random Elements | Already Sorted | Reverse Sorted |
|--------------------|-----------------|----------------|----------------|
| 5000               | 0.000048        | 0.000050       | 0.000051       |
| 10000              | 0.000111        | 0.000190       | 0.000186       |
| 20000              | 0.000222        | 0.000243       | 0.000246       |
| 30000              | 0.000317        | 0.000333       | 0.000654       |
| 40000              | 0.000461        | 0.000442       | 0.000429       |
| 50000              | 0.000539        | 0.000558       | 0.000543       |
| 60000              | 0.000686        | 0.000710       | 0.000716       |

### Two-Way Bubble Sort

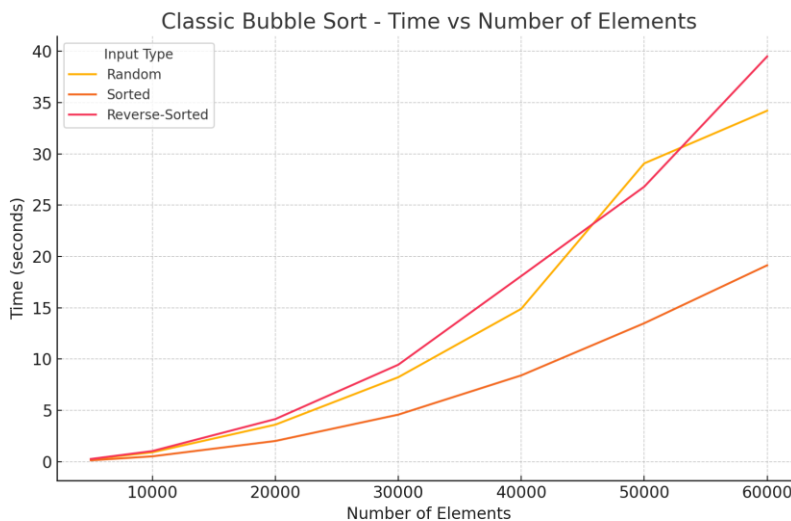
| Number of Elements | Random Elements | Already Sorted | Reverse Sorted |
|--------------------|-----------------|----------------|----------------|
| 5000               | 0.000037        | 0.000035       | 0.000037       |
| 10000              | 0.000082        | 0.000082       | 0.000077       |
| 20000              | 0.000181        | 0.000248       | 0.000179       |
| 30000              | 0.000233        | 0.000231       | 0.000245       |
| 40000              | 0.000340        | 0.000342       | 0.000376       |
| 50000              | 0.000414        | 0.000385       | 0.000388       |
| 60000              | 0.000491        | 0.001052       | 0.000462       |

### My Observations

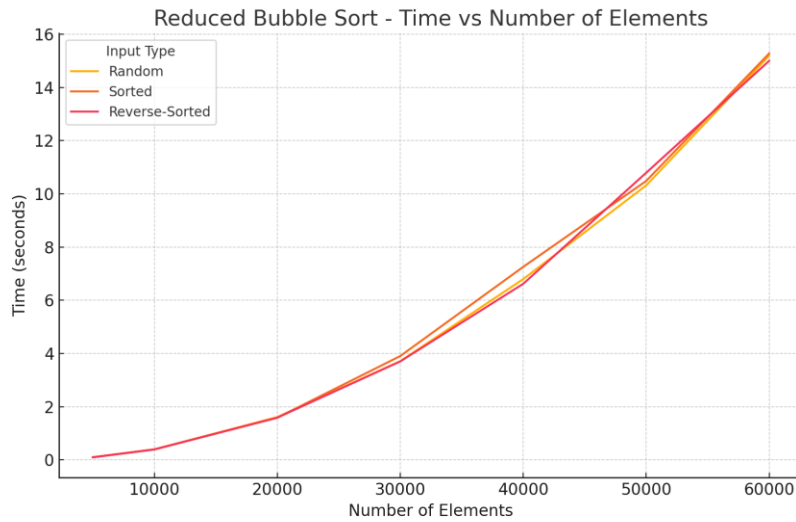
1. Classic Bubble Sort:

- This version is the slowest because it always compares and swaps elements, even when the array is already sorted.
  - Sorting time increases significantly as the number of elements grows. It's very slow for large arrays.
2. **Reduced Bubble Sort:**
- This version is slightly faster than the classic one because it stops checking the already sorted portion of the array.
  - The performance improved for all input types, but it's still not fast enough for large datasets.
3. **Bubble Sort with Flag:**
- This version is much faster when the array is already sorted or becomes sorted early in the process. It stops immediately if no swaps are needed.
  - It performs the best with sorted arrays and is quick even for reverse-sorted ones.
4. **Two-Way Bubble Sort (Cocktail Sort):**
- This version checks the array in both directions (left to right and right to left), which helps balance the workload.
  - It performs well for all input types and is more efficient than the classic and reduced versions.

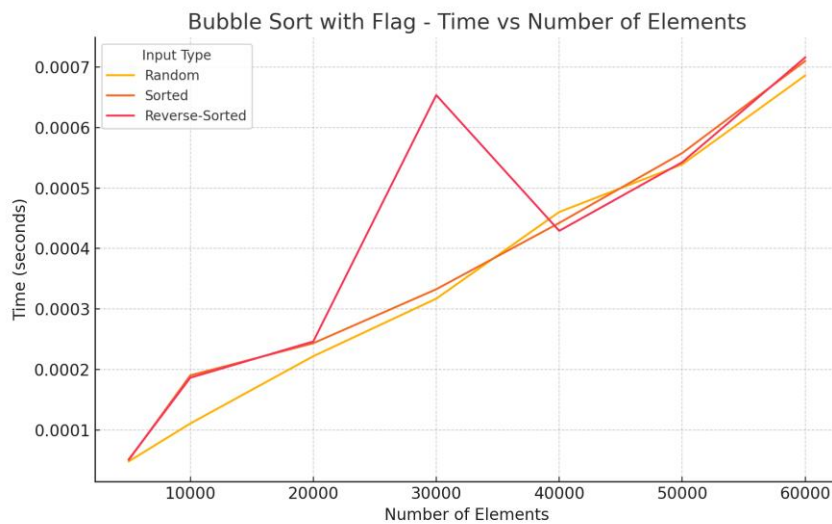
### Classic Bubble Sort - Time vs Number of Elements



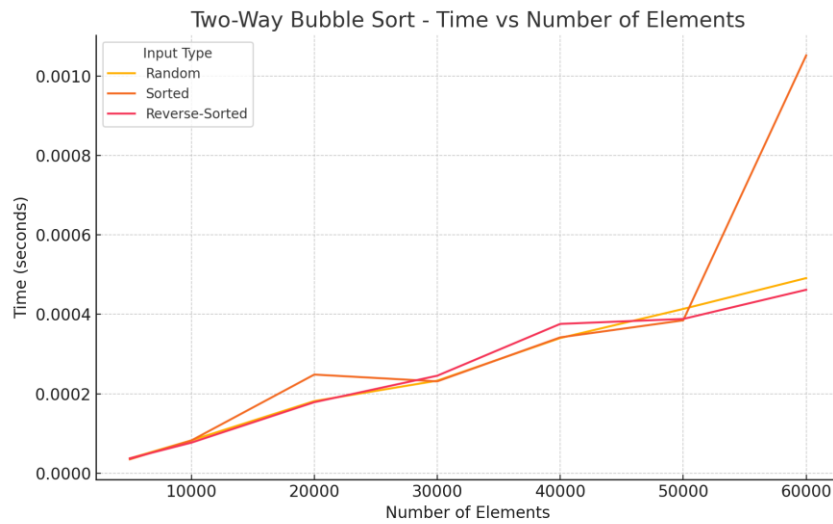
## Reduced Bubble Sort - Time vs Number of Elements



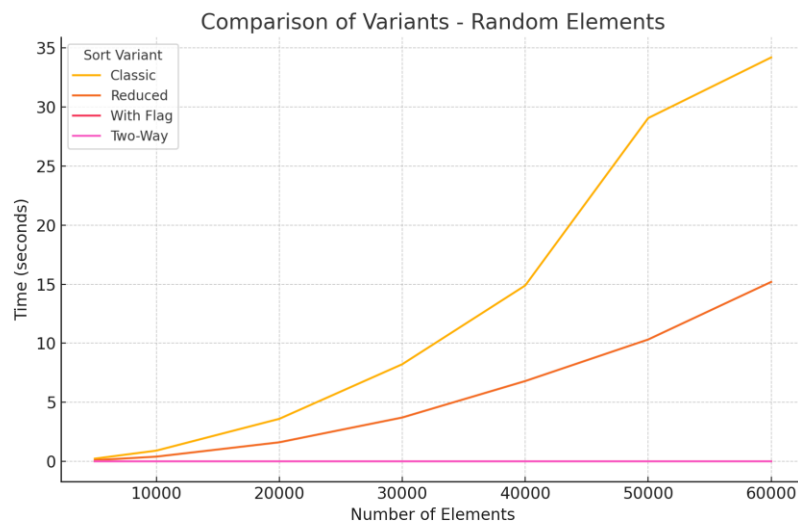
## Bubble Sort with Flag - Time vs Number of Elements



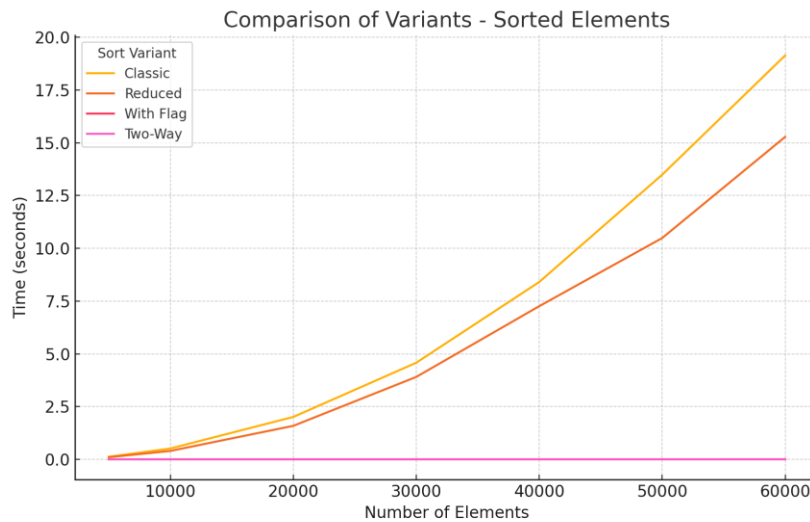
## Two-Way Bubble Sort - Time vs Number of Elements



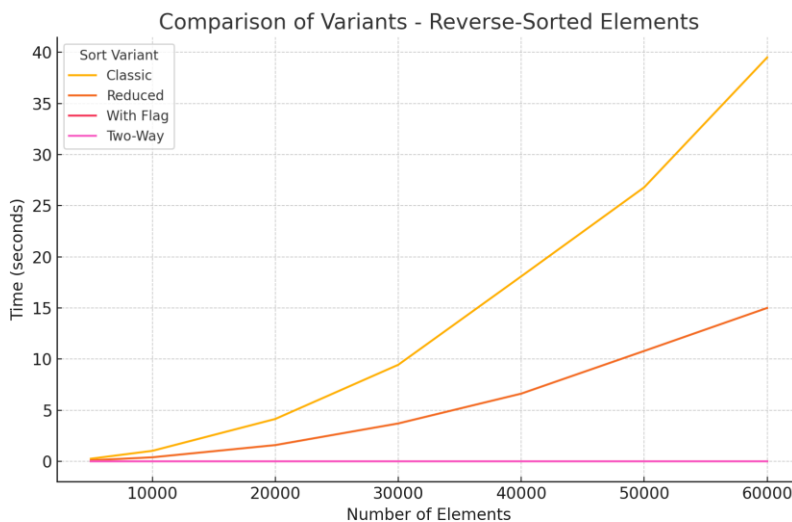
## Comparison of Variants - Random Elements



## Comparison of Variants - Sorted Elements



## Comparison of Variants - Reverse-Sorted Elements



## General Findings

- **Sorted arrays:** The "With Flag" version is the fastest because it can quickly determine that no swaps are needed.
- **Random and reverse-sorted arrays:** The two-way version performs consistently better than others because it processes the array in both directions.
- **Growth in sorting time:** Sorting time increases significantly with the number of elements, especially for the classic and reduced versions. The algorithms still

follow a quadratic time complexity, meaning their time grows very fast as the number of elements increases.

## **Conclusion**

The "Bubble Sort with Flag" is the best option for small or already sorted datasets because of its ability to exit early. The "Two-Way Bubble Sort" is more balanced and works better for random or reverse-sorted data. However, all these algorithms are inefficient for large datasets, and better sorting algorithms like quicksort or mergesort should be used instead.

My output (just the first part)

```
Testing for array size: 5000
Bubble Sort Times:
    Random Elements : 0.226486 seconds
    Already Sorted : 0.123599 seconds
    Reverse Sorted : 0.255183 seconds

Bubble Sort Reduced Times:
    Random Elements : 0.0982306 seconds
    Already Sorted : 0.0996048 seconds
    Reverse Sorted : 0.100824 seconds

Bubble Sort With Flag Times:
    Random Elements : 4.8e-05 seconds
    Already Sorted : 5.03e-05 seconds
    Reverse Sorted : 5.13e-05 seconds

Bubble Sort Two Way Times:
    Random Elements : 3.71e-05 seconds
    Already Sorted : 3.47e-05 seconds
    Reverse Sorted : 3.71e-05 seconds

Testing for array size: 10000
Bubble Sort Times:
    Random Elements : 0.905823 seconds
    Already Sorted : 0.512495 seconds
    Reverse Sorted : 1.0248 seconds

Bubble Sort Reduced Times:
    Random Elements : 0.396547 seconds
    Already Sorted : 0.397634 seconds
    Reverse Sorted : 0.392999 seconds

Bubble Sort With Flag Times:
    Random Elements : 0.0001106 seconds
    Already Sorted : 0.0001902 seconds
    Reverse Sorted : 0.0001863 seconds

Bubble Sort Two Way Times:
    Random Elements : 8.24e-05 seconds
    Already Sorted : 8.21e-05 seconds
    Reverse Sorted : 7.67e-05 seconds

Testing for array size: 20000
Bubble Sort Times:
    Random Elements : 3.59827 seconds
    Already Sorted : 2.00829 seconds
    Reverse Sorted : 4.1423 seconds
```