Linear Regression

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Gradient Derivation

a)

$$\begin{split} \frac{\partial}{\partial \beta_0} \left[\frac{1}{2m} \sum_{i=0}^m (\beta_0 + \beta_1 x^{(i)} - y^{(i)})^2 \right] &= \frac{\partial}{\partial \beta_0} \left[\frac{1}{2m} \sum_{i=0}^m (\beta_0 + \beta_1 x^{(i)} - y^{(i)})^2 \right] \\ &= \frac{1}{2m} \sum_{i=0}^m \left[2(\beta_0 + \beta_1 x^{(i)} - y^{(i)}) \cdot 1 \right] \\ &= \frac{1}{m} \sum_{i=0}^m \beta_0 + \beta_1 \frac{1}{m} \sum_{i=0}^m x^{(i)} - \frac{1}{m} \sum_{i=0}^m y^{(i)} \\ &= \beta_0 + \beta_1 \bar{x} - \bar{y} \end{split}$$

b)

$$\frac{\partial}{\partial \beta_{1}} \left[\frac{1}{2m} \sum_{i=0}^{m} (\beta_{0} + \beta_{1} x^{(i)} - y^{(i)})^{2} \right] = \frac{1}{2m} \sum_{i=0}^{m} \frac{\partial}{\partial \beta_{1}} \left[(\beta_{0} + \beta_{1} x^{(i)} - y^{(i)})^{2} \right]
= \frac{1}{2m} \sum_{i=0}^{m} \left[2x^{(i)} (\beta_{0} + \beta_{1} x^{(i)} - y^{(i)}) \right]
= \frac{1}{m} \sum_{i=0}^{m} \left[\beta_{0} x^{(i)} + \beta_{1} x^{(i)^{2}} - x^{(i)} y^{(i)} \right]
= \beta_{0} \frac{1}{m} \sum_{i=0}^{m} x^{(i)} + \beta_{1} \frac{1}{m} \sum_{i=0}^{m} x^{(i)^{2}} - \frac{1}{m} \sum_{i=0}^{m} x^{(i)} y^{(i)}
= \beta_{0} \bar{x} + \beta_{1} \bar{x^{2}} - \bar{xy}$$

Linear Regression by Gradient Decent Linear Model on Airbnb Data