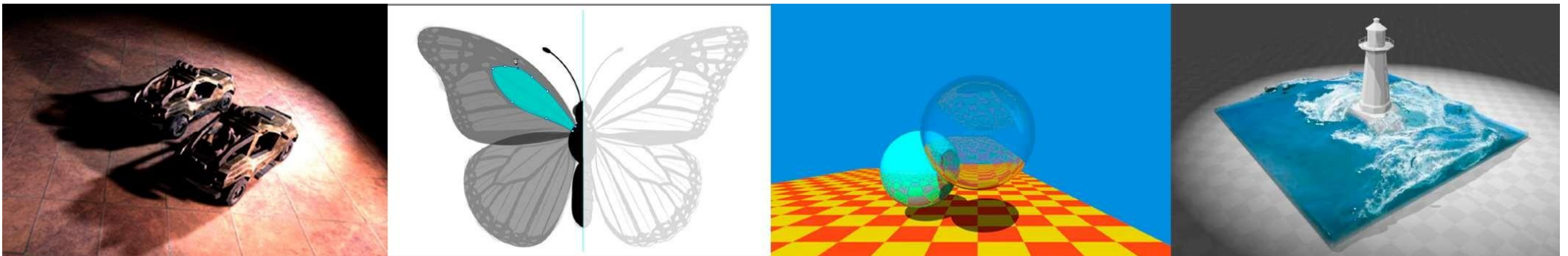


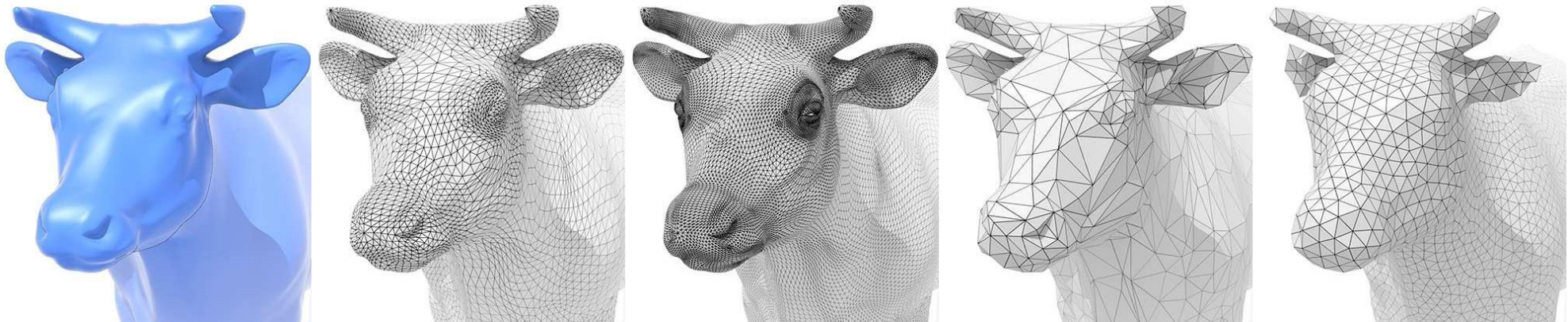
Computer Graphics

Geometry 3 (Mesh Processing)

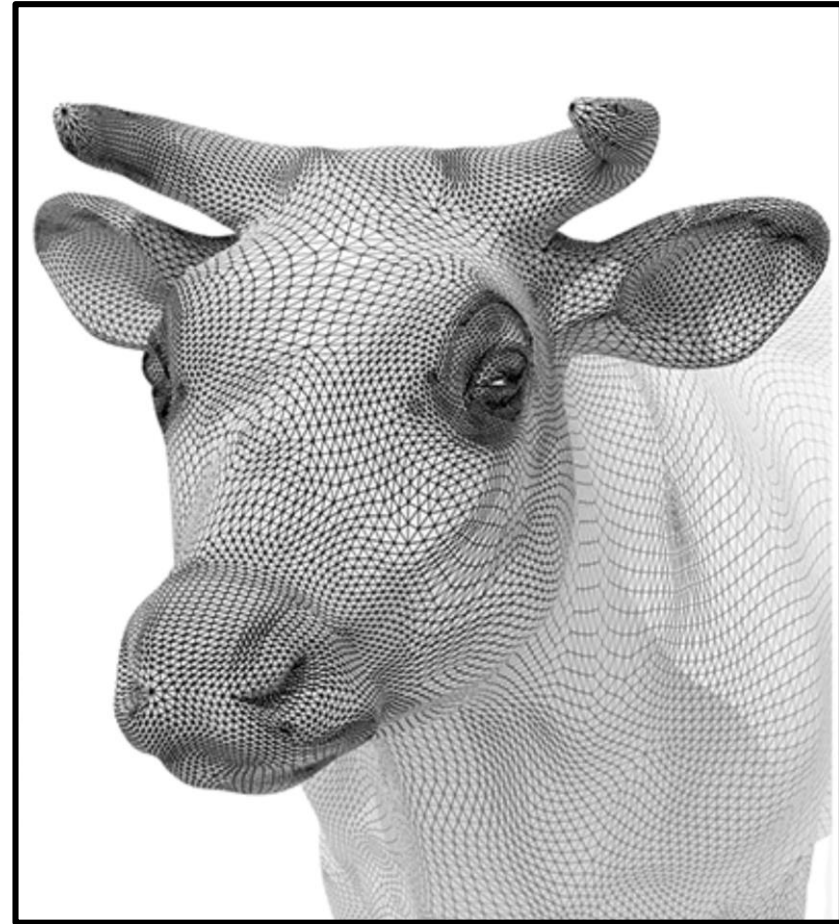
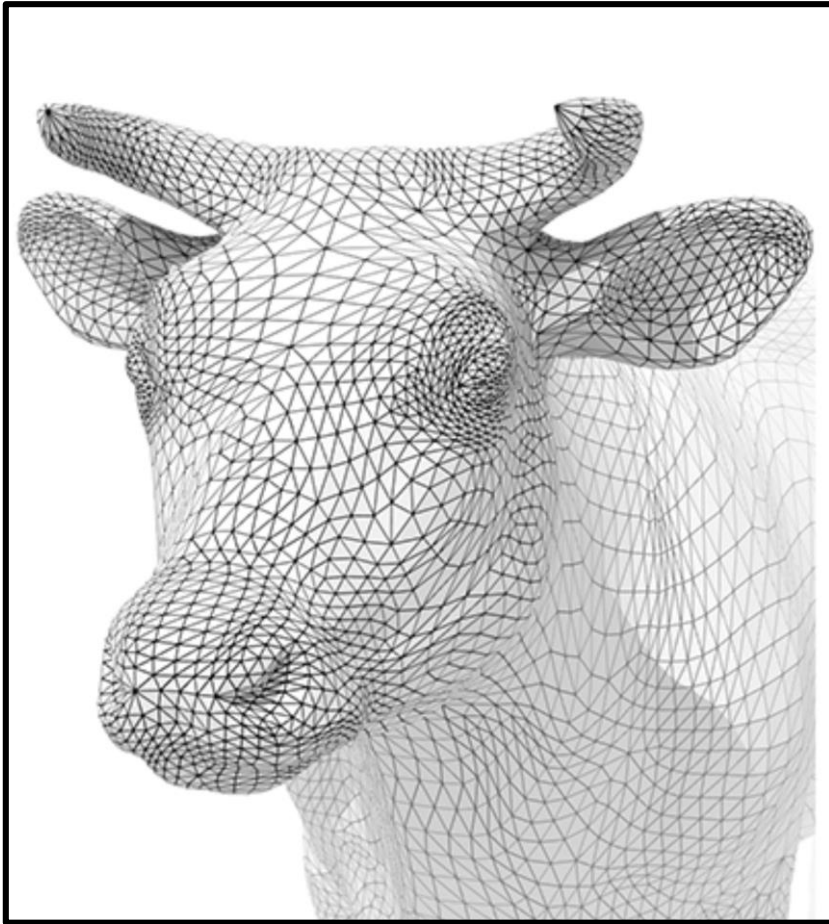


Mesh Operations: Geometry Processing

- Mesh subdivision (网格细分)
- Mesh simplification (网格简化)
- Mesh regularization (网格正则化)

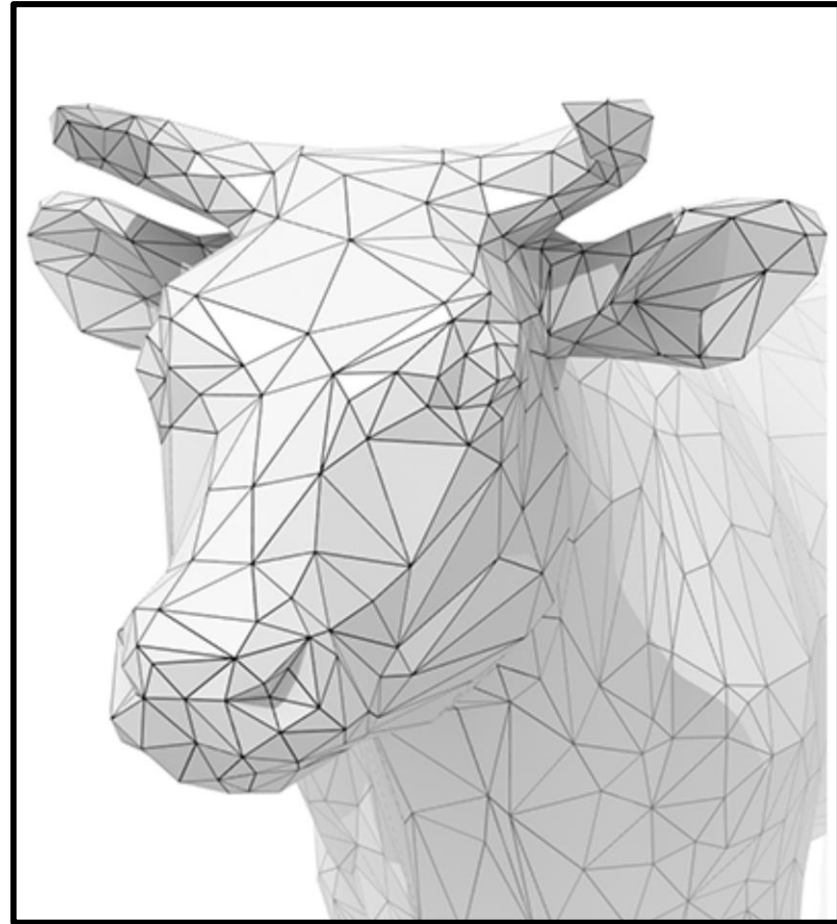
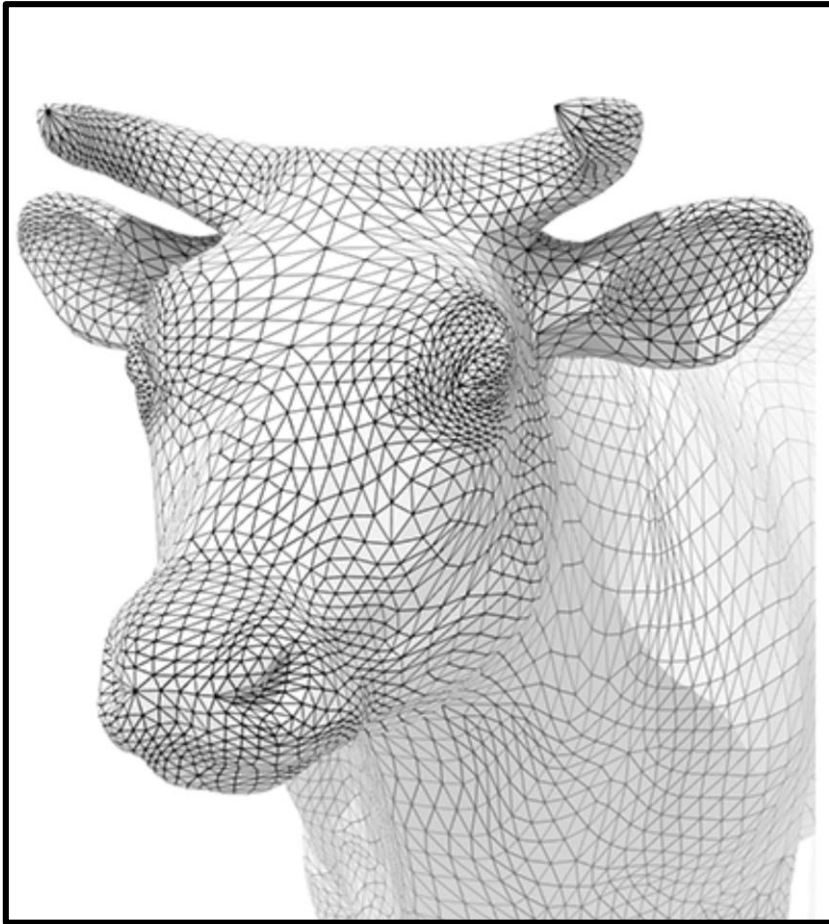


Mesh Subdivision (upsampling)



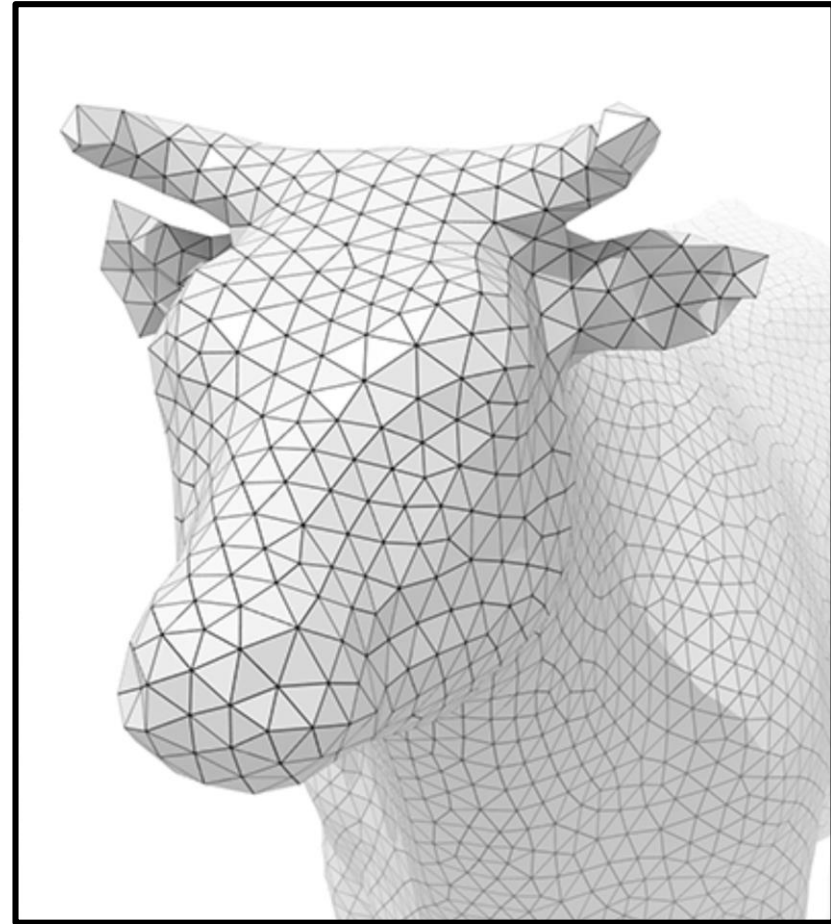
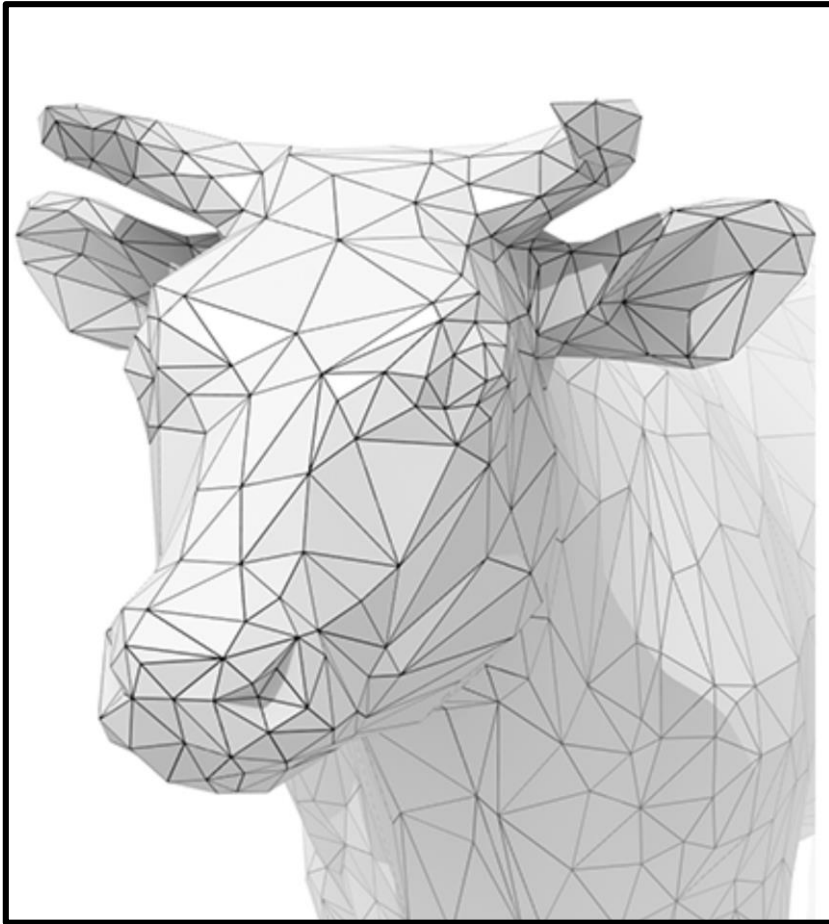
Increase resolution

Mesh Simplification (downsampling)



Decrease resolution; try to preserve shape/appearance

Mesh Regularization (same #triangles)



Modify sample distribution to improve quality

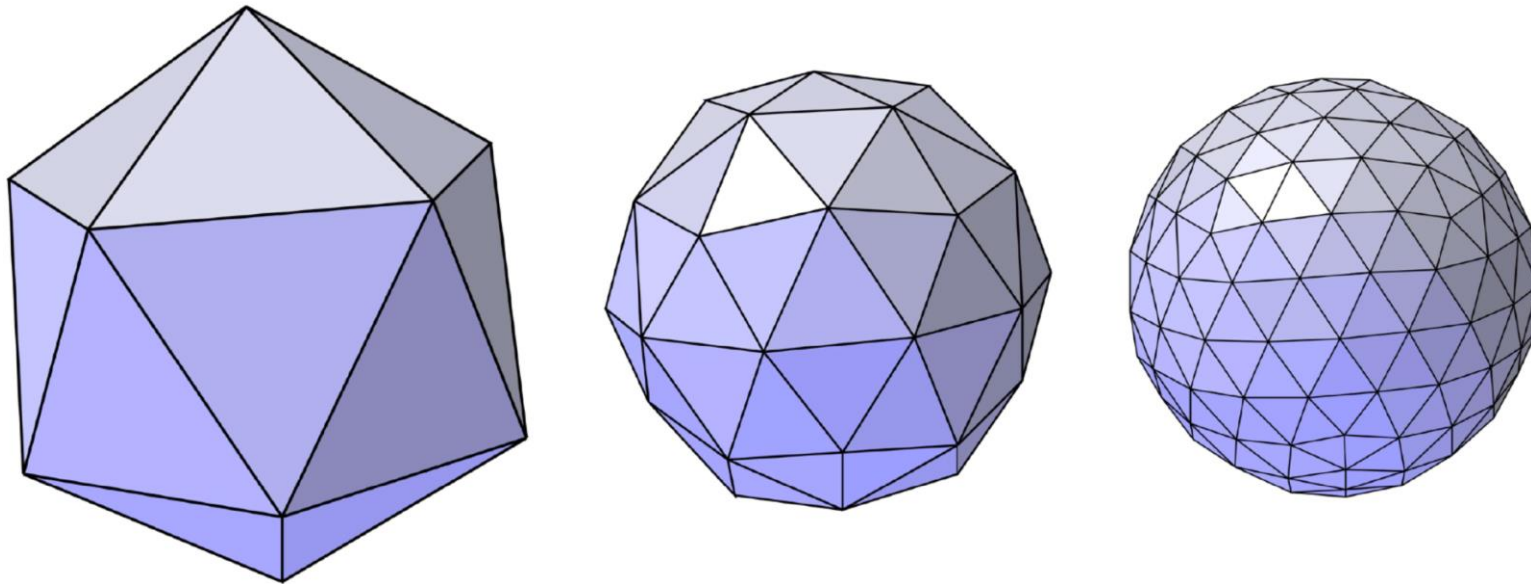
Subdivision

Loop Subdivision

Common subdivision rule **for triangle meshes**

First, create more triangles (vertices)

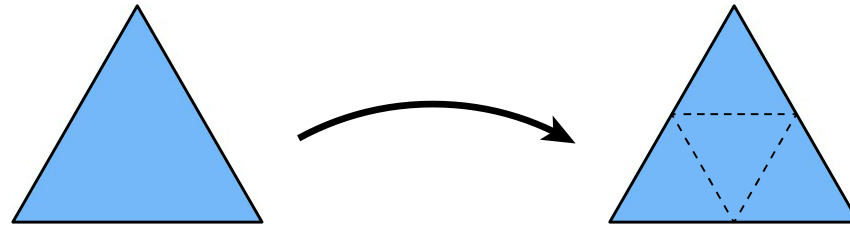
Second, tune their positions



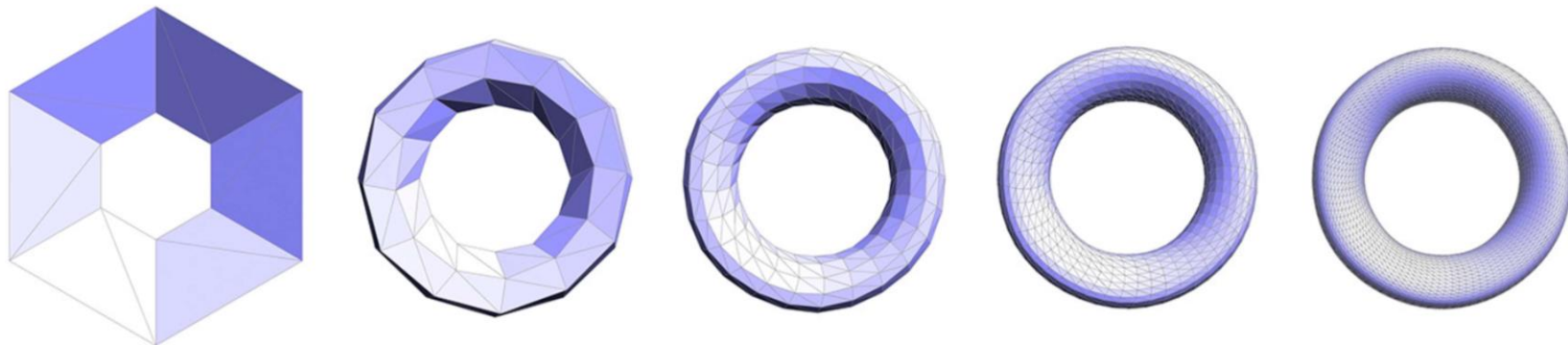
Simon Fuhrman

Loop Subdivision

- Split each triangle into four

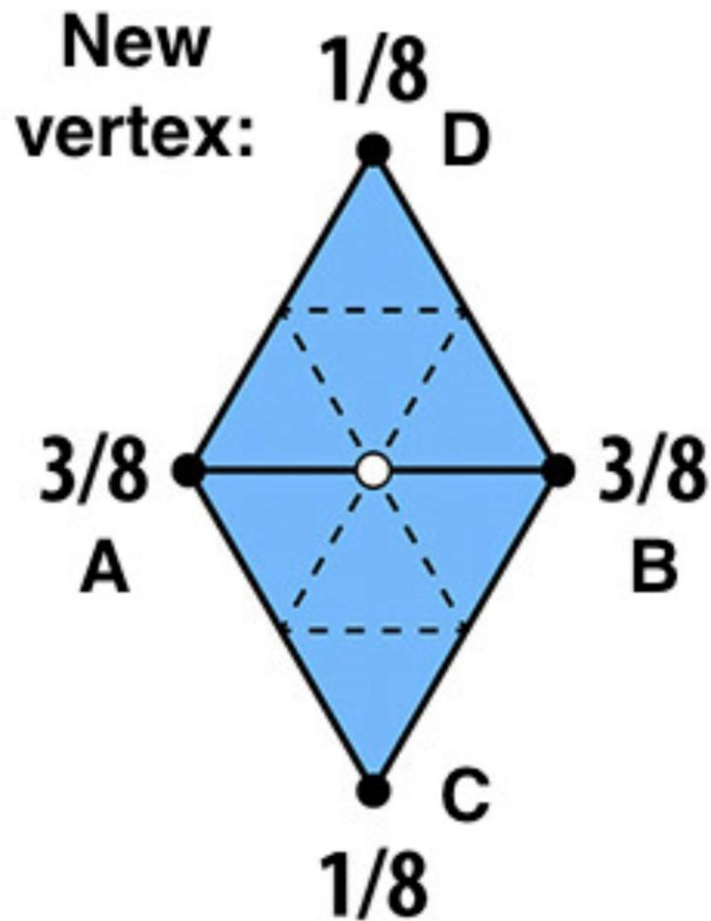


- Assign new vertex positions according to weights
 - New / old vertices updated differently



Loop Subdivision — Update

For new vertices:



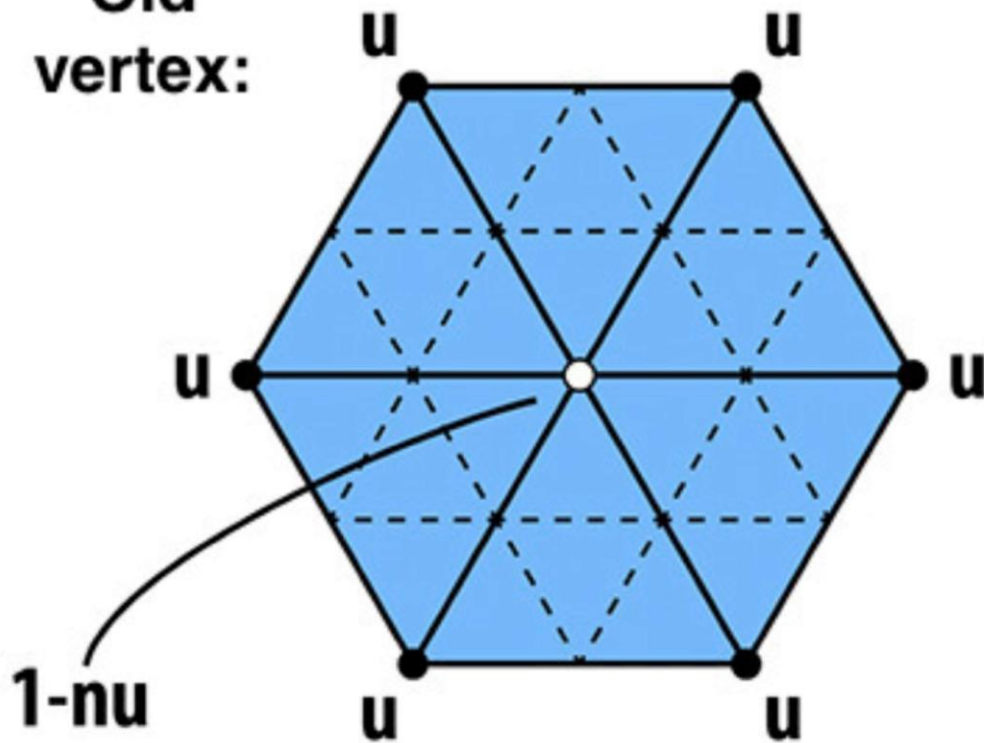
Update to:

$$\frac{3}{8} * (A + B) + \frac{1}{8} * (C + D)$$

Loop Subdivision — Update

For old vertices (e.g. degree 6 vertices here):

Old
vertex:



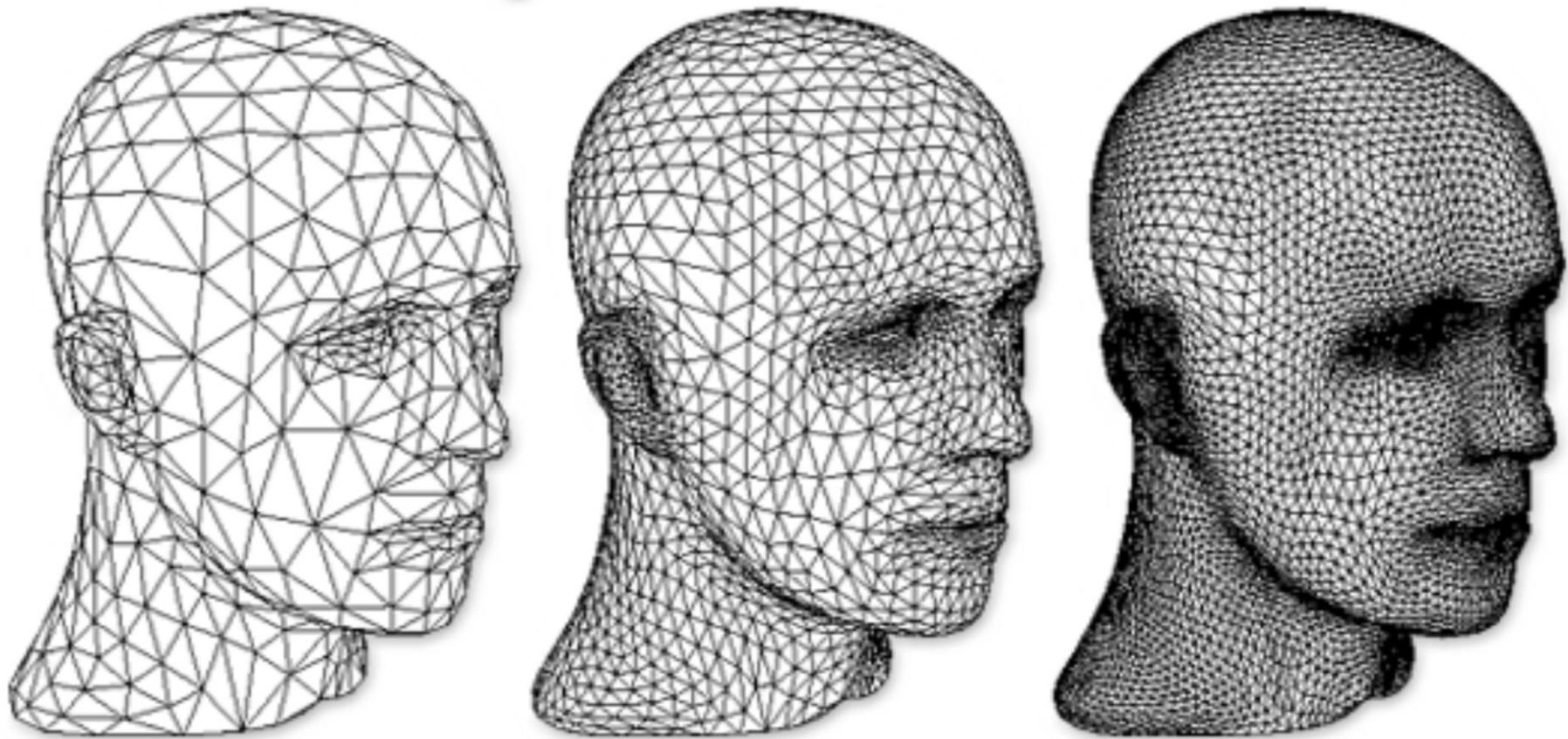
Update to:

$$(1 - n*u) * \text{original_position} + u * \text{neighbor_position_sum}$$

n : vertex degree

u : $3/16$ if $n=3$, $3/(8n)$ otherwise

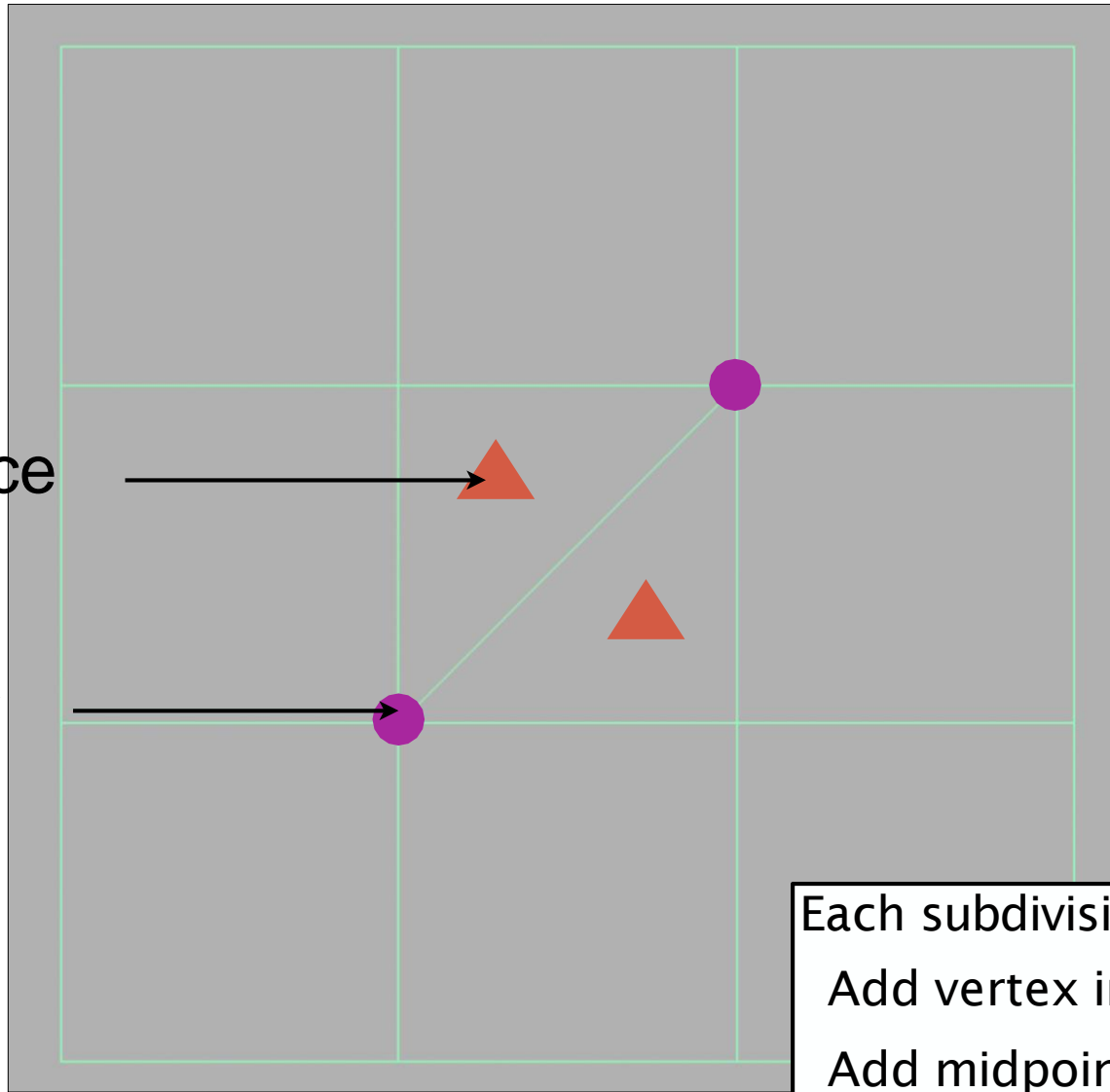
Loop Subdivision Results



Catmull-Clark Subdivision (General Mesh)

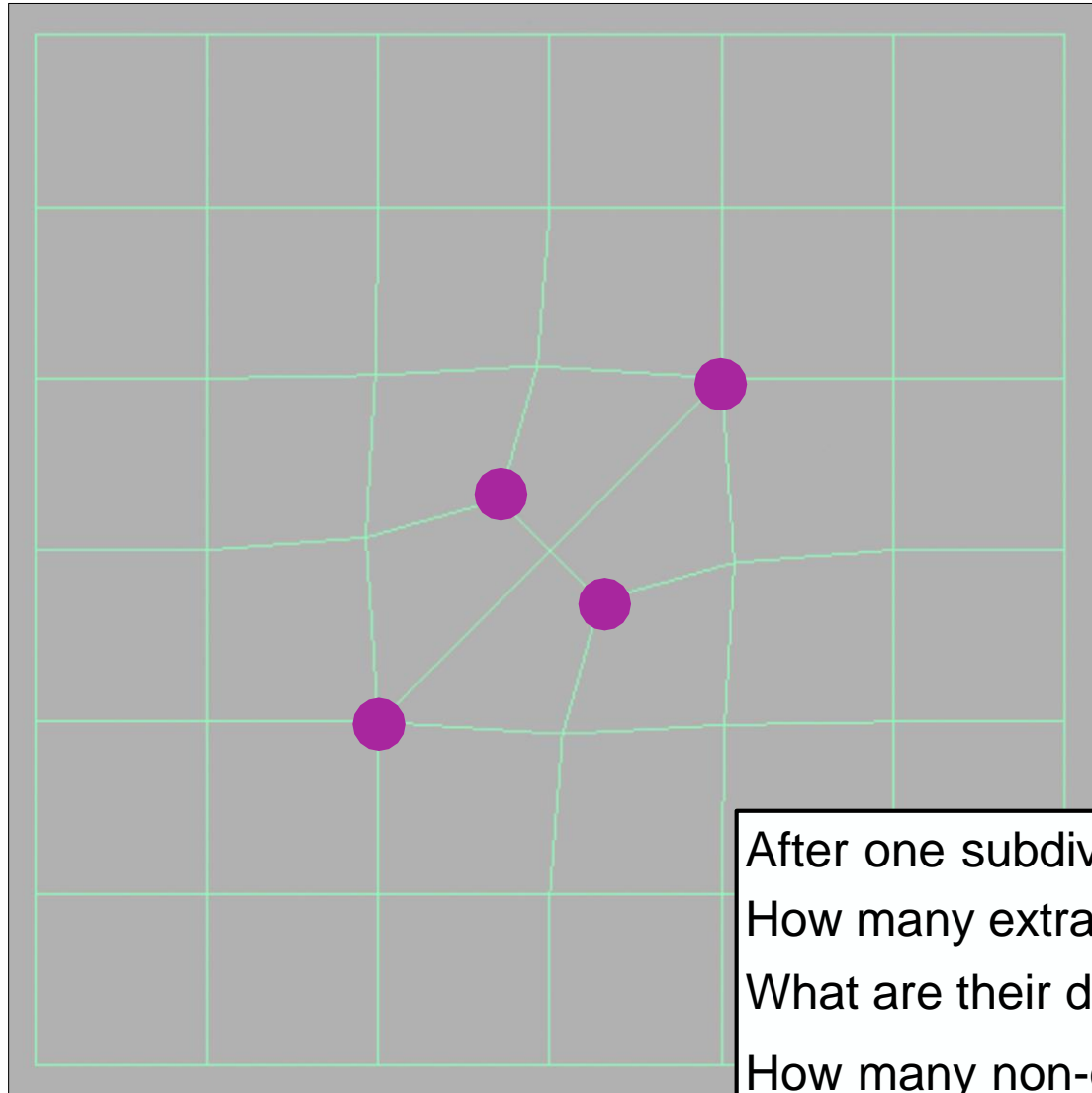
Non-quad face

Extraordinary
vertex (奇异点)
(degree $\neq 4$)



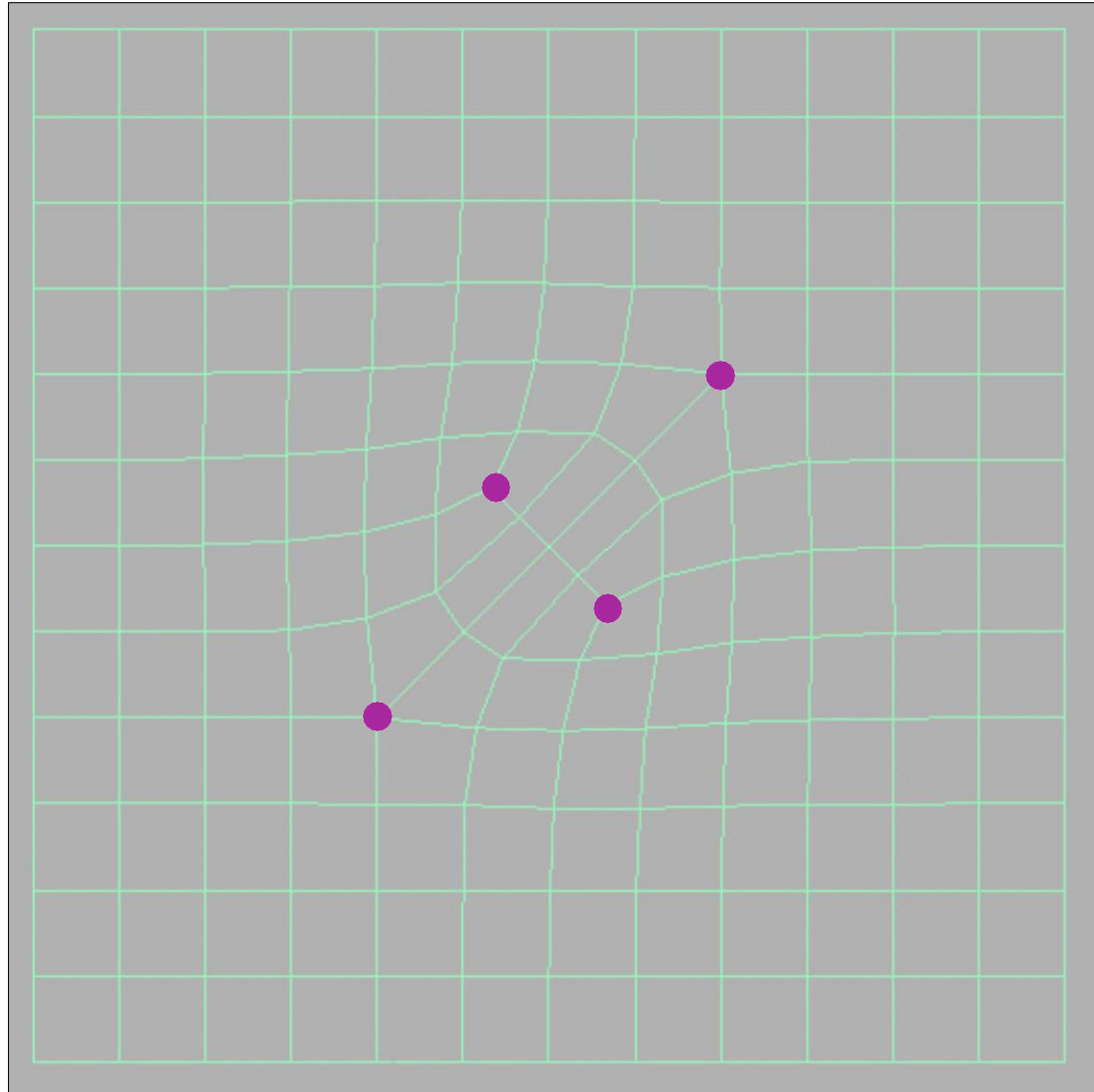
Each subdivision step:
Add vertex in each face
Add midpoint on each edge
Connect all new vertices

Catmull-Clark Subdivision (General Mesh)

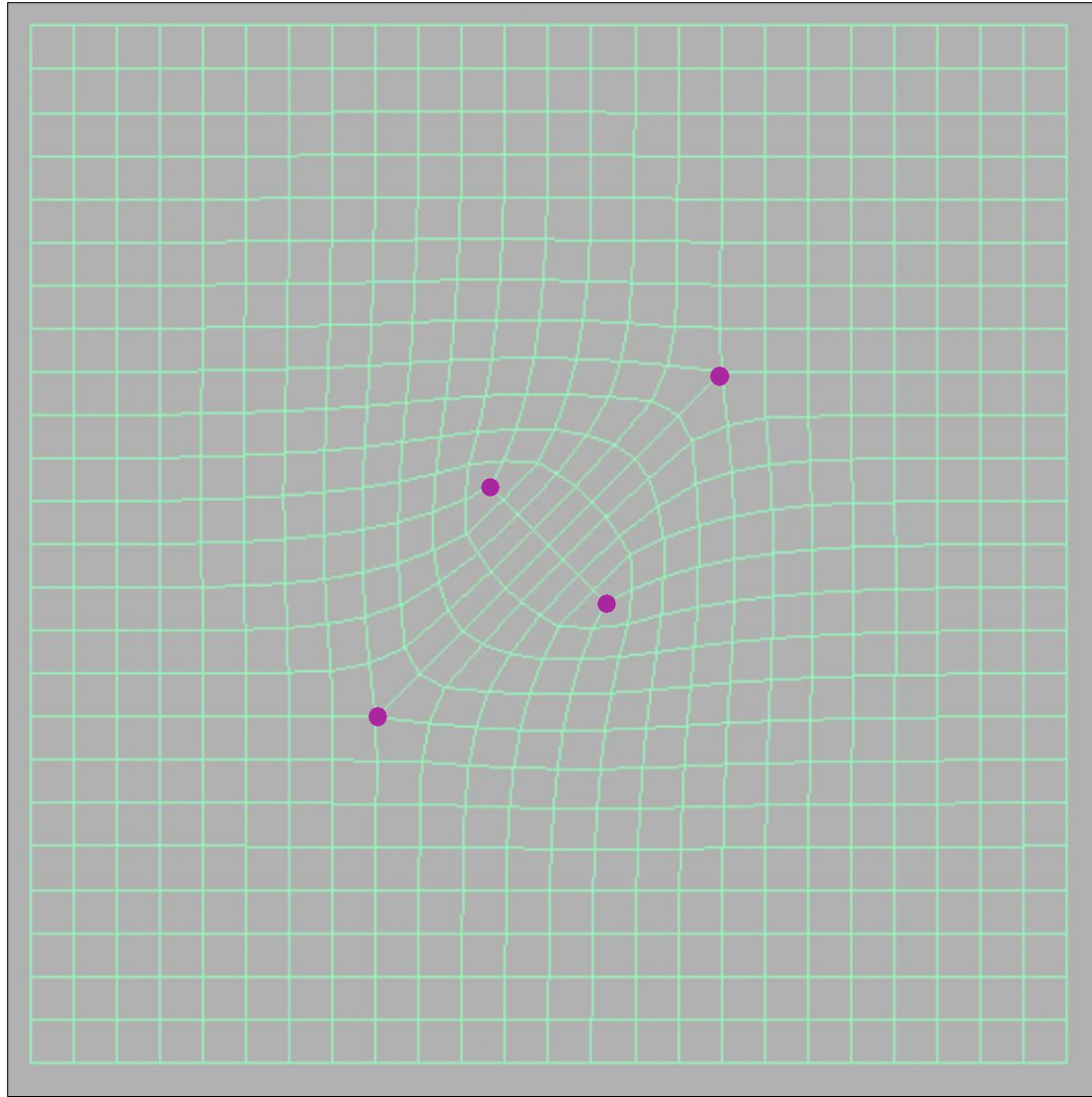


After one subdivision:
How many extraordinary vertices?
What are their degrees?
How many non-quad faces?

Catmull-Clark Subdivision (General Mesh)

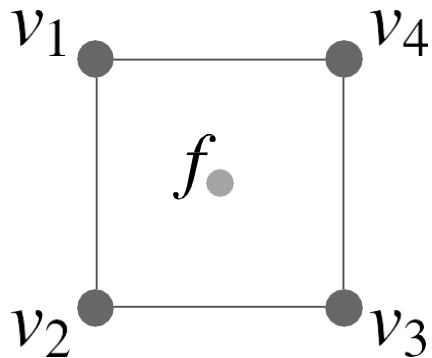


Catmull-Clark Subdivision (General Mesh)



FYI: Catmull-Clark Vertex Update Rules (Quad Mesh)

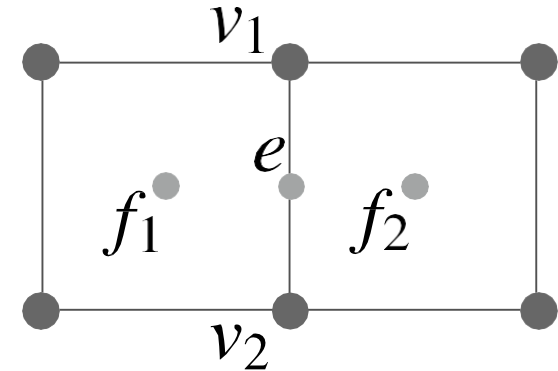
Face point



$$f = \frac{v_1 + v_2 + v_3 + v_4}{4}$$

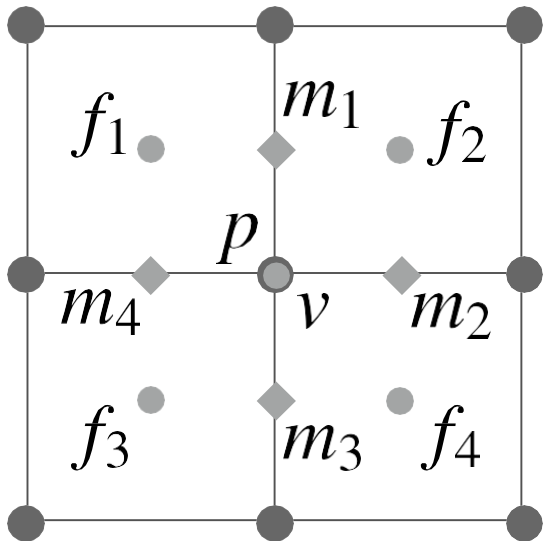
$$e = \frac{v_1 + v_2 + f_1 + f_2}{4}$$

Edge point



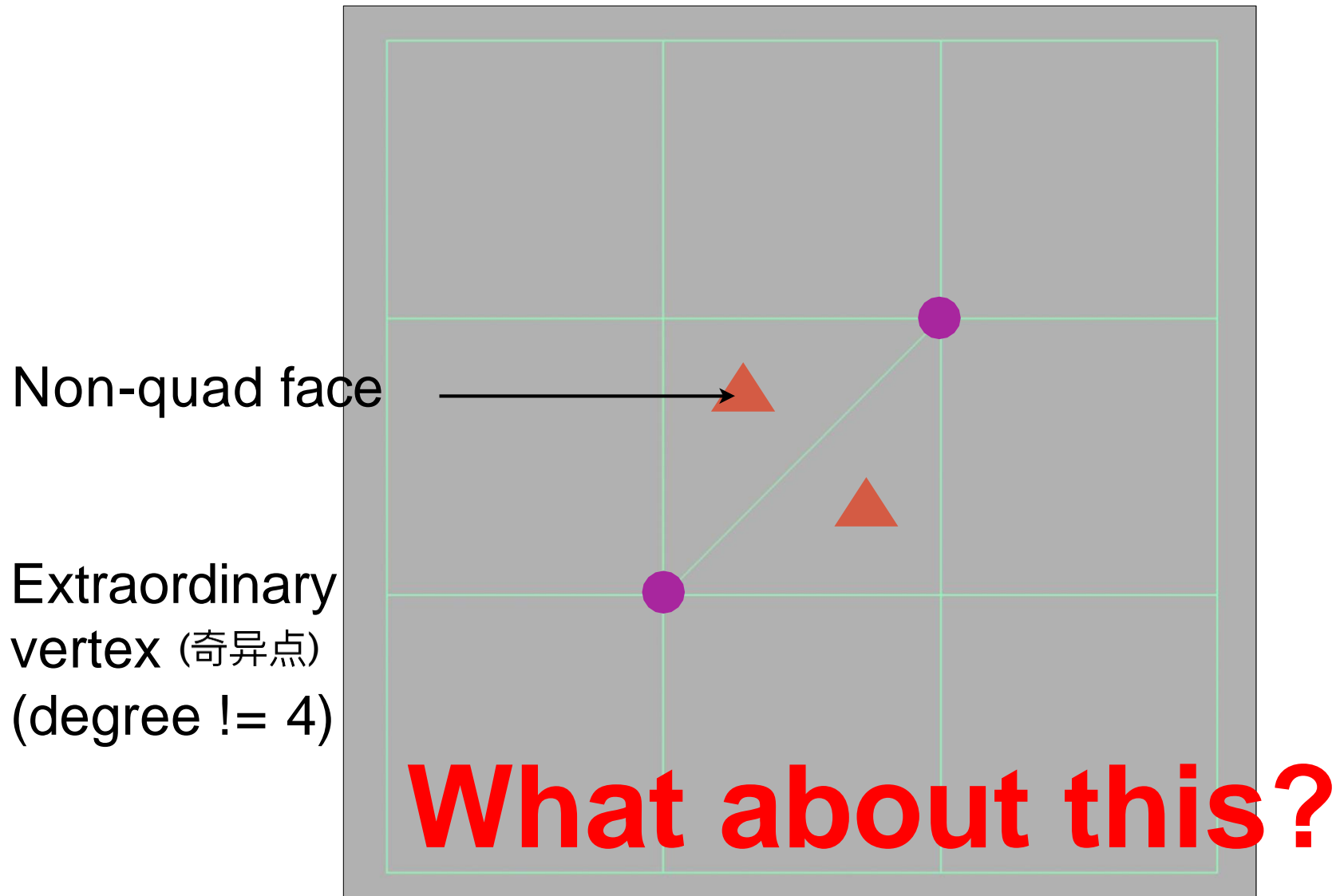
Vertex point

$$v = \frac{f_1 + f_2 + f_3 + f_4 + 2(m_1 + m_2 + m_3 + m_4) + 4p}{16}$$



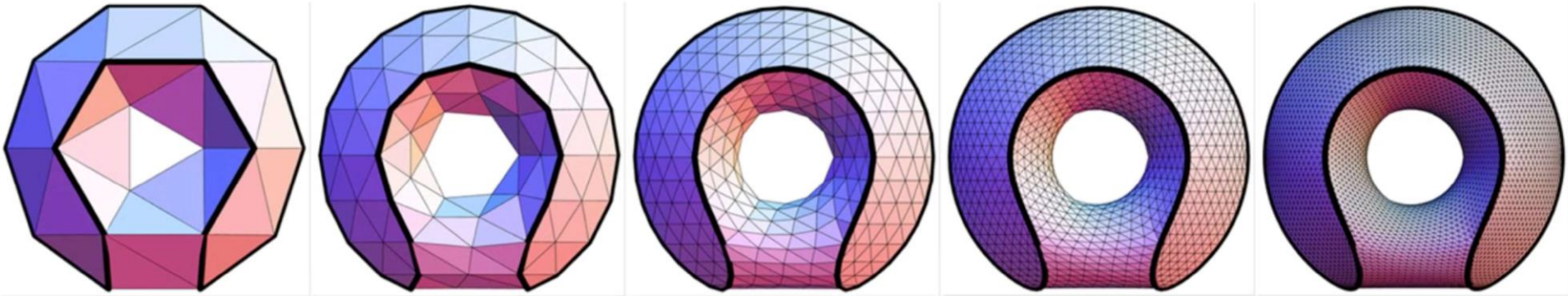
m midpoint of edge
 p old “vertex point”

FYI: Catmull-Clark Vertex Update Rules (Quad Mesh)



Convergence: Overall Shape and Creases

Loop with Sharp Creases



Catmull-Clark with Sharp Creases

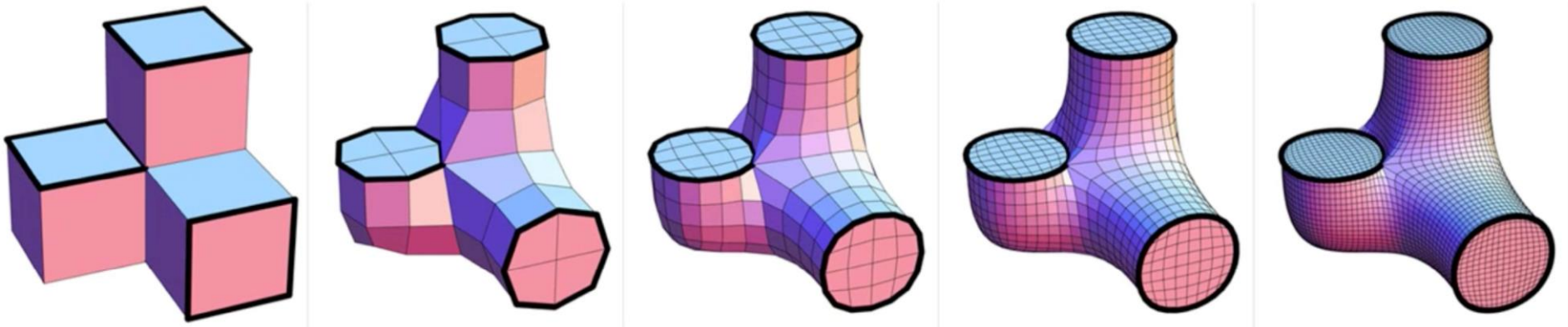
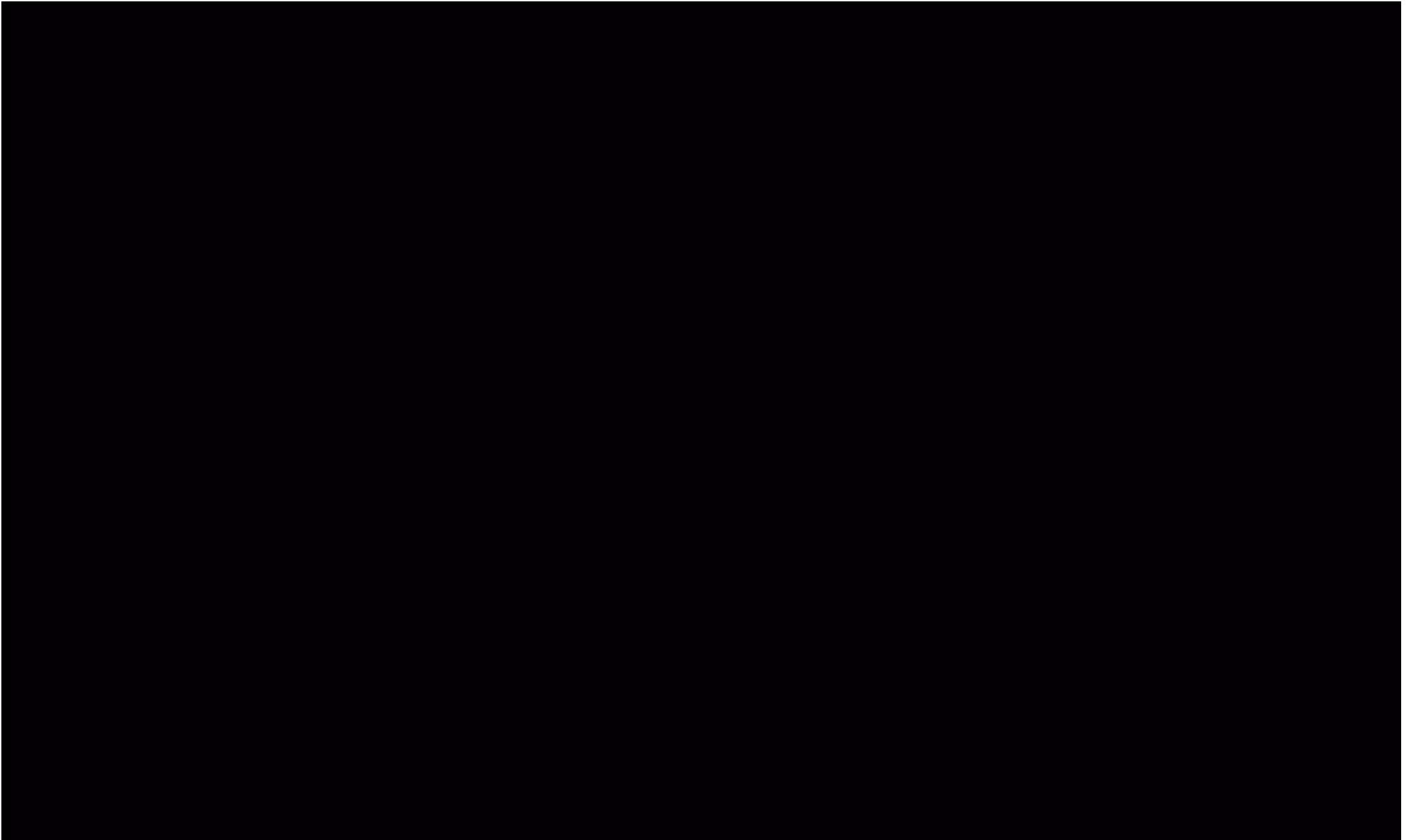


Figure from: Hakenberg et al. Volume Enclosed by Subdivision Surfaces with Sharp Creases

Subdivision in Action (Pixar's "Geri's Game")



Mesh Simplification

Mesh Simplification

Goal: reduce number of mesh elements while maintaining the overall shape



30,000 triangles



3,000



300



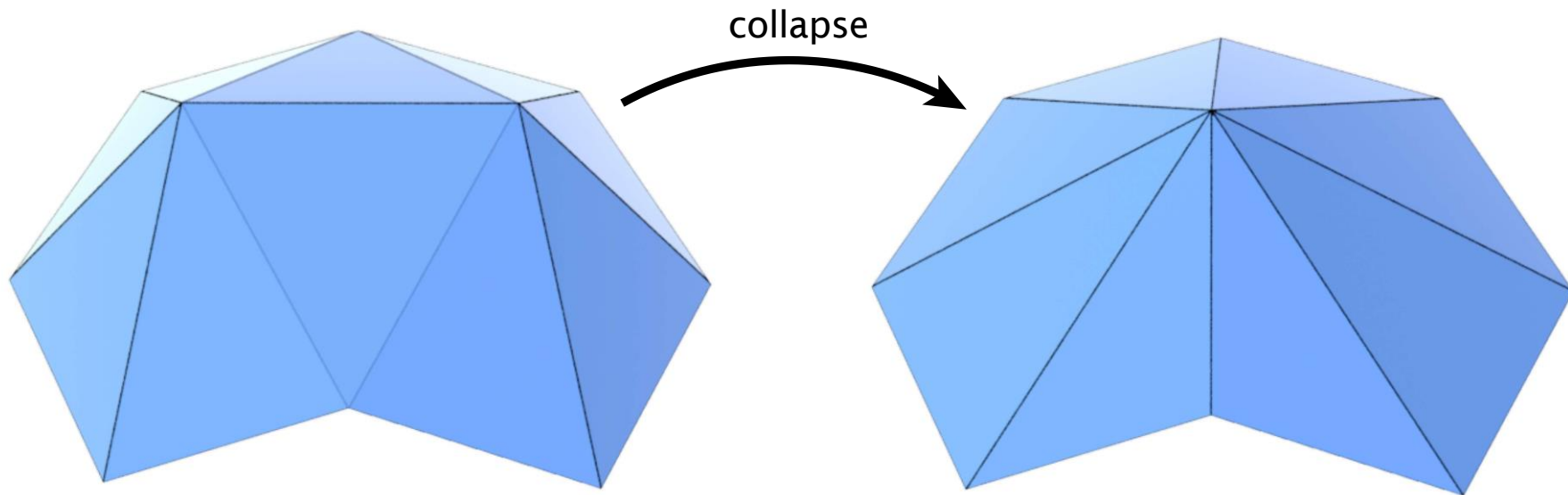
30



How to compute?

Collapsing An Edge

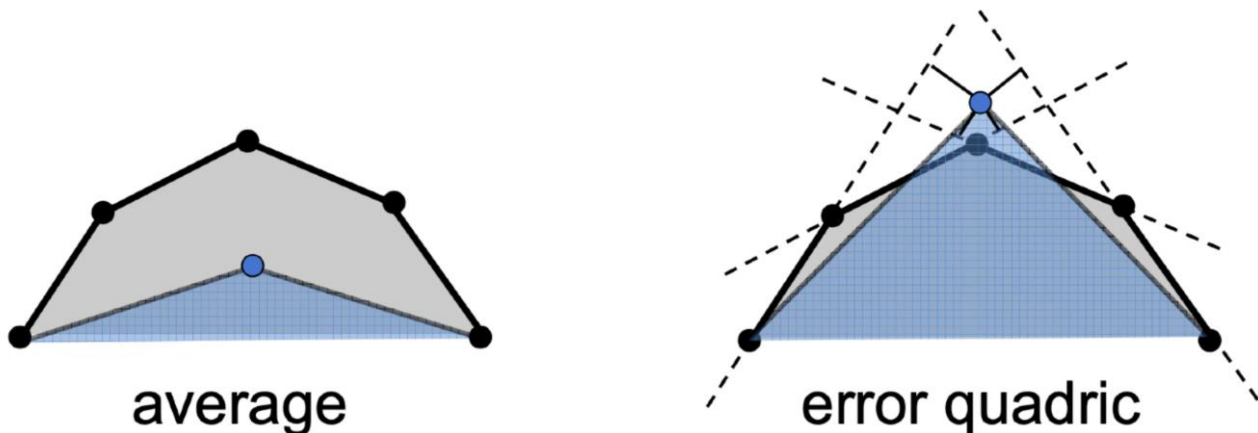
- Suppose we simplify a mesh using **edge collapsing**



Quadric Error Metrics

(二次误差度量)

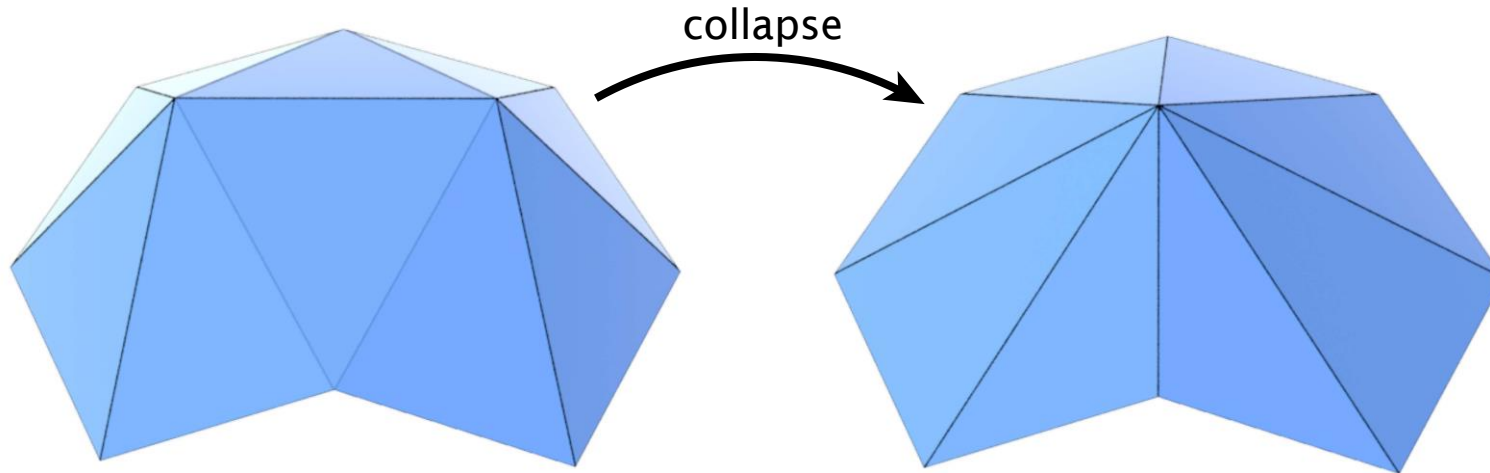
- How much geometric error is introduced by simplification?
- Not a good idea to perform local averaging of vertices
- Quadric error: new vertex should minimize its **sum of square distance** (L2 distance) to previously related triangle planes!



http://graphics.stanford.edu/courses/cs468-10-fall/LectureSlides/08_Simplification.pdf

Quadric Error of Edge Collapse

- How much does it cost to collapse an edge?
- Idea: compute edge midpoint, measure quadric error



- Better idea: choose point that minimizes quadric error
- More details: Garland & Heckbert 1997.

Simplification via Quadric Error

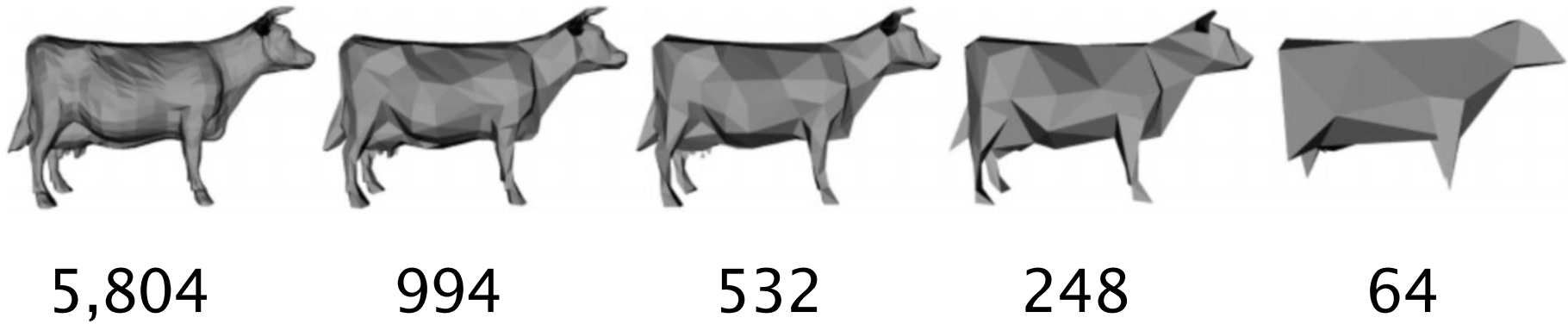
Iteratively collapse edges

Which edges? Assign score with quadric error metric*

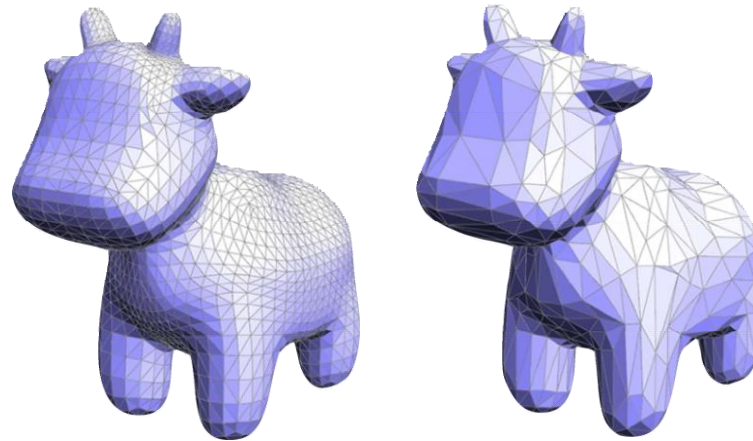
- approximate distance to surface as sum of distances to planes containing triangles
- iteratively collapse edge **with smallest score**
- greedy algorithm... great results!

* (Garland & Heckbert 1997)

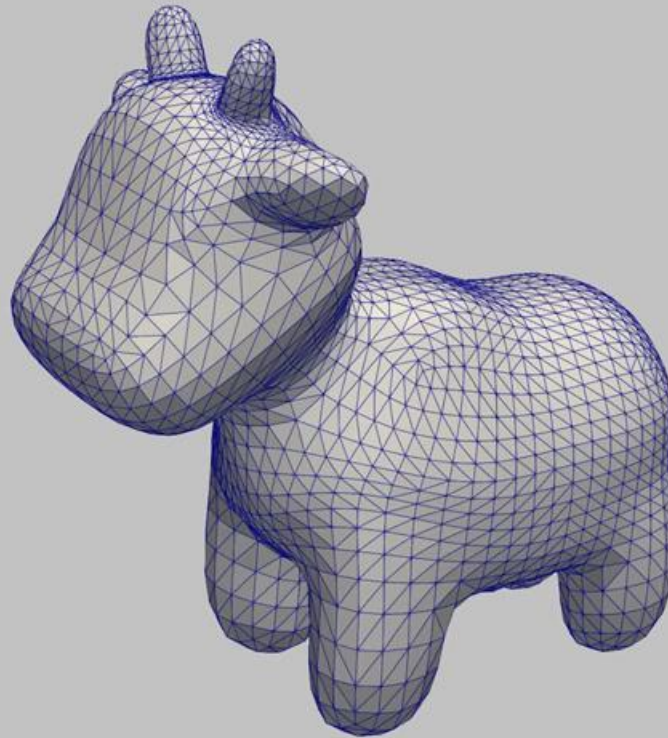
Quadric Error Mesh Simplification



Garland and Heckbert '97



Quadric Error Mesh Simplification



Thank you!