## Hecke

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#### **Abstract**

The naive goal of this notes is to include all the relevant stories around the word Hecke.

## 1 Buzzwords/Summaries

Some of the few terminologies I don't know that I would like to learn at some point:

Abstract Iwahori-Hecke algebra. See [12]. Their representations [13].

Iwahori-Hecke algebra, finite Hecke algebra realised under (p-adic) representation thery. Bump, HKP [1, 2].

Geometric construction of the double affine Hecke algebra via affine flag manifolds [6](?). Geometric realisation of Hecke algebras. See [11].

DAHA, Rational DAHA, Tits DAHA, Cherednik algebra: the people I know are Cherednik, Etingof, Ginzburg. Connection to Macdonald's polynomial and something from mathematical physics (?).

Higher representations: Raphael Rouquier. 2-representations of Kac-Moody. Rouquier [10, 9].

Quiver Hecke algebra?

Hecke eigenvalues, Hecke eigensheaves, Hecke correspondence in Langlands program (?) Geometric Satake as categorification of spherical Hecke (?). See Edward Frenkel for many surveys about this.

Hecke operators in modular forms (?).

### References

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