A Hybrid AB-SFC Macroeconomic Model with an explicit distribution of income and wealth

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Recent developments in Post-Keynesian macroeconomics have found in Stock-Flow Consistent models a general framework to enforce the macroeconomic accounting identities in the models. These models are sometimes extended to include microfoundations (or a microeconomic description) through the use of Agent-Based Models. But despite the progress and the diffusion of AB-SFC models in the last ten years, very few models can replicate the fat-tail distribution of income and wealth observed empirically. Instead, they usually rely on a Kaleckian distinction between workers and capitalists or a segmented labour market (for example low-, mediumand high-skilled workers). This model aims to reproduce a fat-tail distribution in income and wealth, in addition to other stylized facts, by differentiating workers by their skills and the capital goods used in production by their productivity and the skills required to use them. A realistic distribution of income and wealth allows bringing closer this strain of literature with the literature on income and wealth inequality since it makes measuring indexes like Gini or the top5/bottom50 ratio possible. The model includes endogenous innovation and credit rationing as previous models in the literature. Households' consumption is expressed in material terms (i.e. the amount of goods consumed), rather than in monetary value, to be able to differentiate the goods consumed and better characterize the behaviour of low-income households in a future version of the model, relying on empirical stylized fact and the interpretative framework of the Foundational Economy. Furthermore, the model is designed to compare different welfare policies, like minimum wage, minimum income, Universal Basic Income, Universal Basic Services or Job Guarantee programs, and different political orientations in public policies, like the austerity principles of the '10s, a Keynesian demand-led public spending or an entrepreneur state. At the time of writing this abstract, the model has been completely outlined on paper but no numerical simulation has been performed yet.

1 Introduction

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In recent years Stock-Flow Consistent (SFC) models have been recognized as a valuable tool to model macroeconomics (Nikiforos & Zezza, 2017). Particularly, they can represent the financial

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An updated version of this paper and all the source code and the instructions required to replicate the paper will be available at $\frac{\text{https:}}{\text{github.com}}$

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side of the economy, which has been recognized as a necessary feature to model after the financial crisis of the 00s.

Those models are aggregate models which can neither describe microeconomic dynamics and behaviours nor, if it is considered necessary, provide a microfoundation for the model. Agent-Based Models (ABMs) have been used to add a microeconomic description to the macroeconomic model provided by the SFC framework (Caverzasi & Russo, 2018; Dosi & Roventini, 2019).

But in the SB-SFC models literature, very few papers explore the conditions to model a realistic (i.e. fat-tail) distribution of income and wealth among households (e.g. Dafermos & Papatheodorou, 2015; Kinsella et al., 2011), often relying on a Kaleckian framework which studies the distribution between wages and profits (e.g. Dosi et al., 2013) or a segmented labour-market (e.g. Caiani et al., 2019).

Modelling personal income and wealth distribution is a needed step to close the gap between this strain of post-Keynesian literature and the literature on inequality pioneered by Atkinson, Piketty, Zucman and Saez, allowing for example to measure the evolution of inequality indexes (like Gini or the Top5/Bottom50) through time or policies changes.

Some choices in the model are dictated by its long-term goals, specifically comparing disruptive welfare policies (Universal Basic Income, Universal Basic Service, Job Guarantee, ...) and focusing on the different consumption patterns between high- and low-income households, including different compositions of the consumption bundle, the relevance of publicly provided goods and services (including infrastructures) in the consumption bundle, following the Foundational Economy framework (Arcidiacono et al., 2018), the incidence of unpaid domestic and care work on the work provided by individuals in the household, especially from a gender perspective.

Enhancement: Foundational Economy - 1

To better characterize the differences in behaviour among low- and high-income households it is possible to refer to the theoretical framework provided by Foundational Economy (Arcidiacono et al., 2018). It suggests that a significant part of the economic activities are instrumental not to the extraction of rents from capital, but to addressing essential needs and to building up shared infrastructures

"It argues that the well-being of Europe's citizens depends less on individual consumption and more on their social consumption of essential goods and services – from water and retail banking, to schools and care homes – in what we call the foundational economy. Individual consumption depends on market income, while foundational consumption depends on infrastructure and delivery systems of networks and branches, which are neither created nor renewed automatically, even as incomes increase. The distinctive, primary role of public policy should therefore be to secure the supply of basic services for all citizens. If the aim is citizen well-being and flourishing for the many not the few, then European politics at regional, national and EU level needs to be refocused on foundational consumption and securing universal minimum access and quality." (Arcidiacono et al., 2018)

Enhancement: Welfare policies

The first version of the model will be as simple as possible to create a robust baseline. Subsequent iterations of the model will explore different welfare policies and how to model them.

Finally, the model is inspired more by west-European economies (particularly Italy) rather than by north-American ones.

2 General Hypothesis

To simplify the model a close single-country economy is assumed. This is a common hypothesis for SFC models (and macroeconomics in general) because an open economy does not preserve the balance of flows in the model. So, to preserve the consistency of the model the only alternative is to model a multi-countries system, each with its own dynamics. It is worth keeping in mind that this hypothesis prevents to model to replicate economic dynamics strongly dependent on international trade, like the export-led growth path.

Enhancement: Multi-Country Model

A compromise for future development is to model in an AB-SFC setting the main economy of the model while keeping aggregated (SFC only) the other economies.

The microeconomic behaviour of the agent is modelled mostly using adaptive expectations, focusing on the variation of behaviours (as desires or expectations) with regard to the previous period. Exploiting this, to smooth the dynamics of the model each period represents a month (a small amount of time compared to other models) to keep the variations small.

Enhancement: The time scale of the policies

In a future version of the model, the simulation's timespan has to be long enough to observe the effects of introducing a policy. But, at the same time, it is unreasonable to keep the simulation running over 5-10 years after the policy's introduction because, in any real-world context, a government can tune or revert the policy afterwards.

The model includes the six sectors: the Households (\mathcal{H}) , the Firms which produce consumption goods $(\mathcal{F}_{\mathcal{C}})$, the Firms which produce Capital goods $(\mathcal{F}_{\mathbf{K}})$, a consolidated (i.e. aggregated) banking and financial sector (the Bank, \mathcal{B}), the Government (\mathcal{G}) and the Central Bank (\mathcal{C}) . Households and Firms constitute the Agent-Based part of the model.

The model comprises two kinds of real assets: Capital Goods (**K**) and Consumption Goods (**C**). Capital Goods are durable and Consumption Goods are homogeneous.

Enhancement: Foundational Economy – 2

To model the idea of a Foundational Economy the single representative Consumption Good can be split into a representative Foundational Consumption Good and another kind of non-Foundational Consumption Goods. The intuition which can be followed is that each Household aims to consume a certain amount of Foundational Goods before to start consuming the other Goods. Additionally, the non-monetary transfers by the Government should comprise only Foundational Goods.

The model includes five different financial assets. Bank Deposits (\mathbf{D}) of Households and Firms, which are not interest-bearing. Loans (\mathbf{L}) issued by the Banks to Firms, which interest rate is Firm-specific and fixed by the Bank. Bank Shares (\mathbf{S}) held by Households, which interest rate is fixed each period by the Bank. Banks Reserves and Government Account at the Central Bank (\mathbf{R}), which are not interest-bearing. Government Bonds (\mathbf{B}) held by Bank and Central Bank, and which interest rate is fixed by the Central Bank.

3 Matrices

3.1 Balance Sheet Matrix

| | \mathcal{H} | $\mathcal{F}_{\mathbf{C}}$ | $\mathcal{F}_{\mathbf{K}}$ | \mathcal{B} | \mathcal{G} | \mathcal{C} | Tot. |
|---------|-----------------------------|--|--|-----------------------------|-----------------------------|-------------------------------|-----------------------------|
| D | $+\mathbf{D}_{\mathcal{H}}$ | $+\mathbf{D}_{\mathcal{F}_{\mathbf{C}}}$ | $+\mathbf{D}_{\mathcal{F}_{\mathbf{K}}}$ | $-\mathbf{D}$ | | | 0 |
| ${f S}$ | $+\mathbf{S}$ | | | $-\mathbf{S}$ | | | 0 |
| ${f L}$ | | $-\mathbf{L}^{\mathcal{F}_{\mathbf{C}}}$ | $-\mathbf{L}^{\mathcal{F}_{\mathbf{K}}}$ | $+\mathbf{L}$ | | | 0 |
| ${f B}$ | | | | $+\mathbf{B}_{\mathcal{B}}$ | $-\mathbf{B}$ | $+\mathbf{B}_{\mathcal{C}}$ | 0 |
| ${f R}$ | | | | $+\mathbf{R}_{\mathcal{B}}$ | $+\mathbf{R}_{\mathcal{G}}$ | $-\mathbf{R}$ | 0 |
| K | | $+p_{\mathbf{K}}\mathbf{K}_{\mathcal{F}_{\mathbf{C}}}$ | $+p_{\mathbf{K}}\mathbf{K}_{\mathcal{F}_{\mathbf{K}}}$ | | | | $+p_{\mathbf{K}}\mathbf{K}$ |
| Tot. | $+V_{\mathcal{H}}$ | $+V_{\mathcal{F}_{\mathbf{C}}}$ | $+V_{\mathcal{F}_{\mathbf{K}}}$ | $+V_{\mathcal{B}}$ | $+V_{\mathcal{G}}$ | $+\overline{V_{\mathcal{C}}}$ | $+p_{\mathbf{K}}\mathbf{K}$ |

V is the net worth of the sector.

3.2 Transactions Matrix

| | H | $\mathcal{F}_{\mathbf{C}}$ | $\mathcal{F}_{\mathbf{K}}$ | \mathcal{B} | \mathcal{G} | \mathcal{C} | Tot. |
|--|---|--|---|---|---|---|------|
| Consumption | $-p_{\mathbf{C}}\mathbf{C}_{\mathcal{H}}$ | $+p_{\mathbf{C}}\mathbf{C}$ | | | $-p_{\mathbf{C}}\mathbf{C}_{\mathcal{G}}$ | | 0 |
| Investment | | $-p_{\mathbf{K}}\mathbf{K}_{\mathcal{F}_{\mathbf{C}}}$ | $+p_{\mathbf{K}}(\mathbf{K} - \mathbf{K}_{\mathcal{F}_{\mathbf{K}}})$ $-W^{\mathcal{F}_{\mathbf{K}}}$ | | | | 0 |
| Wages | +W | $-W^{\mathcal{F}_{\mathbf{C}}}$ | $-W^{\mathcal{F}_{\mathbf{K}}}$ | | | | 0 |
| Taxes | -T | | | | +T | | 0 |
| Transfers | +M | | | | -M | | 0 |
| $\overline{\mathcal{F} \text{ Profits}}$ | | $-\Pi_{\mathcal{B}}^{\mathcal{F}_{\mathbf{C}}}$ | $-\Pi_{R}^{\mathcal{F}_{\mathbf{K}}}$ | $+\Pi_{\mathcal{B}}$ | | | 0 |
| $\mathcal C$ Profits | | В | \mathcal{B} | ~ | $+\Pi^{\mathcal{C}}$ | $-\Pi^{\mathcal{C}}$ | 0 |
| S Interests | $+r_{\mathbf{S}}\mathbf{S}$ | | | $-r_{\mathbf{S}}\mathbf{S}$ | | | 0 |
| L Interests | | $-r_{\mathbf{L}}\mathbf{L}^{\mathcal{F}_{\mathbf{C}}}$ | $-r_{\mathbf{L}}\mathbf{L}^{\mathcal{F}_{\mathbf{K}}}$ | $+r_{\mathbf{L}}\mathbf{L}$ | | | 0 |
| ${f B}$ Interests | | _ | _ | $+r_{\mathbf{B}}\mathbf{B}_{\mathcal{B}}$ | $-r_{\mathbf{B}}\mathbf{B}$ | $+r_{\mathbf{B}}\mathbf{B}_{\mathcal{C}}$ | 0 |

$_{\circ}$ 4 Sectors

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4.1 Households

In this model, the core agents (consumers, workers, capitalists) represent a household rather than a single individual. This is a very common approximation in economics and I think it is reasonable as long as we are not going into modelling education paths and care and domestic work, where the gender asymmetries become very relevant.

Each agent is characterized by an education level assigned when it enters the simulation replacing a retired agent inheriting their wealth, and gains experience when working for the same firm for consecutive periods. The education level is assigned with a probability related to the inherited wealth and provides the starting skill level.

Skills s evolve like in Dosi et al. (2018), which means $\sigma_t = (1 + \Sigma)^{\delta} \sigma_{t-1}$ where $\delta = 1$ if the household is employed by the same firm of the previous period, $\delta = 0$ if the household is still employed but in a different firm, $\delta = -1$ if the household is unemployed.

Enhancement: Training

Two factors in the development of the skills can be introduced.

One on the welfare policies side is the possibility for the government to organize training programs for the unemployed to prevent the loss of skills on even increase them.

The second one relates to the actual job done: it is reasonable to assume that it is easier to learn new skills if the skills required for the job are closer to the skill level, while demoted and overqualified workers have lower chances to learn new skills. This can be included in the model making $\phi \propto (s-\sigma)^{-1}$, where σ is the minimum skill level required to operate the machinery assigned to the worker in the time step.

Households face two choices: if work and how many consumption goods they desire to consume.

Households flows balance is $y_t = z_t + m_t + r_{\mathbf{S}_t} \mathbf{s}_t = c_t + t_t + \Delta \mathbf{s}_t + \Delta \mathbf{d}_t$, where bold lowercase letters are used to indicate individual value for the correspondent uppercase aggregates and the net wage $(z = w(1 - \max(\tau_M \tanh(\tau_F(\frac{w}{p} - \tau_T)), 0)))$.

I assume, as a heuristic, that taxes (t) and wages (z) can be approximated as constant from the previous period (because salaries increase only by changing employers, which is an unexpected event), while transfers (m) are composed only of unemployment benefits. Additionally, I assume that desired deposits (\mathbf{d}_t^*) at the end of the period are a fraction of the desired consumption $(c_t^* = \mathbb{E}(p_{\mathbf{C}})\mathbf{c}_t^*)$ as insurance against unexpected increases in prices $(\mathbf{d}_t^* = \rho_{\mathcal{H}}c_t^*, \rho_{\mathcal{H}} > 0)$.

Subtracting two consecutive periods and ignoring second-order differences, the in-flow income becomes $\Delta y_t = \Delta z_t + \Delta r_{\mathbf{S}}\mathbf{s}_t$, and calling η the marginal propensity to consume it becomes

$$\eta \Delta c_t = \Delta y_t = \Delta z_t + \Delta (r_{\mathbf{S}}\mathbf{s})_t
= \Delta z_t + r_{\mathbf{S}t}\mathbf{s}_t^* - r_{\mathbf{S}t-1}\mathbf{s}_{t-1}
= \Delta z_t + r_{\mathbf{S}t}\mathbf{s}_t^* - (r_{\mathbf{S}t} - \Delta r_{\mathbf{S}t})(\mathbf{s}_t^* - \Delta \mathbf{s}_t)
\approx \Delta z_t + r_{\mathbf{S}t}\Delta \mathbf{s}_t + \Delta r_{\mathbf{S}t}\mathbf{s}_t^*
= \Delta z_t + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})\mathbf{s}_t^* - r_{\mathbf{S}t}\mathbf{s}_{t-1}$$

where \mathbf{s}_{t}^{*} is the desired amount of shares to hold in the period.

Looking at the balance of a household between the beginning of the period and the purchase of consumption goods, it is possible to write $\mathbf{s}_t^* + \mathbf{d}_t^* + c_t^* = \mathbf{s}_{t-1} + \mathbf{d}_{t-1} + \mathbb{E}(z)_t + \mathbb{E}(m)_t$, and substituting \mathbf{s}_t^* above it becomes

$$\begin{split} \eta \Delta c_{t} &\approx \Delta z_{t} + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{s}_{t-1} + \mathbf{d}_{t-1} + \mathbb{E}(z)_{t} + \mathbb{E}(m)_{t} - \mathbf{d}_{t}^{*} - c_{t}^{*}) - r_{\mathbf{S}t}\mathbf{s}_{t-1} \\ &= (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + z_{t-1} + \phi m_{t-1} - (1 + \rho_{\mathcal{H}})c_{t}^{*}) + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1} \\ &= (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + z_{t-1} + \phi m_{t-1} - (1 + \rho_{\mathcal{H}})c_{t-1}) \\ &- (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(1 + \rho_{\mathcal{H}})\Delta c_{t} + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1} \\ (\eta + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(1 + \rho_{\mathcal{H}}))\Delta c_{t} &\approx (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + z_{t-1} + \phi m_{t-1} - (1 + \rho_{\mathcal{H}})c_{t-1}) + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1} \\ \Delta c_{t} &\approx \frac{(r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + z_{t-1} + \phi m_{t-1} - (1 + \rho_{\mathcal{H}})c_{t-1}) + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1}}{\eta + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(1 + \rho_{\mathcal{H}})} \end{split}$$

To translate this into consumption measured in consumption goods \mathbf{C} , calling ψ the inflation rate updated periodically model-wise and $p_{\mathbf{C}}$ the average purchase price paid by the agent, we

have

$$\Delta c_t^* = \Delta(p_{\mathbf{C}}\mathbf{c})_t \approx \Delta(p_{\mathbf{C}})_t \mathbf{c}_t^* + \mathbb{E}(p_{\mathbf{C}})_t \Delta \mathbf{c}_t$$

$$= (\mathbb{E}(p_{\mathbf{C}})_t - p_{\mathbf{C}_{t-1}})(\mathbf{c}_{t-1} + \Delta \mathbf{c}_t) + \mathbb{E}(p_{\mathbf{C}})_t \Delta \mathbf{c}_t$$

$$= ((1 + \psi)p_{\mathbf{C}_{t-1}} - p_{\mathbf{C}_{t-1}})(\mathbf{c}_{t-1} + \Delta \mathbf{c}_t) + (1 + \psi)p_{\mathbf{C}_{t-1}} \Delta \mathbf{c}_t$$

$$= \psi p_{\mathbf{C}_{t-1}}\mathbf{c}_{t-1} + (1 + 2\psi)p_{\mathbf{C}_{t-1}} \Delta \mathbf{c}_t$$

$$\Delta \mathbf{c}_t^* \approx \frac{\Delta c_t^*}{(1 + 2\psi)p_{\mathbf{C}_{t-1}}} - \frac{\psi}{1 + 2\psi} \mathbf{c}_{t-1}$$

 $r_{\mathbf{S}t}$ is communicated by the Bank before the agent has to choose between consumption and saving. η is calibrated from empirical data (such as Carroll et al., 2017; Fisher et al., 2020) as an exponential or Pareto distribution as $\eta(\frac{\mathbf{s}}{p_{\mathbf{C}}}, \frac{z}{p_{\mathbf{C}}})$, where the price is used to get a-dimensional values.

From these relations, we can model the two choices of households.

First, a household exits from the labour market if the loss of the wage can anyway grant a non-decreasing standard of living, i.e. if

$$\Delta \mathbf{c}_{t}^{*} = \frac{-z_{t-1} + (r_{\mathbf{S}_{t}} + \Delta r_{\mathbf{S}_{t}})(\mathbf{d}_{t-1} + \phi z_{t-1} - (1 + \rho_{\mathcal{H}})c_{t-1}) + \Delta r_{\mathbf{S}_{t}}\mathbf{s}_{t-1}}{(1 + 2\psi)p_{\mathbf{C}_{t-1}}(\eta + (r_{\mathbf{S}_{t}} + \Delta r_{\mathbf{S}_{t}})(1 + \rho_{\mathcal{H}}))} - \frac{\psi}{1 + 2\psi}\mathbf{c}_{t-1} \ge 0$$

Similarly, it re-enters the labour market if the expected salary (i.e. the average salary given the skill level) prevents a loss of consumption, i.e. if

$$\Delta \mathbf{c}_{t}^{*} = \frac{(r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + \phi m_{t-1} - (1 + \rho_{\mathcal{H}})c_{t-1}) + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1}}{(1 + 2\psi)p_{\mathbf{C}t-1}(\eta + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(1 + \rho_{\mathcal{H}}))} - \frac{\psi}{1 + 2\psi}\mathbf{c}_{t-1} < 0$$

$$\Delta \mathbf{c}_{t}^{*} = \frac{\mathbb{E}(z|s)_{t} + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(\mathbf{d}_{t-1} + \mathbb{E}(z|s)_{t} - (1 + \rho_{\mathcal{H}})c_{t-1}) + \Delta r_{\mathbf{S}t}\mathbf{s}_{t-1}}{(1 + 2\psi)p_{\mathbf{C}t-1}(\eta + (r_{\mathbf{S}t} + \Delta r_{\mathbf{S}t})(1 + \rho_{\mathcal{H}}))} - \frac{\psi}{1 + 2\psi}\mathbf{c}_{t-1} \ge 0$$

Second, each household sets the desired total consumption as $\mathbf{c}_t^* = \mathbf{c}_{t-1} + \Delta \mathbf{c}_t^*$. From which follows $c_t^* = (1+\psi)p_{\mathbf{C}_{t-1}}\mathbf{c}_t^*$ and $\mathbf{d}_t^* = \rho c_t^*$. Finally, the household buys shares $\mathbf{s}_t = \mathbf{s}_{t-1} + \mathbf{d}_{t-1} + z_{t-1} + \phi m_{t-1} - \mathbf{d}_t^* - c_t^*$.

Enhancement: Gender, Care work and Feminist Economics

Approximating individuals as household invisibilizes gender differences and the (hidden) work made mostly by women inside the family (childcare, elder care, housekeeping, ...). Gender is an important factor in creating inequalities: for example, unemployment and wages show a strong gender effect (which in both cases penalizes women).

Adding a gender perspective will be an improvement in the model (with relevant policy implications) and will require explicitly modelling education and childcare (which in this first draft is only sketched), the complete life cycle of an agent (here reduced to the working age) and family choices (marriage, pregnancy, ...).

4.2 Firms

Firms are characterized by their position in the supply chain (either Capital or Consumption). Loans are asked to the Bank at the beginning of the period to pay for salaries and to make investments and started to be repaid in the subsequent period. In the case of rationed credit, Firms first pay the salaries of workers, then they pay the salaries of researchers, then they acquire new machinery then they distribute profits, and finally, they repay the bank the loans contracted.

4.2.1 Consumption Firms

Noted s_{t-1} the number of goods sold in the previous period, each Firm sets the desired production as $\mathbf{c}_t^* = \rho_{\mathbf{C}}(1 + g - \psi)s_{t-1} = \rho_{\mathbf{C}}\mathbb{E}(s)_t$, where g is the GDP growth rate.

The maximum output of the available machinery is defined as $b = \sum_{\kappa \in \mathbf{k}} \beta_{\kappa}$. Each Firm set a desired potential output $b_t^* = \frac{1}{u^*} \mathbf{c}_t^* + \gamma b_{t-1}$, where γ is the depreciation rate of capital and u^* is the target capacity utilization rate. From this follows that $\Delta b_t = \max(\frac{\mathbf{c}_t^*}{u^*} - (1 - \gamma)b_{t-1}, 0)$ and the desired investment in monetary units is $i_t^* = (1 + \psi)p_{\mathbf{K}_{t-1}} \frac{\Delta b_t}{\langle \beta \rangle_{t-1}}$, where the average is taken on the current capital stock. Expected expenses for salaries are computed as $w_t^* =$ $\max(w_{t-1}, \frac{\mathbf{c}_t^*}{\langle \beta \rangle_{t-1}} \langle w \rangle_{t-1})$

The request for loans is set to cover salaries and investments, keeping in account revenues,

i.e. $l_t^* = \max(\mathbf{d}_{t-1} - \rho_{\mathcal{F}} w_t^*, \mathbf{d}_{t-1} + (1+\psi) p_{\mathbf{C}_{t-1}} \mathbb{E}(s)_t - \rho_{\mathcal{F}} (w_t^* + i_t^*), 0).$ The markup is set as $\mu_t = \mu_{t-1} (1 + \Theta \frac{s_{t-1} - \mathbb{E}(s)_{t-1}}{\mathbb{E}(s)_{t-1}})$ and the price $p_{\mathbf{C}_t} = (1 + \mu_t + \tau_{\mathbf{C}}) \frac{w_t}{\mathbf{c}_t}$ after the production (like in Caiani et al., 2016), where w is the sum of the wages paid by the firm and $\tau_{\mathbf{C}}$ is the VAT rate.

Each firm distributes profits equal to a fraction of the net income from production, aiming to self-financing the production in the long run, i.e. $\pi_t = r_{\Pi}(p_{\mathbf{C}t}s_t - w_t)$.

4.2.2 Capital Firms

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Capital Firms produce their own machinery, creating a system of two simultaneous equations to determine the desired output. The problem is avoided by approximating $b_t^* = \rho_{\mathcal{F}} \frac{(1+g-\psi)}{u^*} s_{t-1} +$ γb_{t-1} , and $\mathbf{k}_t = \rho_{\mathcal{F}}(1+g-\psi)s_{t-1} + \frac{\Delta b_t}{\langle \beta \rangle} - \hat{\mathbf{k}}_{t-1}$, where $\hat{\mathbf{k}}$ are the inventories unsold from the previous period. The machinery produced for own use is kept separate from those to be sold (the inventories), and valued in the balance sheet with value $p_{\mathbf{K}_t}$.

Additionally, Capital Firms perform research to improve the machinery they sell. They aim to employ a number of researchers $q_t^* = \lfloor q_{t-1}(1 + \frac{\rho_Q}{s_{t-1}}\frac{\pi_{t-1}}{\langle w_Q \rangle_{t-1}}) \rfloor$ where $\langle w_Q \rangle$ is the average salaries of the employees with $\sigma \geq \sigma^*$. This makes $w_t^* = \max(w_{t-1}, \frac{\mathbf{k}_t^*}{\langle \beta \rangle_{t-1}} \langle w \rangle_{t-1} + q_t^* \langle w_Q \rangle_{t-1})$. Finally, we note that $i_t = 0$ and so $l_t^* = \max(\mathbf{d}_{t-1} - \rho_{\mathcal{F}} w_t^*, 0)$

Enhancement: Capital goods market

The approximation that every capital firm produces its own capital goods is chosen to simplify the implementation of the model. A more realistic assumption, which has the potential to introduce interesting market dynamics, is to allow every capital firm to buy its machinery from other firms.

Enhancement: Firms' governance

In a future version, different models of governance can be introduced, particularly regarding the property (not tradeable shares, shares available on the stock market, cooperative ownership, ...), the choice rules (mostly what is the goal of the Firm, like dividend maximization, share values maximization, market share maximisation, wages maximization, top manager retribution maximization, ...) and the expected profit rate required by the owners.

Enhancement: Public Firms

The recent literature has highlighted the important role of the state in technological innovation. Additionally, civil servant wages help to set, particularly when public employment share is relevant, an economy-wide reserve wage. To keep the model simple all the firms are owned by the Bank and the government sustains demand in a way similar to public procurement. It is possible to create an additional kind of Capital Firm, which performs publicly sponsored research and development, and of Consumption Firm, which represent the direct role of the government in the economy (which mostly provides infrastructures and services).

4.3 Bank

Bank agent represents the aggregate banking and financial sector.

Bank is required to maintain both a liquidity $(\Lambda = \frac{R}{D})$ and a capital ratio $(\Gamma = \frac{V}{L})$ (see Caiani et al., 2016). Liquidity is obtained, in case of necessity, by selling Government's Bonds to the Central Bank.

Bank fixes the interest rates on Bank Shares as $r_{\mathbf{S}t} = (1 - \tau_{\mathbf{S}})(r_{\mathbf{B}t} + \lambda(\Gamma - \Gamma^*))$, where $r_{\mathbf{B}t}$ is the Central Bank interest rate and $\tau_{\mathbf{S}}$ is the constant tax rate on financial income.

In this model the Bank does not distribute profits and can access all the needed liquidity from the Central Bank, making the liquidity requirement a tautology. As a consequence, it needs a way to avoid excessive capitalization that does not depends on Λ . The proposed behaviour simulates a profit distribution when the Bank is capitalized over the target, without the need to introduce a market for shares.

Enhancement: Competitive credit market

There are difficulties in setting the Bank Bonds interest rate because there is no competition in the credit market for Household savings, and Central Bank provides free from interest liquidity. The first possibility is to disaggregate the sector and to make interest rates on Bank Bonds a tool of competition among banks. The other is to allow Central Bank to ration the access to liquidity, charging an interest rate on Advances (adding a financial stock in the model).

The Bank rations the credit to Firms, based on the balance sheet of the applicant, and fixes a different interest rate for each loan. The duration of Loans is fixed. Bank is willing to provide new loans to a firm f in the period up to

$$l_{t}^{f_{t}^{*}} = \min(\nu_{0}(p_{\mathbf{K}}\mathbf{k}_{f})_{t-1} - \mathbf{l}_{t-1}^{f}, \max((\nu_{1}N_{F})^{-1}\mathbf{L}_{t-1}(\frac{\Gamma_{t-1}}{\Gamma^{*}} - 1), 0))$$

at a firm-specific interest rate

$$r_{\mathbf{L}_{t}}^{f} = r_{\mathbf{B}} + \nu_{2}(\Gamma^{*} - \Gamma_{t-1}) + \nu_{3}(\frac{\mathbf{l}_{t-1}^{f}}{v_{f_{t-1}}}) - \nu_{4}(\frac{\pi_{f_{t-1}}}{\mathbf{l}_{t-1}^{f}})$$

These relations account for the fulfilment of the capital requirement for the Bank and the presence of sufficient collaterals on the Firm side.

4.4 Government

Government fixes the public expenditure. It additionally collects taxes and pays unemployment benefits. It determines the amount to be transferred to households (both as monetary and non-monetary, as consumption goods).

When liquidity is needed, Government emits Bonds and sells them at will to the Central Bank. As an approximation, fiscal policy is kept constant during the simulation and taxes are collected only from the Household sector during the transactions. Particularly, the model includes four taxes: a VAT on the purchase of consumption goods $(\tau_{\mathbf{C}})$; a flat financial income tax on distributed interests on Bank shares $(\tau_{\mathbf{S}})$; an inheritance tax on wealth with a constant rate (τ_I) ; a progressive income tax computed as $t_W(w) = w \max(\tau_M \tanh(\tau_F(\frac{w}{p} - \tau_T)), 0)$, where w is the annual wage, p is the average price of consumption goods since the last update. Income taxes are paid by the employer every period and arbitraged once a year.

Fixed unemployment benefits $m_t = \phi \max(w_{t-1}, m_{t-1})$ is paid to those who have not exited the job market and are not employed.

Each period government buys consumption goods which distribute to the Households. Particularly each Household receives an amount of Consumption goods equal to $\mathbf{c}_{ht}^{\mathcal{G}} = ((1 - \varepsilon_0) +$ $\varepsilon_0 e^{-\varepsilon_1 \frac{v_{ht-1}}{p}})\Xi_t.$

We define q as the growth rate of the GDP (measured as Government and Households consumptions, including VAT, plus the variation in Capital stock, noted as Y) in the previous periods, $M = \sum_{h \in \mathcal{H}} m_h$, $C^{\mathcal{G}} = \sum_{h \in \mathcal{H}} (p_{\mathbf{C}}\mathbf{c})_h^{\mathcal{G}}$ and $G = M + C^{\mathcal{G}}$. Assuming a Maastricht-like scenario in which Government has a target deficit δ^* to achieve,

the expected balance of the next period can be written as

$$(1+g)\delta^* Y_{t-1} = \mathbb{E}(G)_t + r_{\mathbf{B}t}(\mathbf{B}_{\mathcal{B}t-1} + \frac{\mathbf{B}_{\mathcal{B}t-1}}{\mathbf{B}^{\mathcal{G}}_{t-1}}(1+g)\delta^* Y_{t-1}) - (1+g+\psi)T_{t-1}$$

$$\mathbb{E}(G)_t = (1+\psi+g)T_{t-1} + (1+g)(1-r_{\mathbf{B}t}\frac{\mathbf{B}_{\mathcal{B}t-1}}{\mathbf{B}^{\mathcal{G}}_{t-1}})\delta^* Y_{t-1} - r_{\mathbf{B}t}\mathbf{B}_{\mathcal{B}t-1}$$

But the expected public expenditure can also be written as

$$\mathbb{E}(G)_{t} = \mathbb{E}(M)_{t} + \mathbb{E}(C^{\mathcal{G}})_{t} \approx M_{t-1} + (1+\psi)p\mathbb{E}(\mathbf{C}^{\mathcal{G}})_{t}$$

$$\approx M_{t-1} + (1+\psi)pN_{\mathcal{H}}\langle \mathbf{c}_{ht}^{\mathcal{G}}\rangle = M_{t-1} + (1+\psi)pN_{\mathcal{H}}\langle \xi_{t}\rangle\Xi_{t}$$

$$\approx M_{t-1} + (1+\psi)pN_{\mathcal{H}}\langle \xi_{t-1}\rangle\Xi_{t} = M_{t-1} + (1+\psi)p\frac{\mathbf{C}^{\mathcal{G}}_{t-1}}{\Xi_{t-1}}\Xi_{t}$$

where it is assumed that expenses for unemployment benefits are approximately constant. Finally, the public expenditure is regulated by updating regularly Ξ as

$$\Xi_{t} = \frac{\Xi_{t-1}}{\langle \mathbf{C}^{\mathcal{G}} \rangle} \frac{\mathbb{E}(G) - \langle M \rangle}{(1+\psi)p}$$

$$\mathbb{E}(G) = (1+\psi+g)\langle T \rangle + (1+g)(1-r_{\mathbf{B}t}\langle \frac{\mathbf{B}_{\mathcal{B}}}{\mathbf{B}^{\mathcal{G}}} \rangle)\delta^{*}Y_{t-1} - r_{\mathbf{B}t}\mathbf{B}_{\mathcal{B}t-1}$$

where the averages are taken since the last update.

Enhancement: A Keynesian Government

In this first version of the model, the Government follows an austerity-inspired policy, similar to the one suggested by European Union treaties.

The behaviour of the Government is, in the end, defined by the target deficit imposed which can be substituted with other targets, like growth, unemployment or poverty rate.

4.5 Central Bank

In the model the role of the Central Bank is to fix the Government's Bonds interest rate according to a Taylor rule $r_{\mathbf{B}} = \psi + \alpha_1(\psi - \psi^*) + \alpha_2(u - u^*) - \alpha_3(\omega - \omega^*)$, where ψ is the inflation rate, u is the capacity utilization measured as the fraction of capital goods used in production, ω is the unemployment rate computed among those who have not voluntarily exited the job market, and starred variables are the targets. The variables are computed as the average since the last update.

Additionally, it passively buys and sells Government Bonds on request to the Bank and the Government. Reserves do not grant interests.

In other words, the Central Bank is a lender of last resort for the Government, which then has no accounting limits to spending.

5 Real Assets

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5.1 Consumption Goods

Consumption Goods represent all the consumption (goods and services) of Households and are homogeneous and non-durable.

Enhancement: Foundational Economy – 3

The exact definition of Foundational good (and service) is not easy to give. An intuition can be provided by the Foundational Economy approach (Arcidiacono et al., 2018):

The sphere of the foundational was then demarcated by three criteria: these goods and services were necessary to everyday life; were consumed daily by all citizens regardless of income; and were distributed according to population through branches and networks. They were partly non-market, generally sheltered and one way or another politically franchised.

Operationally, we can imagine the essential goods in a future model as the ones included in the basket used by national statistics offices to determine the poverty line. In this sense, it is a set of goods which continuously mutate to adapt to new life needs.

Enhancement: Housing

Among essential goods, one should require ad hoc modelling: houses. Houses are special for three reasons

First, they are very heterogeneous in prices and quality, and both are strongly related to the position. In other words, including houses requires (quite always) making the model spatially explicit.

Second, the expenses for housing, in form of rent or mortgage, account for a significant part of monthly consumptions for poor individuals (up to one-half).

Third, real estate properties are an important form of rent extraction and an important tool of investment, and so another important channel of redistribution.

Enhancement: Diversified Goods

A subsequent version of the model can include different (abstract) goods to be produced and consumed. This will create two different innovation processes (better technology for existing goods, or technology for new goods) and will account for the empirical fact that the higher the income more diversified the consumptions are (cfr. Di Domenico & Russo, 2022, §2).

5.2 Capital Goods

Capital goods are characterized by their productivity β and the minimum skill level required to operate them σ . The production happens according to a Leontieff-like function in which one worker with at least σ skill can operate a single capital good getting $\beta_{\mathbf{C}}$ consumption goods as output or $\beta_{\mathbf{K}} = k\beta_{\mathbf{C}}$ capital goods. Each period they have a fixed probability to break and disappear from the model, equal to $\gamma = \langle N_{\mathbf{K}} \rangle^{-1}$, where $\langle N_{\mathbf{K}} \rangle$ is the expected life of the machinery.

6 Financial Assets

6.1 Deposits

Deposits represent liquidity for Households and Firms and are not interest-bearing. Bank satisfies any transaction as long as the balance of the account remains positive.

6.2 Bank Shares

Bank Shares are sold and bought at their nominal value. Bank satisfies every transaction both as emission and as buy-back, as long as the accounts remain positive. Households can buy or sell Bank Shares only at the beginning of each period. At the end of each period, interests are paid, according to the rate fixed by the Bank at the beginning of the period.

6.3 Loans

Loans are issued by the Bank to a specific Firm. They have a fixed duration during which an equal share of capital is repaid plus the interest on the remaining debt. Interests are fixed by the Bank at a different value for each Firm at the time of emission.

6.4 Government Bonds

Government Bonds are sold and bought at their nominal value and do not expire. Central Bank satisfies every transaction. Bank can buy Government Bonds only at the beginning of each period. At the end of each period, interests are paid only to the Bank, according to the rate fixed by the Central Bank at the time beginning of the period.

6.5 Reserves

Reserves represent liquidity for Bank and Government and are not interest-bearing. Central Bank satisfies any transaction as long as the balance of the account remains positive.

7 Dynamics

7.1 Consumption Goods market

Each Household sees $\chi_{\mathbf{C}}$ Consumption Firms $\chi_{\mathbf{C}}$ times, each time it buys $\frac{\mathbf{c}^* - \mathbf{c}_h^{\mathcal{G}}}{\chi_{\mathbf{C}}}$ at the lowest offered price until it matches the desired consumption or ends liquidity.

7.2 Capital Goods market

Each Consumption Firm sees $\chi_{\mathbf{K}}$ Capital Firms $\chi_{\mathbf{K}}$ times (including the last one from which it has bought), each time it buys machinery with a total production capacity of $\frac{\Delta b}{\chi_C}$, choosing the one with the lowest value of $\beta p_{\mathbf{C}} - \langle w_{\sigma} \rangle - \frac{p_{\mathbf{K}}}{\langle N_{\mathbf{K}} \rangle}$ until it matches the desired quantity or ends liquidity.

7.3 Labour market

Households are employed by a Firm until they are fired, they chose to exit the job market or they accept an offer from another Firm.

Firms can fire workers only when profits turn negative. In that case, Firms fire workers until the number of workers reaches $u^*\mathbf{k}$. Additionally, in the case the Firm is not able to pay a worker, they is fired. In both cases, Firms start to fire those with lower skills.

Firms match each employed worker with the most productive machinery they can use, starting with those with higher skills. For this purpose, a researcher is treated like a worker assigned to a machinery with productivity σ^* . Then the current potential output (as the sum of the productivity of the used machinery) is computed and vacancies are filled starting from the most productive unused machinery. All research vacancies are filled if possible. For each vacancy, the Firm sees $\chi_{\mathcal{H}}$ workers which have the required skills and earn less than the average salary in the model for the skill level at the end of the previous period. The Firm employs the one with the higher skills offering the average salary in the model for the required skill level.

Each vacancy is filled once and new vacancies are not filled.

Enhancement: Collective bargain

The average wage in the economy used to define the new salary proposed can be replaced by a "collective bargained" salary which is fixed economy-wide for each skill level (eventually differentiating between productive sectors) which increases with the employment rate and the average firm size.

7.4 Retirement and inheritance

When a Household reaches a certain age it is considered retired and is replaced by a new agent in the model which inherits their (taxed) wealth and enters the simulation with a random skill level proportional to the inherited wealth, and a random age proportional to the skill level.

7.5 Non Performing Loans

In the case a Firm is unable to repay the principal of a loan or to pay the interest, the unpaid sum is added to the import of the loan and the duration is increased by one period. Additionally, the loan is marked as non-performing.

7.6 Bankrupt

Once the net value of a Firm becomes negative the Firm declares bankruptcy, fires all the employed households and loose all the financial assets (loans and deposits). It is "replaced" by a new firm which inherits the capital stock.

Enhancement: Variable number of Firms

In this version of the model, the number of Firms is constant in the simulation. It is possible to assume that if the profit rate (or the average markup of a sector) increases over a certain threshold the Bank (or the Firm-owners) starts a new Firm in the sector investing an initial monetary capital.

7.7 Innovation

Each Capital Firm can achieve an innovation each period with a probability $\theta = e^{-\zeta q}$ where R is the number of employed workers not assigned to a Capital Good with skills at least σ^* .

If the innovation is achieved the Capital Goods produced by the Firm increase its productivity $\Delta \beta_{\mathbf{C}} = \text{Beta}(1, b_0)$ and modify the required skills as $\Delta \sigma = (\Delta \beta_{\mathbf{C}} - b_1 \text{Beta}(1, b_2))$.

Enhancement: Imitation and the frontier

Catching up with the leading technology is easier than moving the innovation frontier. This empirical evidence can be modelled in two ways: the first one is to model two different innovation processes, and the other is to make p increasing with $\beta_{\text{MAX}} - \beta$.

²⁷⁵ 8 Model steps

- A Statistics are computed at the relevant frequency
- B Agents variables independent from other agents' decisions are updated
- C [QUARTERLY] Central Bank sets the Government Bonds interest rate
- D.0 Bank sets the interest rate on Bank Bonds
- D.1 Bank buys Government Bonds to reach the liquidity requirement
- D.2 [QUARTERLY] Government update the public spending policy
- E.0 Households set desired consumption and savings
- E.1 Firms set desired output and investment
- F.0 Households acquire Bank Bonds
- F.1 Firms ask the Bank for loans
 - G Labour market and wages payment
 - H Production and price setting
 - I Innovation

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- L.0 Government pays unemployment benefits
- L.1 Government buys and distributes Consumption Goods
 - M Households Consumption Goods market
 - N Capital Goods market
 - O.0 Firms repay loans and interests
 - O.1 Government pays interest on Bonds to the Bank
 - P Firms distribute dividends
 - Q Bank pays interests on Bonds
 - R.0 [YEARLY] Income taxes are arbitraged
 - R.1 Capital depreciation
 - S.0 Households retire and get substituted
- 300 S.1 Firms bankrupt and get substituted

9 Parameters

| | Description | Value | Source |
|----------------------|--|-------|--------|
| Σ | Relative skill variation | | |
| | Distribution parameters to assign initial skill level | | |
| $\rho_{\mathcal{H}}$ | Deposits to consumption ratio | | |
| | Distribution parameters for marginal propensity to consume | | |
| $ ho_{f C}$ | Production over expected sales | | |
| $ ho_{\mathcal{F}}$ | Liquidity over expected wages and investiment ratio | | |
| u^* | Target capacity utilization | | |
| Θ | Markup growth rate | | |
| r_{Π} | Profit distribution rate | | |
| $ ho_Q$ | Number of researcher growth rate | | |
| σ^* | Minimum researchers' skill level | | |
| Λ^* | Target liquidity ratio | | |
| Γ^* | Target capital ratio | | |
| λ | Bank share premium | | |
| ν_0 | Loan to capital ratio for firms | | |
| ν_1 | Number of firms correction to compute maximum loan amount | | |
| ν_2 | Loan rate premium for Bank capitalization | | |
| ν_3 | Loan rate premium for firms loan to net worth ratio | | |
| ν_4 | Loan rate premium for profits to loans ratio | | |
| $	au_{f C}$ | VAT rate | | |
| $	au_{\mathbf{S}}$ | Financial income tax rate | | |
| $	au_I$ | Inheritance tax rate | | |
| $	au_M$ | Maximum labour income tax rate | | |
| $	au_F$ | Labour income tax progressivity | | |
| $	au_T$ | Labour income tax threshold | | |
| ϕ | Unemployment benefits decay rate | | |
| δ^* | Target deficit | | |
| α_1 | Inflation coefficient in Taylor rule | | |
| α_2 | Capacity utilization coefficient in Taylor rule | | |
| α_2 | Unemployment coefficient in Taylor rule | | |
| k | Comsumption goods to capital good output | | |
| γ | Capital depreciation | | |
| $\chi_{\mathbf{C}}$ | Number of Consumption Firms seen | | |
| $\chi_{\mathbf{K}}$ | Number of Capital Firms seen | | |
| $\chi_{\mathcal{H}}$ | Number of Households seen | | |
| ζ | Innovation speed | | |
| \dot{b}_0 | Productivity gain distribution parameter | | |
| b_1 | Maximum required skill loss | | |
| b_2 | Required skill loss distribution parameter | | |

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