

# N1a Collatz MacIntyre

Tucker MacIntyre

March 18th, 2019

$$1. a_{i+1} = \begin{cases} -a_i/2 & \text{if } a_i \text{ is even} \\ 3*a_i + 1 & \text{if } a_i \text{ is odd} \end{cases}$$

Start with Positive Integer. Seems to loop and reach 1 no matter the integer.

$$2. a_{i+1} = \begin{cases} a_i/2 & \text{if } a_i \text{ is even} \\ (3*a_i + 1)/2 & \text{if } a_i \text{ is odd} \end{cases}$$

Start with Positive Integer. Seems to loop and reach 1 no matter the integer.

$$3. a_{i+1} = \begin{cases} (a_i + 2)/2 & \text{if } a_i \text{ is even} \\ 3*a_i + 1 & \text{if } a_i \text{ is odd} \end{cases}$$

Start with Positive Integer. Seems to loop one of the following loops: [6, 4, 3, 10, 6], [40, 21, 64, 33, 100, 51, 154, 78, 40], [22, 12, 7, 22], or if  $a_0 = 2$  [2, 2, 2].

Proof for 1: That all positive integers work, while domain is all real numbers.

Basis Step:

Case 1:(even) Let  $n = a_i$ , and  $n = 2$

$$P(2) = 2/2 = 1 \text{ (odd)}$$

Case 2: (odd) Let  $n = 1$

$$P(1) = 3*1 + 1 = 4 \text{ (Even)}$$

Therefore, even integers create an odd integer, while odd integers create an even integer.

Induction: Now let  $n = k + 1$

Case 1: (even)  $k + 1 = (-k + 1) / 2$  while  $k$  is even ( $2q$ )

$= (-2q + 1) / 2$ , which is within the domain. So  $n + 1$  will work in this scenario. (result odd)

Case 2: (odd)  $k + 1 = (3 * (k+1) + 1)$ ,  $k = 3q+1$

$$= 9q + 6$$

$$= 3 (3q + 2) \text{ which is even and within domain.}$$

Therefore, both cases work and rebound back and forth from even and odd. Hence, Because  $n + 1$  is true, by mathematical induction,  $a_0$  is true for all  $Z^+$

Note: With this being said, I am not quite sure how to show that this will eventually come back to 1 and loop as my program has shown.

Note: Also not sure if this proof by mathematical induction is completely correct or the right way to go about this.