

Due: Tuesday March 17

GENERAL DIRECTIONS: In this project you will create a set of Scheme definitions to implement a polynomial system. You must use Dr Racket. Your source code must be named `polynomials.rkt`. Neatness counts and so does indented code that is easy to read with helpful variable names.

[VERY IMPORTANT NOTE] You may only use the Scheme functions or expressions that we have discussed in class or that appear in my power point slides. I want you solve the problems “from scratch” by working only with the most basic Scheme functions and expressions and recursion. Do not use vectors or the `do` form. Use `define` only to define functions at the global level and to define lists for testing your code. **See last page for list of functions and forms you may use.**

PROJECT: Write a set of Scheme definitions that implement a polynomial system as defined below.

1. A $(value\ exponent)$ tuple is called a **term**. The value may be any real number but the exponent must be a nonnegative integer. A **polynomial** will be represented as a list terms. For example
 $4x^2 + -5x + 10$ can be represented by the list `'((4 2) (-5 1) (10 0))`. The list may not be sorted on the exponent so that $4x^2 + -5x + 10$ can also be represented by the list `'((10 0) (-5 1) (4 2))`. We will always use the symbol `x` as the polynomial unknown.

Any list of $(value\ exponent)$ pairs represents a polynomial. The polynomial might not be simplified. For example, the list `'((6 4) (10 0) (8 2) (-3 5) (3 2) (3 0))` represents the polynomial $6x^4 + 10 + 8x^2 + -3x^5 + 3x^2 + 3$

2. Write the following Scheme functions. The functions should all be in the same file. Use recursion for items d,e, i, m. You may use recursion for the others, if needed.
 - a. `(coeff t)` // returns the value of the term `t`
 - b. `(expon t)` //returns the exponent of the term `t`
 - c. `(printTerm t)` //prints the term `t` in the format $value\ x^exponent$.
 Examples: `(4 2)` will be printed as $4x^2$
`(7 0)` will be printed as 7
`(-4 1)` will be printed as $-4x$
 - d. `(printpoly p)` // prints the polynomial `p` using `printTerm` with a `+` between the terms.
 For example, `'((2.13 3) (1.5 4) (6 3) (4 1) (-3 0))` should be printed as $2.13x^3 + 1.5x^4 + 6x^3 + 4x + -3$
 - e. `(evalpoly p v)` // returns the value of polynomial when $x = v$.
 - f. `(GT t1 t2)` //returns true if exponent of `t1` > exponent of `t2`, else false
 - g. `(EQExp? t1 t2)` //returns true if `t1` and `t2` have the same exponent, else false
 - h. Show that `(sort p GT)` returns polynomial `p` sorted on exponents.

- i. `(simplify p)` // returns a polynomial equivalent to `p` which is simplified, in that all terms have different exponents and are listed in decreasing exponent order. For example, `'((6 4) (8 2) (-3 5) (3 2) (13 0))` should return `'((-3 5) (6 4) (11 2) (13 0))`.
[Hint: Sort `p` and then call a recursive function that simplifies a sorted polynomial]
 - j. `(addpoly p1 p2)` // returns a simplified polynomial which is the sum of `p1` and `p2`
[Hint: first append the two polynomials]
 - k. `(subtractpoly p1 p2)` //returns a simplified polynomial which is the difference between `p1` and `p2` (i.e., $p1 - p2$). [Hint: $p1 - p2 = p1 + (-1)p2$]
 - l. `(multiplyterms t1 t2)` returns the product of the terms `t1` and `t2`. For example, `(multiplyterms '(3 5) '(-2 3))` returns `'(-6 8)`
 - m. `(multiplytermpoly t1 p1)` // returns the simplified polynomial that is the product of `t1` and `p1`
 - n. `(multiplypoly p1 p2)` //returns the simplified polynomial that is the product of `p1` and `p2`. This is a challenge.
3. You may create other helper Scheme functions.
 4. Test your code thoroughly. Run Instructor test cases. I will post them on March 10.
 5. For functions that are incomplete or not working, you must have a "placeholder function" in your .rkt file that returns "incomplete or not working function" whenever it is called. For example,

```
(define multiplypoly
  (lambda (p1 p2)
    "incomplete or missing function" ))
```

Turn in:

- a. Hard copy: Submit (1) `polynomials.rkt` file; (2) runs of posted instructor test cases. Label everything. Names must be listed in the `polynomial.rkt` file. Use a Cover page as in Project 2
Electronic Copy: Upload a single source file called `polynomials.rkt` with your racket definitions to Moodle. Your source file should contain as a comment your name, date and Project. Submit only one file person. (Due at 7am on March 17)

List of Scheme functions and forms you can use for this project:

- define, lambda, if, cond, cons, car, cdr, list, member, list-ref
- predicates : null? list? equal? string? number? member? and others we have used in class
- arithmetic operators, relational operators, logical operators used in class,
- sort, map, filter, length, reverse, append, last, let, let*, letrec, print, begin, newline, display, set!
- If there is a function you think should be added to this list, you need to get your instructor's approval.
- Added functions: expt, apply, min, max, unless