



# Simulation and characterization of integrated optics beam combiners for astrointerferometry

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#### Abstract

Astronomers always tried to see further and further in space with higher and higher resolution. The advances in technology have recently made possible the use of interferometry in order to reach high angular resolution for the purpose of astronomy. Indeed the resolution of an interferometer formed by two individual telescopes only depends of the ratio between the wavelength observed and the separation of these telescopes. Compared to the largest single telescopes (diameter of  $\approx 10 \mathrm{m}$ ) the resolution power of telescopes separated by a few hundreds meters are higher by more than an order of magnitude. This resolution is particularly increased for long wavelength making astrointerferometry a "hot" method to observe cold objects. Until recently the instruments combining the telescopes were made with bulks optics resulting to cumbersome and unstable instruments requiring lots of calibrations. The recent advances in Ultrafast Laser Inscription (ULI) have resulted in a new generation of instruments already delivering high quality results on sky.

The needs to combine as many telescopes as possible at the same times have resulted in different beam combiners geometry, the one studied in this report is the Zig-Zag array. To these needs I simulated and optimized this component and simulations have demonstrated high contrast capabilities and throughput greater than 90%. The simulated retrieved astronomical parameters have resulted to visibility accuracy at  $\pm 5\%$  and phase accuracy up to  $\pm 0.05 rad$  using a signal spectral bandwidth of 20nm centred at 3.4  $\mu m$  and combining 4 telescopes at the same time. More importantly experimental results have shown similar results when combining two beams at a time with a signal of spectral bandwidth 70nm. Limiting factors have been identified and must now be studied in order to reach unprecedented accuracy.

The results presented demonstrate that such discrete beam combiner (DBC) are well suited for interferometric combination of at least 4 telescopes to achieve high quality image reconstruction. Its design is well adaptable to all near to mid-infrared wavelengths.

## Résumé

Les astronomes ont toujours essayé de voir de plus en plus loin dans l'espace avec une résolution de plus en plus élevée. Les progrès de la technologie ont récemment rendu possible l'utilisation de l'interférométrie afin d'atteindre une résolution angulaire élevée pour l'astronomie. En effet, la résolution d'un interféromètre formé par deux télescopes individuels ne dépend que du rapport entre la longueur d'onde observée et la séparation de ces télescopes. Comparé aux plus grands télescopes monopupilles (diamètre de  $\approx 10$ m) le pouvoir de résolution de télescopes séparés par quelques centaines de mètres est supérieur de plus d'un ordre de grandeur. Cette résolution est particulièrement augmentée pour les grandes longueurs d'onde, ce qui fait de l'astro-interférométrie une méthode "hot" pour observer les objets froids. Jusqu'à récemment, les instruments combinant les télescopes étaient fabriqués avec de l'optique fibrée, ce qui donnait des instruments encombrants, nécessitant des étalonnages réguliers. Les progrès récents de l'inscription laser ultrarapide (ULI) ont donné naissance à une nouvelle génération d'instruments offrant déjà des résultats de haute qualité sur le ciel.

La nécessité de combiner autant de télescopes que possible en même temps a donné lieu à différentes géométries d'instruments, celle étudiée dans ce rapport est le "Zig-Zag array". Pour ce besoin, j'ai simulé et optimisé ce composant et les simulations ont démontré des capacités de contraste élevées et une transmission supérieure à 90%. Les simulations ont montré une précision sur la visibilité jusqu'à  $\pm 5\%$  et une précision sur la phase jusqu'à  $\pm 0.05 rad$  en utilisant un signal de bande spectrale 20nm et en combinant 4 télescopes en même temps. Plus important encore, les résultats expérimentaux ont montré des précisions similaires en combinant simultanément deux faisceaux avec un signal de largeur de bande spectrale 70 nm. Les facteurs limitants ont été identifiés et doivent maintenant être étudiés afin d'atteindre une précision sans précédent.

Les résultats présentés montrent que ces instruments sont bien adaptés à la combinaison interférométrique d'au moins 4 télescopes pour obtenir une reconstruction d'image de haute qualité. Sa conception est bien adaptable à toutes les longueurs d'onde de l'infrarouge proche à moyen.

#### Présentation du lieu du stage

Le stage s'est déroulé au premier institut de physique de l'université de Cologne. Ce laboratoire est composé de 6 groupes de recherche travaillant sur des thématiques propres à l'astronomie dont les principales sont :

- L'enseignement
- L'astronomie observationelle
- L'instrumentation
- La modelisation numérique

Le laboratoire acceuille 6 professeurs permanents et plus de 150 chercheurs, ingénieurs, doctorants étudiants et personnel administratif. J'ai été acceuilli dans le groupe de Lucas Labadie, Professeur à l'université de Cologne, j'ai travaillé sur la thématique de l'instrumentation astronomique dans le domaine infrarouge. Le travail que j'ai effectué se situe dans la continuité de celui du Dr. Jan Tepper avec qui j'ai beaucoup colaboré. J'ai également travaillé avec Dominik Strixner, étudiant effectuant sa thèse de master pour la carectérisation expérimentale des MMIs et coupleurs assymetriques. J'ai également colaboré avec un étudiant en thèse au laboratoire de physique de Postdam, qui travaille sur le même type de composants. Ce groupe collabore avec plusieurs laboratoires dont les laboratoires de Postdam, de Iena d'où provient le DBC caractérisé dans ce rapport et le laboratoire de Sydney d'où sont issus les échantillons les plus récents (MMIs, ABCD, Coupleurs...).

L'organisation hiérarchique est la suivante : les professeurs dirigent leurs groupes constitués de chercheurs, ingénieurs et doctorants. Ils travaillent sur différentes thématiques propres au groupe. Chaque groupe peut travailer sur plusieurs des 4 thématiques citées plus haut. Tout groupe fait de l'enseignement. L'organisation du travail est laissée à la libre convenance des chercheurs.

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#### Introduction

Since antiquity and down to our time, astronomers always tried to see further and further in space requiring more and more sensitive instruments. Increasing the telescope diameter is one way to reach higher angular resolution but in the same time make it more sensitive to atmospheric turbulence. Therefore even with the recent progress in adaptative optics, today's largest telescopes can only resolve few of the brightest and nearest stars.

Using individual telescopes to form an interferometer, the resolution is determined by the distance between the telescopes [Gli11]. Until recently the instruments combining the light from individual telescopes were based on costly and cumbersome bulk optics. The recent advances in manufacturing integrated-optics and especially in laser processing have resulted in new instruments that are operational on sky and delivering higher quality results.

The purpose of this work is to optimise and characterise the performance of Integrated optic (IO) beam combiners and especially one promising type of component called discrete beam combiner (DBC). Allowing to retrieve the astronomical parameters without scanning fringes these components could allow to observe fast varying objects. Moreover their structure without bending should provide high throughput thus higher quality measurements.

This report is organised in three parts. In the first part will be presented the motivations and the basis of astronomical interferometry. In the second part simulation results of the DBC as well as its optimisation will be discussed. In the last part the experimental characterisation of the DBC and its accuracy in retrieving the astronomical parameters will be demonstrated.

# 1 Fundamentals of astro-interferometry

All the development of astro-interferometry is essentially based on one fundamental theorem: the Van Cittert-Zernike theorem. This theorem links the spatial coherence of a far source to its angular brightness distribution. In this section will be explained the limitation of one individual telescope in term of resolution and then introduce the advantages of interferometry. This section is based on [Gli11] and lectures given by J.P. Berger at Grenoble-INP Phelma. In order to fully understand the concepts lets first introduce the Mutual coherence function.

#### 1.0.1 Mutual coherence function

Lets consider the light field by its optical disturbance function  $u(\vec{r},t)$  at position  $\vec{r}$  and time t. The optical disturbance is proportional to the electrical and magnetic fields of the light. Lets suppose a far, coherent source illuminating two thin holes situated at position  $\vec{r_1}$  and  $\vec{r_2}$  (like the young experiment) and forming fringe pattern on a screen. At a point P of the screen and time t, the intensity of the light can be expressed by :  $I(P) = \langle u(P,t)u^*(P,t)\rangle$  which can be rewritten if we consider the holes thin enough that the field is constant on their respective surface :

$$I(P) = \left\langle |u(\vec{r_1}, t - \tau_1)|^2 \right\rangle + \left\langle |u(\vec{r_2}, t - \tau_2)|^2 \right\rangle + 2\mathcal{R} \left( \left\langle |u(\vec{r_1}, t - \tau_1)u^*(\vec{r_2}, t - \tau_2)| \right\rangle \right)$$

where  $\tau_1$  and  $\tau_2$  refers to the travel time of the wave from the pin hole to the point P. The last term of this equation is a term of coherence representing the spatial and spectra properties of the source. From this equation we can generalise the measurement of the coherence of a source

by introducing the mutual coherence function (MCF):

$$\Gamma(\vec{r_1}, \vec{r_2}, \tau) = \langle u(\vec{r_1}, t + \tau) u^*(\vec{r_2}, t) \rangle = \lim_{T \to +\infty} \int_{-T}^{T} u(\vec{r_1}, t + \tau) u^*(\vec{r_2}, t) dt$$
 (1)

In the case of astrointerferometry the two pinholes refers to the telescopes and the source to the observed object. The distance between both telescopes is called the baseline vector  $\vec{B} = \vec{r_1} - \vec{r_2}$ .

#### 1.0.2 Van Cittert-Zernike theorem

Now that the MCF has been defined the most fundamental theorem of modern optic can be introduced. We will consider the Van Cittert-Zernike theorem in an adapted to astronomy form. We will consider a surface emitting light. Under the following assumption:

- The source is incoherent  $(\Gamma(P_1, P_2, \tau) = 0 \quad P_1 \neq P_2 \text{ for all } \tau)$
- The source is small compared to the distance of observation (Fresnel approximation)
- The source spectral bandwidth is much smaller than its average frequency (quasi-monochromatic approximation).

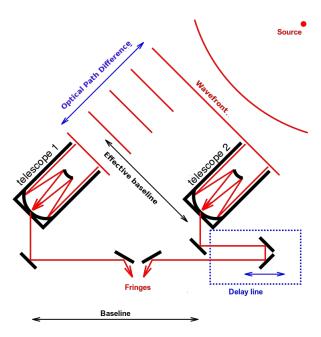


Figure 1: Scheme of the principle of stellar interferometry. (adaptated from https://fr.wikipedia.org/wiki/Interférométre\_optique\_a\_longue\_base)

Under those assumptions the Van Cittert-Zernike theorem states that :

$$\mu(\vec{B}) = \frac{\Gamma(\vec{B}, 0)}{\sqrt{\Gamma(\vec{r_1}, \vec{r_1}, 0)\Gamma(\vec{r_2}, \vec{r_2}, 0)}} = \frac{\int I_b(\vec{\alpha})e^{-ik\vec{B}\cdot\vec{\alpha}}}{d\vec{\alpha}}$$

where alpha is the angle between the line of sight and a point on the observed source and  $\mu$  the normalised MCF at  $\tau = 0$ , called the visibility function.  $I_b(\vec{\alpha})$  is the angular brightness distribution of the source. This is the force of this theorem, linking the angular brightness distribution of an object to the shape of its interferometric signal. The source can be seen as an infinity of points each interfering at the telescope recombination point. But due to their different position their interferogram are shifted relatively to each other reducing the global visibility. This is this effect that the Van Cittert-Zernike theorem means. Thus the amplitude of visibility  $|\mu|$  lay between 0 and 1.

This theorem explain the usability of interferometry to astronomical purpose but it doesn't explain it's main advantage: an increased angular resolution.

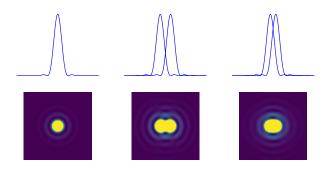


Figure 2: Left : Airy disk / PSF of a circular aperture. Center : Case of the Rayleigh criterion (resolved source). Right : case of an unresolved source

#### 1.0.3 Spatial resolution

Lets now take a simplified example of an individual telescope whose pupil is a disk of diameter D. Fourier's optics tells us that the point spread function (PSF) of such an aperture is a function called Airy's function (see Fig2).

In the case of 2 source observed, one can define the resolution of the telescope as its capacity to separate two punctual sources. This criterion is called the Rayleigh criterion and is defined as the angular separation such as the first "0" of the image of the first source is at the position of the maximum of the image of the second source. This correspond to an angular resolution of  $\Delta \alpha = \frac{1.22\lambda}{D}$ .

One can also define the telescope by its optical transfer function. Doing so it is easy to show that the circular aperture act as a low pass filter (spatial frequency) with a cut off frequency of  $f_c = \frac{D}{\lambda}$ 

When it comes to interferometry with two telescopes separated by a distance  $\vec{B}$  (speaking of the effective baseline) observing two stars of same flux separated by a distance  $\vec{\rho}$ , the visibility function is  $\mu(\vec{f}) = \cos(\pi \vec{f} \vec{\rho})$  where  $\vec{f}$  if the spatial frequency vector  $\vec{f} = \frac{\vec{B}}{\lambda}$  ( $\vec{B}$  and  $\vec{\rho}$  are vectors

defined in the observation plan). In the particular case where  $\vec{\rho} = \frac{\lambda}{2|\vec{B}|} \frac{\vec{B}}{|\vec{B}|}$  the visibility is equal to zero. Therefore we can deduce that the interferometer formed by two telescopes separated by a distance B is equivalent to an individual telescope of diameter B.

An interferometer formed by two telescopes separated by a distance B has a resolution of  $\frac{\lambda}{2B}$  and gives access to spatial frequency  $\frac{B}{\lambda}$ . To be able to fit models to measured visibility and to reconstruct an image of the observed object one must do measurements for as many baselines as possible (and also as many wavelength as possible). The purpose of the work presented in this report is to develop a component able to combine at least 4 telescopes (6 different baselines) at the same time making it able to observe fast varying object.

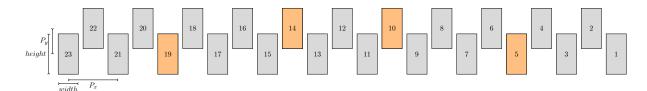


Figure 3: The Zig-Zag array cross section with the numbering convention. The four input waveguides are displayed in orange.

## 2 Simulation of the DBC

The discrete beam combiner is a component made of multiple straight single-mode waveguides close to each other. It has been demonstrated that in the case of a N telescope DBC, an array of more than  $N^2$  waveguides is needed for efficient operation of the DBC [Min12]. But at this point it hasn't been studied the impact of other geometrical parameters such as the spacing between each waveguides.

The component studied is formed of 23 outputs and four inputs to combine the light from four individual telescopes. A cross-section of it is shown on Fig. 3. Both the input configuration and the "Zig-Zag" shape have already been optimised. After a brief explanation of the theory behind the DBC we will focus on optimising it regarding  $P_x$ ,  $P_y$ , width, height and the length of the DBC part (the notations refers to Fig. 3) in the case of monochromatic light. In a second part the performances of the optimised component regarding the bandwidth of the input light are simulated. All simulation are performed using the commercial software Beamprop in scalar mode (a full-vectorial mode would have been more accurate but didn't show much different results for both TE and TM polarisation regarding the condition number of the Visibility to Pixel Matrix (V2PM) -see next section-), correlation mode and transparent boundary condition. The grid size was chosen as a balance between computation time and accuracy. The waveguides are simulated by a step-index core. All simulations doesn't include material dispersion as it is negligible compared to the effects of the geometry in the GLS.

## 2.1 Monochromatic light

In this section is shown the impact on the performances of the DBC regarding its geometry. Two main parameters are studied, the condition number of the V2PM and the throughput as it hasn't been done before.

#### 2.1.1 Mathematical formalism

As stated before the "Zig-Zag" DBC is composed of 23 outputs and can combine the light from 4 individual telescopes. This component has the particularity that all the information about the coherence function of the studied object is included in the way the 23 outputs are related to each other [TMC<sup>+</sup>07]. In the case of monochromatic light the theory is exact. We will do

a brief overview of the theoretical background in this part. For further reading the reader can refer to [TMC<sup>+</sup>07, SMD<sup>+</sup>13, DTL<sup>+</sup>17].

In this part we will consider the light combined from the input A and B at the  $n^{th}$  output. In that case the intensity  $I_n$  at the output can be expressed as:

$$I_n = \kappa_A I_A + \kappa_B I_B + 2\sqrt{\kappa_A I_A \kappa_B I_B} V_{AB}^{inst} V_{AB}^{obj} \cos(\phi_{AB}^{inst} + \phi_{AB}^{obj})$$
 (2)

In this equation  $\kappa_i$  is the transmission coefficient from the input i to the considered output. inst and obj relates to the visibility/phase of the instrument and of the observed object. Equation 2 can easily be reduced to Eq.3 in which the produce of the instrumental and object visibility are reduced in  $V_{AB}$ .

$$I_n = \kappa_A I_A + \kappa_B I_B + 2\sqrt{\kappa_A I_A \kappa_B I_B} V_{AB} \left( \cos(\phi_{AB}^{inst}) \cos(\phi_{AB}^{obj}) - \sin(\phi_{AB}^{inst}) \sin(\phi_{AB}^{obj}) \right)$$
(3)

From Eq.3 the problem of getting the object mutual coherence function can be reduced to the produce of a matrix and a vector. Thus the characteristics of the input fields can be linked to the output intensities by the relation:

$$\vec{I} = V2PM \times \vec{V} \tag{4}$$

In which  $\vec{I} = (I_1, ... I_M)^T$  represent the intensities at the M outputs,  $\vec{V} = (I_1, ..., I_M, V_{12}^{obj}, V_{12}^{ob$ 

$$\begin{pmatrix} \kappa_{11} & \kappa_{21} & \kappa_{31} & 2V_{12}^1 \sqrt{\kappa_{11}\kappa_{21}} cos(\Phi_{12}^{in2t}) & -2V_{12}^1 \sqrt{\kappa_{11}\kappa_{21}} sin(\Phi_{12}^{in2t}) & 2V_{13}^1 \sqrt{\kappa_{11}\kappa_{31}} cos(\Phi_{13}^{in3t}) & -2V_{13}^1 \sqrt{\kappa_{11}\kappa_{31}} sin(\Phi_{13}^{in3t}) & 2V_{23}^1 \sqrt{\kappa_{21}\kappa_{31}} cos(\Phi_{23}^{in3t}) & -2V_{23}^1 \sqrt{\kappa_{21}\kappa_{31}} sin(\Phi_{33}^{in3t}) \\ \kappa_{12} & \kappa_{22} & \kappa_{32} & 2V_{12}^2 \sqrt{\kappa_{12}\kappa_{22}} cos(\Phi_{12}^{in2t}) & -2V_{12}^2 \sqrt{\kappa_{12}\kappa_{22}} sin(\Phi_{12}^{in3t}) & 2V_{13}^2 \sqrt{\kappa_{12}\kappa_{32}} cos(\Phi_{13}^{in3t}) & 2V_{23}^2 \sqrt{\kappa_{12}\kappa_{32}} sin(\Phi_{33}^{in3t}) & -2V_{23}^2 \sqrt{\kappa_{22}\kappa_{32}} cos(\Phi_{23}^{in3t}) & -2V_{23}^2 \sqrt{\kappa_{22}\kappa_{32}} sin(\Phi_{33}^{in3t}) \end{pmatrix}$$

Figure 4: An hypothetical V2PM matrix for a 3 to 2 beam combiner. All visibilities and phases in the matrix are the instrumental ones.

One can find the Pixel to Visibility Matrix (P2VM) by inverting the V2PM matrix with the relation 6 and then the astronomical information from  $\vec{V}$ . To be consistent with the notations introduced in [SMD<sup>+</sup>13],  $\vec{V} = (\Gamma_{11}, ..., \Gamma_{MM}, \mathcal{R}\Gamma_{12}, \mathcal{I}\Gamma_{12}, ..., \mathcal{R}\Gamma_{N(N-1)}, \mathcal{I}\Gamma_{N(N-1)})$  the object phase and visibility can be extracted by :

$$V_{ij}^{obj} = \sqrt{\frac{(\mathcal{R}\Gamma_{ij})^2 + (\mathcal{I}\Gamma_{ij})^2}{\Gamma_{ii}\Gamma_{jj}}} \qquad \Phi_{ij}^{obj} = \arctan(\frac{\mathcal{I}\Gamma_{ij}}{\mathcal{R}\Gamma_{ij}}) \quad i \neq j$$
 (5)

$$P2VM = (V2PM^T \times V2PM)^{-1} \times V2PM^T \tag{6}$$

In the light of this formalism the retrieved coherence function from the P2VM can be inaccurate and one has to minimize the condition number of the matrix in order to minimize the possibility

of a strong amplification of measure inaccuracy. For further explanation on this subject refers to Appendix A.1.

To characterise the instrumental phase and visibility at an output a coherent source is used (thus the object's visibility is 1 and the phase visibility is 0). A cosine is fitted to the simulated curve of the intensity at an output. Then the photo-correction from Eq.?? is applied using the intensity simulated with one of the 4 beams at input. This process is repeated for all 6 baselines to build all the V2PM.

$$V_n(x) = \frac{I_n(x) - \kappa_A I_A - \kappa_B I_B}{2\sqrt{\kappa_A I_A \kappa_B I_B}} = V_{AB}^{inst} V_{AB}^{obj} \cos(\phi_{AB}^{inst} + \phi_{AB}^{obj})$$
 (7)

#### 2.1.2 Impact of evanescent coupling on the output power

The main principle behind the the DBC being the coupling of electromagnetic fields, it is important to understand how much the area chosen to calculate the power at an output could affect the phases relations and visibilities. This part focuses on this problem.

Considering only 3 distinct wave-guides of the DBC Zig-Zag component. The cross section of each WG is a rectangle  $width \times height$ . In such a dielectric wave-guide, there is no analytical solution to the scalar wave equation but according to [Lab08] a good approximation of the transverse field profile is close to a gaussian:

$$\Psi(x,y) \approx \Psi_0 exp\left(\frac{-x^2}{\omega_x^2} + \frac{-y^2}{\omega_y^2}\right)$$

Using this equation and retrieving  $\omega_x$  and  $\omega_y$  from BeamProp simulation by the width of the gaussian at 1/e of its maximal amplitude, we can «calculate» the transverse field profile in the wave-guide.

We simulate this behaviour for the following parameters (in µm):

- Px = 24
- Py = 10.8
- width = 9.5
- height = 17
- $n_{clad} = 2.31$
- $-\delta n = 0.005$

In this case we have  $\omega_x \approx 7.798$  and  $\omega_y \approx 10.114$  at lambda=3.4  $\mu m$  (from beam prop simulations). The resulting electric field for 3 outputs in phase and guiding the same power is shown in Fig. 5.

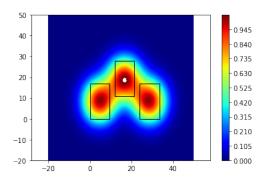


Figure 5: Example of 3 outputs in phase guiding the same power. The modes are Gaussian perfectly centred on the wave-guide

One can see that in this case, where the 3 outputs are in phase, the determination of the power in the middle WG will be badly estimated by a simple power integral as:

$$P \propto \iint_{\mathbb{R}^2} \Psi^*(x, y) \Psi_{sim}(x, y) dx dy \tag{8}$$

where  $\Psi_{sim}$  is the simulated output fields as shown on the upper figure. Actually the exact knowledge of the power guided through one individual output is not needed. But if the outputs are not in phase, estimating the "power" by the previous integral would lead to harmonic in the signal vs the optical path difference (OPD) due to the influence of the neighbouring wave-guides. Therefore the integration should be limited to a small area around the WG. In the next paragraph we verify the impact of this choice on the phases relations and instrumental visibilities thus the V2PM.

**Power of a Gaussian field:** For an isolated gaussian field the power P is given by

$$\frac{P}{\Psi_0^2} \propto \iint_{\mathbb{R}^2} exp\left(\frac{-2x^2}{\omega_x^2} + \frac{-2y^2}{\omega_y^2}\right) dx dy = \frac{\pi}{2}\omega_x \omega_y$$

In the case of our parameters the right hand is equal to 123.88  $\mu m^2$  (a numerical integration using the composite trapezoidal rule lead to 123.76  $\mu m^2$ ). By integrating the whole field as represented in Fig. 5 over the cross-section we obtain 113.70  $\mu m^2$  but the truly guided power in the central wave-guide calculated over the cross-section should only be 87.39  $\mu m^2$  thus an error of 30 %.

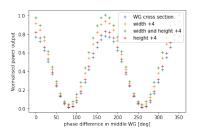
In the opposite case where there is no power in the central wave-guide, and a maximal power in the two surrounding wave-guides we find a guided power in the central wave-guide over the cross-section of  $3.10 \,\mu\text{m}^2$ . It can easily be understood that the simulated (ergo the experimental) interferograms will depend of the considered area (if the outputs signal aren't in phase). The larger this area, the greater the impact of the surrounding wave-guides on the interferogram. In an other hand the smaller this area, the smaller the signal to noise ratio.

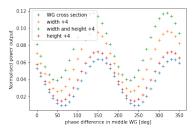
Influence on the simulated phases relations: We have seen that the integrating area used to estimate the guided power should have a great impact on the result, we now try to see

its impact on the simulated phase relations. To do this the 3 gaussian are multiplied by a cosine to simulate a phase dependency. The left and right outputs are set with phases pi/3 and 2pi/3 respectively and the middle one with phase 0. The power is then integrated on different area centred on the waveguide (WG) cross-section.

One can see that in this case, the phase of the output signal is mostly unchanged by the integrating area, but this is only the case for area slightly larger to the WG's cross section. Therefore it might be expected that the phase relation between outputs with comparable power magnitude will stay the same for low variation of the integrating area. The only changed parameter might be the Visibilities.

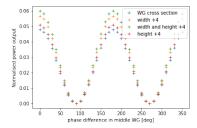
To this point we have only seen the impact of the integrating area when all outputs are guiding the same maximal power. It is now studied the impact on a low guided power in the middle WG comparatively to the left and right ones. Same phases are introduced. The power in the left and right WG are the same and 4 times the power in the middle WG. The results to those simulations are shown in Fig. 6





(a) Simulation with the same power in the middle and the surroundings WG.

(b) Simulation with low power in the middle WG and high in the surroundings.



(c) Simulation with low power in the middle WG and high in the surroundings for a higher x spacing between the WG.

Figure 6: Influence of different parameters on the phases and amplitudes of the interferogram in the middle wave-guide. The phases relations between the outputs are highly influenced by the evanescent coupling

As can be seen, the more the power difference between the middle WG and the sides WG and the larger the integrating area, the more impacted the retrieved phase differences. Therefore it seems that the V2PM matrix of the component should be calculated not only for the isolated component but also with the imaging system. One way to get rid of these dependency would

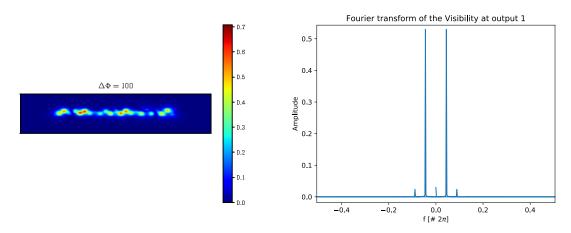
be to have a greater spacing between the WG at the output so that the evanescent coupling is as low as possible (as shown in Fig. 6c). Thus the use of a «fan out» could be an option to calculate the power over a larger area and have a greater integrated power (ergo a smaller signal to noise ratio (SNR)).

#### 2.1.3 Influence of geometrical parameters

Knowing the problem exposed in the previous section, the "ideal" surface over which the power is calculated has to be estimated. Then the influence of the geometrical parameters on the performances (estimated by the condition number of the V2PM) can be studied.

In all the following, the amplitude of visibility (or visibility) refers to  $V_{ij}$  (sometimes to the function  $V_{ij}cos(\phi_{ij})$  where  $\phi_{ij}$  is a function of the OPD. A good approximation of  $\phi_{ij}$  is  $\frac{2\pi x}{\lambda}$  where x is the OPD. V and  $\phi$  are both obtained by fitting the simulated photo-corrected curves with a cosine.

To estimate the critical surface, the power at an output versus the OPD is simulated using the software  $BeamProp^{TM}$ . It has been found that the presence of harmonics in the signal should not be higher than 2% of the main signal (the cosine). A surface corresponding to the waveguide's cross-section appeared to solve this problem for a wavelength of 3.8µm as shown on Fig.7b.



- (a) Example of the output simulated field.
- (b) Spectrum of the visibility at output 1

Figure 7: Origin and presence of harmonics in the output calculated power

All simulations unless explicitly written are performed using the previously determined integrating area. Moreover the base parameters :  $P_x = 24 \mu \text{m}$ ,  $P_y = 10.8 \mu \text{m}$ ,  $width = 9.5 \mu \text{m}$ ,  $height = 17 \mu \text{m}$ ,  $\delta n = 0.005$ ,  $\lambda = 3.4 \mu \text{m}$ , length of the DBC's part = 25 mm, length of the input = 25 mm, together with transparent boundary condition are used. The grid dimensions and z step are chosen as a balance between computation time and desired accuracy. For general results one can choose a «coarse» grid and then narrow it for more accurate results. Results presented are for scalar solution of the wave equation. Therefore they do not incorporate impacts of polarization

effects. Moreover the material are supposedly perfects in the simulation (i.e. isotropic material, no absorption, no scattering...).

To ensure a good accuracy on the retrieved astronomical parameters, the V2PM's condition number must be as close to 1 as possible (see A.1). This part will be focused on lowering the V2PM's condition number by using different geometrical parameters. The launch fields are Gaussian of same power and of 1/e diameter the width and height of the wave-guide. Thus a coupling loss of approximately 10% occurs. Fresnel losses are not included.

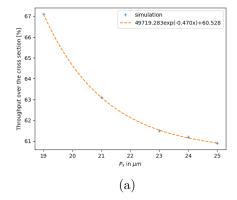
**X and Y spacing:** Simulations were performed for different values of  $P_x$  and  $P_y$  to find which parameters minimizes the condition number. The results are shown in table 1. With the few tested parameters one can only conclude that the V2PM condition number seems to be minimum for  $P_x \approx 24 \mu \text{m}$  and  $P_y \approx 10.8 \mu \text{m}$ . Concerning the throughput, it seems to have a quite linear dependency with  $P_y$  and an exponential decay with  $P_x$  within the tested range (and only within the tested range as the throughput should stay between 0% and 100%). Fitted results are displayed in figure 8. Theses results are obtained for one set of parameters and should be valid only within the tested range.

$\mathbf{P}\mathbf{y} \ [\mu m]$	4.8	6.8	8.8	10.8	12.8
19				10.68 (67.1%)	
21				10.69 (63.1%)	
23				24.77 (61.5%)	
24	24.05 (62.3%)	32.6 (62.0%)	18.77 (61.7%)	7.16 (61.2%)	16.6 (60.8%)
25				11.7 (60.9%)	

Table 1: Condition number and throughput (in parenthesis) for several x and y spacing. The throughput is calculated by the sum of the power at each outputs normalized by the total input power. The power is calculated by a power integral of the simulated field over the wave-guide's cross-section

The cross section: Now that a minimum of the condition number regarding x and y spacing has been found, the wave-guide's dimensions has to be optimized too. In the tested range all dimensions ensure that the wave-guide is mono-mode to have all «ray» traveling at the same speed in z direction (in the fundamental mode, most of the energy is traveling close to the core of the WG). This is to ensure a low modal dispersion and low coupling losses of the input field. These simulations are performed for  $P_x = 24\mu \text{m}$  and  $P_y = 10.8\mu \text{m}$ .

One more time a minimum of the condition number is found for  $width = 7.5\mu m$  and  $height = 17\mu m$ , but as such a width would lead to more birefringence (which our simulation doesn't take into account) a width of 9.5 $\mu$ m will be used instead. The throughput seems to be linear for dimensions of the wave-guides slightly different. But only for dimensions closes to the simulated ones.



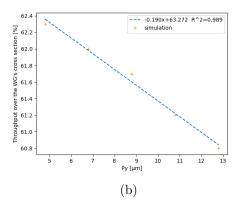


Figure 8: Evolution of the throughput over the cross section with  $P_x$  and  $P_y$  at fixed cross-section and simulation parameters (see text for details). (a) at fixed  $P_y = 10.8 \mu m$ , (b) at fixed  $P_x = 24 \mu m$ 

height	15	16	17	18
7.5			5.07 (45.9%)	
8.5			8.00 (54.1%)	
9.5	7.76 (57.8%)	8.29 (59.5%)	7.16 (61.2%)	10.12 (62.4%)
10.5			14.6 (67.5%)	

Table 2: Condition number and throughput (in parenthesis) over the WG's cross-section for several width and height. The throughput is calculated by the sum of the power at each outputs normalized by the total input power. The power is calculated by a power integral of the simulated field over the wave-guide's cross-section

Optical index difference: The wave-guides used are rectangular dielectric wave-guides with step index. As a higher optical index difference lead to a stronger mode confinement, a higher throughput over the cross section is to be expected with a higher  $\delta n$ . This paragraph focuses on finding the best  $\delta n$  to have an higher throughput together with a low condition number of the V2PM matrix. In this simulation the previously «optimised» geometrical parameters are used (except for the width of the WGs which is  $width = 9.5 \mu m$ ) and the throughput is still calculated over the wave-guide cross-section. The results are shown in table 3.

$\delta n$	condition number	throughput	
0.002	61.3	23%	
0.003	13.5	40%	
0.004	6.1	52%	
0.005	7.16	61%	
0.006	15.0	68%	
0.007	14.6	73%	

Table 3: Condition number and throughput over the WG's cross-section for several values of  $\delta n$ . The throughput is calculated by the sum of the power at each outputs normalized by the total input power. The power is calculated by a power integral of the simulated field over the wave-guide cross-section

It seems that the throughput evolves as the logarithm of  $\delta n$  within the tested range (and only within the tested range) (see fig. 9).

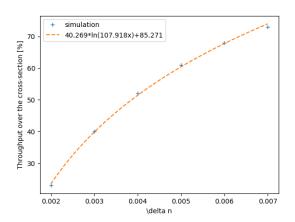


Figure 9: Throughput over the cross section for different optical index differences

The condition number seems to be minimum for  $\delta_n = 0.004$  but as it is only of 1 lower than for  $\delta_n = 0.005$  and the throughput over the wave-guide cross-section is 10% greater in this case,  $\delta_n = 0.005$  would be used as «optimised» optical index difference.

**Lengths:** An other parameter that has to be optimized is the length of the DBC part. To this point all simulations were performed for a length of 25mm. An other length that could be

optimized is the length of the inputs which were also to this point of 25mm, but as the x and y spacing of the inputs ensures that the fields aren't coupled, this shouldn't impact the V2PM condition number. This was verified in the simulation for length greater to 1cm. The results are shown in figure 10. The «1/e» area refers to a rectangle of width and height the 1/e width and height of the fundamental mode of the wave-guide (for  $\delta n = 0.005$  which should contains 91% of the mode power)

The simulations were performed for a length greater than 15mm to be sure that each inputs field propagates through the 23 outputs as can be seen in the figure 11a.

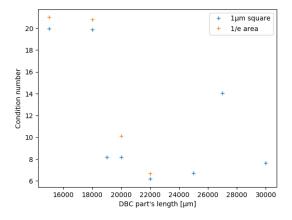
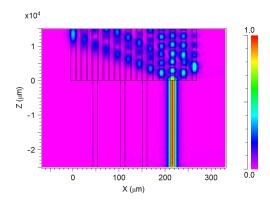


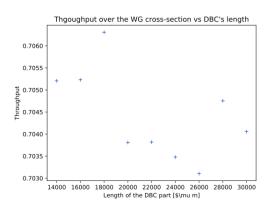
Figure 10: Condition number of the V2PM matrix for different lengths of the DBC part. The power is calculated either over a 1 by 1 micrometer area or the «1/e» area centred on the cross-section. (see text for details)

One can notice that the condition number tend to be higher for a short length of the DBC's part, and have a minimum of 6.15 for a DBC part of 22mm long. Moreover with a higher power integrating area, the condition number seems to behave the same for a large or a small integrating area so that a minimum of the condition number found with an integrating area should remain a minimum for another (if the area isn't too large and doesn't overlap surrounding fields).

Concerning the throughput, it seems to be constant within the tested length (see Fig.11b). Of course our simulated WG doesn't include scattering, surfaces defaults etc. The only kinds of losses that occurs in this simulation are bending losses and radiation in the cladding (absorption is negligible). The reader may have noticed a 10% higher throughput than in the previous sections. This is because the input field in this simulation is a Gaussian of (1/e) width and height the (1/e) width and height of the fundamental mode of the WG. Thus the 10% coupling losses experienced in the previous do not take place in this simulation.

It has be seen that the V2PM matrix is quite dependent of the area over which the power is calculated at the output. One possible way to minimise this dependency would be to design a «fan-out». By increasing the spacing of the outputs, the field should be more centered and no overlapping would occur at the output. The next section will focus on this component.





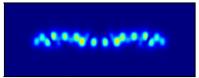
- (a) Propagation of the scalar field from the 4th input. A length of 12mm seems to be a minimum to have the field reaching every single output.
- (b) Throughput over the cross-section for different lengths of the DBC part. Two area are considered to estimate the power at the outputs (see text for details).

Figure 11

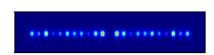
### 2.1.4 Adding a «fan out»

We have seen that both the visibilities and phases relations are dependent of the way the power is calculated. This is caused by the fields overlapping at the outputs. One way to get rid of this effect could be to add a «fan out» at the end of the DBC part and then be able to really take into account of all the flux when calculating the power. Simulations with this have been performed with a spacing of the outputs of 2 times the  $(1/e^3)$  width of the fundamental mode to be certain that no more overlapping will occur (see Fig. 12). The length of the fan-out is chosen in order to limit bending loses and 1 cm appeared to be enough. A short straight section of 2 mm is added in order that all the flux have enough length to be well centred in the WG. By doing this one can estimate the power in a wave-guide over a finite area and knowing which percentage of the power of a Gaussian field is contained in the same area, retrieve the total guided power (assuming that the fundamental mode is a Gaussian). But the point is that with such a device, the way of calculating the power at the output should no more impact neither the visibility nor phase relations, ergo the V2PM condition number (as it is the case with the previous component for large integrating area). Therefore in these simulation the power is calculated by the power integral of the simulated field over the WG's cross-section. Results show that most of the visibilities in that case are between 0.98 and 1.00 (without any polarization effects they should be all of 1) where they could be below 0.3 without the fan out. Moreover with the simulated design the fan-out lead to less than 3% losses (bending losses and radiation in the cladding) as the throughput over the WG's cross-section is up to 68%. A simulation of the throughput where the power at the end of each output is calculated over a large enough area to consider that all the power is being accounted we obtain 96.7% of throughput. This results could seems high but it is to be known that the simulations doesn't take into account scattering, material absorption (which might be very low for the considered material (GLS) at this wavelength) etc... Losses are only radiations in the cladding, bending losses and coupling the WG.

losses with the input field (which we managed to get below 1% in this simulation). Moreover one can see that 68 is almost 71% of 96.7 which is the percentage of the true centred Gaussian field's power calculated over the cross-section of the WG. This shows that at the outputs the fields should be mostly Gaussian centred fields thus the «fan out» might be well designed.







(b) Output of the ZigZag DBC with a «flat» fan-out. Fields are centered in the WG and not overlapping.

Figure 12: Effect of adding a «flat» fan-out at the output. The color-scale is the same (0 in blue to 0.6 in red) and the scalar field is displayed.

With this geometry of the «fan out», the condition number of the V2PM matrix seems to behave the same with the length of the DBC's part. The simulation leads to a condition number of 6.89 for a length of 22mm (11.61 for a length of 20mm and 7.87 for a length of 19mm). Table 4 show for 3 different length of the DBC part and for three area considered to calculate the power, how much the condition number is now «independent» of the considered area. It also

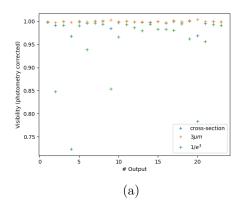
Area	Length [mm]	18	20	22
$1/e^{3}$	_	7.77	11.73	6.89
Cross		7.87	11.61	6.90
$3\mu m$		7.92	11.64	6.89

Table 4: Condition number of the V2PM matrix for 3 different area used to calculate the power at the outputs. The  $(1/e^3)$  correspond to an area of  $27 \times 35 \mu m$  (and contain more than 99% of the fundamental's power), the «Cross» is the wave-guide's cross section and the 3pixels to an area of  $3 \times 3 \mu m$ 

seems that the component with the «fan out» behave the same than the component without it except that the way the power is calculated at the output doesn't impact much more the V2PM matrix, visibility and phases relations as can be seen on figure 13. Of course the visibilities are still impacted but they still are greater than 95% for the majority (and greater than 0.75).

Effect of polarization on the retrieved parameters To this point no polarization effects has been simulated. In this part the V2PM matrix is calculated using monochromatic TE and TM polarized light. It is then studied the impact of using a TM polarization calibrated V2PM on the TE polarization data to retrieve the astronomical parameters (and vice et versa).

First of all the V2PM calibrated matrix using TE polarized light show a condition number of 6.203 and it is 6.124 for the TM polarized light. In the case of the scalar field (no polarization effect) the condition number was 6.161 which is almost the mean of TE and TM ones. Those



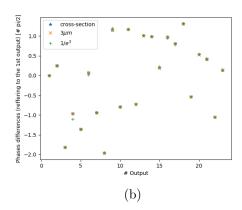


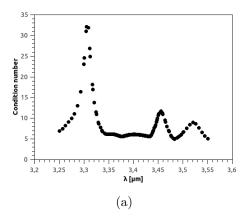
Figure 13: Baseline 1-2 Visibilities and phases relations (referring to the first output) for 3 different area used to calculate the power at the outputs. The  $(1/e^3)$  correspond to an area of  $27 \times 35 \mu m$ , the (1/e) to an area of  $15.596 \times 20.227 \mu m$  and the 3pixels to an area of  $3 \times 3 \mu m$ 

	V2PM	TE		TM	
dat	a	$\epsilon_{\phi}$ [rad]	$\epsilon_V [\%]$	$\epsilon_{\phi} [\mathrm{rad}]$	$\epsilon_V[\%]$
	TE	$6.95 \times 10^{-4}$	$7.14 \times 10^{-4}$	$2.17 \times 10^{-2}$	$2.51 \times 10^{-2}$
	TM	$2.08 \times 10^{-2}$	$2.47 \times 10^{-2}$	$6.36 \times 10^{-4}$	$6.77 \times 10^{-4}$

Table 5: Error on the retrieved parameters from the V2PM calibrated using TE/TM polarized light. The TE/TM data refers as the simulated input fields.

two V2PM matrices are used to retrieve the astronomical parameters from the simulated output fields. The results are shown in Tab.5 in which  $\epsilon_i$  is calculated by  $\epsilon_i = \sqrt{\sum \frac{1}{N}(a-\tilde{a})^2}$  where a is the data,  $\tilde{a}$  the expected parameter (phase or visibility) and N the number of simulated phase and visibility. One can see that the error on the retrieved parameters are between 30 and 40 times higher when using the V2PM calibrated using polarized light on 90 deg shifted polarized light. The impact is still very low and justify not taking into account the polarization for the previous simulation.

adaptability to other wavelength Before simulating the DBC using poly-chromatic light the dependence of the design regarding the wavelength is tested. Of course to have a component that behave the same at an other wavelength one can simply multiply its dimensions by the ratio of the wavelength. But as a component will have to be used using poly-chromatic light it is interesting to see how the condition number is influenced for a given design by the wavelength. The design previously "optimized" is used for this simulation. The results of this simulation is shown in Fig.14. As can be seen both of the curves are very similar at first sight. The component without fan-out show a flat curve for lambda ranging from 3.35 to 3.43 µm where for the component with fan-out this "flat zone" almost doesn't exist. This suggest that the component without fan-out could be more stable than the component with. This can be explained by the fact that the geometry of the fan-out act like if the coupling length were longer. This apparent length is strongly dependent of the wavelength because the coupling of the fields between two nearby



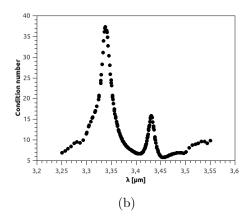


Figure 14: Condition number of monochromatic V2PM matrices at different wavelength. (a) for the component without fan-out, (b) for the component with fan-out. The geometry of the component is the optimized one (see text for details)

waveguides are strongly dependents of the wavelength. The zone where the WGs separates will couple a larger wavelength for a longer length because of the larger overlap integral between the two individual WG's modes for higher wavelength. For further explanation on the coupled mode theory the reader can refers to [BEAS07, DM91].

The evolution of the V2PM's condition number regarding the geometrical parameters and the wavelength has been studied and an optimal configuration has been found. This configuration ensures a condition number of approximately 6 which means that an error on the measured output wouldn't be magnified more than 6 times (in the worst case) by the retrieving algorithm. The evolution of the "usable" throughput through a defined surface has also been studied and result of more than 96% in the case of the component with fan-out and 70% without. This throughput doesn't include the losses from coupling nor Fresnel which should be predominant for this component. The optimized parameters are given in Tab.6. All the previous work has been done using only monochromatic light. But the light from a star is obviously not monochromatic, an it's not wanted to use too narrow-band filters in order to keep high signal to noise ratio (SNR). This is the purpose of the next section.

$P_x$	$2.4 \times 10^{1}$
$P_y$	$1.08 \times 10^{1}$
width	9.5
height	$1.7 \times 10^{1}$
δ	$5 \times 10^{-3}$
λ	3.4
$L_c$	$2.2000 \times 10^4$
$L_i$	$1.0000 \times 10^4$
background index	2.31

Table 6: Optimised set of parameters (distance unit in µm)

## 2.2 Polychromatic light

In order to keep a high enough SNR and also for different needing, the component will be used under poly-chromatic light. In the case of poly-chromatic light, the previous mathematical formalism doesn't hold anymore. In this section will be shown the limitation of the previous formalism, studied the impact of the bandwidth both on the V2MP's condition number and the retrieved mutual coherence function. Experimental results will then be compared to the simulated ones.

## 2.2.1 Mathematical formalism

Using polychromatic light, the interferogram at the  $n^{th}$  output can be expressed as a function of the optical path difference, x, as follow:

$$In(x) = \int_{-\infty}^{+\infty} I_A(\sigma) \kappa_A(\sigma) + I_B(\sigma) \kappa_B(\sigma) + 2\sqrt{I_A(\sigma) \kappa_A(\sigma) I_B(\sigma) \kappa_B(\sigma)} |\mu_{AB}(\sigma)| \cos(\phi_{AB}(\sigma) - 2\pi\sigma x) d\sigma$$
(9)

where  $\kappa_i$  relates the transmission from the  $i^{th}$  input,  $I_i$  the normalized intensity at the  $i^{th}$  input,  $|\mu_{AB}(\sigma)| = |\mu_{AB}(\sigma)^{inst}| \left|\mu_{AB}(\sigma)^{obj}\right|$  the visibility of the interferogram and  $\phi_{AB}(\sigma) = \phi_{AB}^{inst}(\sigma) + \phi_{AB}^{obj}(\sigma)$  the phase of the interferogram. In order to build a V2PM matrix which is independent of the spectrum of the source, it is needed to assume that the spectrum is "flat" within the considered bandwidth. Thus the V2PM matrix will be valid only for quasi-monochromatic light (i.e. a small bandwidth). Doing that the terms  $I_i$  are no more wavelength dependant. Eq. 9 becomes:

$$In(x) = t_A \int_{\sigma} I_A d\sigma + t_B \int_{\sigma} I_B d\sigma + 2\sqrt{I_A I_B} \int_{\sigma} \sqrt{\kappa_A(\sigma)\kappa_B(\sigma)} |\mu_{AB}(\sigma)| \cos(\phi_{AB}(\sigma) - 2\pi\sigma x) d\sigma$$
(10)

In which  $t_i = \frac{\int_{\sigma} I_i(\sigma) \kappa_i(\sigma)}{\int_{\sigma} I_i(\sigma)}$ . As our assumption lead us to be limited to quasi-monochromatic light, the visibility should also be relatively independent of the wavelength, as well as the phase if the dispersion of the instrument is negligible. Thus Eq.10 becomes:

$$In(x) = t_A \int_{\sigma} I_A d\sigma + t_B \int_{\sigma} I_B d\sigma + 2\sqrt{I_A I_B} \left| \mu_{AB} \right| \int_{\sigma} \sqrt{\kappa_A(\sigma) \kappa_B(\sigma)} cos(\phi_{AB} - 2\pi\sigma x) d\sigma \quad (11)$$

In order to use the same formalism as in the monochromatic case, we use the so called photocorrection :

$$\tilde{I}_{n} = I_{n} - t_{A} \int_{\sigma} I_{A} d\sigma - t_{B} \int_{\sigma} I_{B} d\sigma$$

$$V_{AB} = \frac{2\sqrt{I_{A}I_{B}} |\mu_{AB}| \int_{\sigma} \sqrt{\kappa_{A}(\sigma)\kappa_{B}(\sigma)cos(\phi_{AB} - 2\pi\sigma x)d\sigma}}{2\sqrt{t_{A}\int_{\sigma} I_{A}t_{B}\int_{\sigma} I_{B}}} \tag{12}$$

In that case the visibility function is no longer a cosine, but it can be seen as the Fourier transform of the spectral response of the component (in the case of the a flat spectrum signal used at the input). Thus the visibility function is now something like a cardinal sine, and the narrower the bandwidth, the closest to a cardinal sine it gets.

To use the same V2PM format, the amplitude of visibility is taken at the maximum of this interferogram, where  $V_{AB} \approx |\mu_{AB}|$ . The phase is also taken at the position  $x_0$  of this maximum and reduced using the formula  $\Phi_{AB} \approx 2\pi\sigma_0 x_0$  where  $\sigma_0$  is the middle range wave number of the input signal. Taking the nearest point to the "0" OPD is important as will be further explained in the next section.

#### 2.2.2 Influence of the bandwidth on the V2PM

As stated earlier, in order to have a better SNR one has to integrate more flux. Thus the use of a broader spectrum should improve the performances of the DBC. But as explained in the last section the mathematical formalism doesn't hold in the case of polychromatic light. One has to make the assumption of the input signal being "flat-spectrum" as well as considering the spectral response of the component wavelength independent in order to get it work. The aim of this section is to present the results of a study of the performances of the DBC in the case of polychromatic light.

Using the Beam propagation method to simulate the component behaviour, our simulated polychromatic light is composed of the sum of 50 Diracs of same weight in Fourier's space. This should be a good approximation for short bandwidth, less for larger but as those simulations are very time consuming, the number of diracs wasn't increased to keep the same "density of diracs". Nevertheless no sensible differences were seen in the case of more Dirac.

The first studied thing is the impact of the V2PM condition number regarding the bandwidth of the input signal. The simulations are performed on the previously optimized component for a "flat spectrum" centred on  $3.4 \mu m$ . Same parameters of convergence, boundary condition and Padé order are used than in the First case. The result of these simulation are shown in Fig. 15

The integrating area to estimate the phases and visibilities at each outputs is a 1 by 1 micrometer square in the case of the component without fan-out for reasons explained in previous sections. In the case of the component with a fan-out, the area used is the wave-guide cross section, but in this case the V2PM matrix is quite independent of this area (as seen in the previous section).

It appears that for the component without the fan-out, the condition number oscillate between 5.5 an 7.5 for bandwidth narrower than 40 nm. It then slowly rises for bandwidth below 150 nm and issues a sharp increase for higher bandwidth (see Fig. 15). A similar dependency is found for the component with a fan-out except that the condition number issues a drop around 200 nm bandwidth. Moreover the conditions number from both component are similar at lower bandwidth but are almost 2 times lower at higher bandwidth for the component with a fan-out. This suggest that the component with a fan-out could be more stable at larger bandwidth. Similar dependency has been reported by Saviauk et al. [SMD<sup>+</sup>13] for experimental data on a square array DBC.

The dependence of the V2PM condition number regarding the bandwidth of the input signal can be interpreted as the degree of validity of the assumption we made in the mathematical formalism. One can notice that for bandwidth lower than approximately 50 to 70 nm the

condition number of the V2PM is stable within  $\pm 5\%$  in the case of the component without fan-out. This bandwidth is up to 100 nm in the case of the component with fan-out.

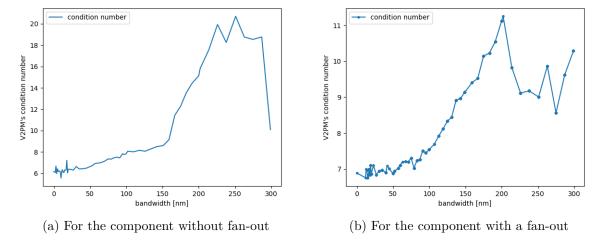


Figure 15: Condition number of the V2PM for different bandwidth using the component with and without fan-out. Both DBC part have the same dimensions.

However the condition number of the V2PM doesn't give a conclusive statement of the performances of the DBC. Therefore a simulation of the retrieved phase and visibility using the P2VM on simulated data has been performed.

#### 2.2.3 Retrieving the visibility function

In order to have a better idea of the performances of the DBC regarding the bandwidth of the signal, simulation of the retrieved visibilities and phases have been ran. To do that the simulated polychromatic light is injected into 2 of the 4 inputs. At one of the input a phase is added just the same as for constructing the V2PM. At each output an interferogram is reconstructed showing the visibility function versus the OPD. These interferogram (in the shape of a matrix where each column is one simulated phase of the baseline (the distance between two individual telescopes) (BL)) are multiplied by the P2VM to obtain the  $\vec{V}$  vector from which the object visibility are calculated as explained in sections 2.1.1 and 2.2.1. The results are presented in Fig.16 and Fig.17

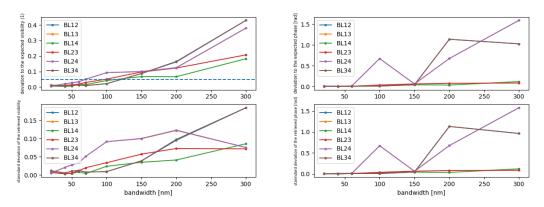
In our simulation no polarization's effects are taken into account so that the visibility of the input source should be 1 at the 0 OPD independently of the phase difference. All simulations were performed with one data point each 12 degrees of phase difference between the inputs from 0 to 360 degrees, for all 50 wavelength evenly spaced in a fixed bandwidth around 3.4 tm and for all 6 baselines.

To estimate the accuracy of the retrieved phases and visibilities, the expected ones are subtracted

from the retrieved ones and the deviation  $\epsilon$  is estimated by the formula :

$$\epsilon = \sqrt{\frac{1}{N} \sum_{1}^{N} (a - \tilde{a})^2} \tag{13}$$

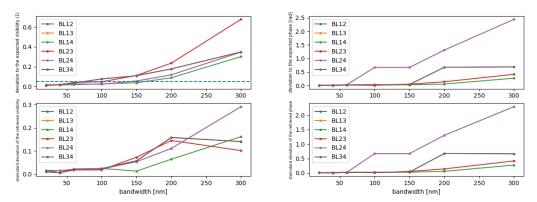
where a is the retrieved parameters,  $\tilde{a}$  the expected one and N the number of tested retrieved parameters (31 in out case). The result is shown in Fig 16. What can be seen is that the retrieved visibilities are close to the expected ones (at  $\pm 5\%$  for bandwidth below 60 nm bandwidth), same as the retrieved phases (at  $\pm 0.05 rad$  below 60 nm bandwidth). Meanwhile the standard deviation of both the retrieved phases and visibilities are found to have a similar dependency to the bandwidth. This means that the larger the bandwidth, the more dispersed the retrieved parameters around their mean value. The results for the component with a "fan-out" is very similar as can be seen in Fig. 17 despite a lower condition number of the V2PM. This clearly shows that the condition number only states the maximum magnification of an error. It also shows that despite the apparent correlation between the retrieved visibilities/phases and the condition number of the V2PM, the impact of this condition number is not the main limiting factor but the approximations of "flat spectral response" is. The broader the bandwidth the more the spatial frequency of the interferogram (i.e the fringe spacing) can get different from 3.4 µm leading to errors on both the retrieved phase and visibility.



(a) Deviation of the retrieved visibilities to the (b) Deviation of the retrieved phases to the expected ones

Figure 16: Deviation of the retrieved phases and visibilities to the expected ones for the component without fan-out. The deviation is calculated by Eq. 13

. In order to compare with the experimental results presented in the following part, the plots of the retrieved visibility and phases with 70nm bandwidth are presented in Appendix A.2. The retrieving algorithm show good accuracy for a bandwidth below 70nm and for each baselines individually. But the component is designed to be used with the 4 input beams at the same time. The next part will present the results of simulations using the 4 beams at the same time.



(a) Standard deviation of the retrieved(b) Standard deviation of the retrieved phases visibilities to the expected ones

Figure 17: Standard deviation of the retrieved phases and visibilities to the expected ones for the component with fan-out. The deviation is calculated by Eq. 13. The blue dashed line is the limit of 5% error. Inputs 1,2,3,4 refers respectively to WG 19,14,10,5 in Fig.3 as seen from the inputs.

#### 2.2.4 Retrieved visibility and phase using the 4 input beams

To this point only retrieved visibility and phases using 2 beams at a time have been presented. The component being designed to combine 4 telescopes at the same time, simulation doing that have been done. to this purpose the previously calibrated P2VM are used and applied to the results of a simulation using the 4 input. The phase of three beams have been fixed and the phase of the last beam has been scanned to simulate the behaviour of the component. Only one test have been done using at  $\lambda_0 = 3.4 \mu m$  and 20nm bandwidth.

First the component without fanout has been simulated. The results are shown in Fig.18 and Fig.19. The retrieved visibility are far less accurate when using 4 beams at the same time than when using only 2 beams at the same time (error up to 25%). The reason to that is the combination of the previously exposed "apparent wavelength" of the interferograms and the fact that in those simulations the "0 OPD" (i.e the maximum of each interferogram) appears for all baselines at approximately the same OPD. Therfore each baselines are less distinguishable from each-other, a phase shift between each of the 6 baselines would probably lead to better results, this would be a thing to try in order to confirm or invalidate this interpretation. Concerning the retrieved phase, the accuracy is relatively good (lower than 0.12 rad of error). Still the error is two times the ones obtained when using two beams at a time. The explanation of this is the same than for the visibility.

Secondly the component with fanout has been simulated. The results are shown in Fig.20 and Fig.21. In that both the errors on the retrieved phase and visibility are good and comparable to the ones obtained using two beams at a time (visibility at  $\pm 5\%$  and phase at  $\pm 0.08rad$ ). The explanation to this could be that the "fan-out" lead to "0 OPD" of each output being further to each other and for each baselines too. More simulations should be done with this component in

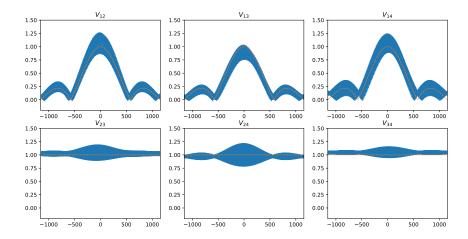


Figure 18: Simulated retrieved visibility using the 4 beams on the component without fanout. The signal bandwidth used is 20nm centred at  $\lambda_0 = 3.4 \mu m$ . The blue line is the retrieved date. The orange dotted line is the expected one. The x-axis is the OPD in  $\xi$ m and the y-axis the visibility.

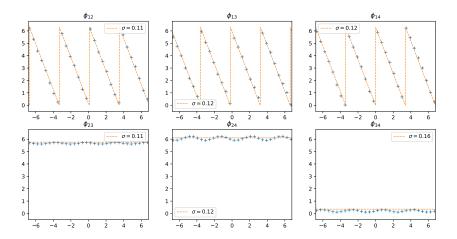


Figure 19: Simulated retrieved phase using the 4 beams on the component without fanout. The signal bandwidth used is 20nm centered at  $\lambda_0 = 3.4 \mu m$ . The blue line is the retrieved date. The orange dotted line is the expected one. The x-axis is the OPD in  $\xi$ m and the y-axis the phase in rad. Sigma is the standard deviation to the expected phase in rad.

order to confirm or invalidate that interpretation.

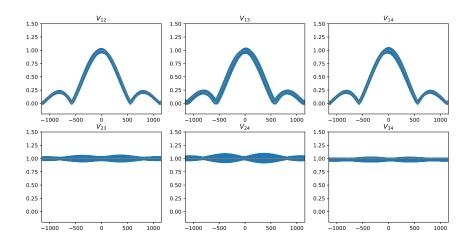


Figure 20: Simulated retrieved visibility using the 4 beams on the component with fanout. The signal bandwidth used is 20nm centred at  $\lambda_0 = 3.4 \mu m$ . The blue line is the retrieved date. The orange dotted line is the expected one. The x-axis is the OPD in  $\mu m$  and the y-axis the visibility.

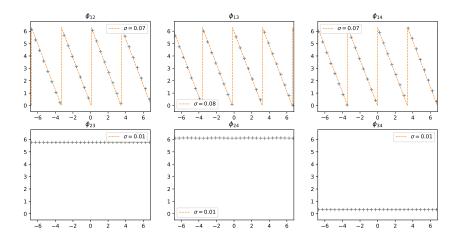


Figure 21: Simulated retrieved phase using the 4 beams on the component with fanout. The signal bandwidth used is 20nm centered at  $\lambda_0 = 3.4 \mu m$ . The blue line is the retrieved date. The orange dotted line is the expected one. The x-axis is the OPD in  $\mu$ m and the y-axis the phase in rad. Sigma is the standard deviation to the expected phase in rad.

The results of these simulations enlighten that the component with fanout could have better performances when used with 4 beams under the exact same conditions than the component without fanout. This difference is expected to be even greater experimentally due to the previously exposed problem of the integrating area. In simulation accuracy of 5% on the retrieved visibility and 0.08 rad on the retrieved phases have been obtained using the 4 inputs at the same

time with the component with "fanout" and a signal's spectral bandwidth of 20nm. When using 2 beams at the same time, a spectral bandwidth of 70nm led to an acceptable simulated accuracy on the retrieved parameters. An experimental demonstration of the usability of the DBC with a signal of 70nm bandwidth (limit of acceptable accuracy using two beams at a time) is still to be done. This is the purpose of the next chapter.

## 3 Laboratory characterization of the DBC

#### 3.1 characterization setup and method

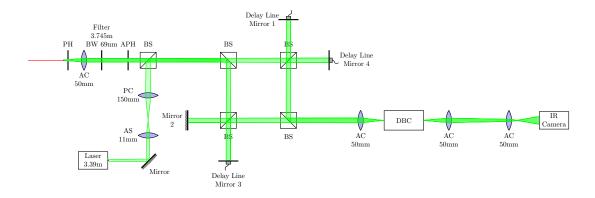


Figure 22: Experimental setup for characterization of the ZigZag DBC integrated optics chip. The last two lens are used to magnify approximately 8 times. AC = Achromatic, AS = Asphere, PH = PinHole, APH = Adjustable PinHole, BS = Beam-Splitter, PC = Plano-Convex.

It has been demonstrated in the previous section that the ZigZag DBC can give accurate results with a bandwidth up to 70nm. The purpose of this part is to verify that experimentally. For that purpose the experimental setup represented in Fig.22 was used. It is a Michelson interferometer with 4 beams. The beams from Mirror 1, 2, 3 and 4 are coupled in the input waveguides 5, 14, 10 and 19 respectively (see Fig 3 as seen from the input side).

The DBC used for the characterization is not the one designed in the previous chapter, but is designed to word at 3.4µm too. As it appear that at 3.4µm all outputs were not illuminated, the source signal was chosen to be a "flat" spectrum signal of 69nm bandwidth centred at 3.745µm. If the component was well inscribed in the glass all photometric signal should be symmetrical (i.e the ones from inputs 2,3 and 4,1 should look alike). As can be seen in Fig.23 this is not the case especially for inputs 4, 1. The reason of this is to be found in the writing technique. As the laser inscription technique is not the purpose of this report we will simply explain how it induce birefringence. To inscribe the waveguides the laser write multiple lines that overlap each-other. This overlapping lines make the result dependant of the order of inscription of the waveguides which cause the birefringence effect responsible of the not symmetrical pattern. This has to be verified using a polariser.

A second point to explain is the presence of the laser. As the Delay-lines were not very accurate in their movement, the laser was here to calibrate the OPD. Using the fringe spacing of the laser's interferogram, one can reconstruct the real OPD introduced by the delay-line. In order to do so in a First experiment the laser was coupled into the DBC together with the supercontinum source (at 3.8 µm). As it appeared that the laser signal was not enough distinguishable from the source signal this technique was not used to obtain the results presented in the following paragraph. Rather than doing that, as the "apparent wavelength" of the high-frequency component of the interferogram has been demonstrated to be quite the same for all output at 70nm bandwidth,

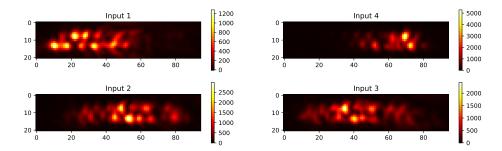


Figure 23: The photometric signal of the DBC. As can be seen the signal from input 4 ans 1 are not symmetrical certainly due to birefringence.

one interferogram was used to calibrate the OPD stating that the fringe spacing was 3.745μm.

This method is valid in the limit of "apparent frequency" not too different from one output to the other. In fact this was verified as for BL-1/2 the apparent wavelength was  $3.73 \pm 0.05 \mu m$ ,  $3.73 \pm 0.04 \mu m$  for BL-1/3,  $3.70 \pm 0.08 \mu m$  for BL-1/4,  $3.78 \pm 0.04 \mu m$  for BL-2/3,  $3.75 \pm 0.05 \mu m$  for BL-2/4 and  $3.69 \pm 0.07 \mu m$  for BL-3/4. This is of the same order of magnitude than what was seen in simulation.

In order to characterize the V2PM, the following measurements are performed for each of the 6 baselines (recording frequency = 100Hz, delay line velocity = 0.08 mm/s):

- 1. Record the signal from the moving delay-line alone  $I_{DL}$  with the delay-line moving (5000 frames).
- 2. Record the photometry from the non-moving input alone  $I_{Fix}$ .
- 3. Record the interferogram (with the 2 beams) I

The obtained result is in the form of a cube of frames. In these frames 1 pixel is chosen to be approximately centred on each output in order to be influenced as little as possible by the surroundings waveguides (as explained in the first chapter. This pixel with the magnification system of 8 should be an area of less than  $4\times4\mu\mathrm{m}$  which was too large in simulation but the best doable with the setup. - In the case of the component with fanout, one would have to integrate all the flux by taking an area around the output in order to have high SNR - . Then the data is processed to build the V2PM as follows:

- 1. The noise is filtered in Fourier's space.
- 2. The OPD is calculated using a chosen interferogram stating that the fringe spacing should be 3.745tm.
- 3.  $I_{DL}$  and  $I_{Fix}$  are subtracted from the interferogram.
- 4. The protocorrection is applied (Eq 12)
- 5. The envelop of the signal is fitted and the instrumental visibility deduced by it's amplitude

- 6. A cosine is fitted to 3 fringes of the interferogram centred at the position of it's maximum to deduce the phase (being  $2\pi x/\lambda_0$ ,  $\lambda_0 = 3.745 \mu m$  in our case)
- 7. the transmission coefficients of the input ( $\kappa_{io}$  for input i to output o) are calculated from the photometric data (averaged along the number of frames) by  $\kappa_{io} = \frac{I_D(o)}{\sum_{all\_pixels} I_D(pixel)}$
- 8. The whole V2PM is calculated as in the case of monochromatic light

The condition number of the V2PM resulting with the tested component (numbered 39.7) is 26. The instrumental visibilities for the majority range between 0.6 and 1. In the simulations visibilities were almost all between 90% and 100%. The difference is induced by polarisation effects and mostly the birefringence. An histogram of the visibilities is shown in Fig.24.

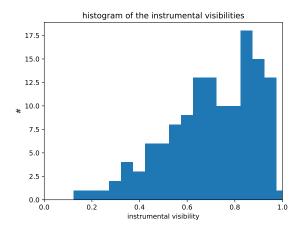


Figure 24: Histogram of the experimental instrumental visibilities of the ZigZag DBC number 39.7

From that V2PM the visibilities and phases of each baselines are retrieved first using directly the data used to calibrate the V2PM, then using data recorded after with 2 or 4 beams in input. The results are presented in the next section.

## 3.2 Retrieving the visibility function

#### 3.2.1 Using two beams at a time

Having experimentally determined the V2PM and inverted it to obtain the P2VM, the object visibility and phase are retrieved from the experimental data. First using the same set of data used to calibrate the V2PM and then using new ones to test the reproducibility of the method.

The results of the retrieved phases from the data used to calibrate the V2PM matrix are shown on Fig.25. These results aren't biased by the calibration of the V2PM because the V2PM only take into account of the visibility and phase of the output interferogram at the position of their maximum. What is flagrant from these results and the simulated ones on a similar component (see A.2) is that experimentally the retrieved visibility tend to oscillate a lot more around

the theoretical one (especially for baseline 14. These oscillations are mostly due to the highly overlapping output signal (as explained in the first chapter), the "apparent wavelength" and the delay-line being not very accurate thus changing the coupling a little from one measurement to the other (this will be verified further). The retrieved visibilities are also a lot impacted by the position of the maximum of the interferogram being not at the same OPD thus leading to the oscillations. With all of these imperfections the retrieve visibility are around the zone of interest (around the maximum) accurate at 10% for the best baselines to 20% for the worst. The visibilities retrieved on the second dataset recorded right after the calibration of the V2PM are presented on figure 26 and are far from as good as the first ones. This is mostly because of the delay-line altering the coupling in their movement and is especially visible on the retrieved visibility for baseline 1-2, 1-3 and 1-4 which were recorded in the same order moving the delay-line of input 1.

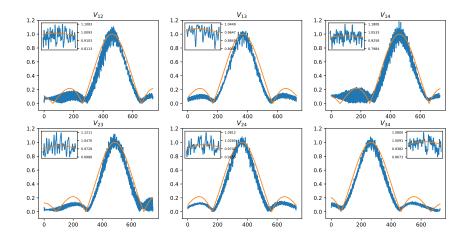


Figure 25: Experimentally retrieved visibility from the dataset used to calibrate the V2PM. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The x-axis is the OPD in  $\mu$ m and the y-axis the visibility. The blue line is the actual retrieved data and the orange line the theoretical result. The inset is a zoom of the  $50\mu$ m opd around the maximum.

Concerning the retrieved phase, the results are presented in Fig.27 for the dataset used to calibrate the V2PM and Fig.?? for the second dataset zoomed around the maximum of the interferogram (the "0" OPD). Comparison with the simulated one on the optimised component at 3.4 $\mu$ m and bandwidth 70nm can be done using Appendix A.2. It appear that the results are better on the second set of data recorded than on the one used to calibrate the V2PM. This suggest that the phase retrieval is less sensitive to the inperfections of the delay-line and that the uncertainties on it's retrieval are more intrinsic to the noise and the "apparent wavelength" explained before. In all case the residues show a standard deviation to 0 ranging from 0.08 to 0.4 rad. This is equivalent to a sensitivity from  $\frac{\lambda_0}{9}$  to  $\frac{\lambda_0}{46}$  depending on the baseline and the quality of the calibration ( $lambda_0$  being the mid-range wavelength thus 3.745 $\mu$ m). In the simulated case with the optimised component (70nm bandwidth centered on 3.4 $\mu$ m wavelength) the residue was about 0.086 rad for all baselines suggesting a possible accuracy of  $\frac{\lambda_0}{40}$  for all baselines. To

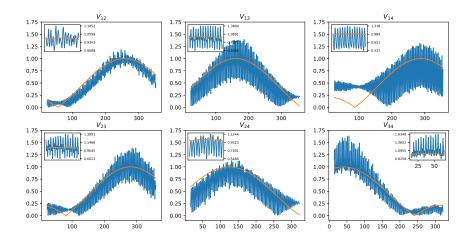


Figure 26: Experimentally retrieved visibility from the data recorded after the V2PM calibration. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The x-axis is the OPD in  $\mu$ m and the y-axis the visibility. The blue line is the actual retrieved data and the orange line the theoretical result. The inset is a zoom of the  $50\mu$ m opd around the maximum.

compare Diener et al. presented retrieved visibility ranging from  $0.96 \pm 0.04$  to  $1.04 \pm 0.06$  and phases residue ranging from 0.13 to 0.18 rad in [DTL<sup>+</sup>17] using a similar component with monochromatic light at  $3.39\mu m$ .

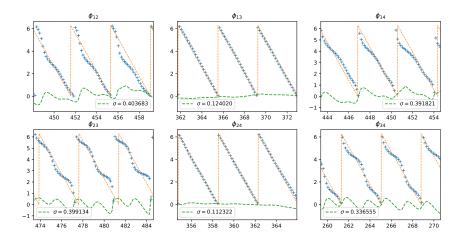


Figure 27: Experimentally retrieved phase from the dataset used to calibrate the V2PM. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The blue line is the actual retrieved data, the orange line the theoretical result and the green line the residues (difference between the blue and orange one).  $\sigma$  is the standard deviation of the residues in rad. The x-axis is the OPD in  $\mu$ m and the y-axis the phase in rad.

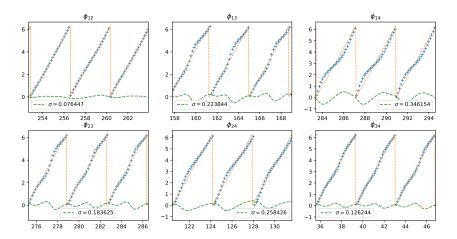


Figure 28: Experimentally retrieved phase from the data recorded after the V2PM calibration. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The blue line is the actual retrieved data, the orange line the theoretical result and the green line the residues (difference between the blue and orange one).  $\sigma$  is the standard deviation of the residues in rad. The x-axis is the OPD in  $\mu$ m and the y-axis the phase in rad.

For now the experimental demonstration of the feasibility and usability of the Zig-Zag DBC has been done using it to combine only 2 beams at a time. The final purpose of this component beeing to combine 4 telescopes one experimental measurement has been done using the 4 beams.

#### 3.2.2 Combining the 4 beams

In order to demonstrate the usability of the Zig-Zag DBC to combine 4 telescopes at a time, the 4 beams where coupled into the component and the P2VM applied to the measured data to retrieve the phases and visibilities of the source. Because of the Delay-line being not very reproducible in its movement only the one that moved the less were used for this measurement (corresponding to input 3, WG 10). The results are sown on Fig.29 and Fig.30. Only the delay-line of input 3 is scanned thus the visibility and phase of BL 1-2, 1-4 and 2-4 are expected to be constant. The visibility and phase of BL 1-3, 2-3 and 3-4 are supposed to look like the ones of Fig.25 and Fig.28 respectively. Once again the retrieving algorythm seems to be more accurate on retrieving the phases than the visibilities. This can be explained by the fact that to retrieve the visibilities, 4 different component of the vector  $\vec{V}$  are used opposed to 2 to retrieve the phase (see Eq.5) making the phase less sensitive to errors.

Concerning the phase of the 3 scanned baselines, the standard deviation of the residue is less than 0.16 rad which is better than in some case using only 2 beams and the same order of magnitude than reported in [DTL<sup>+</sup>17]. This can be explain by more amplitude in the interferograms resulting to higher SNR. The phase of the non scanned baselines shows more volatility (for BLs 1-2 and 1-4 especially).

Concerning the visibilities of the 3 scanned baselines, the shape of the cardinal sine is visible and the maximum around 1 but the error is up to 40% in that case.

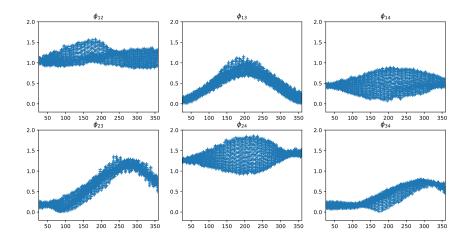


Figure 29: Experimentally retrieved visibility from the data recorded after the V2PM calibration. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The x-axis is the OPD in  $\mu$ m and the y-axis the phase in rad.

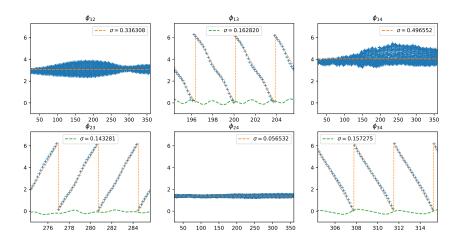


Figure 30: Experimentally retrieved phase from the data recorded after the V2PM calibration. Baselines numbering 1, 2, 3, 4 refers to the input waveguides (respectively 9, 14, 10 and 19). The blue line is the actual retrieved data, the orange line the theoretical result and the green line the residues (difference between the blue and orange one).  $\sigma$  is the standard deviation of the residues in rad. The x-axis is the OPD in  $\mu$ m and the y-axis the phase in rad.

The retrieval of the phase and visibility of a source using the ZigZag-DBC have been demonstrated to be as accurate using a broad-band source of 70nm with similar degree of accuracy than using monochromatic light as reported in [DTL+17] using 2 beams at a time. In the case of using 4

beams the method used showed lower accuracy on retrieving the visibilities. We are convinced that the variation of the coupling due to the delay-lines being not very accurate contributed a lot to the errors and we are convinced that better results could be obtained with better delay-lines (as the simulations showed far better accuracy) and with the component with fanout as suggested the simulations.

## Conclusion and Further-work

The work presented in this report was aimed at optimising the Zig-Zag DBC and experimentally demonstrating it's capabilities to combine the light from 4 individual telescopes at the same time. Because of space and time restriction this work is not all the work done during this internship. Not included in this report are simulations of tri-couplers, asymmetric-couplers and experimental characterizations of asymmetric-couplers and MMIs for nulling purpose.

In the first part the DBC has been optimised at  $\lambda = 3.4 \mu m$  regarding the condition number of the V2PM. A condition number down to 6 was obtained. Moreover the problem of determining the flux truly guided through one output and the presence of harmonics due to the neighbouring WG has led to minimizing the integrating area and developing a design with a fan-out. This fan-out led to 3% of bending losses but considerably increased the usable throughput. Simulations have demonstrated the ability of both design to retrieve the visibility and phase of the simulated punctual source of 1 baseline at a time for signal spectral bandwidth up to 70nm with an accuracy of  $\pm 5\%$  on the visibility and  $\pm 0.05 rad$  on the phase. When it comes to combining the 4 beams at the same time the design with fanout has shown better accuracy (approximately two times) on the retrieved parameters at 20nm bandwidth. To the best of my knowledge these differences are mostly linked to the transmission coefficient  $\kappa$  being highly wavelength dependent leading to an apparent wavelength of the output signal being different from  $3.4\mu m$ . An other limiting factor to better retrieved visibility is the "0 OPD" being at different input OPD for each output and this is mostly impacting the higher bandwidth because of smaller coherence length. Accuracy of  $\pm 5\%$  on the retrieved visibilities and  $\pm 0.08 rad$  on the retrieved phases has been obtained with the component with fanout and a spectral bandwidth of the input signal of 20nm. Further simulation at larger bandwidth should be done to confirm or invalidate the superiority of the component with fanout.

In the second part the experimental demonstration of the capabilities of the DBC was done with a signal spectral bandwidth of 70nm centred at  $3.745\mu m$ . Condition number down to 25 was obtained and errors ranging from 10 to 20% on the retrieved visibility and 0.08 to 0.4 rad on the retrieved phases has been obtained (combining two beams at a time). High sensibility to the coupling has been experienced and those errors are mostly due to the experimental setup, especially the delay-lines being not reproducible in their movement. When combining the 4 beams at the same time, far lower accuracy was obtained (similarly to what was obtained in simulation). Further work with the previously optimized component with fanout would have to be done.

Further work: If would have to continue this work I would identify few axes of work.

The first one would be to continue simulations using the 4 beams for bandwidth up to 70 nm in order to validate or not the superiority of the design with fan-out.

The second one would be to get the transmission coefficients as independent as possible to the wavelength. This could results in better accuracy in retrieving the visibility and phase. Moreover trying to get the optical path difference between each output signal (i.e getting the maximum of their interferogram at the same input OPD) could highly increase the accuracy and the 'bandpass' of the component. To do the first one, one could adapt the work done on asymmetric couplers but doing few short portion of the waveguides at a different optical index and different position. To the best of my knowledge It will not be possible to strictly adapt the same procedure done with asymmetric couplers to the DBC. To do the second one I tested using an array of 17 waveguides, this worked but the condition number of the V2PM sharply increased (as suggested by [Min12]).

The results obtained experimentally with the component showed lower contrast than expected from the simulation. This is probably due to high birefringence induced by the ultra-fast laser inscription method. Measurements on the DBC with a polariser would have to be done in order to verify that. Moreover the dependence of the V2PM matrix regarding the polarisation could be an interesting thing to study as well as the accuracy on the retrieved parameters.

The DBC present interesting and promising capabilities as it demonstrated high contrasts both in simulation and experimentally, and good accuracy on the retrieved astronomical parameters.

A. APPENDIX 37

# A Appendix

#### A.1 The condition number

Considering the following system  $A\vec{x} = \vec{b}$  where A is the matrix describing our system (A is a matrix with real coefficients). An error  $\vec{\delta x}$  on  $\vec{x}$  will lead to an error  $\vec{\delta b}$  on  $\vec{b}$ . The aim is to know how much bigger or smaller is  $\frac{\|\vec{\delta x}\|}{\|\vec{x}\|}$  compared to  $\frac{\|\vec{\delta b}\|}{\|\vec{b}\|}$  (i.e how much an error is magnified by the A matrix).

In the case where A in neither symmetric nor square. Then the matrix  $A^TA$  is a square symmetric matrix and Then can be diagonalized. Lets call  $\lambda_i$  and  $\vec{u_i}$  its eigenvalues and eigenvectors. We can write :

$$A^T A \vec{u_i} = \lambda_i \vec{u_i}$$

Moreover

$$||A\vec{x}||^2 = \vec{x}^T A^T A \vec{x} = \left\| \vec{b} \right\|^2$$

So  $\left\| \vec{b} \right\|^2 \leq \max(|\lambda_i|) \left\| \vec{x} \right\|^2$  and  $\left\| \delta \vec{b} \right\|^2 \geq \min(|\lambda_i|) \left\| \delta \vec{x} \right\|^2$  and then :

$$\boxed{\frac{\left\|\vec{\delta x}\right\|}{\|\vec{x}\|} \leq \frac{\sqrt{\max(|\lambda_i|)}}{\sqrt{\min(|\lambda_i|)}} \frac{\left\|\vec{\delta b}\right\|}{\left\|\vec{b}\right\|}}$$

The number  $\frac{\sqrt{\max(|\lambda_i|)}}{\sqrt{\min(|\lambda_i|)}}$  where  $\min(|\lambda_i|)$  is the minimal non zero eigenvalue of  $A^TA$ , is called the condition number of the A matrix. It means how much an error on the right part of the system can be magnified by the A matrix.

38 A. APPENDIX

## A.2 Simulated retrieved Phase and visibility

In order to compare the results of Fig.25 in a more readable way than with Fig.17 the reader can see the results on the following plot.

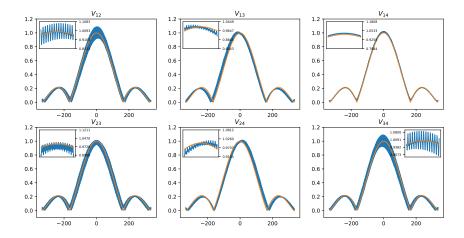


Figure 31: The simulated retrieved visibilities of the optimised component at  $\lambda=3.4\mu m$  and bandwidth=70nm. The x-axis is the OPD in  $\mu m$  and the y-axis the visibility. Baseline numbering follows the ones from Fig.25.The blue line is the actual retrieved data and the orange line the theoretical result.

A. APPENDIX 39

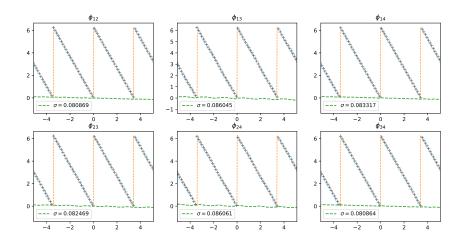


Figure 32: The simulated retrieved phases of the optimised component at  $\lambda=3.4\mu\mathrm{m}$  and bandwidth=70nm. The x-axis is the OPD in  $\mu\mathrm{m}$  and the y-axis the phase in rad. Baseline numbering follows the ones from Fig.27.The blue line is the actual retrieved data the orange line the theoretical result and the green line the residues (difference between the blue and orange one).  $\sigma$  is the standard deviation to 0 of the residues in rad.

### A.3 Gantt

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mulation du SBC - monochromatique																																					
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E divers sur la Y2PM et le DBC (17 guides)									ш	ш	ш	ш			ш	ш		ш			ш																
digrement de bare optique. A faisceure									ш		ш	ш	ш		ш	ш					ш		ш														
à caracterisation des MMIs et du DBC													ш			ш																					

#### Items are:

- Recherche Biblio / Prise en main de Beamprop
- Simulation du tricoupleur / faisabilité d'un ABC
- Simulation du DBC monochromatique
- Simulation du DBC polychromatique
- Caracterisation et simulation coupleurs assymetriques.
- Test divers sur la V2PM et le DBC (17 guides...)
- Realignement du banc optique, 4 faisceaux
- Lab caracterisation des MMIs et du DBC

40 Glossary

# Glossary

**DBC** discrete beam combiner. 1–3

**IO** Integrated optic. 1

**MMI** Multi Mode Interferometer. 1

**OPD** optical path difference. 5, 7

 ${\bf P2VM}\,$  Pixel to Visibility Matrix. 3

 $\mathbf{V2PM}$  Visibility to Pixel Matrix. 2, 5, 7

 $\mathbf{WG}$  waveguide. 5

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