IMAGE PROCESSING & ANALYSIS

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Image enhancement

Point operations

Local operations

Noise reduction / Image smoothing

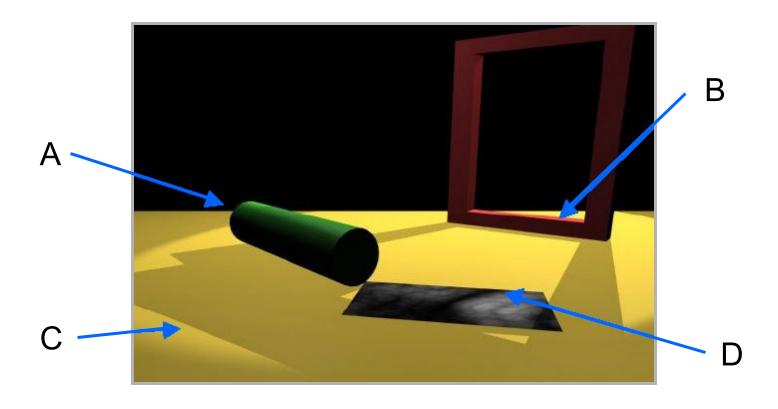
Edge & Line detection

Edge detection First order & second order detectors



- What's an edge?
 - "He was sitting on the edge of his seat."
 - "I almost ran off the edge of the road."
 - "She was standing by the <u>edge of the woods</u>."
 - "Film negatives should only be handled by their <u>edges</u>."
 - "She paints with a <u>hard edge</u>."
 - "We are on the <u>edge of tomorrow</u>."
 - "He likes to live life on the <u>edge</u>."
 - "She is feeling rather <u>edgy</u>."
- The definition of edge is not always clear.
- In Computer Vision, <u>edge</u> is usually related to a <u>discontinuity</u> within a <u>local set of pixels</u>.

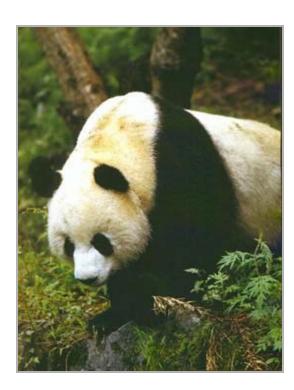




- A: <u>Depth</u> discontinuity: abrupt depth change in the world
- B: Surface normal discontinuity: change in surface orientation
- C: <u>Illumination</u> discontinuity: shadows, lighting changes
- D: Reflectance discontinuity: surface properties, markings



- Devise computational algorithms for the extraction of significant edges from the image.
- What is meant by <u>significant</u> is <u>unclear</u>.
 - Partly defined by the <u>context</u> in which the edge detector is being applied

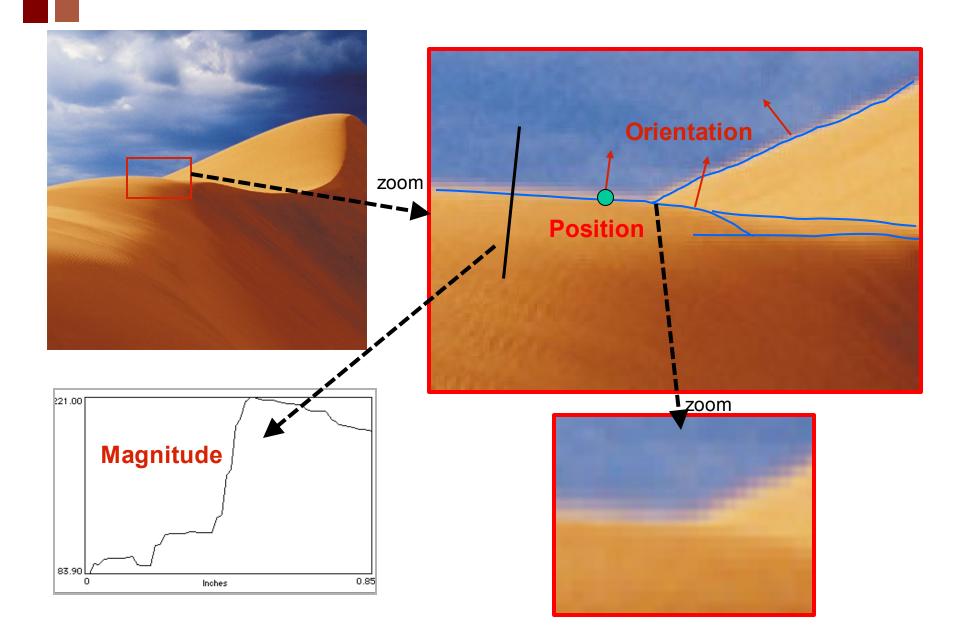






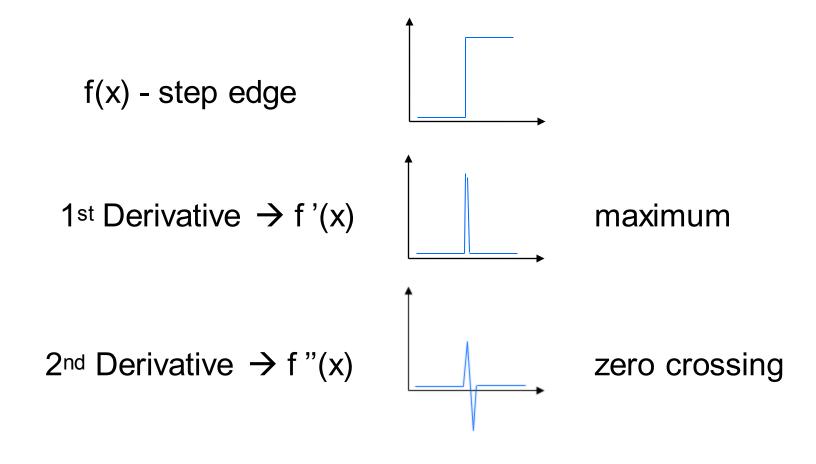
- Define a <u>local edge</u> or <u>edgel</u> to be
 a <u>rapid change</u> in the image function <u>over a small area</u>
 - implies that edgels should be detectable over a local neighborhood
- Edgels are NOT contours, boundaries, or lines
 - edgels <u>may lend support</u> to the existence of those structures
 - these structures are typically constructed from edgels
- Edgels have properties
 - Position
 - Orientation
 - Magnitude







Rapid change in image => high local gradient => differentiation



Edge degradation by noise

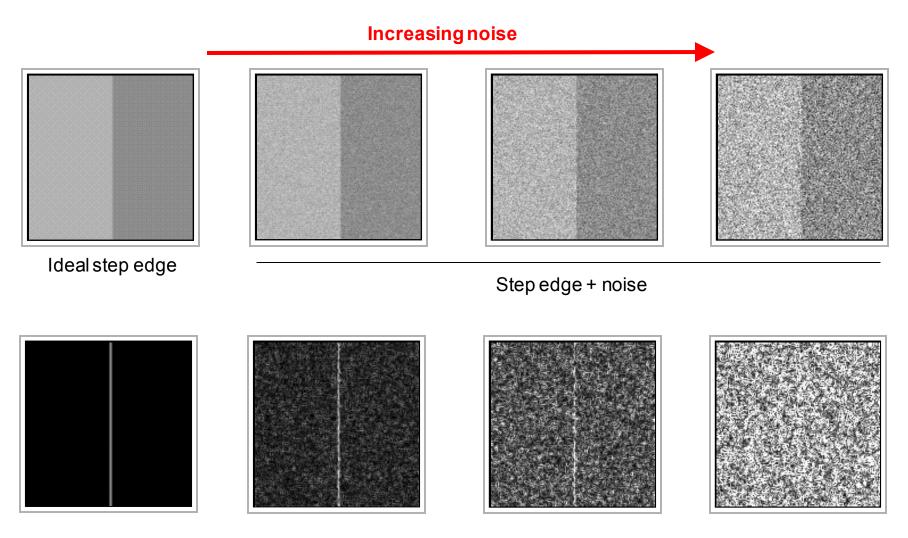


image gradient







Edge Detection: typical steps

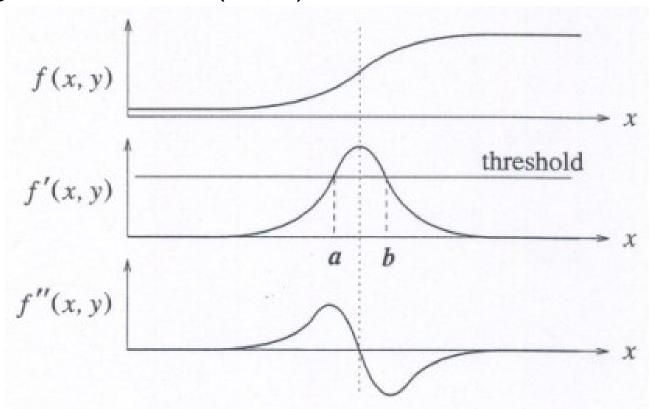
Noise Smoothing

- Suppress as much noise as possible while retaining 'true' edges
- In the absence of other information,
 assume noise with a Gaussian distribution
- Edge Enhancement
 - Design a filter that responds to edges;
 high filter output at edge pixels and low elsewhere
- Edge Localization
 - Determine which edge pixels should be discarded as noise and which should be retained
 - thin wide edges to 1-pixel width (<u>nonmaximum suppression</u>)
 - establish minimum value to declare a local maximum from edge filter to be an edge (<u>thresholding</u>)





Edge Localization (cont.)



If a threshold is used for detection of edges, all points between a and b will be marked as edge pixels. However, by removing points that are not a local maximum in the first derivative, edges can be detected more accurately.

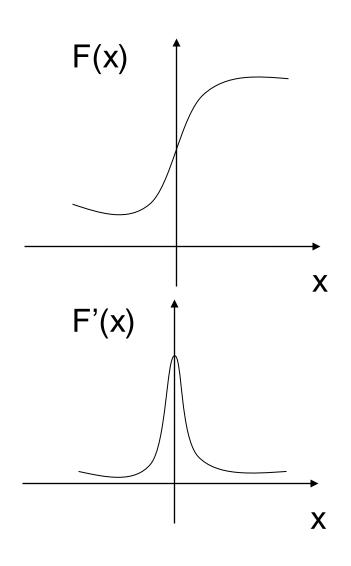
This local maximum in the first derivative corresponds to a zero crossing in the second derivative.

Edge Detection Methods



- Gradient edge detection
 - Prewitt & Sobel detectors
- Compass edge detection
- Canny edge detector
- 2nd Derivative estimate
 - Laplacian
 - Difference of Gaussians
- Parametric Edge Models





Edge= sharp variation



Large first derivative



Assume f is a continuous function in (x,y). Then

$$\Delta_x = \frac{\partial f}{\partial x}, \quad \Delta_y = \frac{\partial f}{\partial y}$$

- are the rates of change of the function f in the x and y directions, respectively.
- The vector (Δ_x, Δ_y) is called the gradient of f.
- This vector has a <u>magnitude</u>: $S = \sqrt{\Delta_x^2 + \Delta_y^2}$

and an orientation:
$$\theta = \tan^{-1} \left(\frac{\Delta_y}{\Delta_x} \right)$$

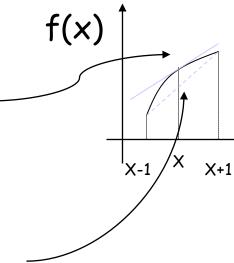
- \bullet is the direction of the maximum change in f.
- S is the size of that change.

Digital approximation



$$\frac{df(x)}{dx} = \lim_{\Delta x \to 0} \frac{f(x + \Delta x) - f(x)}{\Delta x}$$

Convolve with:



$$\frac{df(x)}{dx} \cong \frac{f(x+1) - f(x-1)}{2}$$



Convolve with:

-1	0	1



1x2 Example







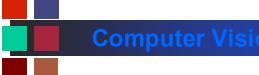
1x2 Horizontal



Combined



Smoothing and Edge Detection



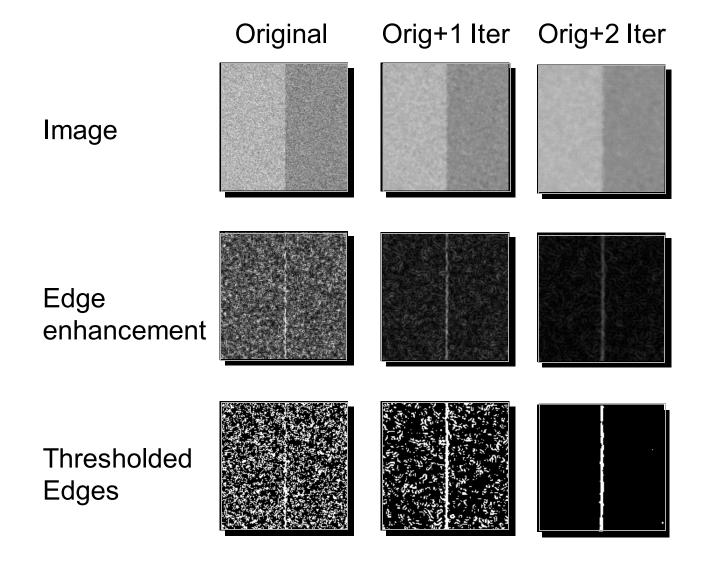
- Derivatives are 'noisy' operations
 - edges are a high spatial frequency phenomenon
 - edge detectors are sensitive to and emphasize noise
- Averaging reduces noise
 - spatial averages can be computed using masks

	1	1	1		1	2	1
1/9 x	1	1	1	1/16 x	2	4	2
	1	1	1		1	2	1

Combine smoothing with edge detection.





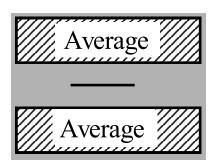




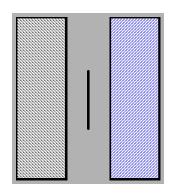
CompCombining Smoothing and Edge Detection

Applying simple averaging before differencing is equivalent to taking the difference of averages on either side of the central pixel.

-1	-1	-1
0	•	0
1	1	1



-1	0	1
-1	•	1
-1	0	1





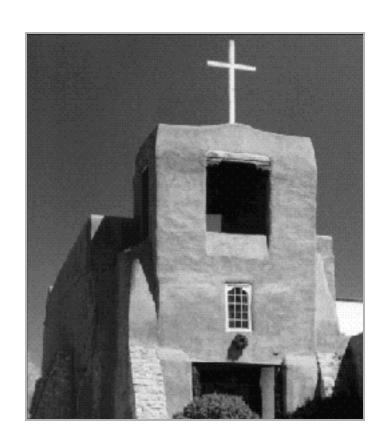
$$P_1 = \begin{array}{c|cccc} -1 & -1 & -1 \\ \hline 0 & 0 & 0 \\ \hline 1 & 1 & 1 \end{array}$$

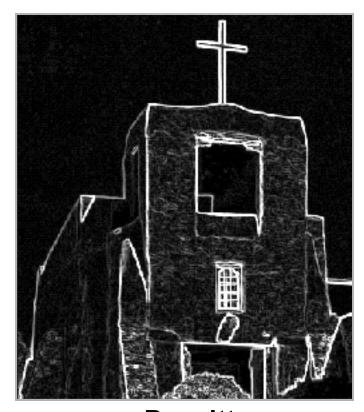
$$P_2 = \begin{array}{|c|c|c|c|c|} -1 & 0 & 1 \\ -1 & 0 & 1 \\ -1 & 0 & 1 \end{array}$$

Edge Magnitude =
$$\sqrt{P_1^2 + P_2^2}$$

Edge Direction =
$$tan^{-1} \left[\frac{P_1}{P_2} \right]$$







Prewitt
horizontal and vertical edges
combined



Kernels

$$S_1 = \begin{vmatrix} -1 & -2 & -1 \\ 0 & 0 & 0 \\ 1 & 2 & 1 \end{vmatrix}$$

$$S_2 = \begin{vmatrix} -1 & 0 & 1 \\ -2 & 0 & 2 \\ -1 & 0 & 1 \end{vmatrix}$$

Gradient/Edge Magnitude =
$$\sqrt{S_1^2 + S_2^2}$$

Gradient Direction =
$$tan^{-1} \left(\frac{S_1}{S_2} \right)$$

NOTES:

- 1) S₁, S₂ represent responses to the kernels (above), not the kernel themselves
- 2) Gradient direction is perpendicular to edge direction

Anatomy of the Sobel

 -1
 0
 1

 -2
 0
 2

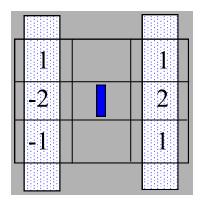
 -1
 0
 1

$$= 1/4 * \begin{bmatrix} -1 & 0 & -1 \end{bmatrix} \otimes \begin{bmatrix} 1 \\ 2 \\ 1 \end{bmatrix}$$

1/4 0 0 0 -1 -2 -1

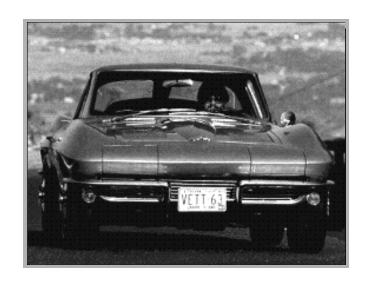
$$= 1/4 * [1 2 1] \otimes \begin{bmatrix} 1 \\ 0 \\ -1 \end{bmatrix}$$

Sobel kernel is separable!



Averaging done parallel to edge





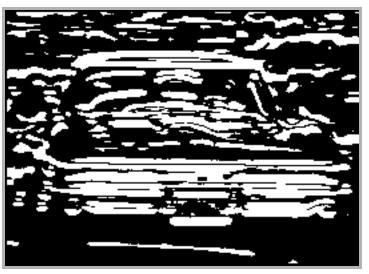
The Intel IPP library, gives the 5x5 horizontal kernel as

1 2 0 -2 -1 4 8 0 -8 -4

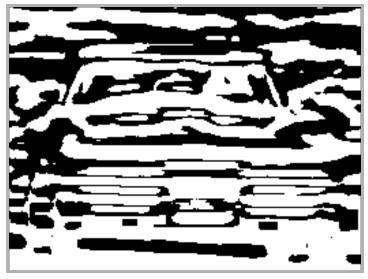
6 12 0 -12 -6

4 8 0 -8 -4

1 2 0 -2 -1

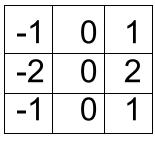


7x7 horizontal edges (only)



13x13 horizontal edges (only)

Robinson Compass Masks



0	1	2
-1	0	1
-2	-1	0

1	2	1
0	0	0
-1	-2	-1

2	1	0
1	0	-1
0	-1	-2









1	0	-1
2	0	-2
1	0	-1

0	-1	-2
1	0	-1
2	1	0

-1	-2	-1
0	0	0
1	2	1

-2	-1	0
-1	0	1
0	1	2





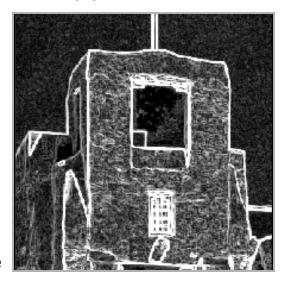


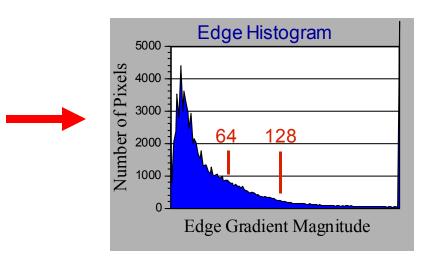


- Select largest response (magnitude)
- Orientation is the direction associated with the largest response

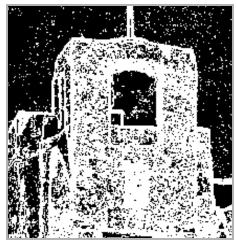


Global approach





edge magnitude



thresholding results

T=64

T=128





- **Edge detection** involves 3 **steps**:
 - Noise smoothing
 - Edge enhancement
 - Edge localization
- J. Canny formalized these steps to design an optimal edge detector
 - J.F. Canny, "A computational approach to edge detection", IEEE Trans. Pattern Anal. Machine Intelligence (PAMI), vol. PAMI vii-g, pp. 679-697, 1986.
- based on a set of <u>criteria</u> that should be satisfied by an edge detector:
 - Good detection. There should be a minimum number of false negatives and false positives.
 - Good localization. The edge location must be reported as close as possible to the correct position.
 - Single response. Only one response to a single edge.
- Probably, most widely used edge detector



Stage 1. Image Smoothing

 The image data is smoothed by a Gaussian function of width specified by the user parameter (σ).

Stage 2. Differentiation

- The smoothed image, retrieved at Stage 1, is differentiated with respect to the directions x and y.
- From the computed gradient values x and y, the magnitude and the angle of the gradient can be calculated



2

3

Stage 3. Non-Maximum Suppression

- The edges can be located at the points of local maximum gradient magnitude.
- It is done via <u>suppression</u> of non-maxima, that is, points, whose <u>gradient magnitudes are not local maxima</u>.
- Non-maxima <u>perpendicular to the edge direction</u>, rather than those in the edge direction, have to be suppressed,
- The algorithm starts off by reducing the <u>angle of gradient</u> to <u>one of the four sectors</u> shown in Figure.
- The algorithm passes the 3x3 neighborhood across the magnitude array.
 At each point the center element of the neighborhood is compared with its two neighbors along line of the gradient given by the sector value.
- If the central value is non-maximum, that is, not greater than the neighbors, it is suppressed.



Stage 4. Edge Thresholding

- The Canny operator uses the so-called "<u>hysteresis</u>" thresholding.
- Most thresholders use a single threshold limit, which means that if the edge values fluctuate above and below this value, the line appears broken.
 - This phenomenon is commonly referred to as "streaking".
- Hysteresis counters streaking by setting an upper and lower edge value limit.
- Considering a line segment,
 - If a value lies above the upper threshold limit it is immediately accepted.
 - If the value lies below the low threshold it is immediately rejected.
 - Points which lie between the two limits are accepted if they are connected to pixels which exhibit strong response.
- The likelihood of streaking is reduced drastically since the line segment points must fluctuate above the upper limit and below the lower limit for streaking to occur.
- <u>J. Canny</u> recommends in [Canny86] the <u>ratio of high to low limit</u> to be in the range of <u>two or three to one</u>, based on predicted signal-to-noise ratios.



Canny Edge Detector



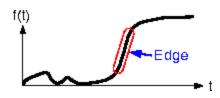
Original image

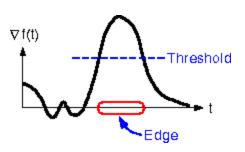


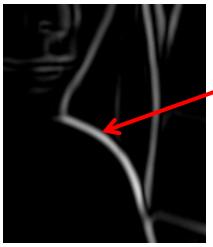
Gradient magnitude



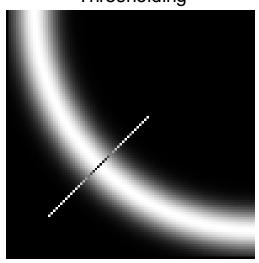
Thresholding







How to turn these thick regions of the gradient into curves?



Non-maximum supression

Hysteresis thresholding





Problem: pixels along this edge didn't survive the thresholding



Hysteresis thresholding

 Use a high threshold to start edge curves, and a low threshold to continue them.





original image



high threshold (strong edges)



Iow threshold (weak edges)



hysteresis threshold







 σ =1, T2=255, T1=1

Hysteresis threshold method allows to add weaker edges (those above T1) if they are neighbors of stronger edges (those above T2).





 σ =1, T2=255, T1=220



 σ =1, T2=128, T1=1

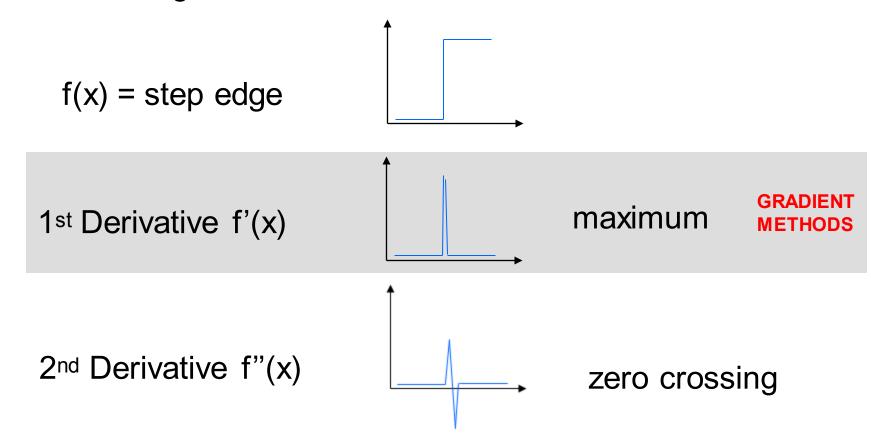


 σ =2, T2=128, T1=1

M. Heath, S. Sarkar, T. Sanocki, and K.W. Bowyer, "A Robust Visual Method for Assessing the Relative Performance of Edge-Detection Algorithms" IEEE Transactions on Pattern Analysis and Machine Intelligence, Vol. 19, No. 12, December 1997, pp. 1338-1359.

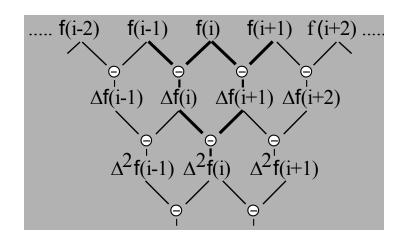


 Digital gradient operators estimate the first derivative of the image function in two or more directions.





- Second derivative = rate of change of 1st derivative.
- Maxima of first derivative = zero crossings of 2nd derivative.
- For a discrete function, derivatives can be approximated by differencing.
- Consider the one dimensional case:



$$\Delta^2 f(i) = \Delta f(i+1) - \Delta f(i)$$

= f(i+1) - 2 f(i) + f(i-1)

Mask: 1 -2 1



- Now consider a two-dimensional function f(x,y).
- Can be shown that the smallest possible isotropic second derivative operator is the Laplacian:

$$\nabla^2 f = \frac{\partial^2 f}{\partial x^2} + \frac{\partial^2 f}{\partial y^2}$$

Two-dimensional discrete possible approximations:

	1	
1	-4	1
	1	

1	1	1
1	-8.	1
1	1	1

-1	2	-1
2	-4	2
-1	2	-1

Example Laplacian Kernels

9X9

Note that these are <u>not</u> the <u>optimal</u> approximations to the Laplacian of the sizes shown.

Example Application



5x5 Laplacian filter

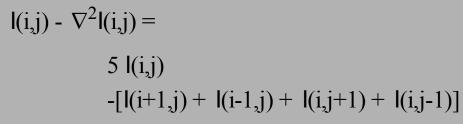


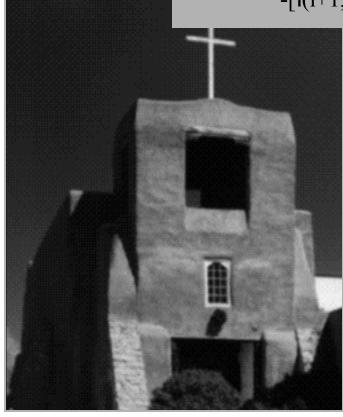
9x9 Laplacian filter

- Edges are located at zero crossings.
- To avoid detection of insignificant edges, only the zero crossings whose corresponding first derivative is above some threshold should be selected as edge points.
- Note: for display purpose, zero is represented as a mid-level gray.

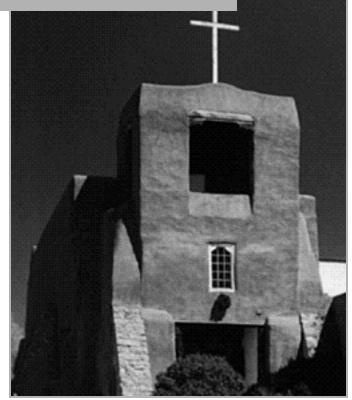


Computer Vision Enhancement using the Laplacian





Blurred original



3x3 Laplacian enhanced

Effect is one of deblurring the image



- Marr and Hildreth approach:
 - 1. Apply Gaussian smoothing using σ 's of increasing size:

2. Take the Laplacian of the resulting images:

$$\nabla^2 (G \circledast I)$$

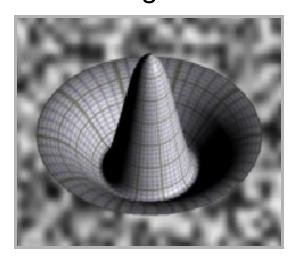
- 3. Look for zero crossings.
- Second expression can be written as: $(\nabla^2 G) \circledast I$
- Thus, can take <u>Laplacian of the Gaussian</u> (LoG) and use that as the operator.

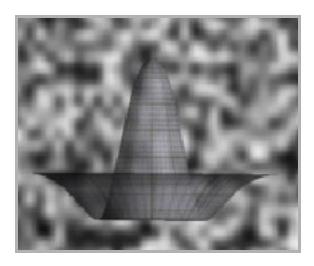


Laplacian of the Gaussian

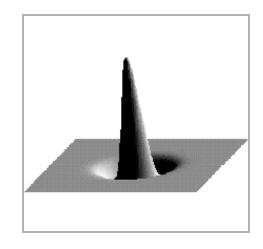
$$\nabla^{2}G(x,y) = \frac{-1}{\pi\sigma^{4}} \left[1 - \frac{(x^{2} + y^{2})}{2\sigma^{2}} \right] e^{-\left[\frac{(x^{2} + y^{2})}{2\sigma^{2}}\right]}$$

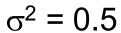
- ho ∇^2 G is a circularly symmetric operator.
- Also called the hat or Mexican-hat operator.
- Sometimes <u>approximated as the difference of 2 Gaussians</u> with different sigma values

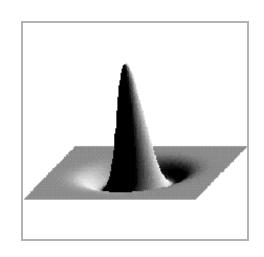




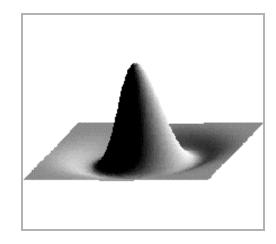








 $\sigma^2 = 1.0$



 $\sigma^2 = 2.0$



5x5

17 x 17





13x13 Kernel





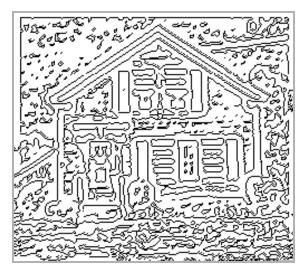
13 x 13 LoG filter



Thesholded Negative



The sholded Positive

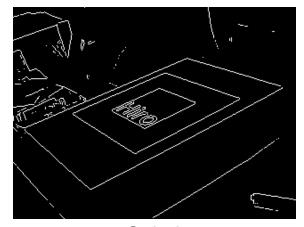


Zero Crossings

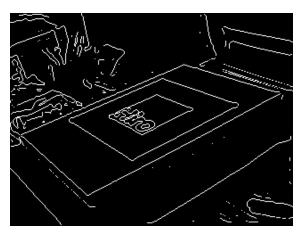




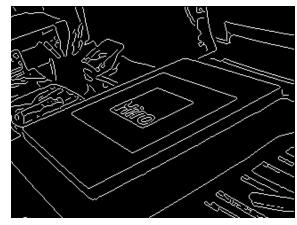
Original image



Sobel



LoG



Canny

(detection thresholds automatically chosen by Matlab functions)

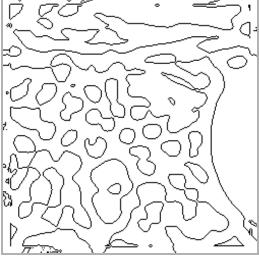








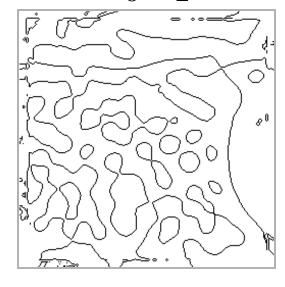
$$\sigma^2 = \sqrt{2}$$



$$\sigma^2 = 2\sqrt{2}$$

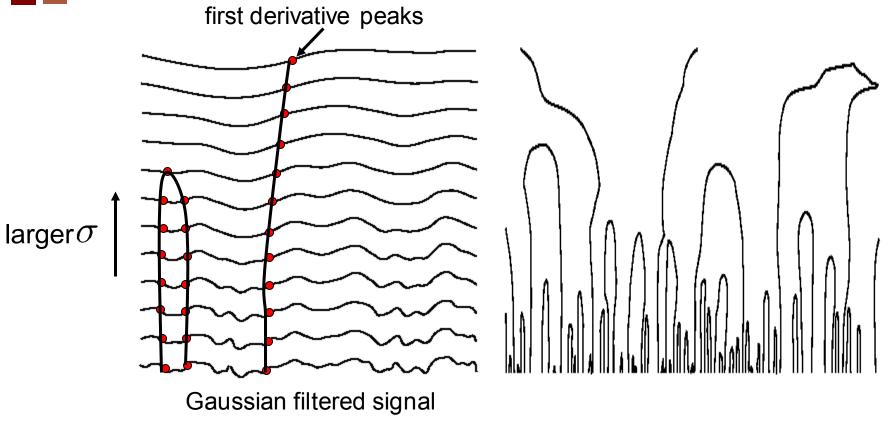


$$\sigma^2 = 2$$



$$\sigma^2 = 4$$

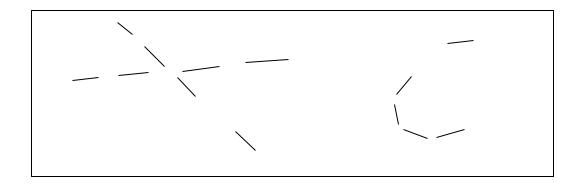




- Properties of scale space (w/ Gaussian smoothing) Witkin'83
 - edge position may shift with increasing scale (σ)
 - two edges may merge with increasing scale
 - an edge may not split into two with increasing scale



Given local edge elements:



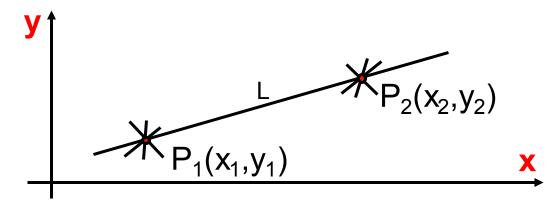
- Can we organize these into more 'complete' structures, such as straight lines?
- Group edge points into lines?
- Consider a fairly simple technique...



- Given a set of local edge elements
 - with or without orientation information
- How can we extract longer straight lines?
- General idea:
 - Find an <u>alternative space in which lines map to points</u>
 - Each edge element 'votes' for the straight line which it may be a part of.
 - Points receiving a <u>high number of votes</u> might correspond to actual <u>straight lines</u> in the image.
- The idea behind the Hough transform is that a change in representation converts a point grouping problem into a peak detection problem



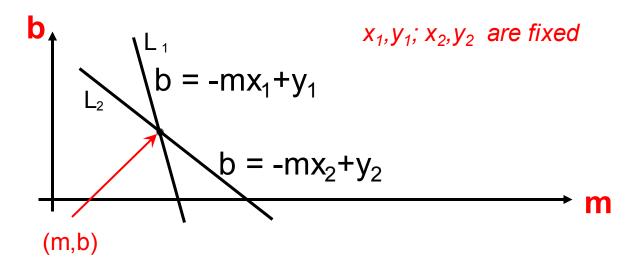
Consider two (edge) points, P(x,y) and P'(x',y') in image space:



- The set of all lines through P=(x,y) is
 - y=mx + b, for appropriate choices of m and b.
- But this is also the equation of a line in (m,b) space, or parameter space
 - $\mathbf{b} = -\mathbf{xm} + \mathbf{y}$



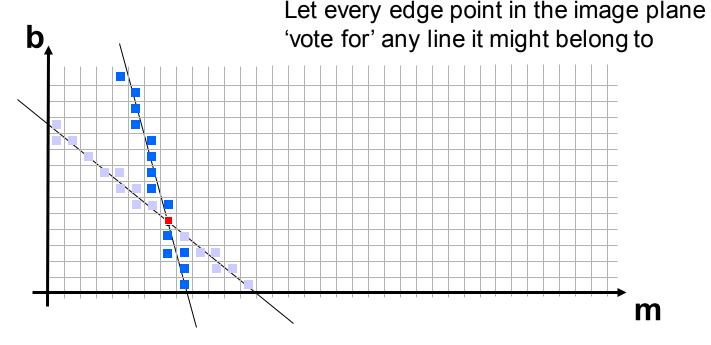
The intersection represents the parameters of the equation of a line y=mx+b going through both (x1,y1) and (x2,y2).



- The more colinear edgels there are in the image, the more lines will intersect in parameter space
- Leads directly to an algorithm (Hough Transform)

Quantized Parameter Space





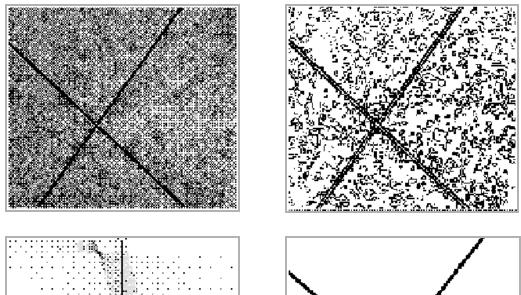
single votes two votes

The problem of line detection in image space has been transformed into the problem of cluster detection in parameter space

Edges

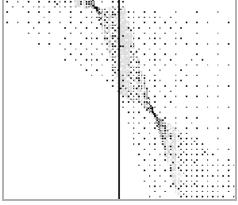


The problem of <u>line detection in image space</u>
 has been transformed into
 the problem of <u>cluster detection in parameter space</u>



Accumulator Array

Image

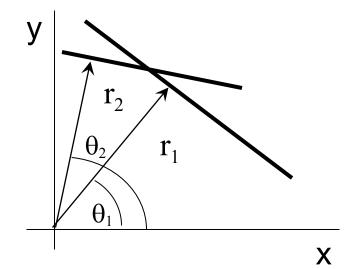


Result



- Problem: vertical lines have infinite slopes
 - difficult to quantize m to take this into account.
- Solution: use alternative parameterization of a line
 - polar coordinate representation:

$$r = x \cos \theta + y \sin \theta$$

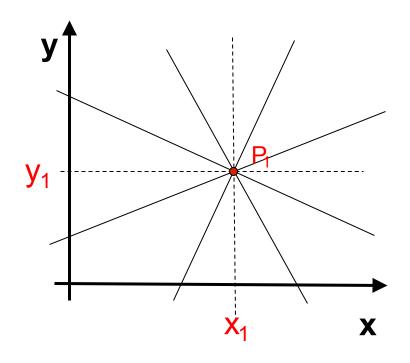


$$r_1 = x \cos \theta_1 + y \sin \theta_1$$

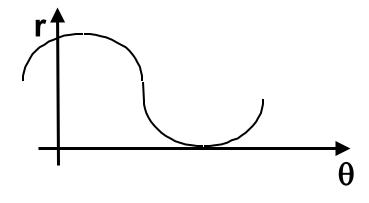
 $r_2 = x \cos \theta_2 + y \sin \theta_2$



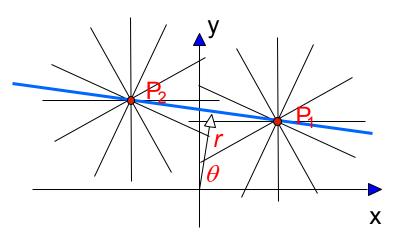
A point P1=(x1,y1) in image space
 is represented by a sinusoid in (r,θ) space



$$r = x_1 \cos \theta + y_1 \sin \theta$$





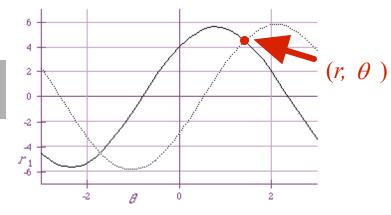


$$P_1 = (4,4)$$
 \Rightarrow $r = x_1 \cos \theta + y_1 \sin \theta =$
= $4 \cos \theta + 4 \sin \theta$

$$P_2 = (-3,5)$$
 \rightarrow $r = x_2 \cos \theta + y_2 \sin \theta =$
= $-3 \cos \theta + 5 \sin \theta$

2 eq.s on (r, θ) Possible to solve for (r, θ)



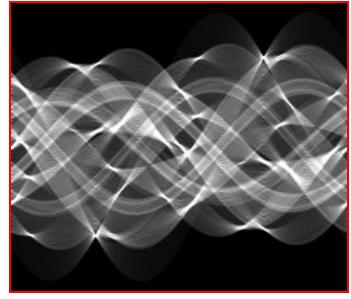


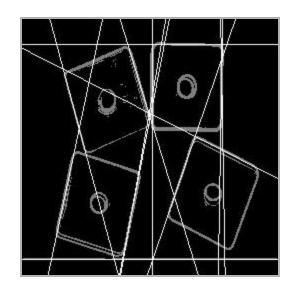


Image



Edges



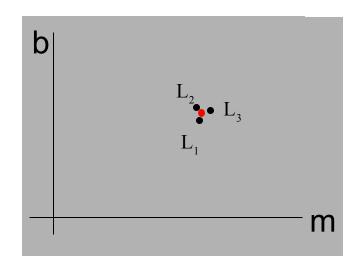


Result

Accumulator Array



'Average' point in Hough Space:



Leads to an 'average' line in image space:

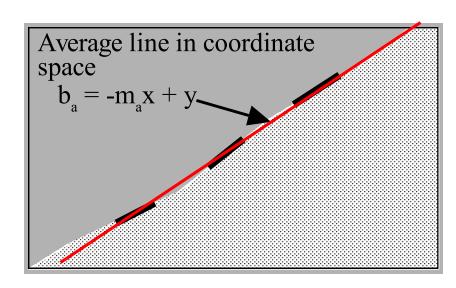
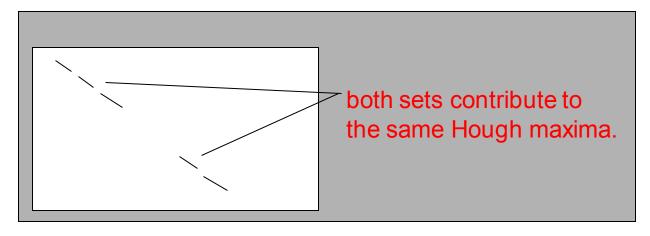




Image space localization is lost:



- Consequently, we still need to do some image space manipulations, e.g., something like an edge 'connected components' algorithm.
- Heikki Kälviäinen, Petri Hirvonen, L. Xu and Erkki Oja, "Probabilistic and nonprobabilistic Hough Transforms: Overview and Comparisons", Image and Vision Computing, Volume 13, Number 4, pp. 239-252, May 1995.



Hough technique generalizes to any parameterized curve:

$$f(x,a) = 0$$
parameter vector (axes in Hough space)

- Success of technique depends upon the quantization of the parameters:
 - too coarse: maxima 'pushed' together
 - too fine: peaks less defined
- Note that exponential growth in the dimensions of the accumulator array with the the number of curve parameters restricts its practical application to curves with few parameters





- Circles have three parameters
 - Center: (a,b)
 - Radius: r
- Circle: $f(x,y,r) = (x-a)^2 + (y-b)^2 r^2 = 0$
- Task:

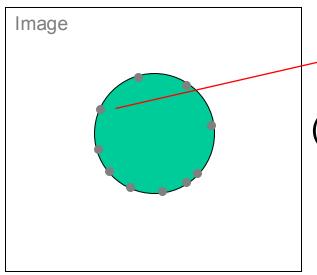
Find the center of a circle with known radius r given an edge image with no gradient direction information (edge location only)

Given an edge point at (x,y) in the image, where could the center of the circle be?

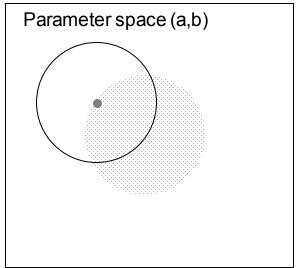


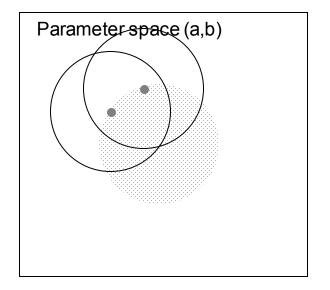


If radius is known

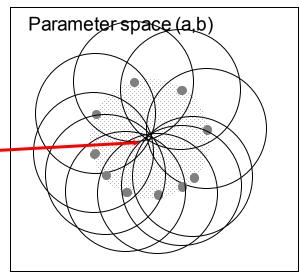


fixed (i,j) $(i-a)^2 + (j-b)^2 - r^2 = 0$





Circle Center (lots of votes!)





If we don't know r, accumulator array is 3-dimensional

- Hough can be extended in many ways.... see, for example:
 - Ballard, D. H.
 Generalizing the Hough Transform to Detect Arbitrary Shapes,
 Pattern Recognition 13:111-122, 1981.
 - Illingworth, J. and J. Kittler,
 Survey of the Hough Transform,
 CVGIP, 44(1):87-116, 1988

Hough Transform - Summary

- Hough Transform is a "voting" scheme
 - points vote for a set of parameters describing a line or curve.
- The more votes for a particular set
 - the more evidence that the corresponding curve is present in the image.
- Can detect MULTIPLE curves in one shot.
- Computational cost increases
 with the number of parameters describing the curve.