Copyright Notice

These slides are distributed under the Creative Commons License.

<u>DeepLearning.Al</u> makes these slides available for educational purposes. You may not use or distribute these slides for commercial purposes. You may make copies of these slides and use or distribute them for educational purposes as long as you cite <u>DeepLearning.Al</u> as the source of the slides.

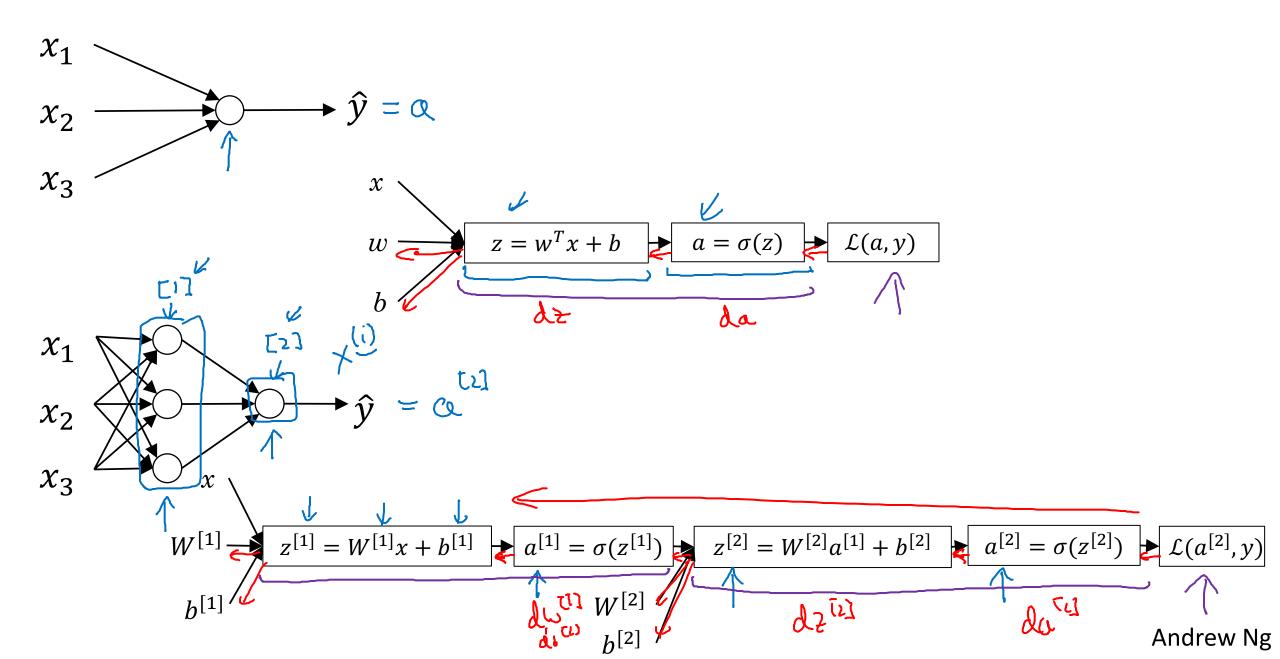
For the rest of the details of the license, see https://creativecommons.org/licenses/by-sa/2.0/legalcode



One hidden layer Neural Network

Neural Networks Overview

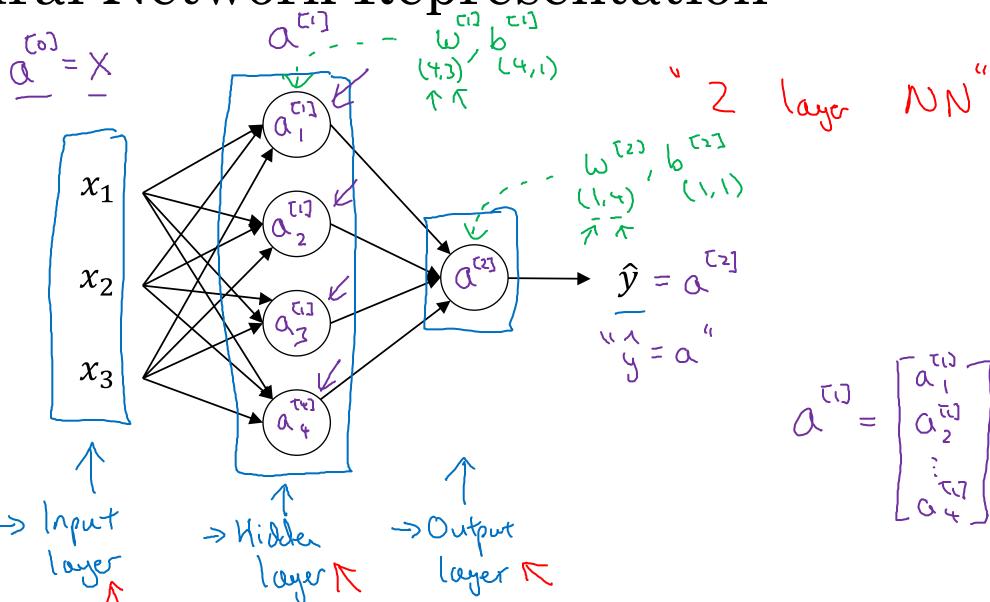
What is a Neural Network?





One hidden layer Neural Network

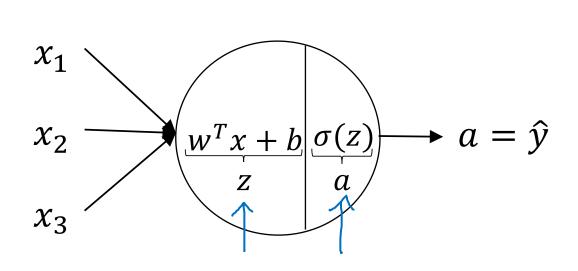
Neural Network Representation



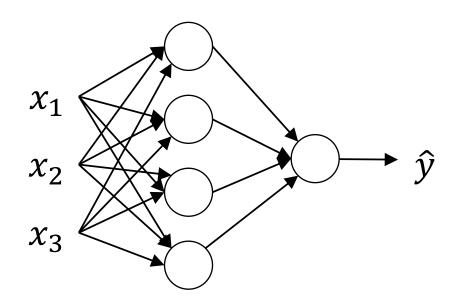


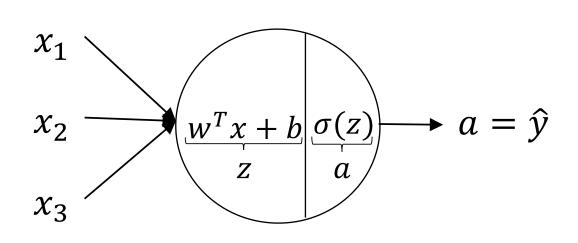
One hidden layer Neural Network

Computing a Neural Network's Output

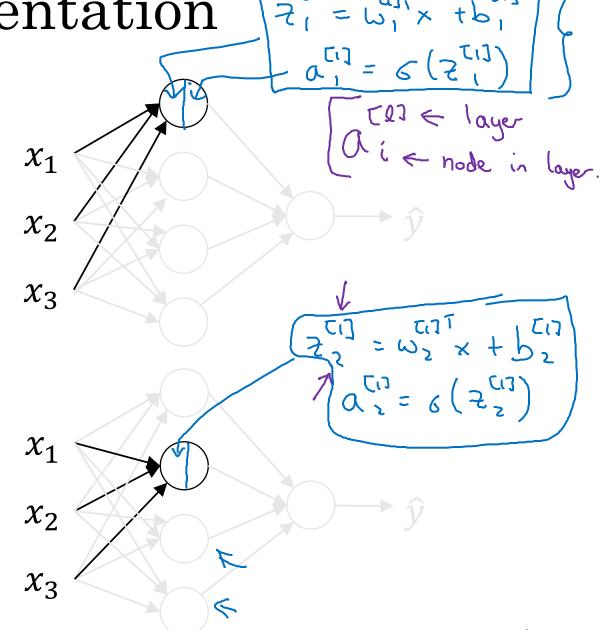


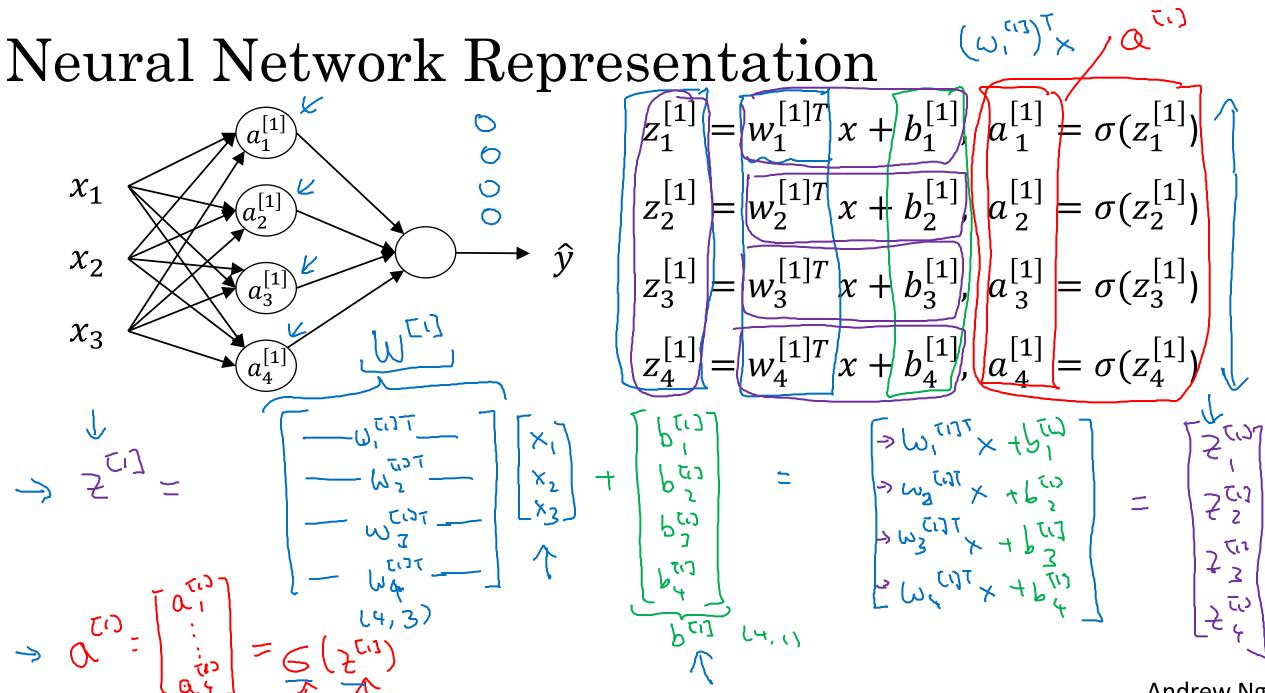
$$z = w^T x + b$$
$$a = \sigma(z)$$





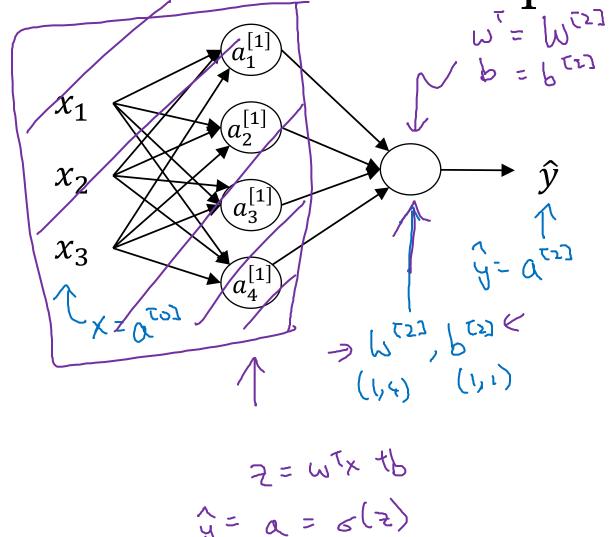
$$z = w^T x + b$$
$$a = \sigma(z)$$





Andrew Ng

Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$(4,1) = \sigma(z^{[1]})$$

$$(4,1) = (4,1)$$

$$z^{[2]} = W^{[2]} a^{[1]} + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

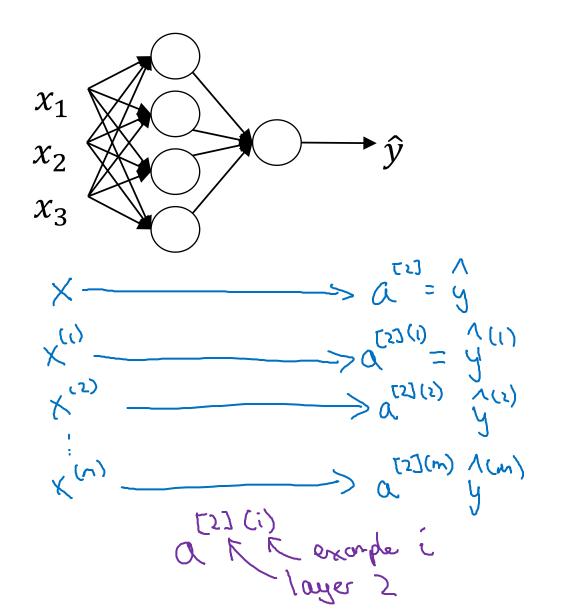
$$(1,1) = (1,1) + b^{[2]}$$

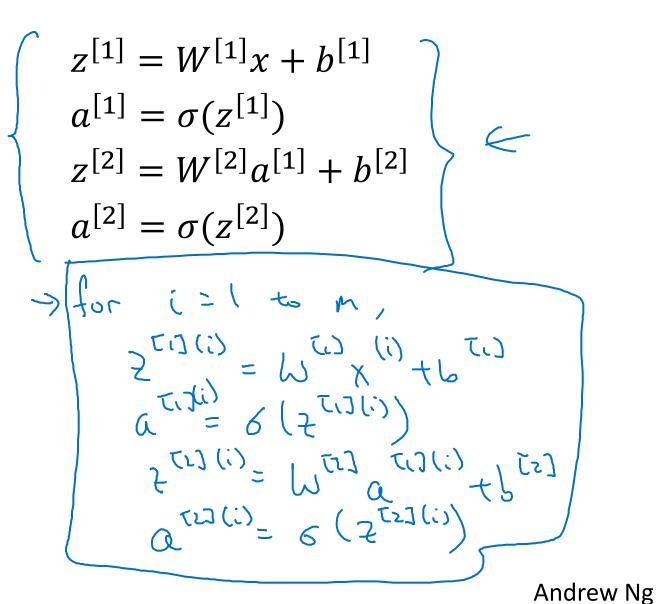


One hidden layer Neural Network

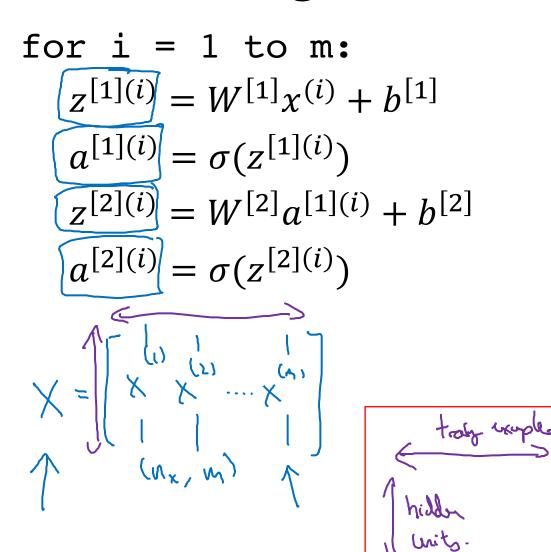
Vectorizing across multiple examples

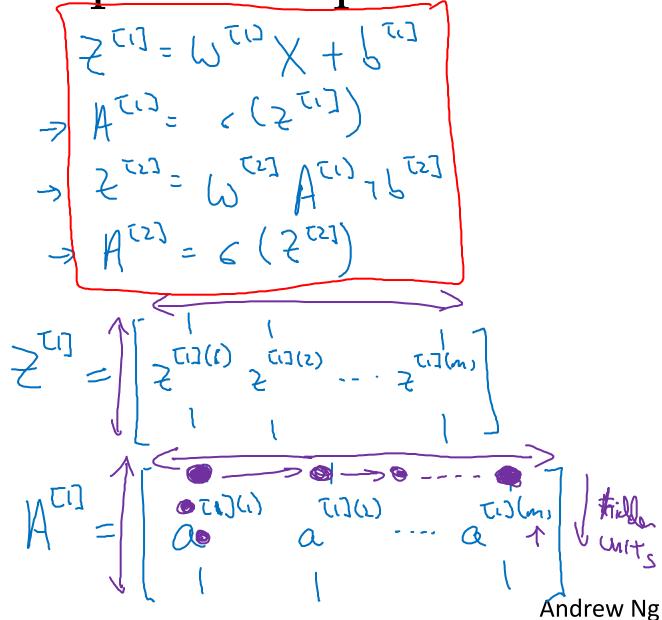
Vectorizing across multiple examples





Vectorizing across multiple examples



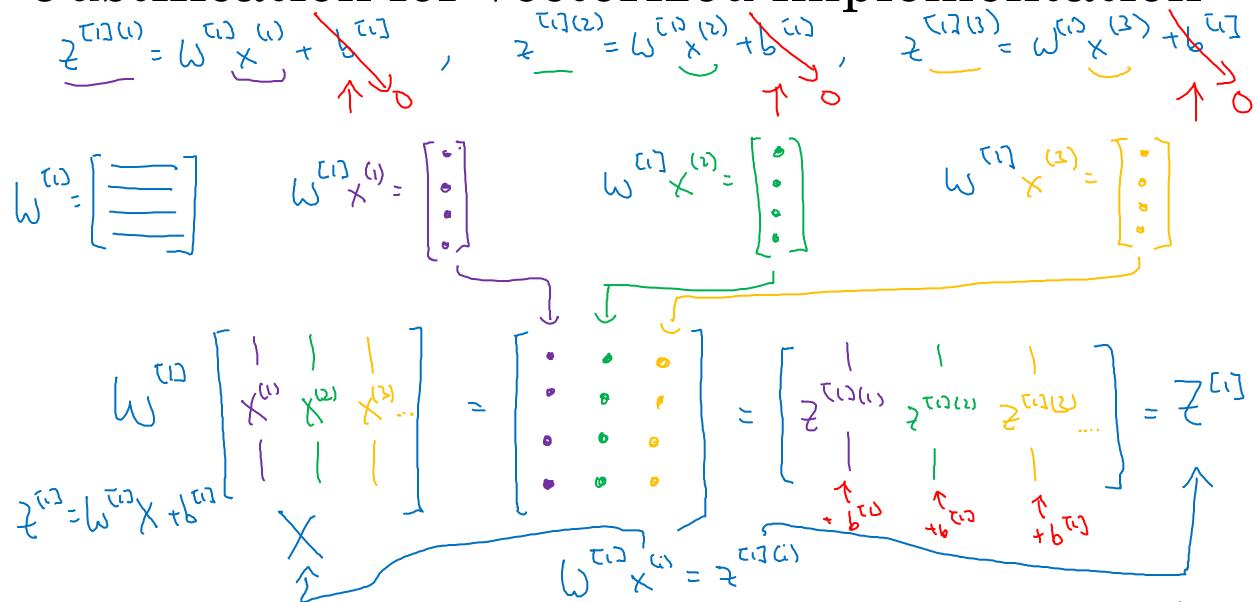




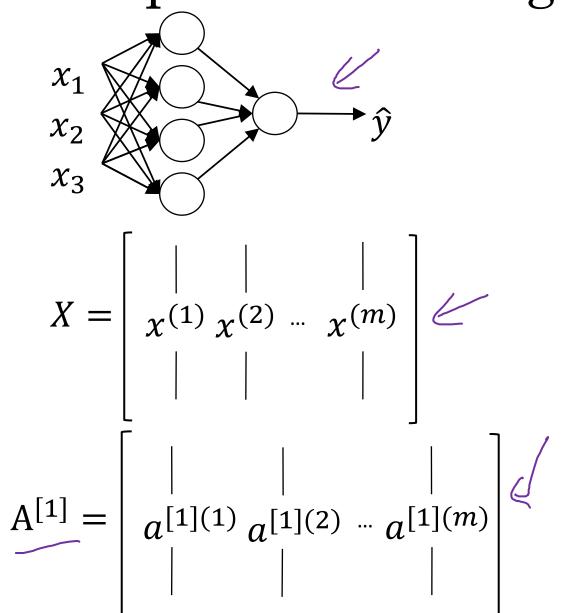
One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



Recap of vectorizing across multiple examples



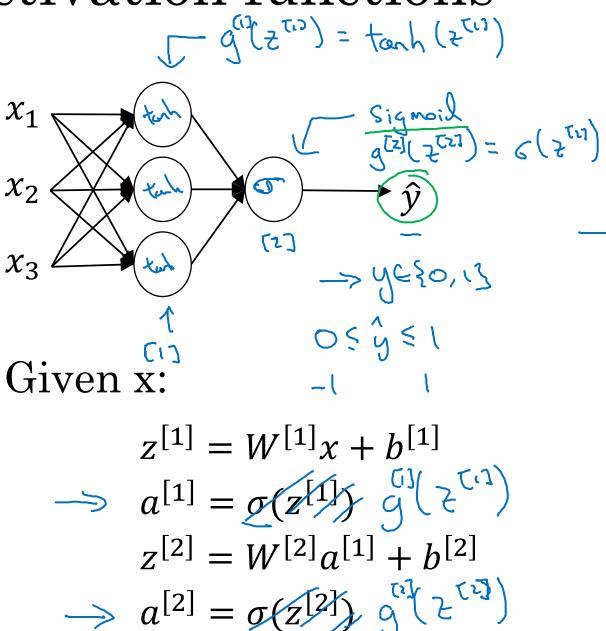
```
for i = 1 to m
                                     + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
                                    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
                                  \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
                            \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                                                                                                                                                                                                                      \chi = \alpha^{(0)} \quad \chi = \alpha^{(0)} \quad \chi^{(0)} = \alpha^{(0)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
         A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
     A^{[2]} = \sigma(Z^{[2]})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Andrew Ng
```

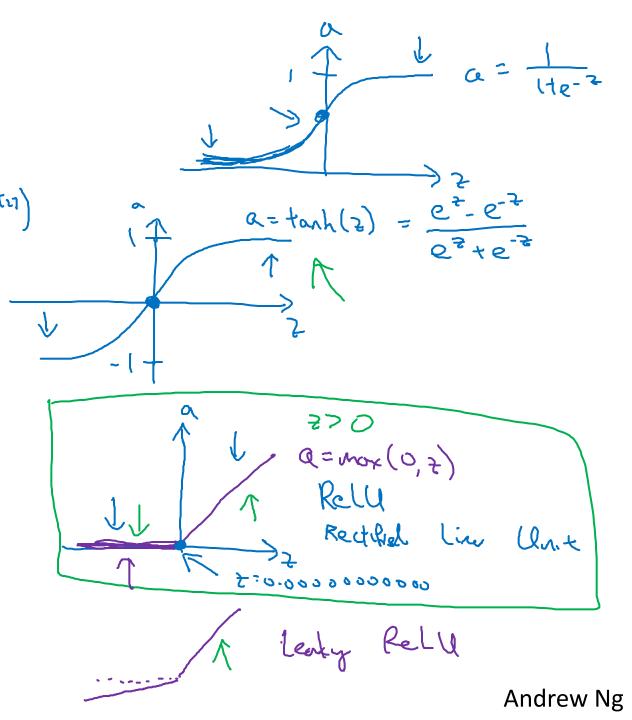


One hidden layer Neural Network

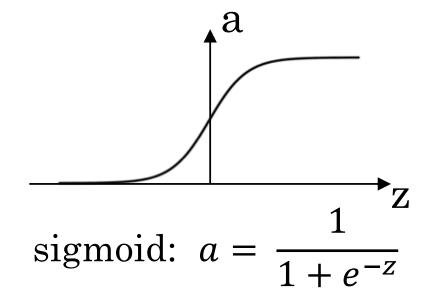
Activation functions

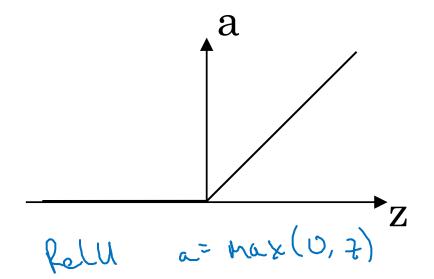
Activation functions

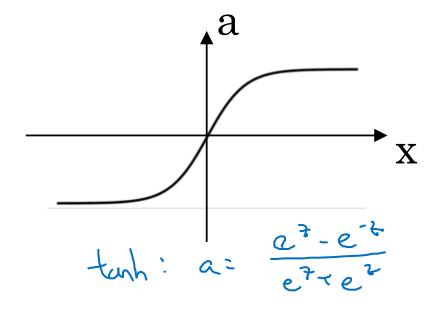


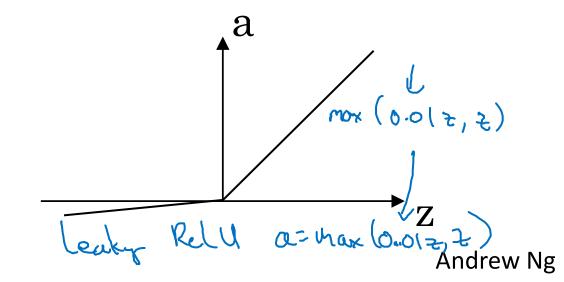


Pros and cons of activation functions







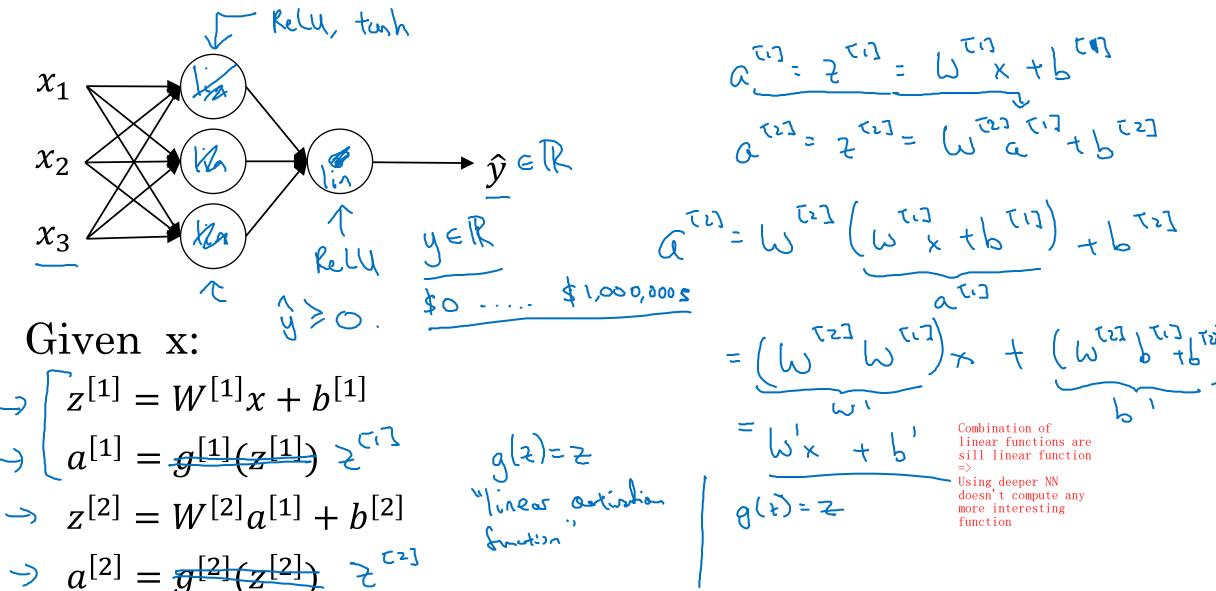




One hidden layer Neural Network

Why do you need non-linear activation functions?

Activation function





One hidden layer Neural Network

Derivatives of activation functions

Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

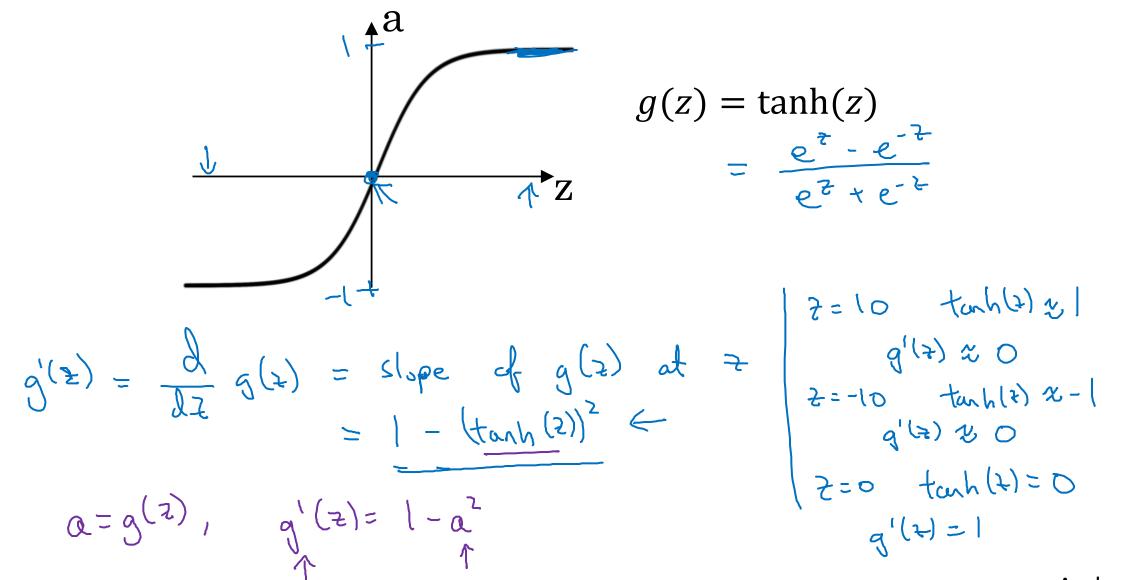
$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

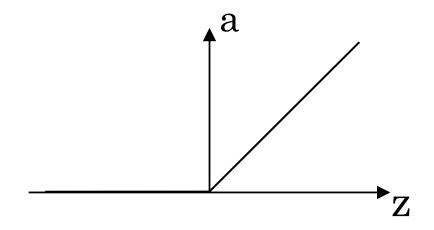
$$\frac{1}{1 + e^{-z}}$$

$$\frac$$

Tanh activation function



ReLU and Leaky ReLU

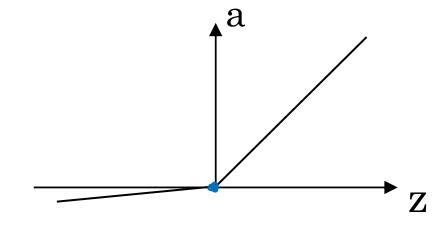


ReLU

$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } 2 < 0 \\ 1 & \text{if } t > 0 \end{cases}$$

$$\Rightarrow \frac{1}{2} = 0.0000...00$$



Leaky ReLU

$$g(z) = \max(0.01z, z)$$
 $g'(z) = \{0.01 \text{ if } z > 0\}$



One hidden layer Neural Network

Gradient descent for neural networks

Gradient descent for neural networks

Porometers:
$$(D_1)$$
 (D_2) (D_3) (D_4) (D_4)

Formulas for computing derivatives

Formal propagation!

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}Y + U_{(2)}Y + U_{($$

Back propagation:

$$Az^{[i]} = A^{[i]} = Y$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} A^{[i]} T$$

$$Ab^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = U^{[i]} Az^{[i]} + g^{[i]} (Z^{[i]}) (n^{[i]}, m)$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} \times T$$

$$Az^{[i]} \times T$$

$$Ab^{[i]} = \frac{1}{m} np. sum (Az^{[i]}, ani = 1, keepdins = True)$$

$$Andrew Andrew Andrew$$

Andrew Ng



One hidden layer Neural Network

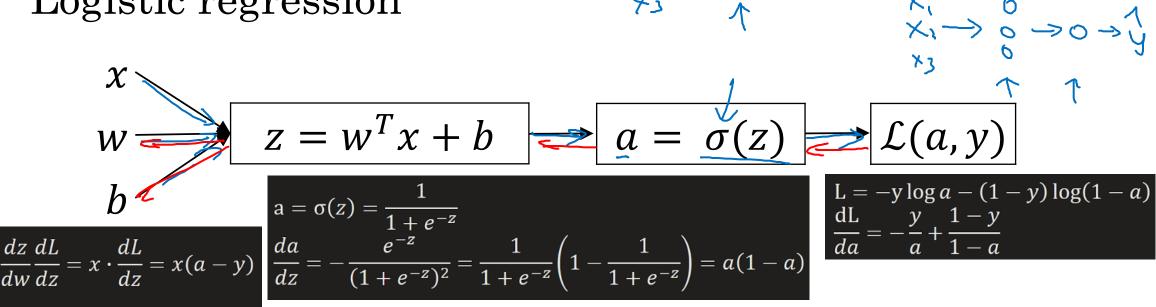
Backpropagation intuition (Optional)

Computing gradients

Logistic regression

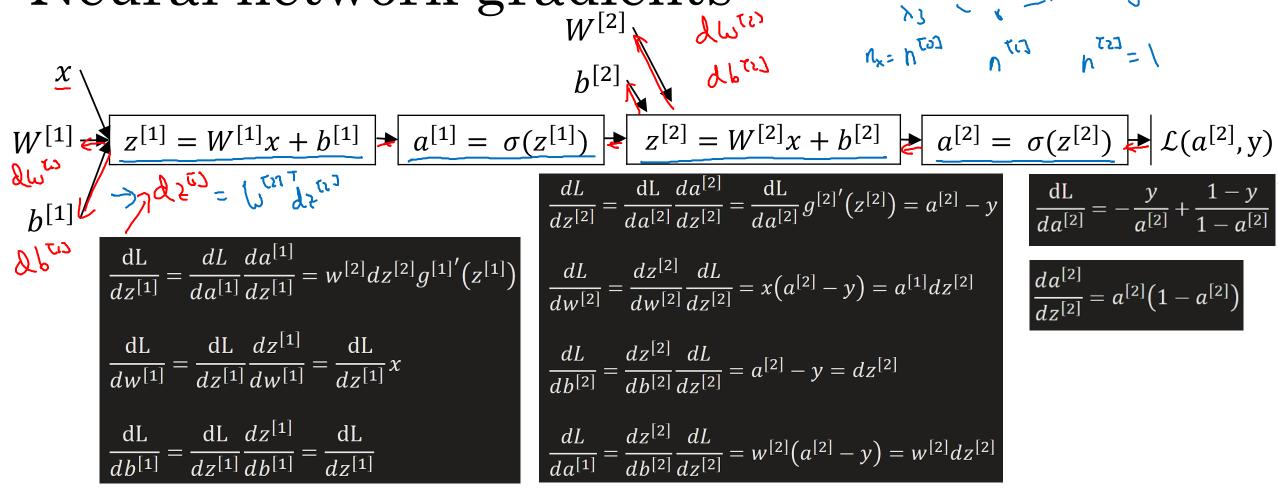
dw dz

 $\overline{db} \, \overline{dz}$



 $\frac{dL}{dz} = \frac{dL}{da}\frac{da}{dz} = \frac{dL}{da}g'(z) = (a-1)y + a(1-y) = a-y$

Neural network gradients



$$\sigma(z^{[2]}) = \mathcal{L}(a^{[2]}, y)$$

$$\frac{dL}{da^{[2]}} = -\frac{y}{a^{[2]}} + \frac{1-y}{1-a^{[2]}}$$

$$\frac{da^{[2]}}{dz^{[2]}} = a^{[2]}(1-a^{[2]})$$

Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$
 $db^{[2]} = dz^{[2]}$
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$
 $dW^{[1]} = dz^{[1]}x^T$
 $db^{[1]} = dz^{[1]}$

Vectorized Implementation:

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[2]} = \frac{1}{m}dz^{[2]}A^{[1]^T}$$

$$dz^{[2]} = \frac{1}{m}np. sum(dz^{[2]}, axis = 1, keepdims = True)$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

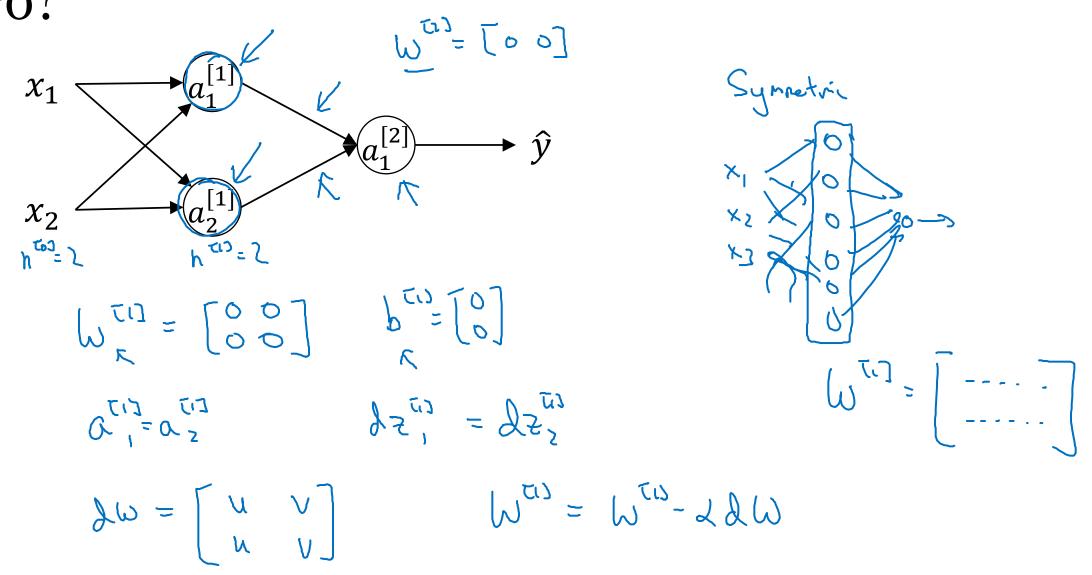
$$dy^{[1]} = \frac{1}{m}np. sum(dz^{[1]}, axis = 1, keepdims = True)$$



One hidden layer Neural Network

Random Initialization

What happens if you initialize weights to zero?



Random initialization

