



---

**ECE 251 : Signals and Systems Fundamentals****Course Project Description****Fall 2024**

---

**1 Objectives:**

- Become familiar with Matlab / GNU-Octave.
- Use Matlab / GNU-Octave to deal with signals in time and frequency domain.
- Use Matlab / GNU-Octave to design Butterworth band-pass filters.

**2 Steps:**

1. (4%) Generate the signal  $x(t)$  defined as follows:

$$x(t) = \cos(2\pi f_1 t) + \cos(2\pi f_2 t) + \cos(2\pi f_3 t) + \cos(2\pi f_4 t)$$

where  $f_1 = 500$  Hz,  $f_2 = 1000$  Hz,  $f_3 = 1500$  Hz, and  $f_4 = 2000$  Hz.

2. (4%) Store the generated signal  $x(t)$  as an audio file with extension (\*.wav)
3. (4%) Plot the signal  $x(t)$  versus time  $t$ .
4. (4%) Compute the energy of the signal  $x(t)$ .
5. (4%) Compute the frequency spectrum  $X(f)$  of this signal.
6. (4%) Plot the magnitude of  $X(f)$  in the frequency range  $-f_s/2 \leq f \leq f_s/2$ , where  $f_s$  is the sampling frequency.
7. (4%) Compute the Energy of the signal  $x(t)$  from its frequency spectrum  $X(f)$ , and hence you can verify Parseval's theorem.
8. (4%) Design a Butterworth low-pass filter with filter order 20 and cut-off frequency of 1.25 kHz.
9. (4%) Plot the magnitude and phase response of the Butterworth LPF you've designed.
10. (4%) Apply the signal  $x(t)$  to this Butterworth LPF and let's denote the output signal as  $y_1(t)$ .
11. (4%) Store the generated signal  $y_1(t)$  as an audio file with extension (\*.wav)
12. (4%) Plot the signal  $y_1(t)$  versus time  $t$ .
13. (4%) Compute the energy of the signal  $y_1(t)$ .
14. (4%) Compute the frequency spectrum  $Y_1(f)$  of this signal.
15. (4%) Plot the magnitude of  $Y_1(f)$  in the frequency range  $-f_s/2 \leq f \leq f_s/2$ .

**ECE 251 : Signals and Systems Fundamentals**  
**Course Project Description**  
**Fall 2024**

---

16. (4%) Compute the Energy of the signal  $y_1(t)$  from its frequency spectrum  $Y_1(f)$ , and hence you can verify Parseval's theorem.
17. (4%) Design a Butterworth high-pass filter with filter order 20 and cut-off frequency of 1.25 kHz.
18. (4%) Plot the magnitude and phase response of the Butterworth HPF you've designed.
19. (4%) Apply the signal  $x(t)$  to this Butterworth HPF and let's denote the output signal as  $y_2(t)$ .
20. (4%) Store the generated signal  $y_2(t)$  as an audio file with extension (\*.wav)
21. (4%) Plot the signal  $y_2(t)$  versus time  $t$ .
22. (4%) Compute the energy of the signal  $y_2(t)$ .
23. (4%) Compute the frequency spectrum  $Y_2(f)$  of this signal.
24. (4%) Plot the magnitude of  $Y_2(f)$  in the frequency range  $-f_s/2 \leq f \leq f_s/2$ .
25. (4%) Compute the Energy of the signal  $y_2(t)$  from its frequency spectrum  $Y_2(f)$ , and hence you can verify Parseval's theorem.

### 3 Useful Matlab / GNU-Octave Commands:

1. buttord, butter
2. zp2sos, sosfilt
3. freqz
4. fft, fftshift
5. audioread, audiowrite

1. Each **group of 4/5 students** should work together and submit one report.
2. Please prepare one compressed file that includes the following items:
  - (a) Your Matlab / GNU-Octave codes (\*.m files).
  - (b) A report (pdf files Only) that includes your output waveform, the energy values to be computed, plots of the filtered signal, etc.
  - (c) In your report make sure to clearly indicate the contribution of each member of the group.
  - (d) The audio files generated by your code.
3. Project will be submitted via the course page on LMS on before 11 : 59 PM on December 27<sup>th</sup> 2024.