



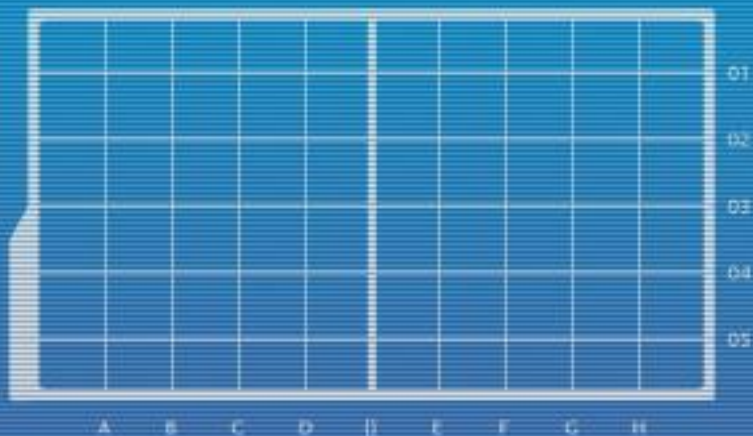
DEPARTMENT OF
INFORMATION SYSTEMS
AND COMPUTER SCIENCE

Basic Applications of Physics II

Aiming for Collisions



```
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Lecture Time!

- ▶ Collision Response: Mass Effect
- ▶ Impulse: Because Force Takes Too Long

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DISCS

Collision

- After determining acceleration and computing for new positions and velocities, check for collision

```
// the code template below is wrong
```

```
// what should it be?
```

```
for( int i = 0; i < numObjects; i++ )  
{  
    // move object[i]  
    // collision check for object[i]  
}
```

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Collision

- Would there be a problem moving the object, checking for its collisions, then moving the next object (and repeating)?

```
// the code template below is wrong
```

```
// what should it be?
```

```
for( int i = 0; i < numObjects; i++ )
```

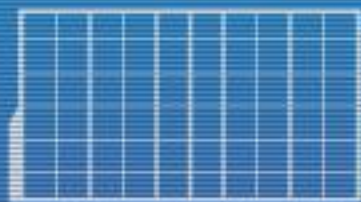
```
{
```

```
    // move object[i]
```

```
    // collision check for object[i]
```

```
}
```

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DISCS

Collision

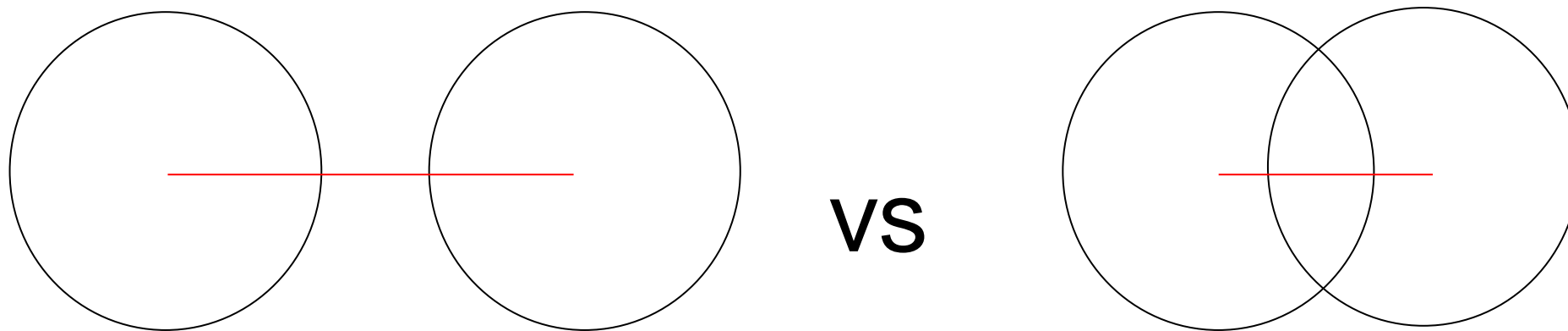
- ▶ First, do a pairwise check for overlap
 - ▶ For shapes other than circles, you'll have to figure that out yourself (or wait for later lessons for convex polygons)
- ▶ Then, if there is overlap, check if the two objects are actually moving into each other
 - ▶ Both stationary or moving away from each other? No collision!

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Collision

- ▶ Check for overlap between circles by comparing radii and distance
 - ▶ If the sum of the radii is greater than the distance between centers, what does that mean for circle collision?



Collision (After Overlap Check)

- ▶ First, determine a normal vector for the point of collision
 - ▶ Easy for circles – it's the vector we use to determine distance
 - ▶ Easy for edges – it's a vector perpendicular to the edge (facing away)
 - ▶ For other stuff – you'll have to look it up

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Collision (After Overlap Check)

- ▶ Next, determine relative velocity of one object to the other
 - ▶ Relative velocity of object A to object B
 $= \text{velocity_of_A} - \text{velocity_of_B}$
 - ▶ **IMPORTANT:** ALL equations (including the one above) in this slide set assume collision normal is pointing from object B to object A

Collision (After Overlap Check)

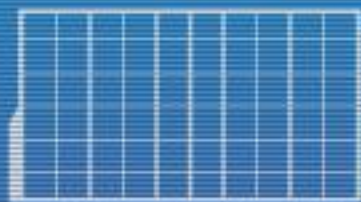
- ▶ At this point, you have a collision normal vector and a relative velocity vector
 - ▶ What does it mean if they're pointing away from each other?
 - ▶ What does it mean if they're pointing in more or less the same direction?
 - ▶ And how do we determine where they're pointing (relative to each other) in code?



Collision (After Overlap Check)

- ▶ If the relative velocity vector is pointing away from the collision vector (more than 90 degrees) then you have a collision
- ▶ Now we should determine what happens as a result of the collision
 - ▶ In other words, we need to use various collision response equations
 - ▶ No need to normalize collision normal for now

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Impulse

- ▶ Since we need to change object velocities instantaneously, we need to compute for impulse and apply it to the object velocities
 - ▶ Can't rely on applying forces normally because it'll take at least one timestep for the resulting change in accelerations to affect velocities

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Impulse

- ▶ However, just like friction, the effect of impulse depends on the objects' masses
 - ▶ Lighter objects should be more easily moved
 - ▶ Incredibly heavy objects (i.e. infinite mass) shouldn't budge at all
 - ▶ We're actually changing momentum (which affects velocity)



Impulse

- ▶ How impulse (j) will be used:
 - ▶ $\text{new_velocity_of_A} = \text{old_velocity_of_A} + ((j / \text{mass_of_A}) * \text{collision_normal})$
 - ▶ $\text{new_velocity_of_B} = \text{old_velocity_of_B} - ((j / \text{mass_of_B}) * \text{collision_normal})$
 - ▶ Remember: Collision normal is assumed to point from B to A

Impulse

- Solving for impulse:
 - $$\frac{-(1 + \text{elastic_coefficient}) \cdot (\text{relative_velocity} \bullet \text{collision_normal})}{(\text{collision_normal} \bullet \text{collision_normal}) \cdot (\text{reciprocal_of_mass_of_A} + \text{reciprocal_of_mass_of_B})}$$

Impulse

► Solving for impulse:

$$\begin{aligned} & \text{► } - ((1 + \text{elastic_coefficient}) \\ & \quad * (\text{relative_velocity} \bullet \text{collision_normal})) \\ & / \\ & ((\text{collision_normal} \bullet \text{collision_normal}) \\ & \quad * (\text{reciprocal_of_mass_of_A} \\ & \quad + \text{reciprocal_of_mass_of_B}))) \end{aligned}$$

► With circles, if you got this far, you already solved for this... what is it?

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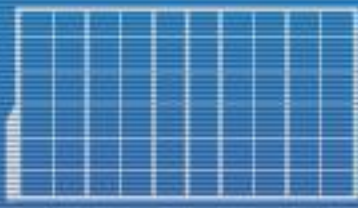
Impulse

► Solving for impulse:

$$\begin{aligned} &\text{► } - \left((1 + \text{elastic_coefficient}) \right. \\ &\quad \left. * \left(\text{relative_velocity} \bullet \text{collision_normal} \right) \right) \\ &\quad / \\ &\quad \left(\left(\text{collision_normal} \bullet \text{collision_normal} \right) \right. \\ &\quad \left. * \left(\text{reciprocal_of_mass_of_A} \right. \right. \\ &\quad \left. \left. + \text{reciprocal_of_mass_of_B} \right) \right) \end{aligned}$$

► You also already solved for this... when?

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DISCS

Homework

- ▶ Modify your previous homework:
 - ▶ Your program should now require a command-line argument X that is an integer between 1 and 35, inclusive
 - ▶ In addition to the player-controlled circle, create X more circles
 - ▶ Positions should no longer be random to avoid initial overlapping



Homework

- ▶ Modify your previous homework (continued):
 - ▶ These circles are also air hockey pucks, but the only time they should move is when another puck collides with them
 - ▶ Make sure none of the circles are initially overlapping (player-controlled circle included)

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Homework

- ▶ Modify your previous homework (continued):
 - ▶ All non-player-controlled pucks should have the same mass
 - ▶ Their mass can be the same as the mass of the player-controlled one, but provide a way to easily change the mass of either the player puck or the other X pucks in between compilations

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Homework

- ▶ Modify your previous homework (continued):
 - ▶ Friction should still be a toggle
 - ▶ Collision with the edges of the program window should still be totally elastic
 - ▶ Both friction (if enabled) and window edge collision should also apply to the non-player-controlled circles

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