

```

# Load the necessary library
library(here)

## here() starts at C:/Users/mutse/OneDrive/Desktop/UCT/Courses/Multivariate/Multivariate-Analysis

library(dplyr)

##
## Attaching package: 'dplyr'

## The following objects are masked from 'package:stats':
##
##   filter, lag

## The following objects are masked from 'package:base':
##
##   intersect, setdiff, setequal, union

library(reshape2)
library(ggplot2)
library(patchwork)
library(tidyr)

##
## Attaching package: 'tidyr'

## The following object is masked from 'package:reshape2':
##
##   smiths

# Read the dataset
data <- read.csv(here("CA\\CA1\\CA1.csv"))
str(data)

## 'data.frame':   150 obs. of  5 variables:
##  $ MaxBreadth: int   131 125 131 119 136 138 139 125 131 134 ...
##  $ BasHeight  : int   138 131 132 132 143 137 130 136 134 134 ...
##  $ BasLength  : int    89 92 99 96 100 89 108 93 102 99 ...
##  $ NasHeight  : int    49 48 50 44 54 56 48 48 51 51 ...
##  $ TimePeriod: int     1 1 1 1 1 1 1 1 1 1 ...

#Qtn 1
# Compute the sample mean vectors for each time period
mean_vectors <- data %>%
  group_by(TimePeriod) %>%
  summarise(
    MaxBreadth = mean(MaxBreadth, na.rm = TRUE),
    BasHeight = mean(BasHeight, na.rm = TRUE),
    BasLength = mean(BasLength, na.rm = TRUE),
    NasHeight = mean(NasHeight, na.rm = TRUE)
  )

mean_vectors

```

```
## # A tibble: 5 x 5
##   TimePeriod MaxBreadth BasHeight BasLength NasHeight
##       <int>       <dbl>    <dbl>    <dbl>    <dbl>
## 1         1         131.     134.     99.2     50.5
## 2         2         132.     133.     99.1     50.2
## 3         3         134.     134.     96.0     50.6
## 4         4         136.     132.     94.5     52.0
## 5         5         136.     130.     93.5     51.4
```

```
# #Qtn 2 function
# # Function to generate a heat map for a given time period
# generate_heat_map <- function(time_period) {
#   filtered_data <- data[data$TimePeriod == time_period,]
#   cor_matrix <- cor(filtered_data[,1:4]) # Assuming the first four columns are the variables
#
#   # Melt the correlation matrix for ggplot
#   melted_cor_matrix <- melt(cor_matrix)
#
#   # Plot
#   ggplot(melted_cor_matrix, aes(x = Var1, y = Var2, fill = value)) +
#     geom_tile() +
#     geom_text(aes(label = sprintf("%.2f", value)), color = "black", size = 3) +
#     #scale_fill_gradient2(low = "blue", high = "red", mid = "white",
#     #                      midpoint = 0, limit = c(-1,1), space = "Lab",
#     #                      name="Pearson\nCorrelation") +
#     theme_minimal() +
#     theme(axis.text.x = element_text(angle = 45, vjust = 1, size = 9, hjust = 1, family = "Arial"),
#           axis.text.y = element_text(size = 9, family = "Arial"),
#           plot.title = element_text(size = 14, family = "Arial")) +
#     labs(x = '', y = '', title = paste("Correlation Matrix Heat Map \n for Time Period", time_period))
# }
```

```
# #Q2 cntd
# # Generate heat map for time periods
# time_periods <- unique(data$TimePeriod)
# plot_list <- list()
#
# for (time_period in time_periods) {
#   plot_list[[time_period]] <- generate_heat_map(time_period)
# }
#
# # Combine the plots. Adjust the layout with `plot_layout()`
# combined_plot <- wrap_plots(plot_list, ncol = 3) +
#   plot_layout(guides = 'collect')
#
# #save plots
# #ggsave("correlation_heatmaps.png", plot = combined_plot, width = 10, height = 6, units = "in")
#
# combined_plot
```

```
# Q3
# Filter data for period 1
data_period_1 <- data[data$TimePeriod == 1,]
```

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# Extract vectors for X1 and X3
x1 <- data_period_1$MaxBreadth
x3 <- data_period_1$BasLength

# Compute deviation vectors from their means
x1_dev <- x1 - mean(x1)
x3_dev <- x3 - mean(x3)

# Calculate the cosine of the angle using the dot product
cos_angle <- sum(x1_dev * x3_dev) / (sqrt(sum(x1_dev^2)) * sqrt(sum(x3_dev^2)))
cos_angle

```

```
## [1] 0.0150425
```

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# Calculate the angle in radians
angle_radians <- acos(cos_angle)

# Convert the angle to degrees
angle_degrees <- angle_radians * (180 / pi)

angle_degrees

```

```
## [1] 89.1381
```

```

#Qtn 3 Bonus Qtn
period1_obs2 <- data_period_1[1:2,]

x1_dev <- period1_obs2$MaxBreadth - mean(period1_obs2$MaxBreadth)
x2_dev <- period1_obs2$BasHeight - mean(period1_obs2$BasHeight)
x3_dev <- period1_obs2$BasLength - mean(period1_obs2$BasLength)
x4_dev <- period1_obs2$NasHeight - mean(period1_obs2$NasHeight)

dev_vectors <- rbind(c(x1_dev), c(x2_dev), c(x3_dev), c(x4_dev))
dev_vectors

```

```

##      [,1] [,2]
## [1,]  3.0 -3.0
## [2,]  3.5 -3.5
## [3,] -1.5  1.5
## [4,]  0.5 -0.5

```

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dev_vectors_df <- data.frame(
  "x" = dev_vectors[,1],
  "y" = dev_vectors[,2],
  "vector" = c('d1', 'd2', 'd3', 'd4'))
dev_vectors_df

```

```

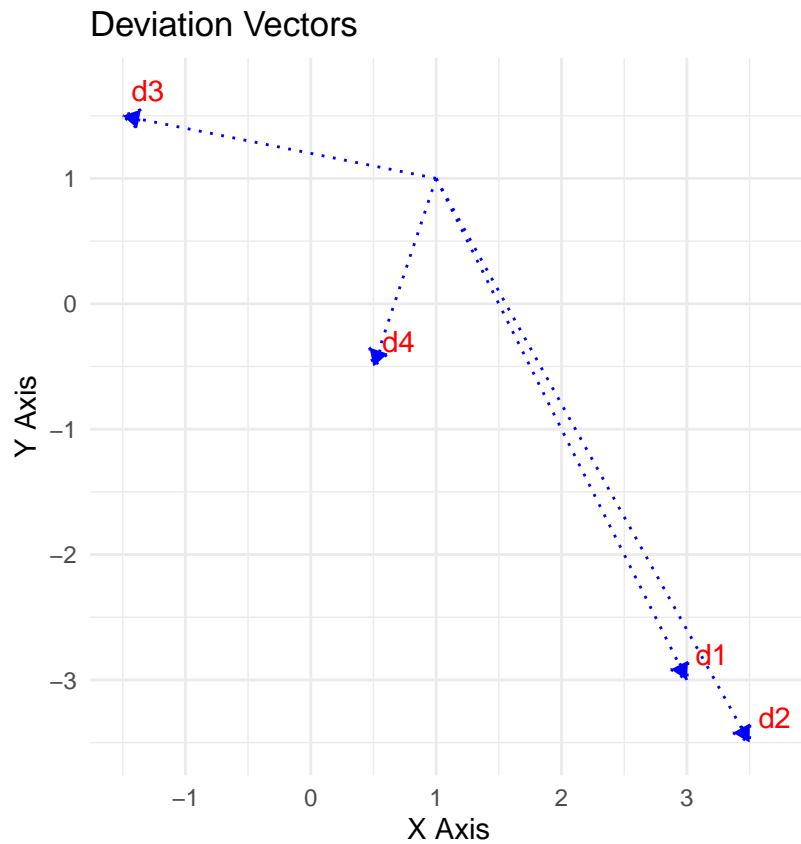
##      x      y vector
## 1  3.0 -3.0     d1
## 2  3.5 -3.5     d2
## 3 -1.5  1.5     d3
## 4  0.5 -0.5     d4

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#Qtn 3 Bonus Qtn ctnd
# Plot vectors
ggplot(dev_vectors_df, aes(xend = x, yend = y)) +
  geom_segment(aes(x = 1, y = 1, xend = x, yend = y),
    arrow = arrow(type = "closed", length = unit(0.1, "inches")),
    color = "blue",
    linetype = "dotted") +
  geom_text(aes(x = x, y = y, label = vector), nudge_x = 0.2, nudge_y = 0.2, color = "red") +
  coord_fixed() +
  theme_minimal() +
  labs(title = "Deviation Vectors", x = "X Axis", y = "Y Axis")

```



```

#Qtn 4
b <- c(-1,0,0,3)
means_matrix <- as.matrix(mean_vectors[, 2:ncol(mean_vectors)])
y_means <- means_matrix %*% b
#means for y1 to y5
y_means

```

```

##           [,1]
## [1,] 20.23333
## [2,] 18.33333
## [3,] 17.23333
## [4,] 20.40000
## [5,] 17.93333

```

```

#now calculating the covariance matrix
data = data %>% mutate(Y = 3*NasHeight - MaxBreadth) #the y value for each data data point
y_data <- data %>% select(TimePeriod, Y)

#create an index to match data points ie 30 data points for 5 periods
index <- rep(seq(1,30), times = 5)
y_data$index <- index
y_data_wide <- pivot_wider(y_data, names_from = TimePeriod, values_from = Y) #pivot data to use cov fun
head(y_data_wide)

```

```

## # A tibble: 6 x 6
##   index   '1'    '2'    '3'    '4'    '5'
##   <int> <dbl> <dbl> <dbl> <dbl> <dbl>
## 1     1    16    20    19    25    13
## 2     2    19    11    12    18    11
## 3     3    19    -3    12     6    43
## 4     4    13     5    20    18    26
## 5     5    26     9     1     5     3
## 6     6    30    21    10    19    30

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y_data_wide <- y_data_wide %>% select(-index) #remove the index from cov calculation
y_covariances <- cov(y_data_wide)
y_covariances

```

```

##           1           2           3           4           5
## 1 51.5643678  1.402299  23.32299  -7.924138  0.2229885
## 2  1.4022989 90.712644  -6.08046  29.862069  2.8850575
## 3 23.3229885 -6.080460 120.11609 -10.131034 -33.4321839
## 4 -7.9241379 29.862069 -10.13103  74.731034  14.6482759
## 5  0.2229885  2.885057 -33.43218  14.648276 165.0298851

```