



ALGORITHM FOR DECISION TREE INDUCTION

- o Basic algorithm (a greedy algorithm)
 - · Tree is constructed in a top-down recursive divide-andconquer manner

 - At start, all the training examples are at the root
 Attributes are categorical (if continuous-valued, they are discretized in advance)
 - Examples are partitioned recursively based on selected attributes
 - Test attributes are selected on the basis of a heuristic or statistical measure (e.g., information gain)
- Conditions for stopping partitioning
 - All samples for a given node belong to the same class
 - There are no remaining attributes for further partitioning – majority voting is employed for classifying the leaf

 There are no samples left

BRIEF REVIEW OF ENTROPY Entropy (Information Theory) A measure of uncertainty associated with a random • Calculation: For a discrete random variable Y taking m distinct values $\{y_1, \dots, y_m\}$, ullet $H(Y) = -\sum_{i=1}^m p_i \log(p_i)$, where $p_i = P(Y = y_i)$ Interpretation: Higher entropy => higher uncertainty Lower entropy => lower uncertainty Conditional Entropy $H(Y|X) = \sum_{x} p(x)H(Y|X = x)$

GAIN RATIO FOR ATTRIBUTE SELECTION (C4.5)

- o Information gain measure is biased towards attributes with a large number of values
- \circ C4.5 (a successor of ID3) uses gain ratio to overcome the problem (normalization to information gain)

SplitInfo_A(D) =
$$-\sum_{j=1}^{\nu} \frac{|D_j|}{|D|} \times \log_2(\frac{|D_j|}{|D|})$$

- GainRatio(A) = Gain(A)/SplitInfo(A)
- Ex. $SplitInfo_{income}(D) = -\frac{4}{14} \times \log_2(\frac{4}{14}) \frac{6}{14} \times \log_2(\frac{6}{14}) \frac{4}{14} \times \log_2(\frac{4}{14}) = 1.557$
 - gain_ratio(income) = 0.029/1.557 = 0.019
- The attribute with the maximum gain ratio is selected. as the splitting attribute

ENHANCEMENTS TO BASIC DECISION TREE INDUCTION

- o Allow for continuous-valued attributes
 - Dynamically define new discrete-valued attributes that partition the continuous attribute value into a discrete set of intervals
- o Handle missing attribute values
 - Assign the most common value of the attribute
 - Assign probability to each of the possible values
- o Attribute construction
 - Create new attributes based on existing ones that are sparsely represented
 - · This reduces fragmentation, repetition, and replication



BAYESIAN CLASSIFICATION: WHY?

- A statistical classifier: performs probabilistic prediction, i.e., predicts class membership probabilities
- o Foundation: Based on Bayes' Theorem.
- o Performance: A simple Bayesian classifier, naïve Bayesian classifier, has comparable performance with decision tree and selected neural network classifiers
- o Incremental: Each training example can incrementally increase/decrease the probability that a hypothesis is correct - prior knowledge can be combined with observed data
- o Standard: Even when Bayesian methods are computationally intractable, they can provide a standard of optimal decision making against which other methods can be measured

BAYES' THEOREM: BASICS

- Total probability Theorem? $(B) = \sum_{i=1}^{M} P(B|A_i)P(A_i)$
- o Bayes' Theorem: $P(H | \mathbf{X}) = \frac{P(\mathbf{X} | H)P(H)}{P(\mathbf{X})} = P(\mathbf{X} | H) \times P(H) / P(\mathbf{X})$
 - Let ${\bf X}$ be a data sample ("evidence "): class label is unknown
 - Let H be a hypothesis that X belongs to class C
 - Classification is to determine P(H | X), (i.e., posteriori probability): the probability that the hypothesis holds given the observed data sample X
 - P(H) (prior probability): the initial probability o E.g., X will buy computer, regardless of age, income, ...
 - P(X): probability that sample data is observed
 - $P(X \mid H)$ (likelihood): the probability of observing the sample X, given that the hypothesis holds
 - E.g., Given that X will buy computer, the prob. that X is 31...80, medium income



Prediction Based on Bayes' Theorem

• Given training data **X**, posteriori probability of a hypothesis H, P(H | X), follows the Bayes' theorem

$$P(H | \mathbf{X}) = \frac{P(\mathbf{X} | H)P(H)}{P(\mathbf{X})} = P(\mathbf{X} | H) \times P(H) / P(\mathbf{X})$$

- o Informally, this can be viewed as posteriori = likelihood x prior/evidence
- Predicts X belongs to C_i iff the probability $P(C_i|X)$ is the highest among all the $P(C_k | X)$ for all the k classes
- o Practical difficulty: It requires initial knowledge of many probabilities, involving significant computational

LASSIFICATION IS TO DERIVE THE MAXIMUM OSTERIORI

- Let D be a training set of tuples and their associated class labels, and each tuple is represented by an n-D attribute vector $\boldsymbol{X} = (\boldsymbol{x}_1,\,\boldsymbol{x}_2,\,...,\,\boldsymbol{x}_n)$
- ${\color{red} \bullet}$ Suppose there are m classes $\mathbf{C_1},\,\mathbf{C_2},\,...,\,\mathbf{C_m}.$
- Classification is to derive the maximum posteriori, i.e., the maximal $P(C_i | \mathbf{X})$
- o This can be derived from Bayes' theorem

$$P(C_i|\mathbf{X}) = \frac{P(\mathbf{X}|C_i)P(C_i)}{P(\mathbf{X})}$$

• Since P(X) is constant for all classes, only $P(C_i|\mathbf{X}) = P(\mathbf{X}|C_i)P(C_i)$

needs to be maximized



RULE EXTRACTION FROM A DECISION TREE

- Rules are easier to understand than large trees
- One rule is created for each path from the
- Each attribute-value pair along a path forms conjunction: the leaf holds the class
- Rules are mutually exclusive and exhaustive
- o Example: Rule extraction from our buys_computer decision-tree

IF age = young AND student = noIF age = young AND student = yes THEN $buys_computer = no$ THEN $buys_computer = yes$

IF age = mid-age

THEN $buys_computer = yes$ IF age = old AND credit_rating = excellent THEN buys_computer = net

IF $age = old AND credit_rating = fair$

THEN $buys_computer = yes$

RULE INDUCTION: SEQUENTIAL COVERING METHOD

- o Sequential covering algorithm: Extracts rules directly from training data
- o Typical sequential covering algorithms: FOIL, AQ, CN2, RIPPER
- Rules are learned sequentially, each for a given class C, will cover many tuples of C_i but none (or few) of the tuples of other classes
- - · Rules are learned one at a time
 - Each time a rule is learned, the tuples covered by the rules are removed
 - Repeat the process on the remaining tuples until termination condition, e.g., when no more training examples or when the quality of a rule returned is below a user-specified threshold
- o Comp. w. decision-tree induction: learning a set of rules simultaneously

