

1.

- a. $(37)_{10} = (100101)_2$
- b. $(65)_{10} = (1000001)_2$
- c. $(138)_{10} = (10001010)_2$

	Quotient	Remainder	a
138/2	69	0	0
69/2	34	1	1
34/2	17	0	2
17/2	8	1	3
8/2	4	0	4
4/2	2	0	5
2/2	1	0	6
$\frac{1}{2}$	0	1	7

2.

- a. $(101101)_2 = (45)_{10}$
- b. $(111001)_2 = (57)_{10}$
- c. $(1100111)_2 = (103)_{10}$

$$\begin{aligned}
 &(1100111)_2 \\
 &= (1 \times 2^6) + (1 \times 2^5) + (0 \times 2^4) + (0 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (1 \times 2^0) \\
 &= 64 + 32 + 0 + 0 + 4 + 2 + 1 \\
 &= 103
 \end{aligned}$$

3.

- a. $(123)_{10} = (173)_8$
- b. $(249)_{10} = (371)_8$

	Quotient	Remainder	a
249/8	31	1	0
31/8	3	7	1
$\frac{3}{8}$	0	3	2

4.

a. $(58)_{10} = (3A)_{16}$

b. $(249)_{10} = (F9)_{16}$

	Quotient	Remainder	a
249/16	15	9	0
15/16	0	15 (F)	1

5.

a. $(673)_8 = (1AA)_{16}$

$$(673)_8 = (110\ 111\ 011)_2 = (1\ 1011\ 1011)_2 = (0001\ 1011\ 1011)_2 = (1AA)_{16}$$

b. $(23EF9)_{16} = (0437371)_8 = (437371)_8$

$$\begin{aligned}(23EF9)_{16} &= (0010\ 0011\ 1110\ 1111\ 1001)_2 \\ &= (00\ 100\ 011\ 111\ 011\ 111\ 001)_2 \\ &= (000\ 100\ 011\ 111\ 011\ 111\ 001)_2 \\ &= (0437371)_8\end{aligned}$$

6.

a. $(36.375)_{10} = (100011.011)_2$

	Quotient	Reminder	a
35/2	17	1	0
17/2	8	1	1
8/2	4	0	2
4/2	2	0	3
2/2	1	0	4
$\frac{1}{2}$	0	1	5

$= (100011)_2$

	Integer	Fraction	a
0.375 X2	0	0.75	-1
0.75 X2	1	0.5	-2
0.5 X2	1	0	

$= (.011)$

$\Rightarrow (100011.011)_2$

b. $(10110.0101)_2 = (22.3125)_{10}$

$$\begin{aligned}(10110.0101)_2 \\ = (1 \times 2^4) + (0 \times 2^3) + (1 \times 2^2) + (1 \times 2^1) + (0 \times 2^0) + (0 \times 2^{-1}) + (1 \times 2^{-2})\end{aligned}$$

$$\begin{aligned}
 &+ (0 \times 2^{-3}) + (1 \times 2^{-4}) \\
 &= 16 + 0 + 4 + 2 + 0 + 0 + 0.25 + 0 + 0.0625 \\
 &= 22.3125
 \end{aligned}$$

7.

a. $10011 - 10001 = (00010)_2 = (2)_{10}$

$$\begin{array}{r}
 \text{2's complement of :} \quad 10001 \\
 \text{flip} \quad 01110 \\
 \text{add +} \quad 1 \\
 \quad 01111 \\
 \text{add +} \quad 10011 \\
 \quad 100010 \\
 \text{rule 1:} \quad 00010
 \end{array}$$

$$(00010)_2 = (2)_{10}$$

b. $100010 - 101011 = (\underline{0}001001)_2 = -9$

$$\begin{array}{r}
 \text{2's complement of :} \quad 101011 \\
 \text{flip} \quad 010100 \\
 \text{add +} \quad 1 \\
 \quad 010101 \\
 \text{add +} \quad 100010 \\
 \quad 110111 \\
 = \quad \underline{0}110111
 \end{array}$$

Rule 2: 2's complement of : 110111

$$\begin{array}{r}
 \text{flip:} \quad 001000 \\
 \text{add:} \quad + \quad 1 \\
 \quad 001001
 \end{array}$$

$$\text{Result} = (\underline{0}001001)_2 = (-9)_{10}$$

8.

a. $(+29)_{10} + (-49)_{10}$

$$(29)_{10} = (0011101)_2$$

$$(49)_{10} = (0110001)_2$$

In 8 bit CPU:

$$(+29) = \underline{0} \ 0011101$$

$$(-49) = \underline{1} \ 1001111 \text{ (2's complement of } 0110001 = 1001110 + 1 = 1001111)$$

$$\underline{0}0011101 + \underline{1}100111 = \underline{1}1011100 = -1101100$$

$$\text{2's complement of: } 1101100 = 0010011 + 1 = 0010100$$

$$\text{Result: } (-0010100)_2 = (-20)_{10}$$

b. $(-29)_{10} + (-49)_{10}$

In 8-bit CPU:

$$(-29) = \underline{1} \ 1100011 \text{ (2's complement of } 0011101 = 1100010 + 1 = 1100011)$$

$$(-49) = \underline{1} \ 1001111 \text{ (from 8(a))}$$

$$\underline{1}1100011 + \underline{1}1001111 = \underline{1}10110010 = \underline{1}0110010 = -0110010$$

$$\text{2's complement of: } 0110010 = 1001101 + 1 = 1001110$$

$$\text{Result: } (-1001110)_2 = (-79)_{10}$$

9.

a. Unsigned binary format

$$10110110 = (1 \times 2^7) + (0 \times 2^6) + (1 \times 2^5) + (1 \times 2^4) + (0 \times 2^3) + (1 \times 2^2)$$

$$+ (1 \times 2^1) + (0 \times 2^0)$$

$$= 128 + 0 + 32 + 16 + 0 + 4 + 2 + 0$$

$$= 182$$

$$(10110110)_2 = (182)_{10}$$

b. Signed 1's complement format

10110110 in 8 bit CPU

$$= \underline{1} \ 0110110 = -0110110$$

$$\text{1's complement of: } 0110110 = 1001001$$

$$(1001001)_2 = 2^6 + 0 + 0 + 2^3 + 0 + 0 + 2^0 = 64 + 8 + 1 = (73)_{10}$$

$$\text{Result} = (-1001001)_2 = (-73)_{10}$$

c. Signed 2's complement format

10110110 in 8 bit CPU

$$= \underline{1} \ 0110110 = -0110110$$

$$\text{2's complement of: } 0110110 = 1001001 + 1 = 1001010$$

$$(1001010)_2 = 2^6 + 0 + 0 + 2^3 + 0 + 2^1 + 0 = 64 + 8 + 2 = (74)_{10}$$

$$\text{Result} = (-1001010)_2 = (-74)_{10}$$

d. BCD format

$$(10110110)_2 = (182)_{10} \text{ (from 9.a)} = (0001\ 1000\ 0010)_{\text{BCD}}$$

$$\text{In 8-bit CPU: } (000110000010)_{\text{BCD}} = (1000\ 0010)_{\text{BCD}} = (82)_{10}$$