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matgame • EN

# Game on a Matrix (matgame)

John is playing a game on a square matrix of dimensions  $N \times N$ . The rows and the columns of the matrix are numbered from 1 to N. Cell (i, j) is the cell located in the j-th column of the i-th row. The matrix contains integers in each cell, specifically, the number written in cell (i, j) is  $a_{i,j}$ .

The game consists of a sequence of moves of the form:

- Select a cell (i, j).
- The score of the move is the value  $a_{i,j}$  written in cell (i,j).
- Remove the i-th row and the j-th column from the matrix.
- Repeat the same process until the matrix becomes empty.

The score of the game is defined as the **minimum of the scores of the moves**. John asks you to determine the maximum possible score of a game that can be played on the given matrix.

Among the attachments of this task you may find a template file matgame.\* with a sample incomplete implementation.

### Input

The first line of input contains N, the number of rows and columns of the matrix.

Each of the next N lines contains N numbers. The j-th number in the i-th line is the value  $a_{i,j}$ , i.e., the number written in cell (i,j).

## Output

Output a single number, representing the maximal possible score achievable in a game.

#### **Constraints**

- 1 < N < 1000.
- $0 \le a_{i,j} \le 10^9$  for each  $i = 1 \dots N$  and  $j = 1 \dots N$ .

### Scoring

Your program will be tested against several test cases grouped in subtasks. In order to obtain the score of a subtask, your program needs to correctly solve all of its test cases.

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- Subtask 1 (0 points) Examples.

- Subtask 2 (10 points) N \le 10.

- Subtask 3 (30 points) N \le 300, 0 \le a_{i,j} \le 1 for each i = 1 \dots N and j = 1 \dots N.

- Subtask 4 (45 points) N \le 100.
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## **Examples**

input	output
3	7
8 0 7	
8 0 7 5 6 9	
1 7 9	

### **Explanation**

In the sample case, one possible optimal way of playing the game is as follows:

- First, select cell (1,1) with the value 8, and remove the first row and the first column. The matrix becomes this:  $\begin{pmatrix} 6 & 9 \\ 7 & 9 \end{pmatrix}$
- Then, select the cell (2,1) of this new matrix with the value 7, and remove the second row and the first column. The matrix will consist of a single value 9.
- Finally, select the single value 9 in the matrix, and remove it so that the matrix becomes empty.

The score of the game is the minimum of the scores of the moves, which is 7.

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