COURSE: PHYSICS 1 (PHY 1101)
SEMESTER: SPRING [2021-2022]

CREDIT: 3 CREDIT HOURS

MARKS DISTRIBUTION

ATTENDANCE AND PERFORMANCE: 10 (10%)

ASSESSMENTS (QUIZZES) : BEST TWO OUT OF THREE : 40 (40 %)

MIDTERM ASSESSMENT: 50 (50%)

TOTAL = 100 POINTS/MARKS

Outline up to Mid term

Reference Book: Fundamentals of Physics (10th Edition)

Written by Halliday, Resnick and Walker

Book chapter no	Chapter name
4	Motion in Two and Three Dimensions
5	Force and Motion-I
6	Force and Motion-II
7 and 8	Kinetic Energy and Work And Conservation of Energy
9	Center of Mass and Linear Momentum
10	Rotation
11	Rolling, Torque, and Angular Momentum

Lecture 1

BOOK CHAPTER 4

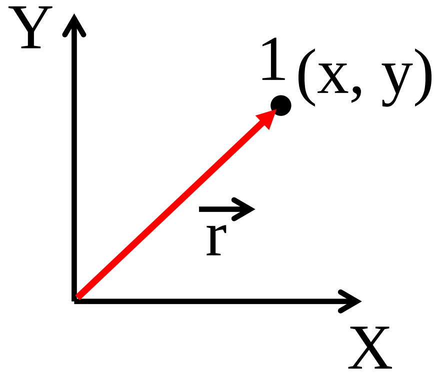
Motion in Two and Three Dimensions

Outline of Lesson 1

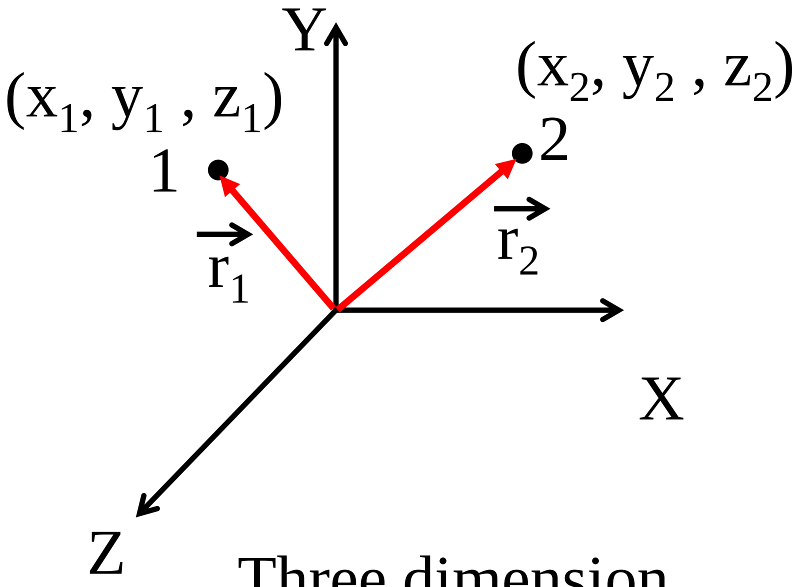
- Position and Displacement
- Average Velocity and Instantaneous Velocity
- Average Acceleration and Instantaneous Acceleration

Position:

One dimension



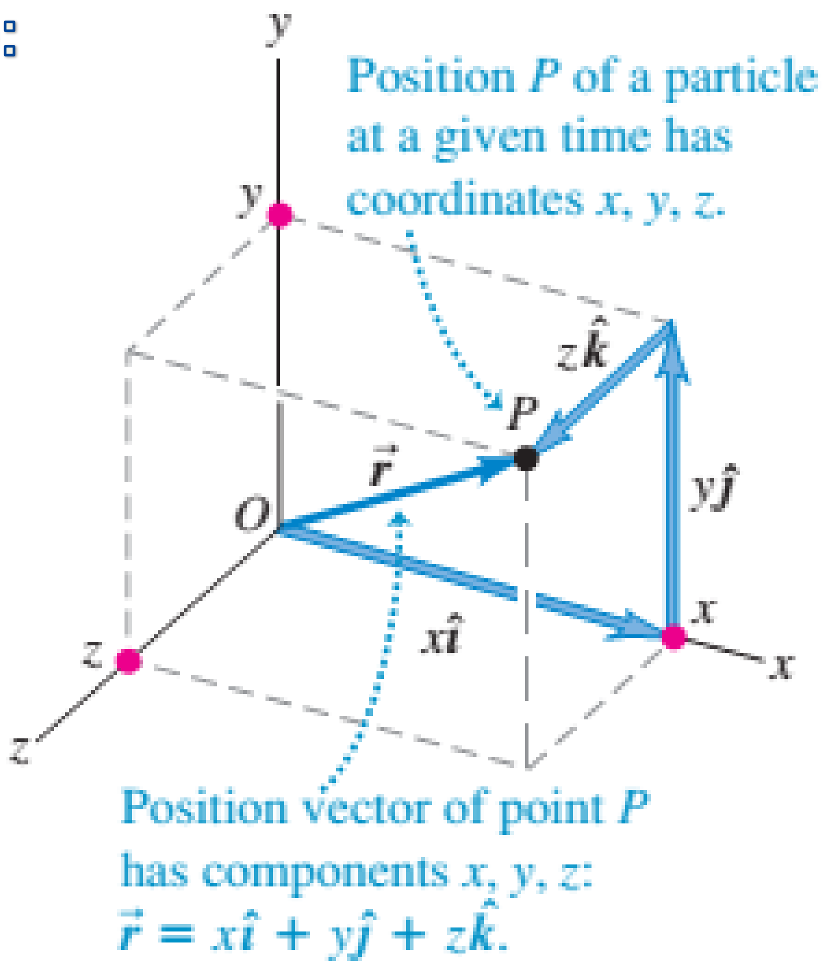
Two dimension



Three dimension

Position Vector (three-dimension):

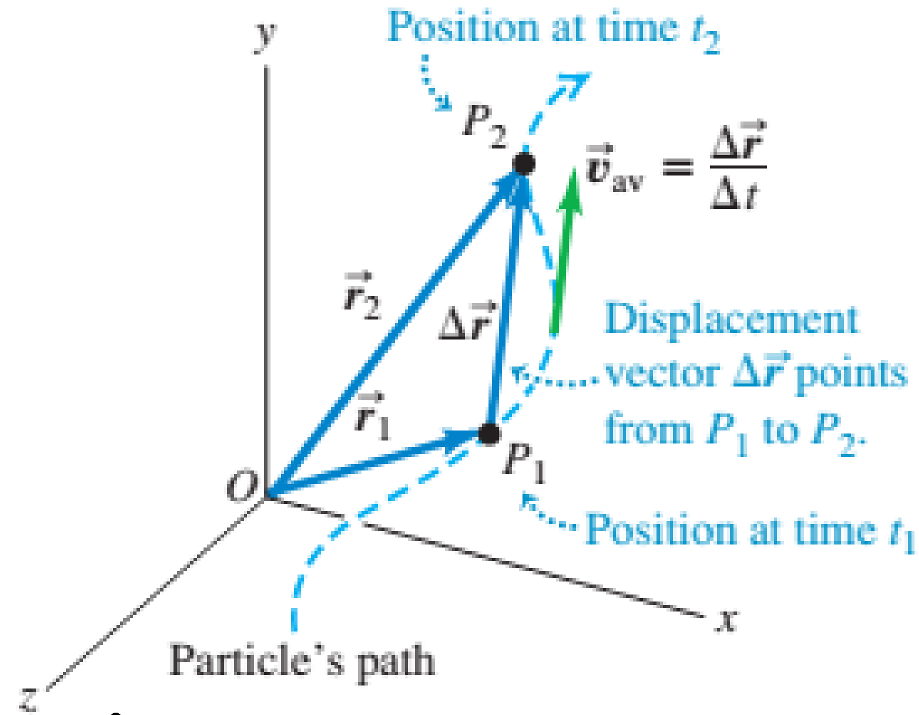
To describe the *motion* of a particle in space, we must first be able to describe the particle's *position.* Consider a particle that is at a point *P* at a certain instant. The **position vector** $\vec{r}$ of the particle at this instant is a vector that goes from the origin of the coordinate system to the point *P* (as shown in the figure). The Cartesian coordinates *x*, *y*, and *z* of point *P* are the *x*-, *y*-, and *z*-components of vector $\vec{r}$.Using the unit vectors we can write



$$\vec{r} = x\hat{\imath} + y\hat{\jmath} + z\hat{k}$$

Position Vector and Displacement Vector:

During a time interval Δt the particle moves from P_1, where its position vector is $\vec{r}_1$ to P_2, where its position vector is $\vec{r}_2$.The change in position (the displacement) during this interval is



$$\Delta\vec{r} = \vec{r}_2 - \vec{r}_1$$

$$\Delta\vec{r} = x_2\hat{\imath} + y_2\hat{\jmath} + z_2\hat{k} - \left(x_1\hat{\imath} + y_1\hat{\jmath} + z_1\hat{k}\right)$$

$$\Delta\vec{r} = (x_2 - x_1)\hat{\imath} + (y_2 - y_1)\hat{\jmath} + (z_2 - z_1)\hat{k}$$

$$Displacement, \Delta\vec{r} = \Delta x\hat{\imath} + \Delta y\hat{\jmath} + \Delta z\hat{k}$$

Average Velocity and Instantaneous Velocity:

If a particle moves through a displacement $\Delta\vec{r}$ in a time interval Δt, then its **average velocity** $\vec{v}_{avg}$ is

$$\vec{v}_{avg} = \frac{\vec{r}_2 - \vec{r}_1}{t_2 - t_1} = \frac{\Delta\vec{r}}{\Delta t}$$

Instantaneous velocity (simply, velocity $\vec{v}$) is the limit of the average velocity as the time interval approaches zero, and it equals the instantaneous rate of change of position with time. That is

$$\vec{v} = \lim_{\Delta t \to 0} \frac{\Delta \vec{r}}{\Delta t} = \frac{d\vec{r}}{dt}$$

The *magnitude* of the vector $\vec{v}$ at any instant is the *speed* of the particle at that instant. The *direction* of $\vec{v}$ at any instant is the same as the direction in which the particle is moving at that instant.

Note: At every point along the path, the instantaneous velocity vector is tangent to the path at that point.

- Create a particle's position vector as a function of time and evaluate its (instantaneous) velocity vector.

$$\vec{r}(t) = x\hat{\imath} + y\hat{\jmath} + z\hat{k}$$

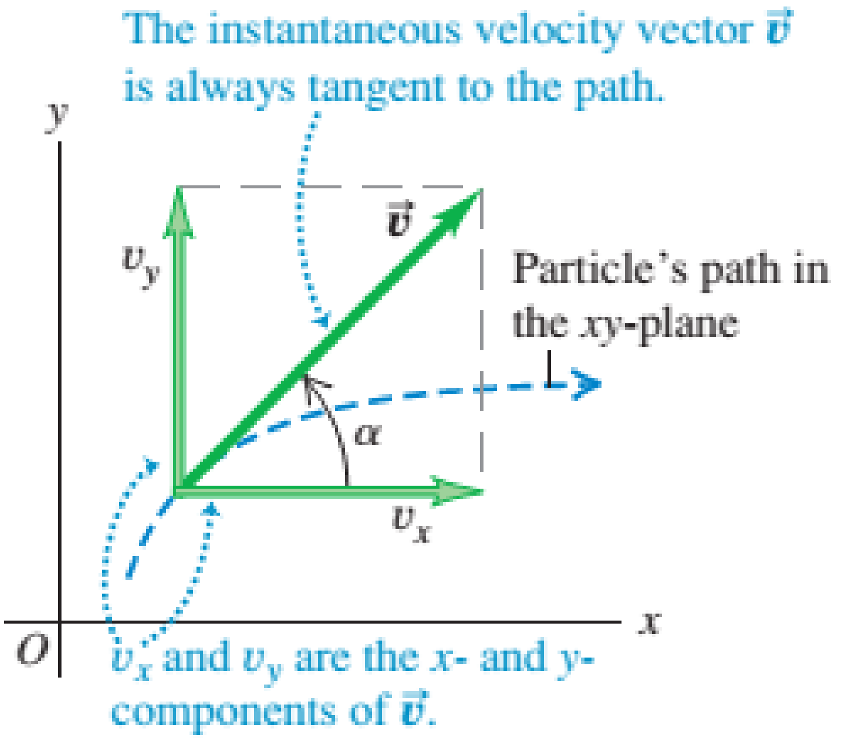
We have the definition of velocity vector,

$$\vec{v} = \frac{d\vec{r}}{dt}$$

$$\vec{v} = \frac{d}{dt}\,(x\hat{\imath} + y\hat{\jmath} + z\hat{k}) = \frac{dx}{dt}\hat{\imath} + \frac{dy}{dt}\hat{\jmath} + \frac{dz}{dt}\hat{k} = v_x\hat{\imath} + v_y\hat{\jmath} + v_z\hat{k}$$

The **magnitude** of the instantaneous velocity vector $\vec{v}$ —that is, the speed—is given in terms of the component v_x, v_y and v_z by the Pythagorean relation:

$$|\vec{v}| = v = \sqrt{v_x^2 + v_y^2 + v_z^2}$$



The adjacent Figure shows the situation when the particle moves in the *xy*-plane. In this case, *z* and v_z are zero. Then the speed (the magnitude of $\vec{v}$) is

$$v = \sqrt{v_x^2 + v_y^2}$$

The **direction** of the instantaneous velocity is given by the angle $\boldsymbol{\alpha}$ *(the* Greek letter alpha) in the figure.

$$\tan\alpha = \frac{v_y}{v_x}$$

And

$$\alpha = \tan^{-1}\frac{v_y}{v_x}$$

If a body's (or particle's) velocity changes from $\vec{v}_1$ to $\vec{v}_2$ in time interval Δt , its average acceleration during Δt is

$$\vec{a}_{avg} = \frac{\vec{v}_2 - \vec{v}_1}{t_2 - t_1} = \frac{\Delta\vec{v}}{\Delta t}$$

If Δt approaches to zero about some instant, then in the limit $\vec{a}_{avg}$ approaches the **instantaneous acceleration** (or **acceleration**) at that instant; that is,

$$\vec{a} = \lim_{\Delta t \to 0} \frac{\Delta\vec{v}}{\Delta t} = \frac{d\vec{v}}{dt}$$

- ❑ Create a particle's velocity vector as a function of time and evaluate its (Instantaneous) acceleration vector.

$$\boldsymbol{\vec{v}(t)} = v_x\boldsymbol{\hat{\imath}} + v_y\boldsymbol{\hat{\jmath}} + v_z\boldsymbol{\hat{k}}$$

$$\vec{a} = \frac{d\vec{v}}{dt} = \frac{d}{dt}\left(v_x\boldsymbol{\hat{\imath}} + v_y\boldsymbol{\hat{\jmath}} + v_z\boldsymbol{\hat{k}}\right) = \frac{dv_x}{dt}\hat{\imath} + \frac{dv_y}{dt}\hat{\jmath} + \frac{dv_z}{dt}\hat{k}$$

$$\boxed{\vec{a} = a_x\hat{\imath} + a_y\hat{\jmath} + a_z\hat{k}}$$

Problem 3 (Book chapter 4)

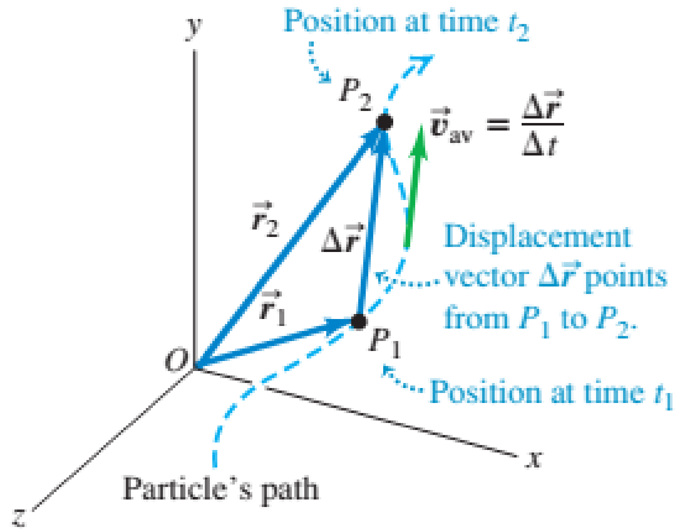
A positron undergoes a displacement $\Delta\vec{r} = 2\hat{\imath} - 3\hat{\jmath} + 6\hat{k}$, ending with the position vector $\vec{r} = 3\hat{\jmath} - 4\hat{k}$, in meters. What was the positron's initial position vector?

Answer:

$$\vec{r}_1 + \Delta\vec{r} = \vec{r}$$

$$\vec{r}_1 = \vec{r} - \Delta\vec{r} = 3\hat{\jmath} - 4\hat{k} - \left(2\hat{\imath} - 3\hat{\jmath} + 6\hat{k}\right) = 3\hat{\jmath} - 4\hat{k} - 2\hat{\imath} + 3\hat{\jmath} - 6\hat{k}$$

$$\boxed{\vec{r}_1 = -2\hat{\imath} + 6\hat{\jmath} - 10\hat{k}}$$



Problem 13 (Book chapter 4)

A particle moves so that its position (in meters) as a function of time (in seconds) is $\vec{r} = \hat{\imath} + 4t^2\hat{\jmath} + t\hat{k}$. Write expressions for (a) its velocity and (b) its acceleration as functions of time.

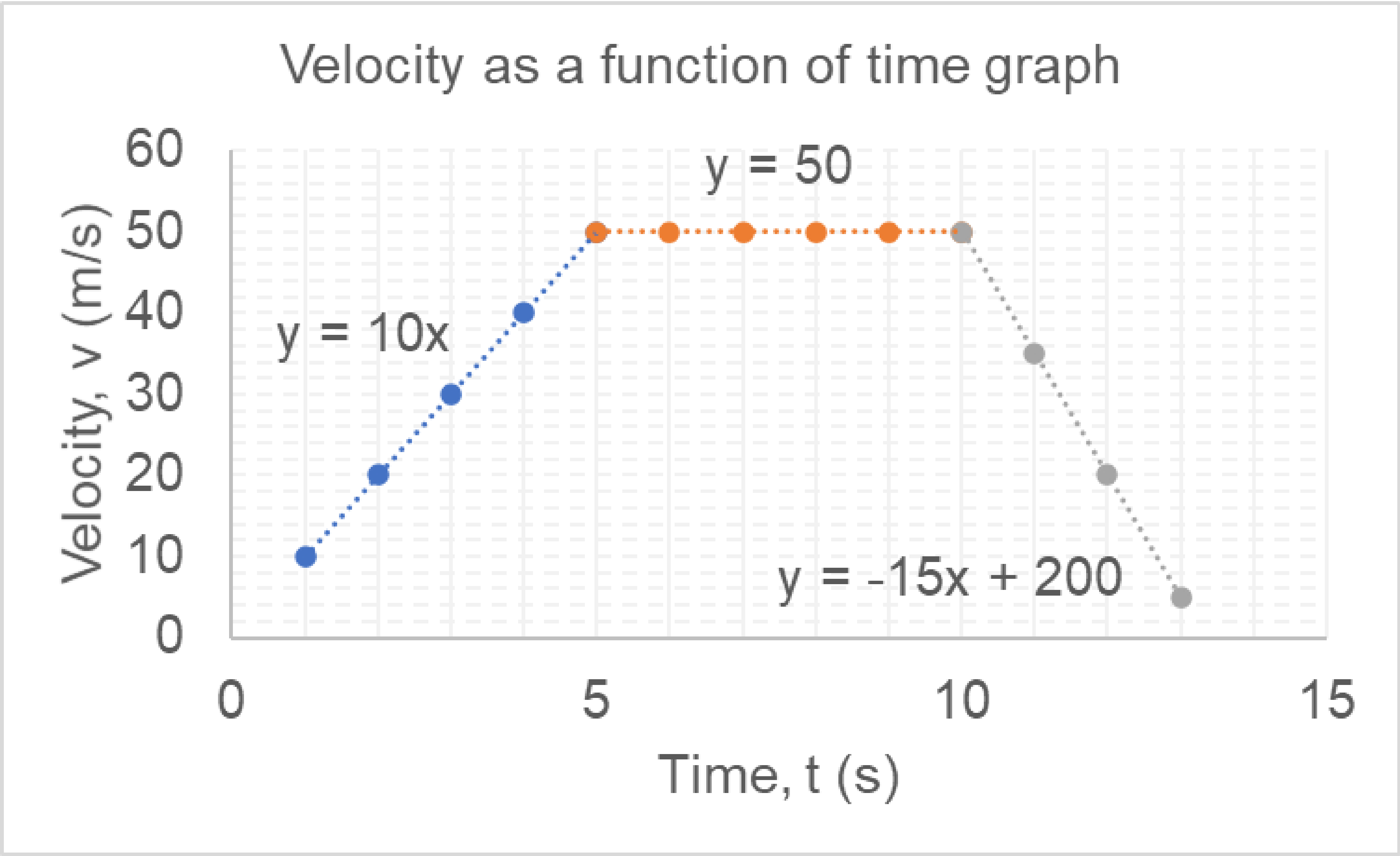
Answer:

We have $$\vec{v} = \frac{d\vec{r}}{dt}$$

$$\vec{v} = \frac{d}{dt}\left(\hat{\imath} + 4t^2\hat{\jmath} + t\hat{k}\right) = 0 + 8t\,\hat{\jmath} + \hat{k} = 8t\,\hat{\jmath} + \hat{k}$$

Again, we have $$\vec{a} = \frac{d\vec{v}}{dt}$$

$$\vec{a} = \frac{d}{dt}\left(8t\,\hat{\jmath} + \hat{k}\right) = 8\,\hat{\jmath} + 0 = 8\,m/s^2\,\hat{\jmath}$$


Velocity as a function of time graph
Velocity, v (m/s)
Time, t (s)
y = 10x
y = 50
y = -15x + 200
0
10
20
30
40
50
60
0
5
10
15