

```

n = 3; % the number of equations
A=[1 1 1; 1 1 2; -1 2 2]; %define the 3x3 matrix A
b=[1;2;1]; %define the column vector b
B = [A b] % 3x4 matrix
L = eye(3) % 3x3 identity matrix
P=eye(n) %3x3 matrix for permutation matrix P

for k=1:n-1 % step number (and row to be multiplied)
    display('Step')
    k
    %%%%Partial pivoting strategy
    [t,r]=max(abs(B(k:n,k))); %stores the maximum absolute value of b_{ik}
    %for i=k,...n
    %r stores the index of the element t
    %row number is offset by k-1
    r=k-1+r;
    %interchange row (B(k,:)) and row (B(r,:)) of B
    B([k r],:)=B([r k],:);
    %interchange row (P(k,:)) and row (P(r,:)) of P
    P([k r],:)=P([r k],:);
    %interchange L(k,1:k-1) and L(r,1:k-1)
    L([k r],1:k-1)=L([r k],1:k-1);
    %%%%%%%%%end of partial pivoting strategy
    for i=k+1:n %row number to be changed
        L(i,k)=B(i,k)/B(k,k); % this is the multiplier
        B(i,:)= B(i,:)-L(i,k)*B(k,:) % row operation
    end
    display('Matrix after the k-th elimination step is ')
    B

end

display('Upper triangular matrix U= ')
U=B(:,1:n) %Upper triangular matrix U

display('Lower triangular matrix L= ')
L %Lower triangular matrix L

display('LU=')
L*U

%perform backward substitution
x=B(:,n+1);
x(n)=B(n,n+1)/B(n,n);
for i=n-1:-1:1
    x(i)=(B(i,n+1)-B(i,i+1:n)*x(i+1:n))/B(i,i);
end
%solution
display('The computed solution is x=')
x

```

B =

1 1 1 1

$$\begin{array}{cccc} 1 & 1 & 2 & 2 \\ -1 & 2 & 2 & 1 \end{array}$$

L =

$$\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array}$$

P =

$$\begin{array}{ccc} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{array}$$

Step

k =

$$1$$

B =

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ -1 & 2 & 2 & 1 \end{array}$$

B =

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 3 & 3 & 2 \end{array}$$

Matrix after the k-th elimination step is

B =

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 0 & 1 & 1 \\ 0 & 3 & 3 & 2 \end{array}$$

Step

k =

$$2$$

B =

$$\begin{array}{cccc} 1 & 1 & 1 & 1 \\ 0 & 3 & 3 & 2 \\ 0 & 0 & 1 & 1 \end{array}$$

Matrix after the k-th elimination step is

B =

1	1	1	1
0	3	3	2
0	0	1	1

Upper triangular matrix U=

U =

1	1	1
0	3	3
0	0	1

Lower triangular matrix L=

L =

1	0	0
-1	1	0
1	0	1

LU=

ans =

1	1	1
-1	2	2
1	1	2

The computed solution is x=

x =

0.3333
-0.3333
1.0000