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%1.i
x = zeros(1,40);
xn = 3;
n=1; %Initial Conditions
while n~= 41 %Started a while loop to iterate untill n = 41 so that it calculates from 1 to 40 for n
    x(1,n) = xn;%assigning values to the nth place in the vector x
    xn = 5^n *sqrt(4*(2- sqrt(4-(xn/5^n)^2))); %calculating the next iteration in the sequence and assigning it to xn
    n = n+1;%keeping track of iterations
end
fprintf("1.i) the vector x is \n")
fprintf('%1.4f ',x)%formatting and printing the vector keeping an appropriate precision

%1.ii
naxis = (1:40);
constant = ones(1,40)*3.0366;%setting up other 1D arrays for plotting
subplot(1,2,1) %I went for a subplot as i like the direct comparison
plot(naxis,constant,naxis,x),axis([-1,41,-1,4]), legend('x vector','alpha'),xlabel('value of n'),ylabel('value of x_n'), title('The Sequence of x_n')%plotting the first vector x against the constant

%1.v
y = zeros(1,40); %See question 1.i for the comments on these lines of working as it is the same code again
yn = 3;
n = 1;
while n ~= 41
    y(1,n) = yn;
    yn = (4*yn)/(sqrt(4*(2+ sqrt(4-(yn/5^n)^2))));
    n = n+1;
end
fprintf("\n\n1.v) the vector y is \n")%Slightly different formatting so everything prints to console nicely spaced
fprintf('%1.4f ',y)

%1.vi
naxis = (1:40); %See question 1.ii
constant = ones(1,40)*3.0366;
subplot(1,2,2)
plot(naxis,constant,naxis,y),axis([-1,41,2.99,3.05]), legend('y vector','alpha'),xlabel('value of n'),ylabel('value of y_n'),title('The Sequence of y_n')

%2.a
xn = 2;
n = 0;
test = true;
x = zeros(1);%Setting up initial conditions
while test == true %my logic tests are within the loop as i like the flexibility this affords when coding at the expense of a clean look
    xn2 = (16*xn^5 + 1)/(20*xn^4 - 1);%assigning the value of the next iteration to a separate value for comparison test
    n = n+1;%tracking number of iterations
    x(1,n)=xn;%assigning value to vector for plotting
    xn = xn2;%resetting value for next loop
end

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    if ((xn - xn2)^2) < 10^(-20)%testing first endpoint condition, i did not use abs here as
i thought this would be more elegant but in retrospect it probably wasnt
        if ((4*xn2^5 - xn2 -1)^2) < 10^(-20)%testing second endpoint condition
            test = false;%setting test variable to false so that the next while loop will end
the looping
        end
    end
    if n == 1000%testing if the sequence likely isnt converging
        test = false;%ending loop
    end
end
fprintf("\n\n2.a)the final value of x is ")
fprintf('%f \n',x(1,n))%formatting and printing to console, this could have been done in one l
ine but i was originally going to do it differntly and im a lazy coder
figure(2)%switching to my next figure as im creating a seperate graph
naxis = (1:n);%setting up graph variables
plot(naxis,x),xlabel('value of n'),ylabel('value of x_n'),title("Curve of Newtons Method") %J
ust plotting

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1.i) the vector x is

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1.v) the vector y is

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2.a)the final value of x is 0.857804



