

Big O = Upper bound

$$f(x) \leq c.g(x) \\ \Rightarrow f(x) = O(g(x))$$

For eg. $n - 1 \leq c.n$
So, $n - 1 = O(n)$

Now, find time complexity of below given code :

```
flag = 0 ..... O(1)
for (int i=0; i<n; i++) ..... O(n)
{
    if( A[i] == key ) .... O(n)
        flag=1 ... O(n) in worst case
}
```

$$O(1) + O(n) + O(n) + O(n) = O(n)$$

$$O(n) + O(n) + O(n)$$
$$= 2n + 3n + 4n \text{ (for example)}$$

$$= 9n$$

$\leq 10n$, for all values of n

$$= O(n)$$

[Since, Big O is upper bound
and we neglect constants in the
analysis]

```
for (int i=0; i<n; i++)  
{  
    for(int j=0; j<i; j++)  
    {  
        .....  
    }  
}
```

$i=0 \Rightarrow 0$ time

$i=1 \Rightarrow 1$ time

$i=2 \Rightarrow 2$ time

.....

$i=n-1 \Rightarrow n-1$ times

Sum of total steps

$= n * (n-1) / 2$

$= (n^2 - n) / 2$

$= O(n^2)$

[Neglect lower powers]

```
for (int i=1; i<=n; i=i*2)
{
    ....
}
```

1, 2, 4, 8 $\leq n$

no. of steps = $\log_2 (n)$

A quick note

```
# include <bits/stdc++.h>
```

= includes all STL libraries in c++

Common Errors in online platforms

1. Compile time error (CE)

2. Wrong answer (WA)

eg. Yes \neq YES .

So, read Input output format carefully

3. Time limit exceeded (TLE)

In general, Time Limit : 1 or 2 seconds

Improve the time complexity of code

Use fast I/O

4. Runtime error (RE) or
Segmentation Fault

FAST I/O with cin & cout

```
int main()
{
    ios_base::sync_with_stdio(false);
    cin.tie(NULL);
    cout.tie(NULL);

    .....
}
```

Reasons for Runtime Error (RE)

1. accessing out of bound index of array .

eg. `A[-1]` , `A[size]`, `A[size+2]`

2. divide by 0

eg. `4 / 0`, `a / 0`

3. for overflow : (also gives WA sometimes)

```
int a=1000000000, b=1000000000;
```

```
int c= a*b; //  $10^{14}$  , which is  $\gg 10^9$  (the range of int in C++)
```


Preventing overflows

```
int a, b;  
long long c = a + b ; // overflow still there
```

```
long long c = (long long)a + b ;  
// now, okay
```

```
long long a,b;  
c=a+b;  
// this is also okay but better, as saves time
```

Another note

$$O(1) < O(\log N) < O(\sqrt{N})$$

$$< O(N) < O(N \log N) < O(N^2) < O(N^3)$$

$$< O(N^4) \dots < O(2^N) < O(N^N)$$

In 1 second, 10^7 or 10^8
operations are performed :

Eg. $O(N^2)$, $N=10^3$ // work

$O(N \log N) = N = 10^5$ // work

$O(N^2)$, $N=10^5$ // will give TLE

```
float a =3.99322;  
float b=3.99322;  
if( a==b)  
cout<<"equal"; // bad practise  
// For floating point comparisons,  
// don't simply use ==  
// You would get Wrong Answer
```

```
const float eps = 0.0000001 ;//1e-6  
float a,b;  
if ( abs(a-b) <eps )  
    // good  
    // equality check
```

```
2.9090000000000001  
2.9090000000000002
```