

Leptogenesis: A non-relativistic study

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1. Introduction

2. Outline of baryogenesis

One way to describe the observed baryonic asymmetry is by postulating, that the universe has been in an asymmetric state just from the beginning and that the matter and antimatter is concentrated in big domains throughout the universe, which come into contact just at their outer borders. Technically there is no reason for the universe not to have started in an asymmetric state, in that case one would measure high gamma rates due to the matter-antimatter-annihilation right between these distinct regions.

Since there is no kind of such radiation seen, patches of different kinds of matter have to be as big as the presently observable universe. Because this doesn't seem very plausible, so the baryonic asymmetry had to arise dynamically from an universe where matter and antimatter existed in the same amounts.

Actually in 1967 the Soviet physicist Andrei Sakharov postulated the criteria, which have to be met in order for an excess of baryons over anti-baryons to be generated out of a fully symmetrical universe.

2.1. Sakharov Conditions

As mentioned above there are three crucial properties of nature, the Sakharov conditions, which are required to produce a net baryon number greater than zero. These three conditions are:

1. B-violating process(es)
2. C and CP violation
3. Departure from or loss of thermal equilibrium

For a general insight of these three conditions the first one will be skipped, since it is quite obvious, that in a totally symmetric universe there has to be at least one B-violating process in order to cause an imbalance in matter and antimatter.

The general importance of the other two will be discussed in the following.

2.1.1. C and CP-violation

Charge conjugation (C), parity (P) and their combination (CP) are two or more specifically three basic symmetries of the universe. C symmetry states, that physical processes are the same, even after exchanging particles for their respective anti-particles, while P-symmetry guarantees invariance under the transformation $\vec{r} \rightarrow -\vec{r}$. CP symmetry then simply is a sequence of a C followed by a P transformation.

To explain why C has to be violated for baryogenesis being possible, consider the B-violating reaction

$$X \rightarrow Y + B$$

with X and Y particles with $B=0$ and B representing the excess baryons. This reaction happens with a certain rate, which is, using C as a symmetry, just the same as the reaction rate for the conjugate process.

$$\Gamma(X \rightarrow Y + B) = \Gamma(\bar{X} \rightarrow \bar{Y} + \bar{B}) \quad (2.1)$$

Eq. 2.1 implies, that under C exactly the same amount of baryons and anti-baryons will be produced and therefore no excess baryons are left after the annihilation. This means C must be violated.

But additionally to this CP violation is essential for baryogenesis. To illustrate why, take a closer look at the also clearly B violating X decay with its two channels:

$$\begin{aligned} X &\rightarrow q_L q_L \\ X &\rightarrow q_R q_R \end{aligned}$$

with q an arbitrary quark. The subscripts L and R denote the the left - or right-handedness chirality of the decay products. CP then effects each particle as follows

$$\begin{aligned} X &\xrightarrow{CP} \bar{X} \\ q_L &\xrightarrow{CP} \bar{q}_R \\ q_R &\xrightarrow{CP} \bar{q}_L \end{aligned}$$

So CP doesn't just change matter for anti-matter, but the handedness of the particles as well. So if CP holds as a symmetry the consequences for the reaction rates are:

$$\Gamma(X \rightarrow q_L q_L) = \Gamma(\bar{X} \rightarrow \bar{q}_R \bar{q}_R) \quad \Gamma(X \rightarrow q_R q_R) = \Gamma(\bar{X} \rightarrow \bar{q}_L \bar{q}_L)$$

Adding these two results in

$$\Gamma(X \rightarrow q_L q_L) + \Gamma(X \rightarrow q_R q_R) = \Gamma(\bar{X} \rightarrow \bar{q}_R \bar{q}_R) + \Gamma(\bar{X} \rightarrow \bar{q}_L \bar{q}_L) \quad (2.2)$$

Eq. 2.2 implies, that as long as there are as many particles X as anti-particles \bar{X} in the initial state of the universe, which is just the starting point of the modell the Sakharov conditions try to describe, there can only be an asymmetry between left and right-handed particles be achieved, but that isn't a baryon asymmetry, which is clearly needed for baryogenesis. CP must be violated.

So the bottom line here is, that the existence of B-violating processes is not sufficient for baryogenesis, but that there also has to be C and also CP violation, since without this kind of symmetry breaking any baryonic excess would be washed out by the corresponding C or CP conjugated process, as shown with the simple examples above.

2.1.2. Departure from thermal equilibrium

The last condition to be met in order for baryogenesis to be achievable is that the the B, C and CP violating processes must occur outside the thermal equilibrium. To illustrate this we first consider the phase space distribution of a species X of quantum particles

$$f(E_X) = \frac{1}{e^{\frac{E_X - \mu_X}{T}} \pm 1} \quad (2.3)$$

The energy E_X and the momentum \vec{p}_X are related via the relativistic energy-momentum-relation $E^2 = \vec{p}^2 + m^2$. μ_X describes the chemical potential of the particle species X, which is an important quantity for describing thermal equilibrium states, as the chemical potentials of two species X and Y, which are in thermal equilibrium are related by $\mu_X = \mu_Y$ or for more species $\sum_i \mu_i = 0$. Using eq. 2.3 to compute the particle density of a certain particle species one gets

$$n_X = g_X \int \frac{d^3 p}{(2\pi)^3} f_X(E) \quad (2.4)$$

where g_X denotes the number of inner degrees of freedom of X.

In the non-relativistic limit there holds $m \gg E - \mu \gg T$. With this approximation the denominator

of the exponential function in eq. 2.3 gets small compared to the numerator so the exponential itself gets so big that the ± 1 can be neglected, in the non-relativistic limit, you get the same particle density for fermions and bosons. By dividing the energy E_X into the rest energy m_X and the kinetic energy E_{kin} and after approximating

$$E_{\text{kin}} \approx \frac{p^2}{2m} \quad (2.5)$$

for non-relativistic particles, integrating according to 2.4 yields

$$n_X = g_X \frac{4\pi}{(2\pi)^3} \int dp p^2 e^{\frac{\mu - m_X}{T}} e^{-\frac{p^2}{2m_X T}} = g_X \left(\frac{m_X T}{2\pi} \right)^{\frac{3}{2}} e^{-\frac{m_X - \mu_X}{T}} \quad (2.6)$$

Analogously you get the number density for the corresponding anti-particle \bar{X}

$$n_{\bar{X}} = g_{\bar{X}} \left(\frac{m_{\bar{X}} T}{2\pi} \right)^{\frac{3}{2}} e^{-\frac{m_{\bar{X}} - \mu_{\bar{X}}}{T}} \quad (2.7)$$

Now suppose X and its anti-particle \bar{X} with $B_X = -B_{\bar{X}} \neq 0$ are in thermal equilibrium than the condition $\mu_X = \mu_{\bar{X}}$ holds. Comparing eq. 2.6 and 2.7 one sees, that the chemical potential is the only property that could differ for particles and antiparticles. Now using the equilibrium condition for chemical one finally gets

$$n_X = n_{\bar{X}} \quad (2.8)$$

Looking at eq 2.8 it is quite obvious that even with B , C and CP violating any produced excess baryon number B will be washed out in equilibrium by other processes happening in equilibrium. This illustrates the final Sakharov Condition, that next to B , C and CP violation a departure from equilibrium is needed for a dynamic production of excess baryons.

Interesting to note is, that there is quite an easy way of approximately determining if reactions take place in thermal equilibrium is by comparing the reaction rate with the expansion of universe, described by the Hubble constant H , which isn't actually a constant but changes with time. So if the relation

$$\Gamma \gtrsim H \quad (2.9)$$

holds, the reactions take place fast enough for them to be in equilibrium. This can be made understandable, it is useful to look at this from the rest frame of the particles taking part in the reactions. Then the particles don't notice any expansion of the universe since they move and react too fast with each other, therefore the expansion doesn't really affect the equilibrium state. Otherwise if the reactions occur slower than the universe expands, so if

$$\Gamma < H \quad (2.10)$$

is valid, than the expansion happens fast enough that particles get separated too far from each other, so they can't react anymore and the reactions fall out of equilibrium.

2.2. Baryogenesis in the Standard Modell

Although nowadays there are no records or experimental proofs of baryon number violating processes, that doesn't mean there is a need for physics outside the Standard Modell (SM) of particle physics, at least on a qualitative level.

2.2.1. Electroweak baryogenesis

As it turns out the electroweak part of the SM with its $SU(2)_L \times U(1)_Y$ symmetry groups suits best for describing baryogenesis. The following discussions will illustrate how the SM satisfies all three Sakharov conditions.

C and CP violation It is already proven theoretically und experimentally by numerous well-known experiments, like for example the Wu experiment in 1956, that C symmetry is maximally violated by the weak interaction in the leptonic as well as in the hadronic sector. As shown by Kobayashi and Maskawa through expanding the Cabibbo hypothesis and experimentally confirmed, weak interactions in the hadronic sector also violate CP invariance, which manifests as an complex phase in the CKM quark mixing matrix. In the leptonic sector however the CP violation through a complex phase only got postulated in the PMNS neutrino mixing matrix to try to describe neutrino oscillations, but this phase still needs to be measured.

Nevertheless the elektroweak part of the SM, more precise the weak interactions, since electromagnetism doesn't violate C or even P, satisfies at least one of the three Sakharov conditions.

B violation Although the first Sakharov condition, the necessity of baryon number violating processes, seems to be the most obvious, the way these are realised in the SM is a bit more difficult than it seems.

Since at the first look the baryonic and, since it is going to play an important role during the following discussion, the leptonic current are conserved

$$\partial^\mu J_\mu^B = 0 \quad (2.11)$$

$$\partial^\mu J_\mu^L = 0 \quad (2.12)$$

one would assume there is no way the SM could produce an baryon asymmetry. However, by considering quantum fluctuation meaning orders higher than just tree level one finds, that the currents for the left- and right-handed parts f_L and f_R respectively, where stands for quarks and leptons equally, aren't conserved and not the same [1]

$$\partial^\mu \bar{f}_L \gamma_\mu f_L = -c_L \frac{g^2}{32\pi^2} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \quad (2.13)$$

$$\partial^\mu \bar{f}_R \gamma_\mu f_R = +c_R \frac{g^2}{32\pi^2} F_{\mu\nu}^a \tilde{F}^{a\mu\nu} \quad (2.14)$$

where g denotes the gauge coupling, $F^{a\mu\nu}$ the field tensor, $\tilde{F}^{a\mu\nu}$ the dual field tensor and c_L and c_R depend on the representation of f_L and f_R . This behaviour of the currents at quantum levels is known as Adler-Bell-Jackiw or chiralty anomaly. Since $SU(2)_L$ gauge boson only couples with left-handed particles $c_R^W=0$, while the $U(1)_Y$ gauge boson couples to both handednesses, but with different strength, therefore $c_R^Y \neq c_L^Y$. Although this section only focuses on electroweak baryogenesis, it is mentionable that with the $SU(3)_c$ gauge bosons of the strong interactions don't produce any chiralty anomaly because they couple with left as well as right-handed particles with the same strenght, so $c_R^c = c_L^c$ and both currents in (2.13) and (2.14) cancel each other out in the case of strong interactions.

Putting this and eqautions 2.11 - 2.14 together, gives a pretty interesting result

$$\partial^\mu J_\mu^B = \partial^\mu J_\mu^L = \frac{n_F}{32\pi^2} \left(-g_w^2 W_{\mu\nu}^a \tilde{W}^{a\mu\nu} g'^2 G_{\mu\nu}^a \tilde{G}^{a\mu\nu} \right) \quad (2.15)$$

with $W^{a\mu\nu}$ and $G^{a\mu\nu}$ the field strenght tensors of the $SU(2)_L$ and $U(1)_Y$ gauge groups and $n_F=3$ the number of particle families.

Analyzing eq. 2.15 one easily figures out, that although baryon and lepton number are not conserved separatedly the difference B-L of these numbers is very well conserved. Integrating both sides of eq. 2.15 as shown in [1, pp. 15f.] results in

$$\Delta B = \Delta L = n_F \Delta N_{CS} \quad (2.16)$$

where ΔN_{CS} is the difference of so called Chern-Simons numbers. How exactly these numbers are derived and what their integral representation is can also be looked up in [1, 2, 3], but isn't of great interest for this thesis. However one property of these numbers is quite relevant for baryon asymmetry, namely that each integer valued Chern-Simons number describes one distinct vacuum state of the infinite electroweak vacua with minimal energy, which are separated by a potential barrier. The difference of these numbers of two vacuum states right next to each other is $\Delta N_{CS} = \pm 1$, so changing from one vacuum state N_i to another N_f results in $\Delta N_{CS} \neq 0$ and therefore a change in baryon and lepton number is induced. Also interesting to notice is, since the number of particle families $n_F=3$ baryon and lepton numbers change at least by three units each.

The last question regarding B violation in the SM is about how such a transition between two vacuum states can be accomplished. One way is through a quantummechanical effect called the instanton, where the system simply tunnels through the barrier between two vacuum states with different Chern-Simons numbers. However 't Hooft, the one showing B violation by the chiral anomaly, also showed [1, Ref. 22,24] that the cross section for such a tunneling process is about

$$\sigma \propto e^{-\frac{4\pi}{\alpha_w}} \sim 10^{-164} \quad (2.17)$$

with $\alpha_w = \frac{g^2}{4\pi} \cong \frac{1}{30}$. This cross section is so small, that such an instanton transition between two vacua probably didn't happen even once during the whole lifetime of the universe.

A second way such a change of vacua can be induced is through the so called sphaleron processes. The requirement for these processes to take place is that the system has enough energy to go over the potential barrier instead of tunneling through. The minimum energy needed, known as the sphaleron energy, is about [1, 2]

$$E_{sph} = \frac{4\pi}{g_2} v(T) \cong 8 - 13 \text{ TeV} \quad (2.18)$$

where λ describes the four-Higgs interaction and the function f lives on an interval [1.56, 2.72]. The temperature dependent quantity $v(T)$ describes the vacuum expectation value of the Higgs field at the temperature T , which will be important later on.

In fact these kind of processes are quite possible for temperatures above around 100 GeV, however below this temperature the rate of sphaleron processes is exponentially suppressed by a Boltzmann factor. It is also mentionable that comparing the sphaleron rate for temperatures above 100 GeV, which are proportional to the fourth power of the temperature [1, p. 19], with the Hubble constant, gives information about when these processes are in thermal equilibrium and numerical evaluations yield that the sphaleron processes are in thermal equilibrium for

$$100 \text{ GeV} \lesssim T \lesssim 10^{12} \text{ GeV}$$

So as shown in section 2.1.2, even though the SM provides the necessary tools for C, CP and B violation, below the temperature of around 10^{12} GeV any produced net baryon number will be washed out and below 100 GeV the temperature isn't even high enough to induce sphaleron processes.

Departure from thermal equilibrium and electroweak phase transition The final question to answer regarding baryogenesis in the SM is how the last Sakharov condition, the departure from thermal equilibrium is realized. The most common way is by using the electroweak phase transition.

This phenomenon heavily relies on the vacuum expectation value (VEV) of the $SU(2)_L$ Higgs doublet and its behaviour during the early times of the universe. At the present day the VEV isn't

equal to zero, which leads to a gauge symmetry breaking and therefore masses of every massive particle. But it has already been shown [1, Ref. 32], that for high temperatures the VEV of the universe equals zero and the $SU(2)_L \times U(1)_Y$ gauge symmetry is still intact, even at the ground states. This obviously means, that at some point during the evolution of the universe and at some critical temperature $T=T_c$ the VEV changed from zero to non-zero, or in other words a phase transition from a totally symmetrical phase to a phase with broken symmetry happened at some point. In order to generate a departure from thermal equilibrium for the B violating reaction this transition must be strongly of first order, meaning at $T=T_c$ the VEV changes discontinuously from zero to non-zero.

Just as with cooling steam this process can be imagined with bubbles of phases with broken symmetries forming and expanding inside the phase of unbroken symmetry, just as droplets of water form in the vapor and expand, until they connect and finally cover all space. Now the way this phase transition leads to a baryon asymmetry is as follows.

First of all consider a thin wall, so that the area where quarks and fermions interact with the walls can be approximated as a step function. Also, to simplify matters, assume that the expansion of the bubbles of broken symmetry is spherical symmetric, so this problem can be reduced to one dimension.

At the start of this baryon asymmetry generating process there is the same amount of particles and anti-particles.

While the bubble expands left- and right-handed quarks and anti-quarks from the unbroken phase hit the bubble wall, get reflected under CP violating processes and change their handedness because of angular momentum conservation and since charge conservation holds (anti-)quarks are only allowed to scatter into (anti-)quarks. The scattering processes are the following

$$q_L \rightarrow q_R$$

$$q_R \rightarrow q_L$$

$$\bar{q}_L \rightarrow \bar{q}_R$$

$$\bar{q}_R \rightarrow \bar{q}_L$$

Since these scattering processes are not CP conserving the reflection coefficients are not the same for all of the reactions above.

$$\Delta R = R_{\bar{L} \rightarrow \bar{R}} - R_{R \rightarrow L} = R_{\bar{R} \rightarrow \bar{L}} - R_{L \rightarrow R} \quad (2.19)$$

Using CPT invariance yields

$$R_{\bar{L} \rightarrow \bar{R}} = R_{L \rightarrow R} \quad (2.20)$$

$$R_{\bar{R} \rightarrow \bar{L}} = R_{R \rightarrow L} \quad (2.21)$$

These relations alone imply that there still is no net baryon number since the differences J_q^L of the fluxes of \bar{q}_R and q_L and the J_q^R of q_R and \bar{q}_L reflected back into the symmetric phase are the same and cancel each other out. But considering that the (B+L) violating sphaleron processes because of their electroweak origin only interact with left-handed quarks and right-handed anti-quarks J_q^L changes while J_q^R stays the same since it only takes right-handed quarks and left-handed antiquarks into account. This leads to a non-zero baryon number and especially if $J_q^L > 0$ then there are more left-handed quarks than right-handed anti-quarks and therefore $\Delta B > 0$ in the symmetric phase away from the wall. If the bubble then expands over the region of a net baryon number greater zero this B gets frozen in, since in the broken phase the (B+L) violating processes that could wash out the asymmetry are strongly suppressed by the Boltzmann factor as stated above.

Taking into account that particles from the broken phase can transmit into the symmetric phase

and evaluating this quantitative as shown in [1, pp. 36-37] yields the result mentioned above. For an net baryon number greater than zero the CP violating processes at the bubble wall have to act in such way that the current J_q^L is greater than zero as well.

2.2.2. Failures of the SM

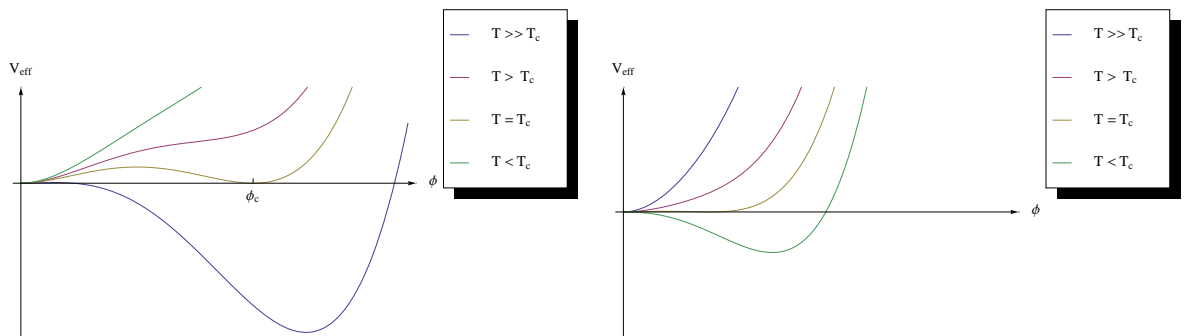
Since the SM offers everything needed to describe baryogenesis in the early universe one could naively say that the only thing left is the experimental proof to be delivered.

Having said this recent experiments have shown that the SM alone, despite containing possible B, C and CP violating processes, isn't able to provide an phase transition of strong enough first order or more precisely a phase transition of first order at all, what will be shown in the following. According to the Landau theory phase transitions are described by the behaviour of a so called order parameter. So for a first order phase transition the order parameter has to change discontinuously at the critical point, while for a second order transition the order parameter has to change drastically as well, but this change occurs continuously. In this case of the electroweak phase transition the order parameter is the expectation value of the Higgs field, denoted as ϕ . In addition to this one needs to describe the temperature dependent free energy of the system as a function of the parameter which result in the effective potential $V_{\text{eff}}(\phi, T)$. This potential describes the energy of a system in a state with the Higgs expectation value ϕ . Since in general this state isn't one of minimal energy and because every system prefers to minimize its energy, it changes into a state described by the minimum of the potential where the expectation value of the Higgs is by definitisch the Higgs VEV.

As it is already known, that the Higgs VEV had to change from zero at the big bang to a non-zero value while the universe cooled down to the temperature measured nowadays, so it is just natural to look the change of this value with temperature. The change of the VEV can now happen continuously in which case the system undergoes a second order phase transition or discontinuously what is needed for an first order transition and especially for elektroweak baryogenesis. Both cases are shown in figure 1 for the effective Higgs potential including 1-loop corrections [3]

$$V_{\text{eff}} = D(T^2 - T_0)^2 \phi^2 - ET\phi^3 - \frac{1}{4}\lambda\phi^4 \quad (2.22)$$

for different non-zero temperature regimes. D and E are constant factors which aren't of great interest for this discussion and λ describes the already mentioned 4 Higgs self coupling.



(a) Effective Higgs field for first order transition (b) Effective Higgs field for second order transition

Figure 1

Analyzing figure 1a clearly shows the first order characteristics of the phase transition. While for high temperatures the VEV equals zero for the highly symmetric phase, the potential slowly develops a second minimum for decreasing temperature until at the critical temperature $T=T_c$

there are two energetically degenerated minima, one at $\phi_1=0$ and one at $\phi_2=\phi_c$, which are separated by an energy barrier. However the system can change from the minimum at ϕ_1 to the one at ϕ_2 via tunneling through the barrier what results in a discontinuous change of the VEV and therefore induces a first order phase transition. While the universe keeps on cooling down because of the universe's expanding the new minimum is getting energetically lowered while the original one stays at $V_{\text{eff}}=0$ and thus becomes a maximum, leaving an unstable state where once was a symmetric vacuum state.

How this can be imagined in the early universe is, that at some point in space and time the universe tunneled from one minimum to another thus breaking SM symmetry locally and producing a local bubble of broken phase. These bubbles get bigger with time and combine with other bubbles whose production gets much more likely as the lower temperatures lower the barrier between the minima and increase the tunneling probability.

On the other hand figure 1b shows how the universe would develop in case of a second order transition. In this case even at $T=T_c$ there are no two degenerated minima but the new one develops gradually while the original minimum gradually becomes the unstable maximum you also get in figure 1a for low temperatures. Since there are no two minima the universe can choose between there is also no bubble formation but instead a continuous condensation throughout the universe what isn't enough to induce baryogenesis.

Now that the two possibilities of the electroweak phase transition were represented the question how and why the SM fails to provide a strong enough first order phase transition still needs to be answered.

To do this it is useful to define a quantity that corresponds to the strength of the phase transition, which for this cause will be

$$\frac{v_{T_c}}{T_c} \gtrsim 1 \quad (2.23)$$

The reason why 2.23 is a good way to represent the strength of the phase transition is that by using equation 2.18 and the fact that the B+L violating sphaleron processes are exponentially suppressed by a Boltzmann factor inside of the phases with broken symmetry one gets for the rate of these sphalerons at the critical temperature

$$\Gamma_{\text{sphaleron}} \propto e^{-E_{\text{sph}}(T_c)/T_c} \propto e^{-v_{T_c}/T_c} \quad (2.24)$$

So equation 2.24 really shows that the sphaleron rates inside the bubbles with a Higgs VEV greater than zero are suppressed exactly by the quantity given 2.23. So in order for these processes to be suppressed adequately has to be at least 1, which results in a suppression factor of roughly 0.36, for the phase transition to be strong enough to cause baryogenesis.

There are various methods to use the condition in 2.24 in order to calculate the Higgs mass and what the biggest mass is the Higgs particle can have in order for a first order phase transition to be possible which results in about $m_H < 70$ GeV [4, pp. 3f.].

This theoretical result together with the experimental discovery that the Higgs mass is greater than 114 GeV [6, pp. 100ff.] clearly shows that the electroweak phase transition and therefore the SM as a whole isn't able to explain how the observed baryonic asymmetry arose during the early times of the universe.

A solution for this problem is expanding the SM in such a way that the new elements are able to explain problems the SM couldn't. One of these expansions results in leptogenesis, what will be the topic of the following sections.

3. Outline of leptogenesis

3.1. Expandig the SM

4. Non-relativistic leptogenesis

5. Summary

A. Appendix

References

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