

Sinusoid to phasor

$$A \sin(\omega t + \theta) = A \cos(\omega t + 90 + \theta) = A \angle (\theta + 90)$$

$$B \cos(\omega t + \theta) = B \angle \theta$$

Phasor to sinusoid

$$(-r + j4)A \angle 126.87 = 5 \cos(\omega t + 126.87)$$

$$j8e^{-j20} = j8 \angle -20 = (1 \angle 90)(8 \angle -20) = 8 \angle 70$$

The $(1 \angle 90)$ is omdat vermenigvuldigen met j gewoon roteren met 90 is.

Differentieëren

$$\frac{dv}{dt} \rightarrow j\omega V$$

integreren

$$\int v dt = \frac{1}{j\omega} V = -\frac{1}{\omega} V$$

(delen door j is vermenigvuldigen met $-j$)

Rotatie van phasors met 90

$$A = r e^{j\theta} \rightarrow A_j = r e^{j(\theta + 90)}$$

Solving of diffEqs with phasors, example

$$\begin{aligned} 4I + 8 \int I dt - 3 \frac{dI}{dt} &= 50 \cos(2t + 75) \\ j\omega I &= 50 \angle 75 \quad \text{\textit{since t is 2, and dividing by j is multiplying with -j,}} \\ 4I - 4Ij - 6Ij &= 50 \angle 75 \\ I(4 - 10j) &= 50 \angle 75 \\ I &= \frac{50 \angle 75}{4 - 10j} = 4.64 \angle 143 \end{aligned}$$

Multiplying by j is phase shifting by 90 deg.

Phasor relationships

resistors

$$V = IR = R \operatorname{Im}(\cos(\omega t + \theta)) = R I_m \angle \theta$$

Inductors

Assume $I = \operatorname{Im}(\cos(\omega t + \theta))$ TOBECONTINUED