

# Computer Languages

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*CS Saturday*

# CS Saturdays

- Context
- Q: Should I do it?

# Agenda

- How humans read
- How computers read
- Why study compilers?
- History of computer languages
- How Compilers Work
- Grammars
- Top down parsing
- Writing our own parser

# Key Takeaways

- Your program is also a piece of data
- Compilers have four main stages (lexing, parsing, optimization, code generation)
- Programming languages are defined by grammars
- There are two primary ways to parse a given language into a grammar, top-down and bottom-up

# How We Understand Language

# How humans read

This is a sentence.

word wordword word

Tihs is a steennce.

## NOT EVERYONE CAN READ THIS

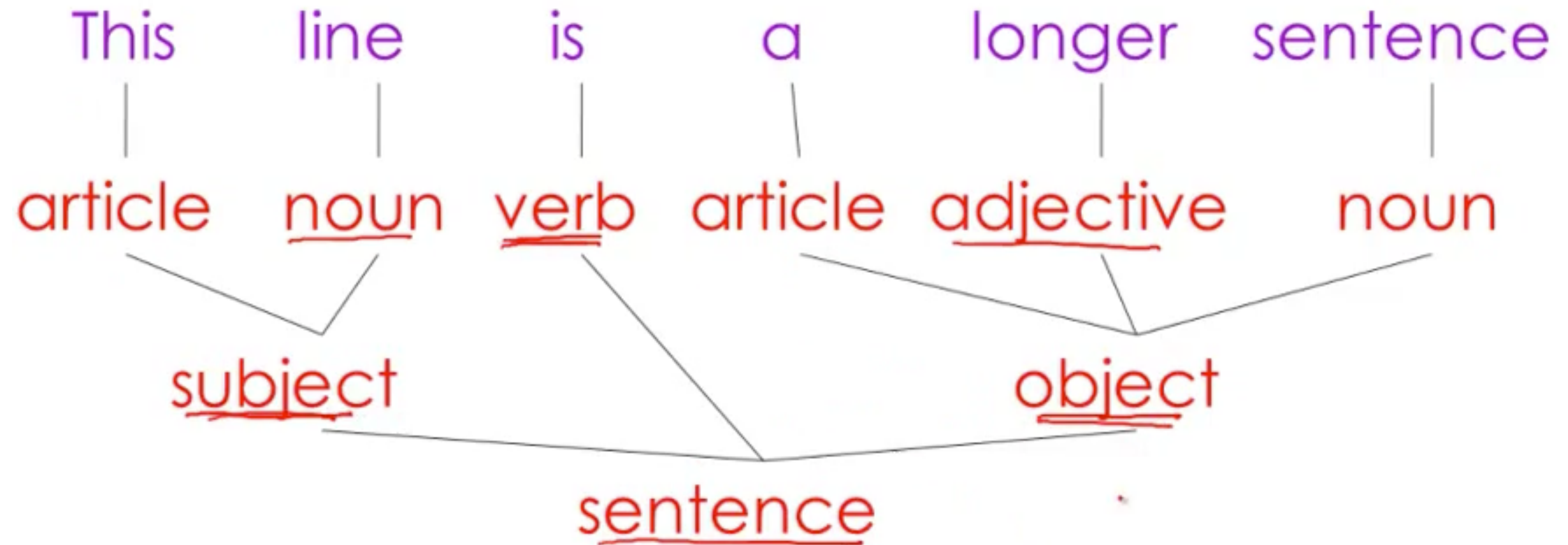
Aoccdrnig to a rscheearch at Cmabrigde Uinervtisy, it deosn't mttair in waht oredr the ltteers in a wrod are, the olny iprmoetnt tihng is taht the frist and lsat ltteer be at the rghit pclae. The rset can be a toatl mses and you can sitll raed it wouthit porbelm. Tihs is bcuseae the huamn mnid.....

# Parsing

This	line	is	a	longer	sentence
article	<u>noun</u>	<u>verb</u>	article	adjective	noun



# Parsing





# How humans read

- Semantic Meaning

- Jack said John forgot his homework at home.
- There wasn't a single person at the party.

- Meaning is given by context, usually humans can disambiguate

# How humans read

- Grammar very important
- "Eats, shoots and leaves" versus "Eats shoots and leaves"



# Generation

- The words and grammar combine to generate meaning or action in our minds

# Phases of Understanding

- **Four phases:**
  - Lexing (we do this so quickly we don't even notice)
  - Parsing (grammar)
  - Semantic Analysis
  - Generation

# How computers read

- **Similar to us:**

- Convert a program (program.js) into a string of words (tokens)
- Parse those tokens into a grammar
- Semantically Analyze (is this program correct?)
- Generate a lower level of code (machine code or IR - intermediate representation)

- **Not similar to us:**

- Can't handle ambiguous semantics
- Definition of languages is strict and formal - grammar is very important
- Lots of focus on optimization

# How computers read

- The systems that convert program code into another form (usually for execution) are called either compilers or interpreters
- They follow a 5 stage process:
  - Lexing
  - Parsing
  - Semantic Analysis
  - Optimization
  - Generation

# Why study compilers



# Why study compilers

- **Compiler theory is a third/fourth year CS course**
- **Compilers combine a lot of different CS fields**
  - Data structures
    - Parse trees
    - Symbol tables
  - Algorithms
    - Memory allocation
    - Register allocation
    - Stack management
    - Code optimization and minimization (tree-shaking, dead code elimination)

# Why study compilers

- **Practical:**

- Implementing a programming language is a fun exercise and a pretty sure path to fame
- Compilers/parsers are embedded in a lot of tools we use

- **We already use a lot of compilers in our day to day work:**

- Angular: *\$parse* service (evaluate basic JavaScript like expressions)
- React: *JSX transformer* (convert HTML to JavaScript code)
- babel.js (convert ES6 to ES3, 4 5)
- ESLint (parses JavaScript to look for errors)
- SCSS (compiles SCSS to CSS)
- Uglify (minifies JS code for)
- ng-annotate (compiles DI to Inject statements)

# History of Compilers

# Ada Lovelace

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1842

*Invention of the first computer  
programming language for Babbage's  
Analytical Engine*



# Ada Lovelace

- Things Ada Lovelace foresaw in the Analytical Engine
  - Variables and Data Storage
  - Cycles (Loops, Nested Loops)
  - Sequences (Blocks)
  - Subroutines (Functions)

(6.)  $(\div), \sum (+1)^p (\times, -)$  or  $(1), \sum (+1)^p (2, 3)$ ,  
where  $p$  stands for the variable ;  $(+1)^p$  for the function of the variable,  
that is, for  $\phi p$  ; and the limits are from 1 to  $p$ , or from 0 to  $p - 1$ ,  
each increment being equal to unity. Similarly, (4.) would be,—

(7.)  $\sum (+1)^n \{ (\div), \sum (+1)^p (\times, -) \}$

the limits of  $n$  being from 1 to  $n$ , or from 0 to  $n - 1$ ,

(8.) or  $\sum (+1)^n \{ (1), \sum (+1)^p (2, 3) \}$ .

<http://blog.stephenwolfram.com/2015/12/untangling-the-tale-of-ada-lovelace/>



# Alan Turing

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*1936*

*Describes Turing Machine*



# Grace Hopper

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1952

*Creates the first compiler for a language called A-0. Later worked on COBOL.*





# John Backus

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*1953*

*Inventor of Backus-Naur Form - a  
grammar for describing languages  
and creator of Fortran*

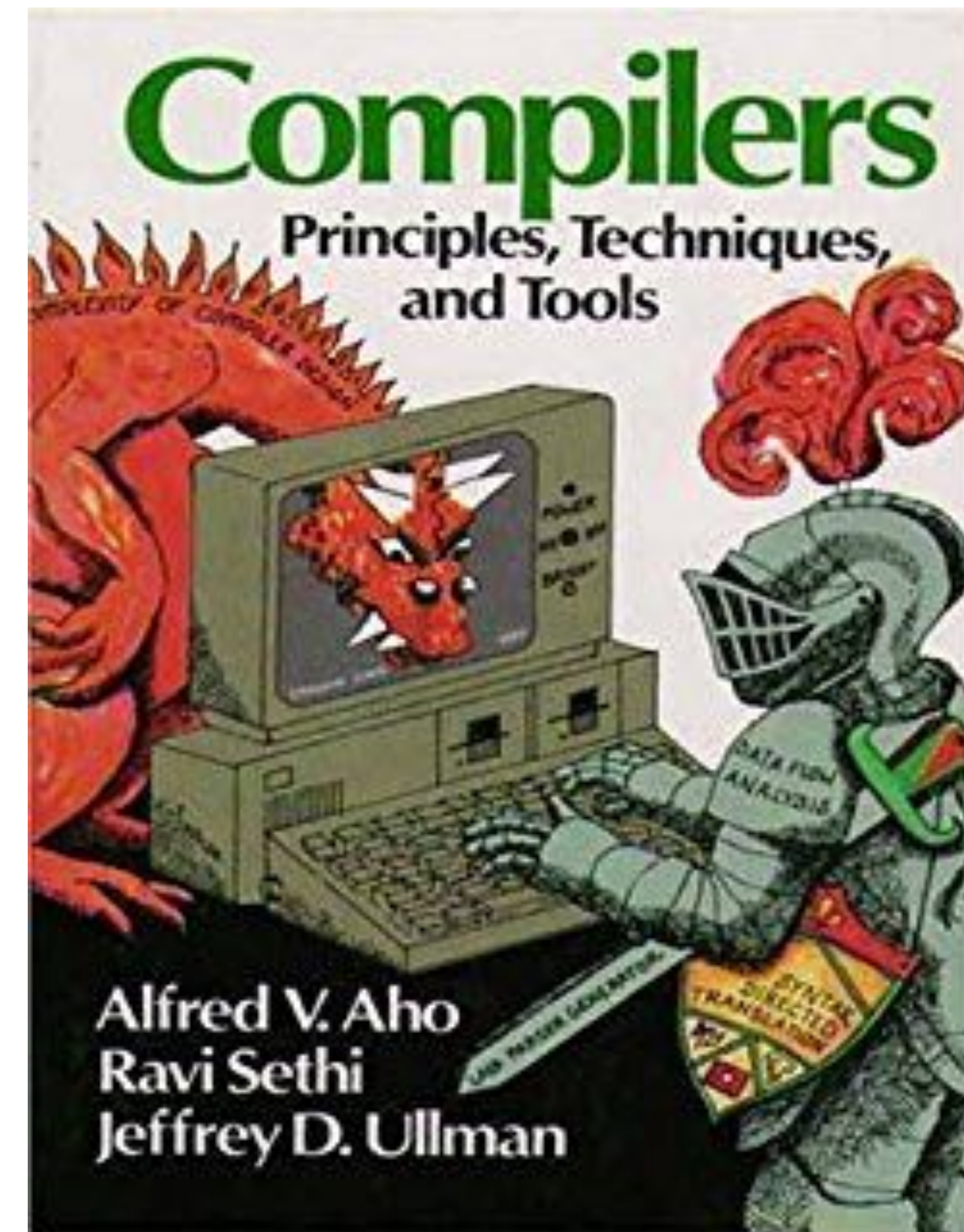


# Alfred Aho

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*Present*

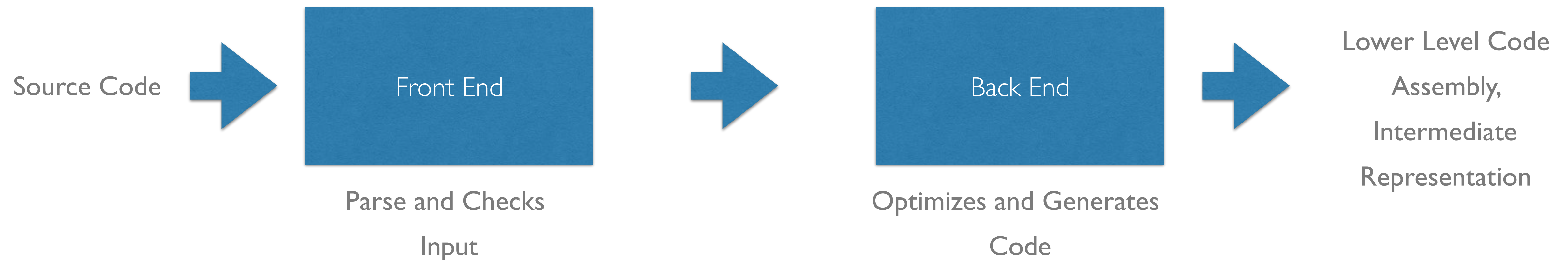
*Author of the "Dragon book" and  
professor at Columbia University.*



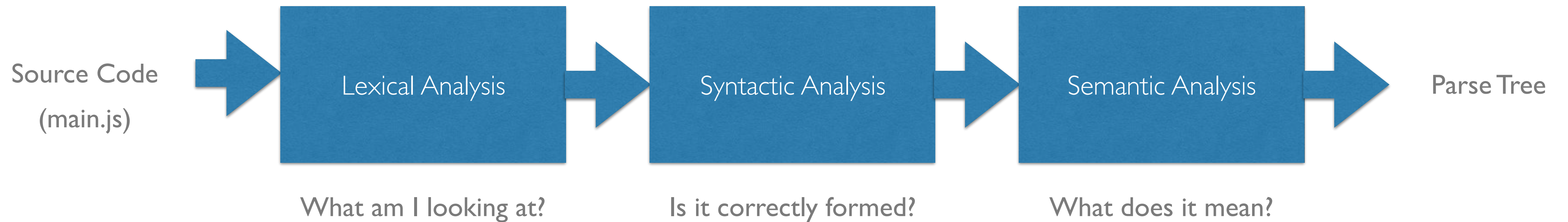
# How Compilers Work



# How Compilers Work



# Frontend



# Lexical Analysis

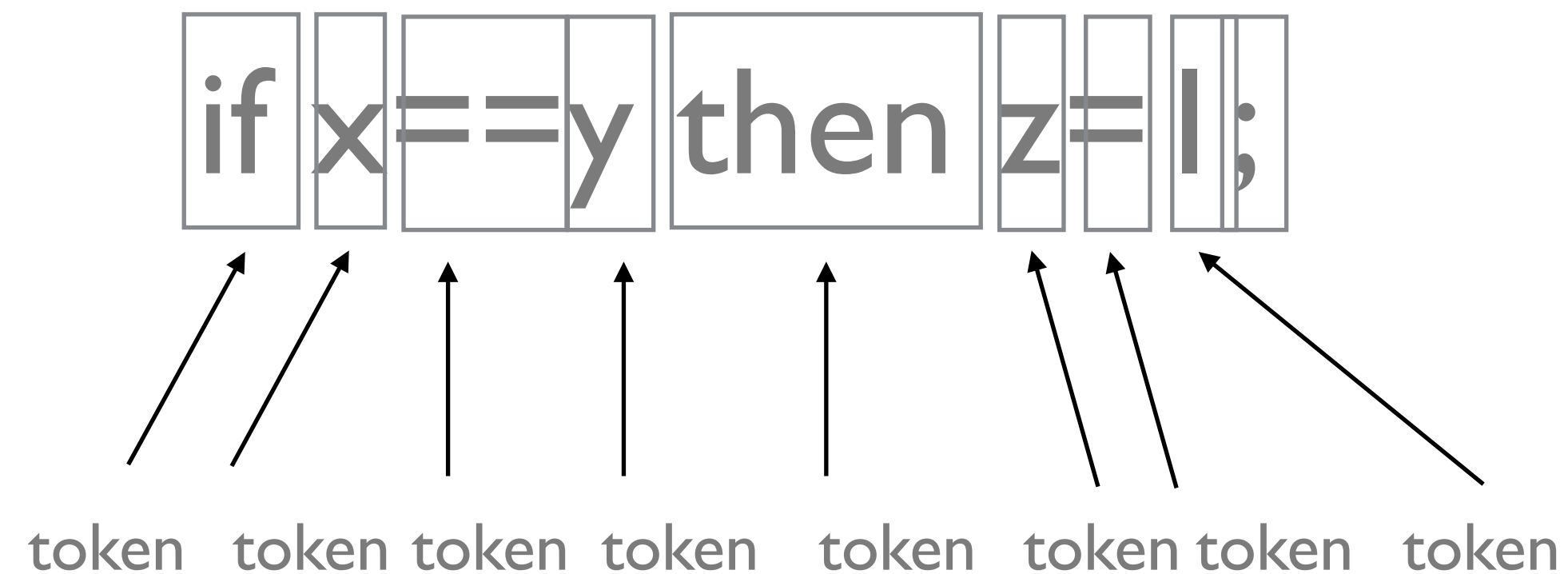
This is a sentence.

word wordword word

if x==y then z=l;

token token token token token token token token

# Lexical Analysis



[IF] [ID X] [EQL] [ID Y] [THEN] [ID Z] [ASSIGN] [NUMBER 1] [SEMI]

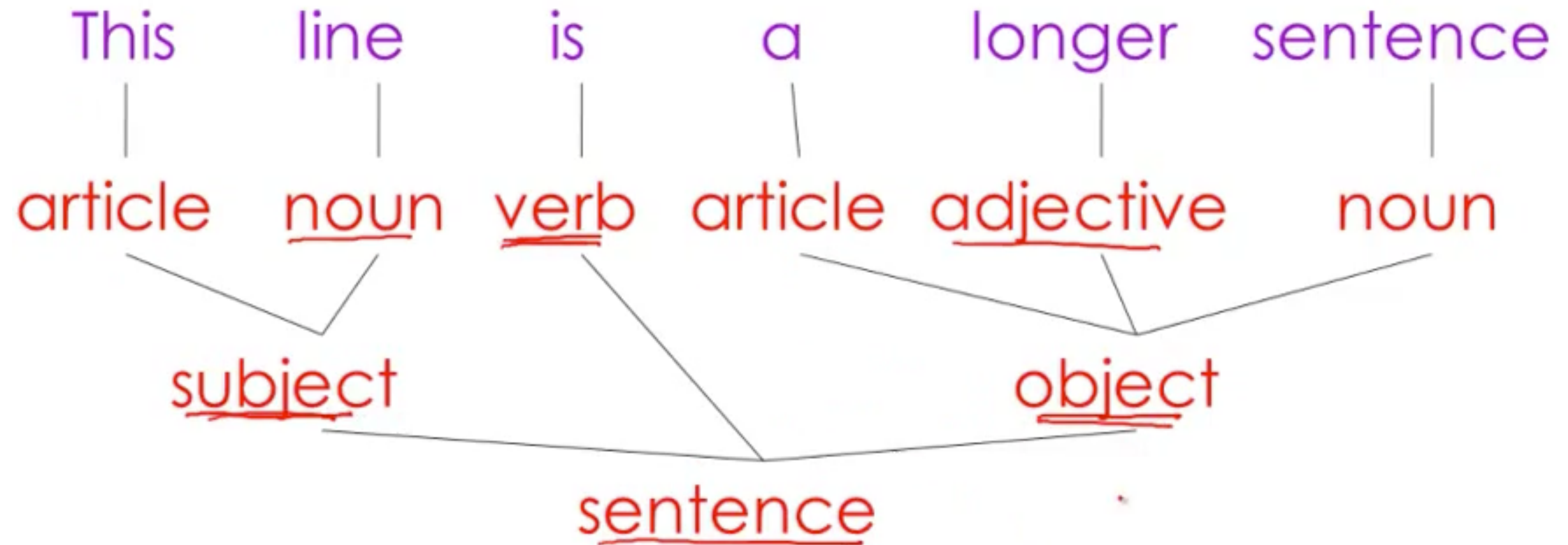
Often referred to as the "token stream"



# Parsing

This	line	is	a	longer	sentence
article	<u>noun</u>	<u>verb</u>	article	adjective	noun

# Parsing



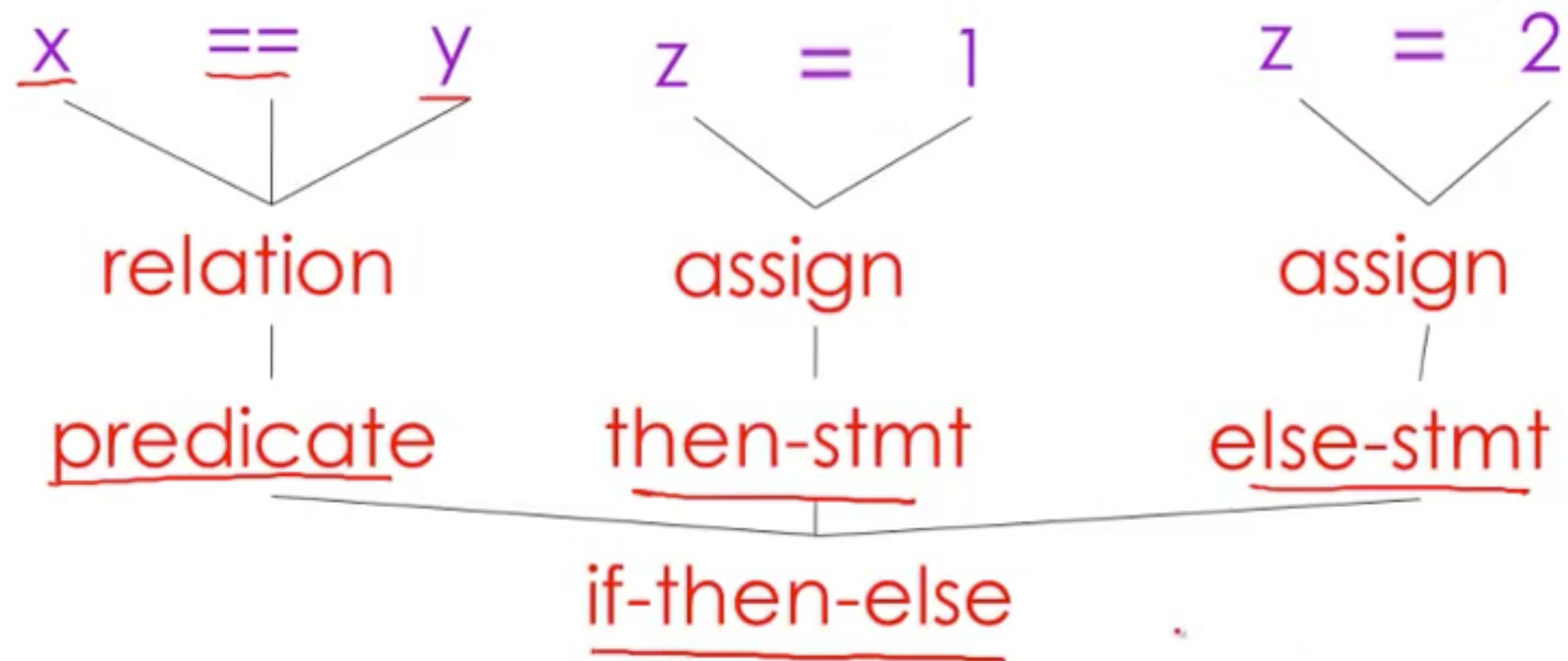
# Parsing

if x == y then z = 1; else z = 2;

x == y z 1 z 2

# Parsing

if x == y then z = 1; else z = 2;



# Token Parsing Table

- What makes a valid token?
- List of all valid keywords (if, else, class, function)
- List of valid identifiers (variable names)
- List of valid literals (what numbers, strings look like)
- Defined using regular expressions
- <https://www.ecma-international.org/ecma-262/8.0/index.html#sec-identifier-names>

# Grammars



# Switch your thinking...

- Let's talk about simple math formulas
- If someone asked you - what are some basic rules you could create to generate simple math formulas...
- Start with some thing ( $E$ ) that can turn into other things (including itself) while creating sentences... e.g.  $E \rightarrow E + E$



# Grammar for Mathematical Expressions

- E = Expression
- Start your sentence as an abstract idea of an expression: E
- $E \Rightarrow E + E$
- $E \Rightarrow E - E$
- $E \Rightarrow E * E$
- $E \Rightarrow -E$
- $E \Rightarrow (E)$
- $E \Rightarrow \text{num}$

token

# Grammar for Mathematical Expressions

- $E = \text{Expression (start = E)}$

- $E \Rightarrow E + E$

- $E \Rightarrow E - E$

- $E \Rightarrow E * E$

- $E \Rightarrow -E$

- $E \Rightarrow (E)$

- $E \Rightarrow \text{num}$

production rule  
left-hand side can produce right  
hand side

# Grammar for Mathematical Expressions

- $E = \text{Expression (start = E)}$

- $E \Rightarrow E + E$

- $E \Rightarrow E - E$

- $E \Rightarrow E * E$

- $E \Rightarrow -E$

- $E \Rightarrow (E)$

- $E \Rightarrow \text{num}$

Left hand side of a production rule must be a single symbol

These symbols are called "non-terminals"

This grammar only has one (E) but most grammars can have many non-terminals

# Grammar for Mathematical Expressions

- $E = \text{Expression (start = E)}$

- $E \Rightarrow E + E$

Right hand side is a string of 0 or more symbols.

- $E \Rightarrow E - E$

- $E \Rightarrow E * E$

- $E \Rightarrow -E$

- $E \Rightarrow (E)$

- $E \Rightarrow \text{num}$

Symbols that are not non-terminals are called "terminals" Terminals do not appear on the left-hand side.

Here: + - \* ( ) num are terminals

# How Grammar creates Languages

- The language created by a grammar is the **set of all terminal strings** that can be **generated** using the **production rules** of that grammar.
- **Corollary:**
  - If a valid parse tree can be generated from a terminal string using the production rules of the grammar, then that terminal string is in the language defined by the grammar.
  - e.g. the language of JavaScript is defined by the production rules of the grammar of JavaScript.
  - If a string of JavaScript code (terminal string) can be parsed using the production rules of JavaScript, that file is a valid JavaScript language file.

# Parse Trees and Languages



# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree

$1 + 2 \times 3$

$E$

← sentence symbol

# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

$$E \rightarrow E \times E$$

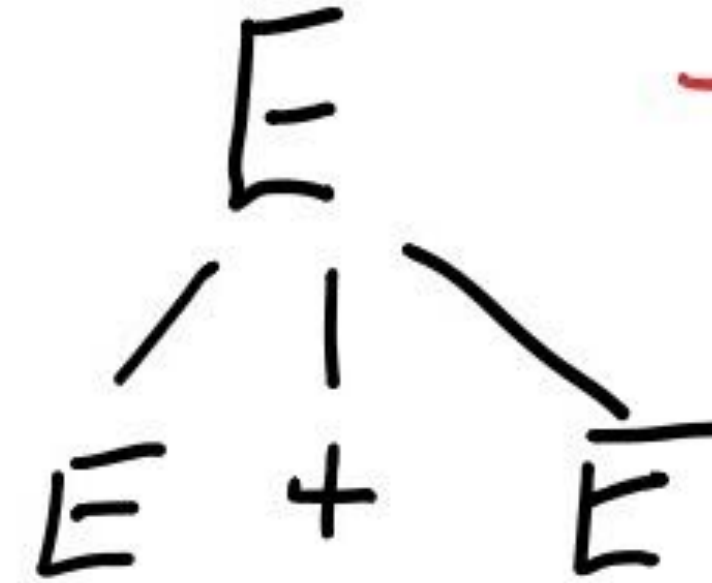
$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree

$1 + 2 \times 3$



Parent = LHS  
Children = RHS

# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

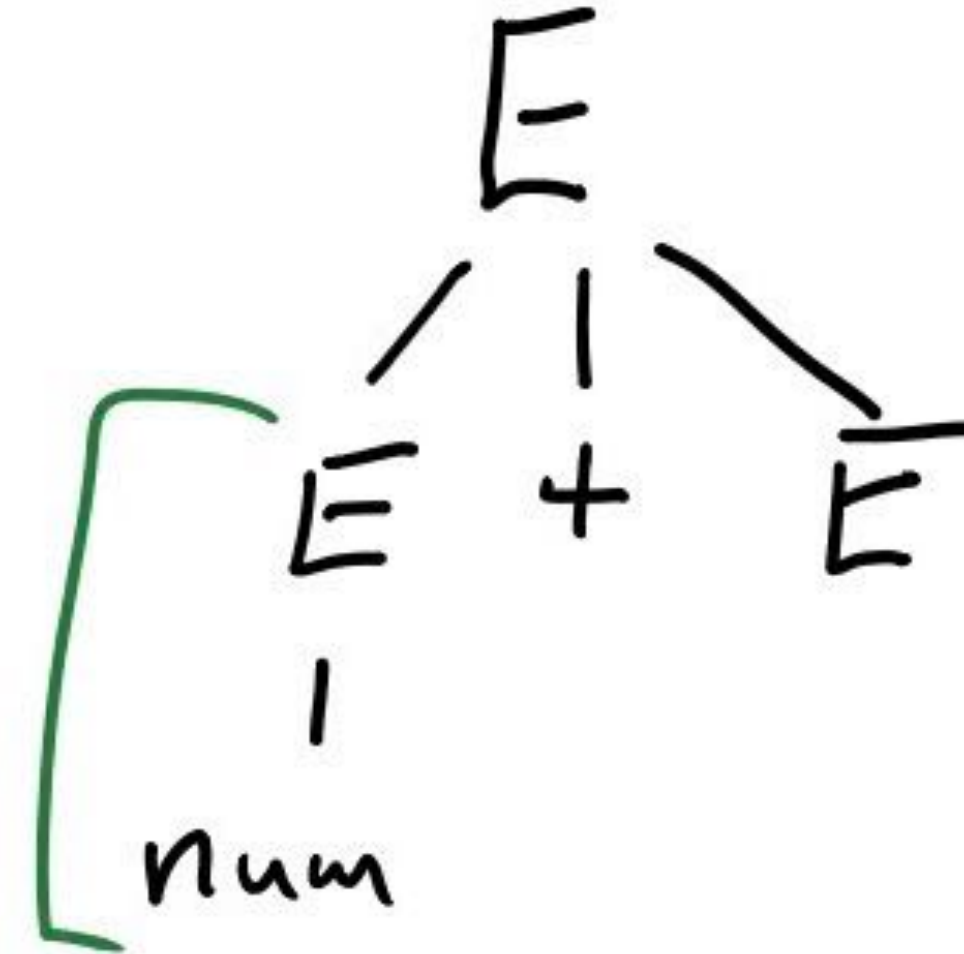
$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree  
1 + 2 x 3





# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

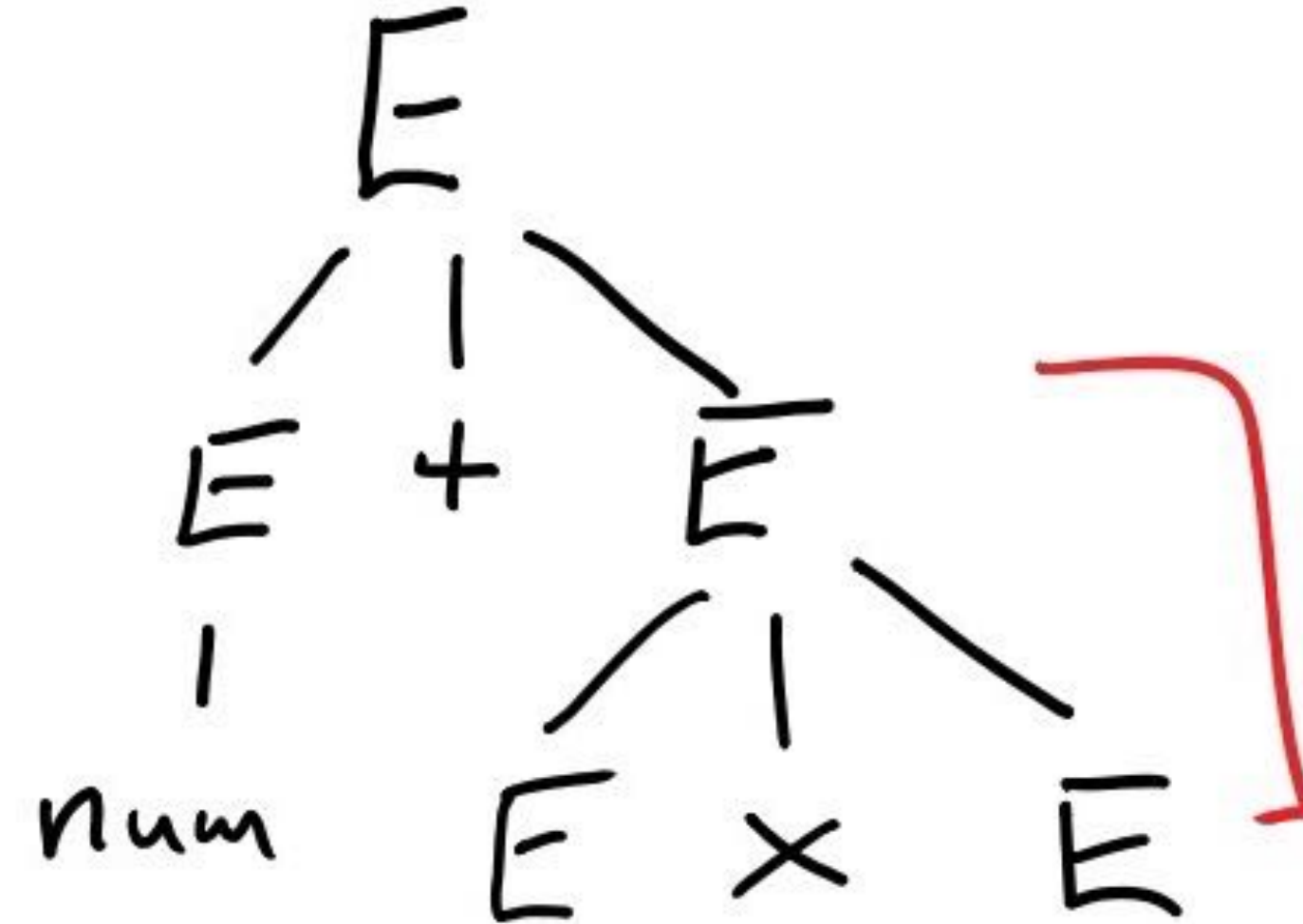
$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree  
1 + 2 x 3



# Grammar for Mathematical Expressions

$E \rightarrow E + E$

$E \rightarrow E - E$

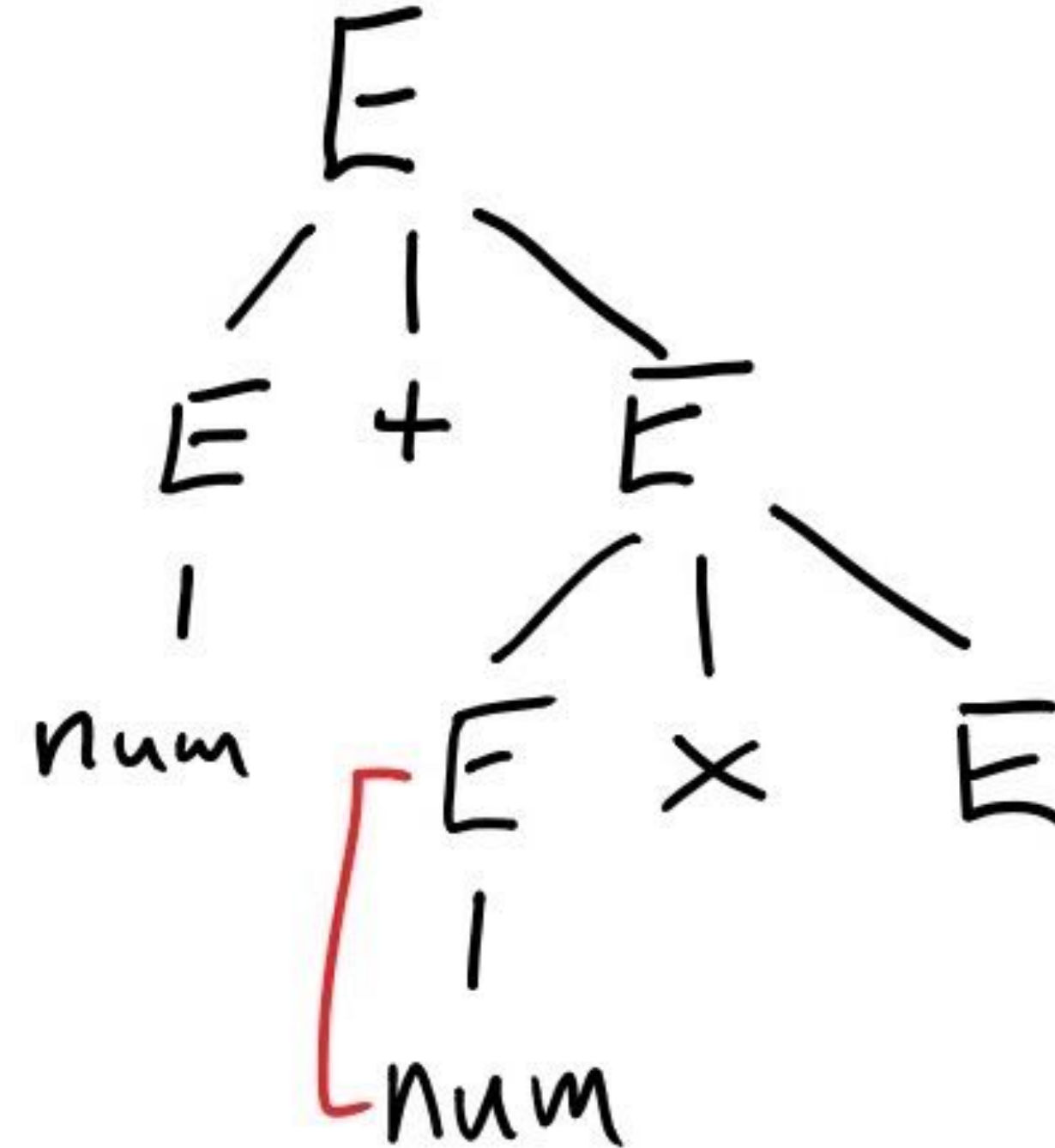
$E \rightarrow E \times E$

$E \rightarrow -E$

$E \rightarrow (E)$

$E \rightarrow \text{num}$

Parse tree  
 $1 + 2 \times 3$



# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

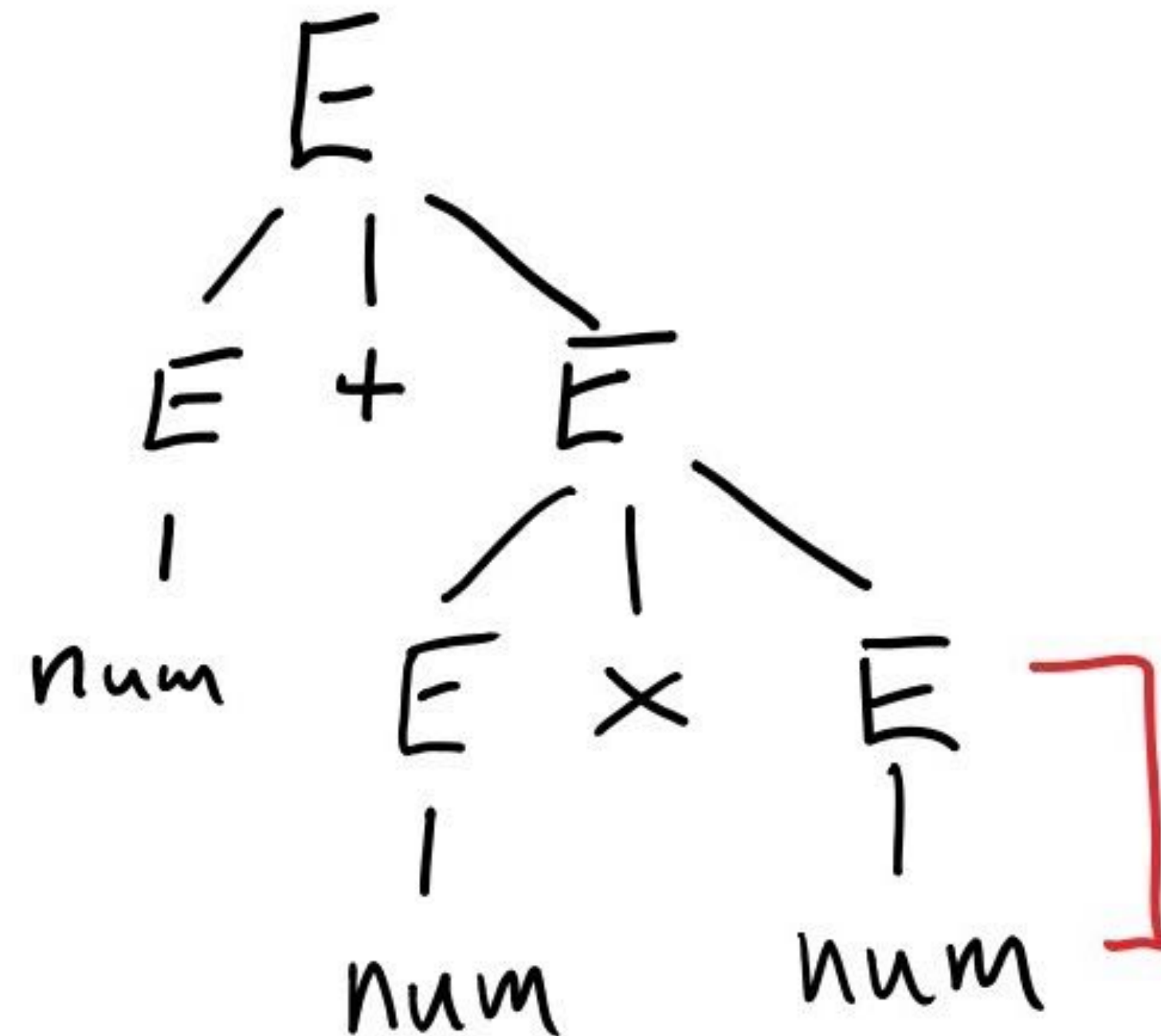
$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree  
1 + 2 x 3





# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

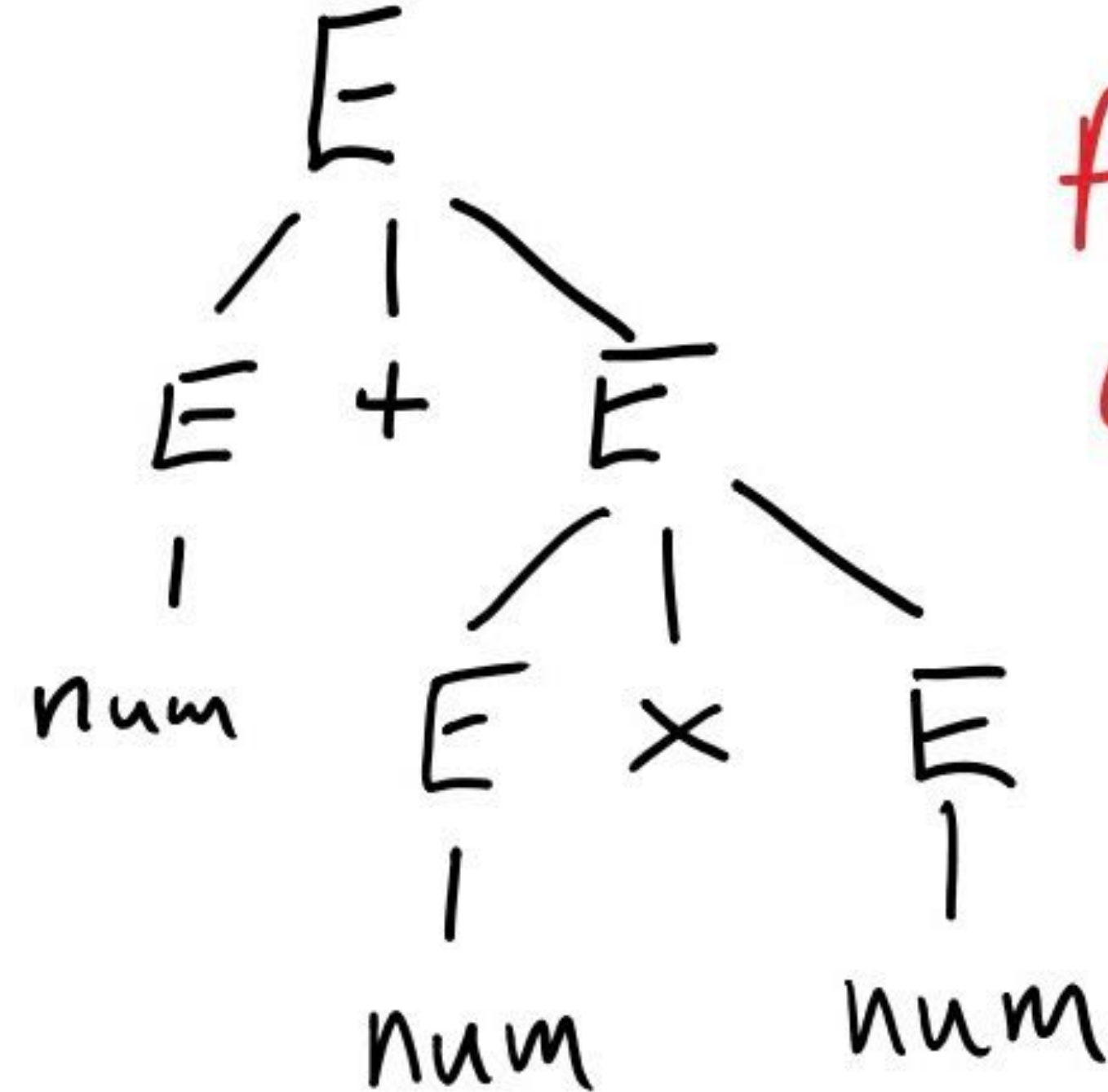
$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree  
1 + 2 x 3



All leaves  
are terminals

# Grammar for Mathematical Expressions

$$E \rightarrow E + E$$

$$E \rightarrow E - E$$

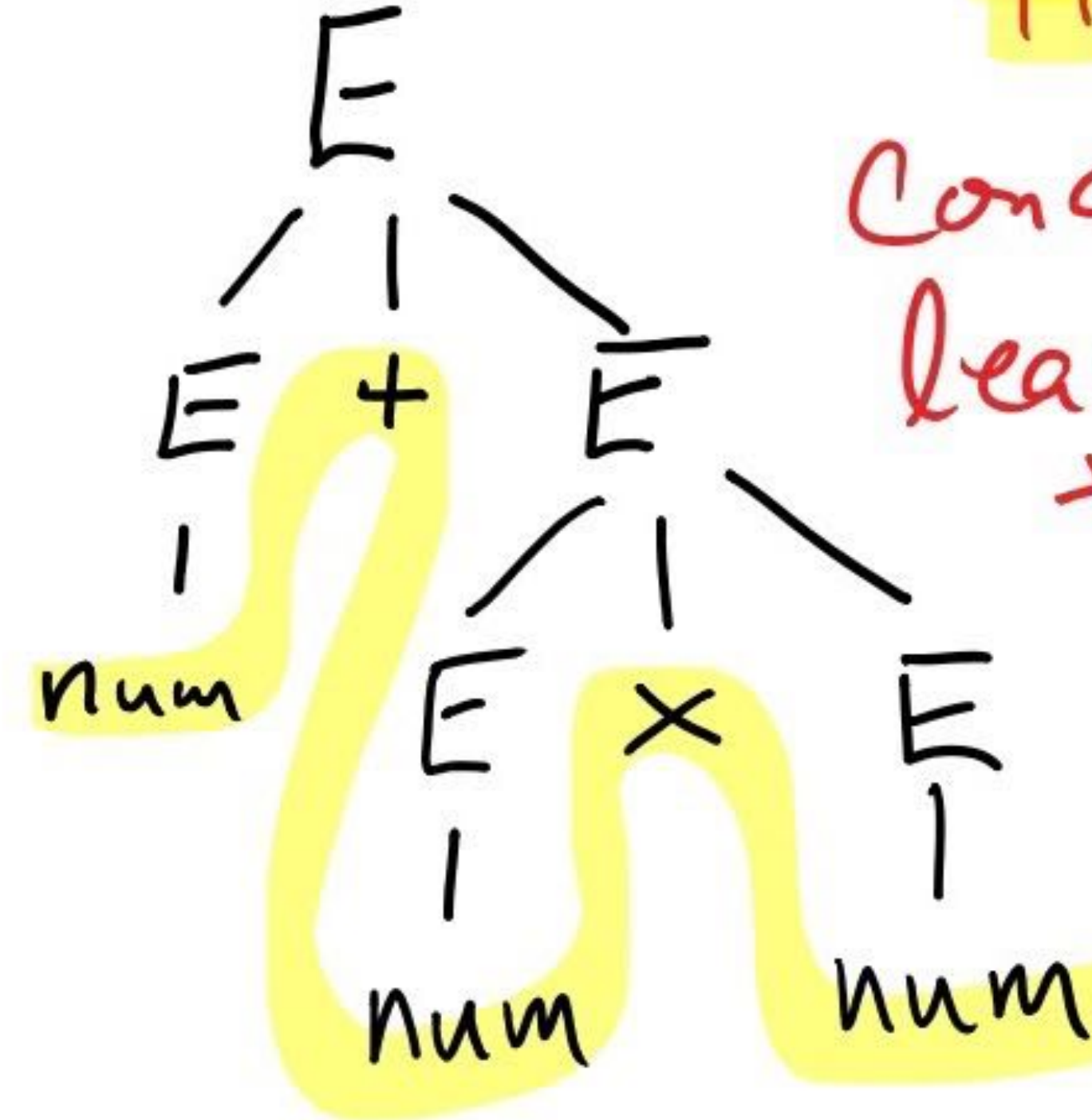
$$E \rightarrow E \times E$$

$$E \rightarrow -E$$

$$E \rightarrow (E)$$

$$E \rightarrow \text{num}$$

Parse tree  
 $1 + 2 \times 3$



Yield

Concatenate  
leaves of  
tree from  
left to  
right.

$\text{num} + \text{num} \times \text{num}$  is in language of grammar.

# Grammar Summary

- Grammar defines production rules
- Given various productions of a grammar you can create statements in a language
- Given statements language, can you parse it back into a tree of the production rules?



# Parsing Approaches

- **Top Down**
  - Recursive Descent
  - Predictive parser
- **Bottom-Up**
  - Backtracking (recursion)
  - Shift Reduce (token table generation)

# Stack Implementation of Shift-Reduce Parsing

Grammar:

$E \rightarrow E + E$

$E \rightarrow E * E$

$E \rightarrow ( E )$

$E \rightarrow \text{id}$

Find handles  
to reduce

Stack	Input	Action
\$	<b>id+id*id\$</b>	shift
<u>\$id</u>	<b>+id*id\$</b>	reduce $E \rightarrow \text{id}$
\$E	<b>+id*id\$</b>	shift
\$E+	<b>id*id\$</b>	shift
<u>\$E+id</u>	<b>*id\$</b>	reduce $E \rightarrow \text{id}$
\$E+E	<b>*id\$</b>	shift (or reduce?)
\$E+E*	<b>id\$</b>	shift
<u>\$E+E*id</u>	\$	reduce $E \rightarrow \text{id}$
<u>\$E+E*E</u>	\$	reduce $E \rightarrow E * E$
<u>\$E+E</u>	\$	reduce $E \rightarrow E + E$
\$E	\$	accept

How to  
resolve  
conflicts?

# Recursive Descent Parsing

- Manual Parser Creation
- Usually do it with a grammar that's defined as *LL(1)*
- LL = Left to right, Left-most derivation
- 1 = look one token ahead in the token array
- Some caveats:
  - The production rules have to be defined in a certain way
  - Have to be able to determine which production rule ( $E \Rightarrow E + E$ ) to parse based only on next token
  - No left recursions:  $E \Rightarrow E + E$  (recursion will never end)



# Grammar for Mathematical Expressions

- $E = \text{Expression (start with } E\text{)}$

- $E \Rightarrow E + E$

- $E \Rightarrow E - E$

- $E \Rightarrow E * E$

- $E \Rightarrow -E$

- $E \Rightarrow (E)$

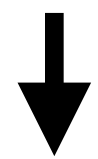
- $E \Rightarrow \text{num}$

NEED TO REMOVE LEFT  
RECURSION

# Removing Left Recursion

- ◉  $E \Rightarrow E + T$

- ◉  $E \Rightarrow T$



- ◉  $E \Rightarrow T E'$

- ◉  $E' \Rightarrow + T E'$

- ◉  $E' \Rightarrow \textit{epsilon} (\epsilon)$

- ◉ Read more: <http://www.csd.uwo.ca/~moreno/CS447/Lectures/Syntax.html/node8.html>

# Grammar for Mathematical Expressions

- ◉ E = Expression, T = Term, F = Factor, {A, B} => placeholders

- ◉ E => T A

- ◉ A => + T A

- ◉ A => - T A

- ◉ A => *epsilon*

- ◉ T => F


- ◉ T => F \* F

- ◉ T => F / F

- ◉ F => ( E )

- ◉ F => -F

- ◉ F => number

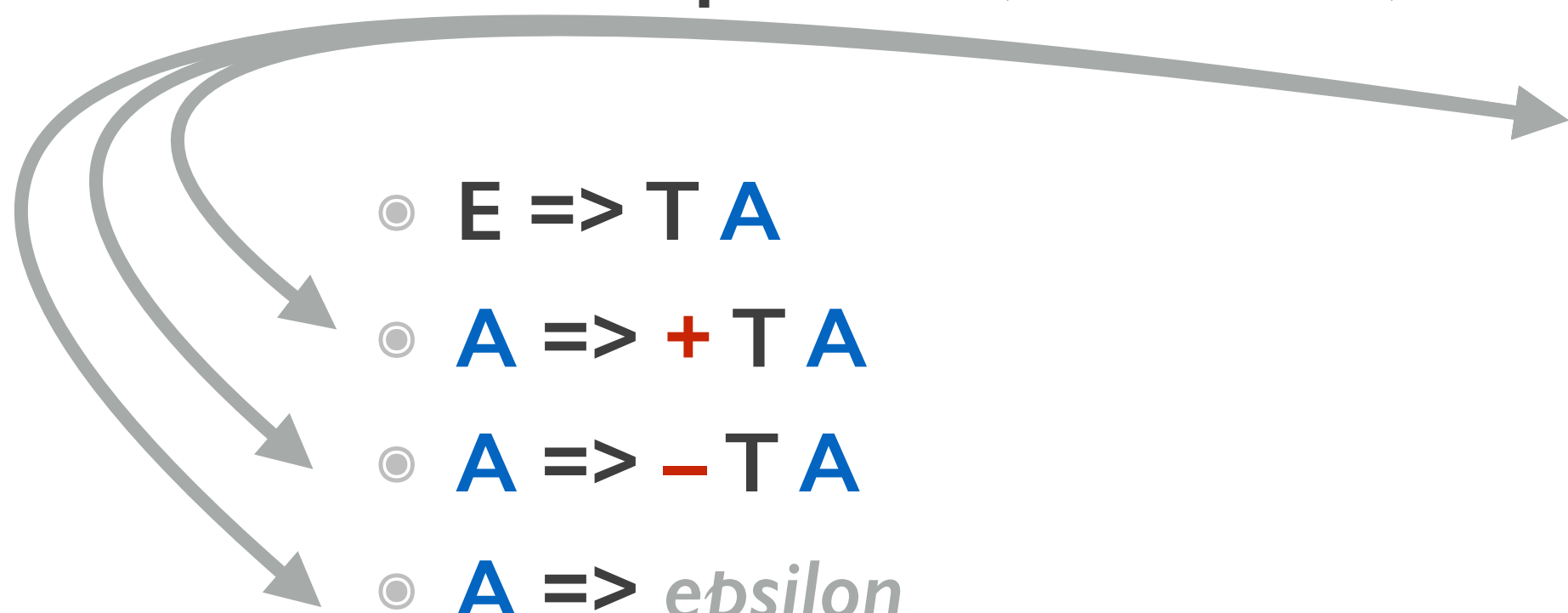


```
function parseExpression() {  
    var t = parseTerm();  
    var a = parseA();  
    return TreeNode('Expression', t, a);  
}
```

# Grammar for Mathematical Expressions

- ◉ E = Expression, T = Term, F = Factor, {A, B} => placeholders

- ◉ E => T A
- ◉ A => + T A
- ◉ A => - T A
- ◉ A => *epsilon*
- ◉ T => F
- ◉ T => F \* F
- ◉ T => F / F
- ◉ F => ( E )
- ◉ F => -F
- ◉ F => number



```
function parseA() {  
    var nextToken = this.peek();  
    if (nextToken.name == "ADD") {  
        this.get();  
        var t = parseTerm();  
        var a = parseA();  
        return new TreeNode("A", "+", t, a);  
    } else if (...) { ...  
    } else {  
        return new TreeNode("A"); // no children  
    }  
}
```

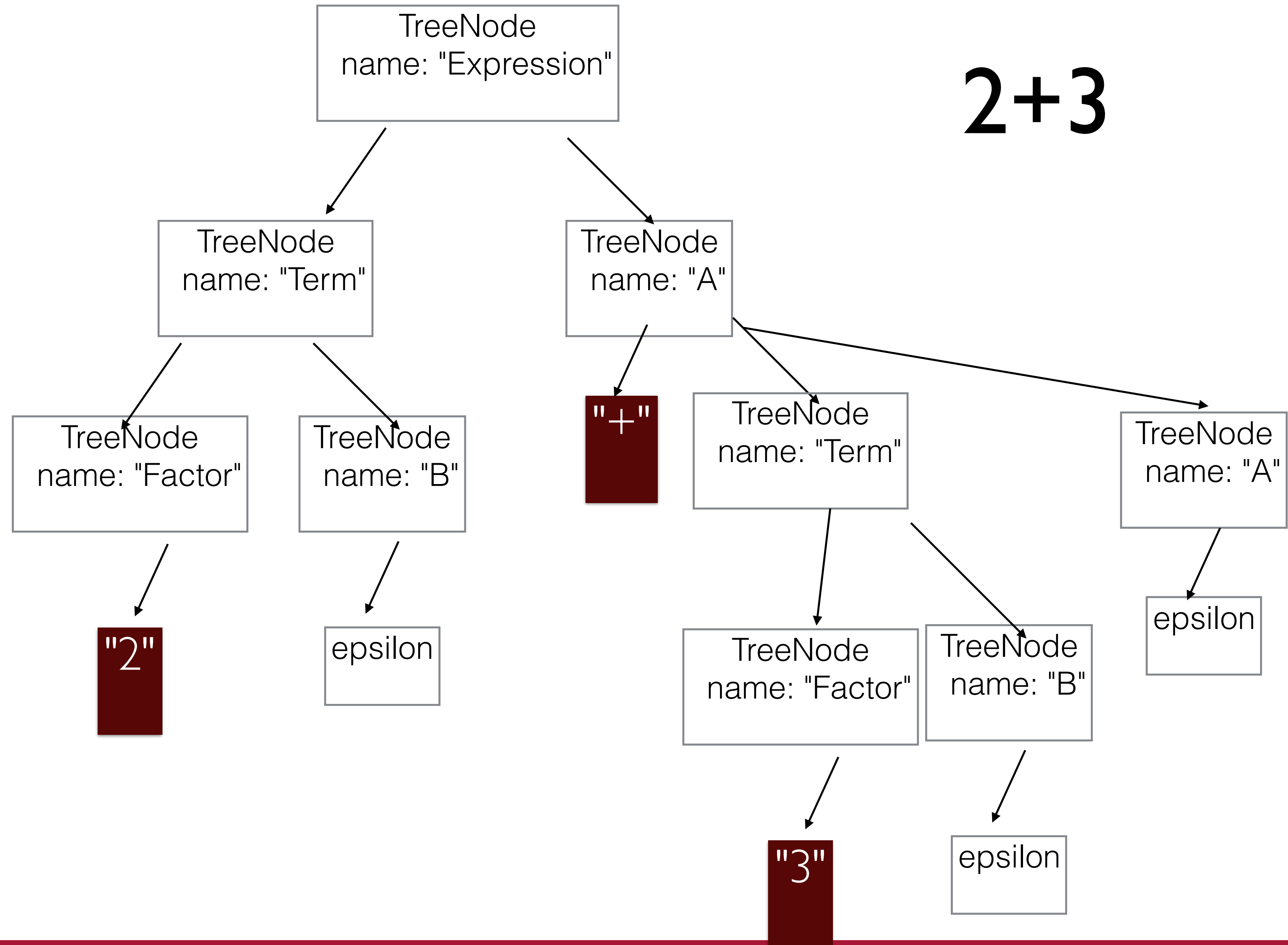
# Grammar for Mathematical Expressions

- ◉ E = Expression, T = Term, F = Factor, {A, B} => placeholders

- ◉  $E \Rightarrow T A$
- ◉  $A \Rightarrow + T A$
- ◉  $A \Rightarrow - T A$
- ◉  $A \Rightarrow \textit{epsilon}$
- ◉  $T \Rightarrow F B$
- ◉  $B \Rightarrow * F B$
- ◉  $B \Rightarrow / F B$
- ◉  $B \Rightarrow \textit{epsilon}$
- ◉  $F \Rightarrow ( E )$
- ◉  $F \Rightarrow -F$
- ◉  $F \Rightarrow \textit{number}$

```
function parseA() {  
    var nextToken = this.peek();  
    if (nextToken.name == "ADD") {  
        this.get();  
        var t = parseTerm();  
        var a = parseA();  
        return new TreeNode("A", "+", t, a);  
    } else if (...) { ...  
    } else {  
        return new TreeNode("A"); // no children  
    }  
}
```

2+3





# Grammar

- ◎ **Examples of Grammars**

- <http://zaach.github.io/jison/demos/calc/>
- <https://github.com/zaach/jison/blob/master/examples/jscore.jison>

- ◎ **Parser Generators**

- Lex/Yacc
- Flex/Bison
- Jison - [jison.org](http://jison.org)

- ◎ **Parsers**

- Esprima - <http://esprima.org/>

```
1 // Life, Universe, and Everything
2 var answer = 6 * 7;
3
```

No error

Syntax node location info (start, end):

- ☐ Index-based range
- ☐ Line and column-based
- ☐ Attach comments

Syntax

Tree

Tokens

```
{
  "type": "Program",
  "body": [
    {
      "type": "VariableDeclaration",
      "declarations": [
        {
          "type": "VariableDeclarator",
          "id": {
            "type": "Identifier",
            "name": "answer"
          },
          "init": {
            "type": "BinaryExpression",
            "operator": "*",
            "left": {
              "type": "Literal",
              "value": 6,
              "raw": "6"
            },
            "right": {
              "type": "Literal",
              "value": 7,
              "raw": "7"
            }
          }
        }
      ],
      "kind": "var"
    }
  ],
  "sourceType": "script"
}
```

```
1 // Life, Universe, and Everything
2 var answer = 6 * 7;
3
```

No error

Syntax node location info (start, end):

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- ☐ Attach comments

Syntax

Tree

Tokens

Expand All

Collapse All

- ▼ Program body [1]
  - ▼ VariableDeclaration
    - ▼ declarations [1]
      - ▼ VariableDeclarator
        - ▼ id
          - ▼ Identifier
            - name: answer
        - ▼ init
          - ▼ BinaryExpression
            - operator: \*
            - ▼ left
              - ▼ Literal
                - value: 6
                - raw: 6
            - ▼ right
              - ▼ Literal
                - value: 7
                - raw: 7

kind: var

```

1 // Life, Universe, and Everything
2 var answer = 6 * 7;
3

```

No error

Syntax node location info (start, end):

- ☐ Index-based range
- ☐ Line and column-based
- ☐ Attach comments

Syntax

Tree

Tokens

```

[
  {
    "type": "Keyword",
    "value": "var"
  },
  {
    "type": "Identifier",
    "value": "answer"
  },
  {
    "type": "Punctuator",
    "value": "="
  },
  {
    "type": "Numeric",
    "value": "6"
  },
  {
    "type": "Punctuator",
    "value": "*"
  },
  {
    "type": "Numeric",
    "value": "7"
  },
  {
    "type": "Punctuator",
    "value": ";"
  }
]

```

# Key Takeaways

# Key Takeaways

- Your program is itself a piece of data
- Compilers first two main tasks are lexing and parsing
- Programming languages are defined by grammars
  - Backus-Naur Form (BNF)
- There are two primary ways to parse a given language into a grammar, top-down and bottom-up
- Top-down parsing can be done using recursive-descent if the grammar is LL(1) (Left to right, left recursive, 1 token lookahead)



# Workshop 1

- **Implement a recursive-descent parser for mathematical expressions**
  - Verify that your tree is correct
  - Output your tree
  - Convert your tree into Reverse Polish Notation