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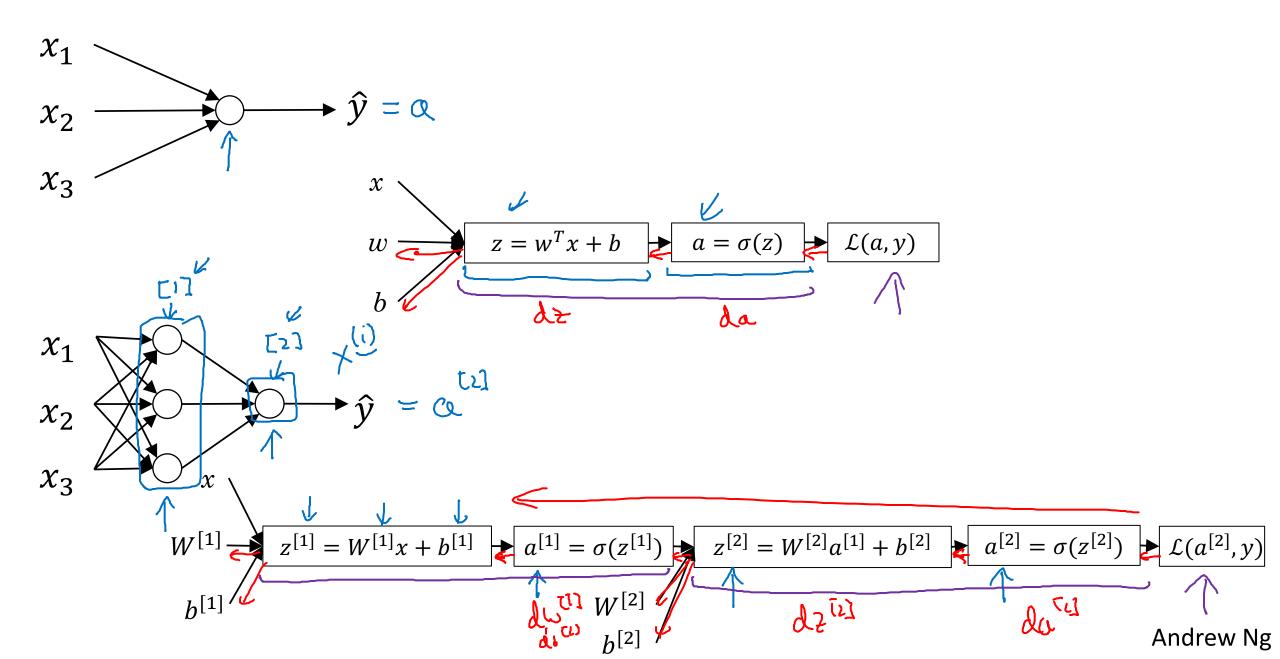
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## One hidden layer Neural Network

# Neural Networks Overview

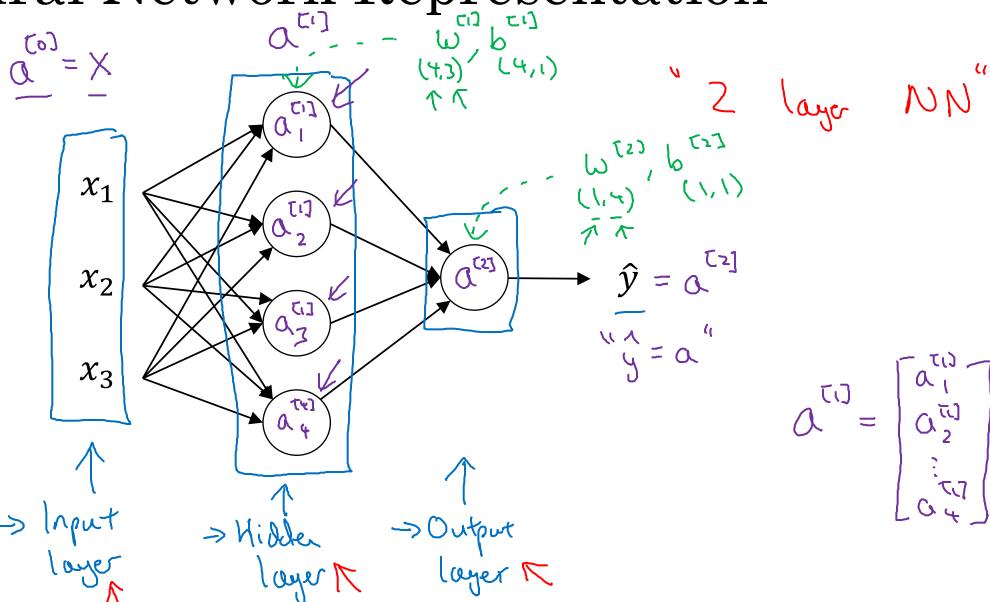
#### What is a Neural Network?





## One hidden layer Neural Network

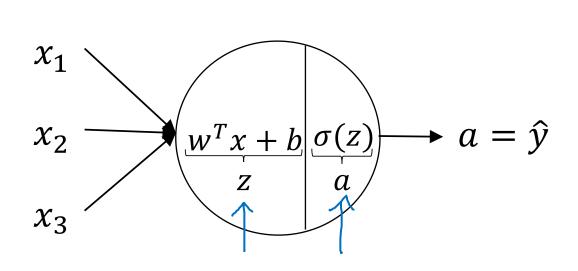
Neural Network Representation



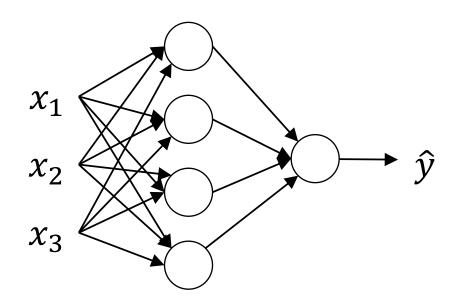


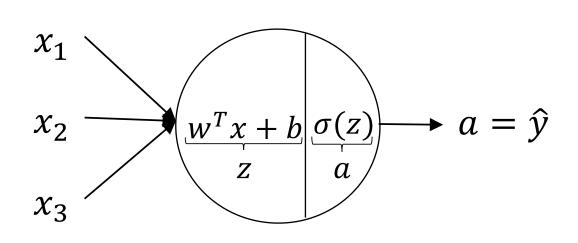
## One hidden layer Neural Network

Computing a Neural Network's Output

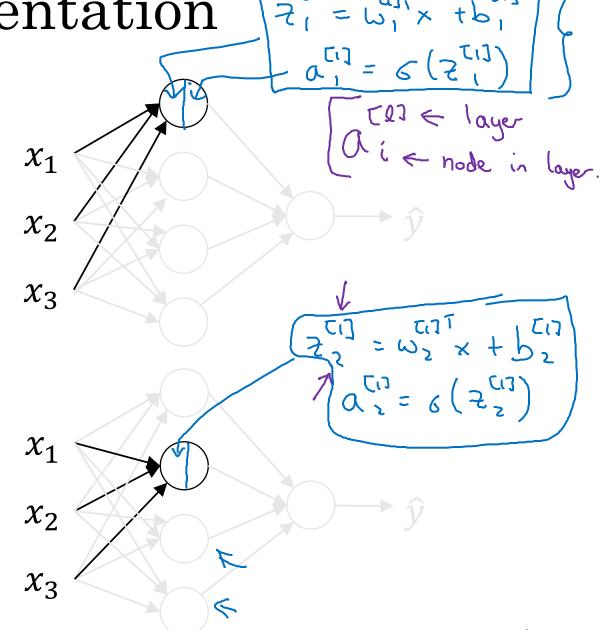


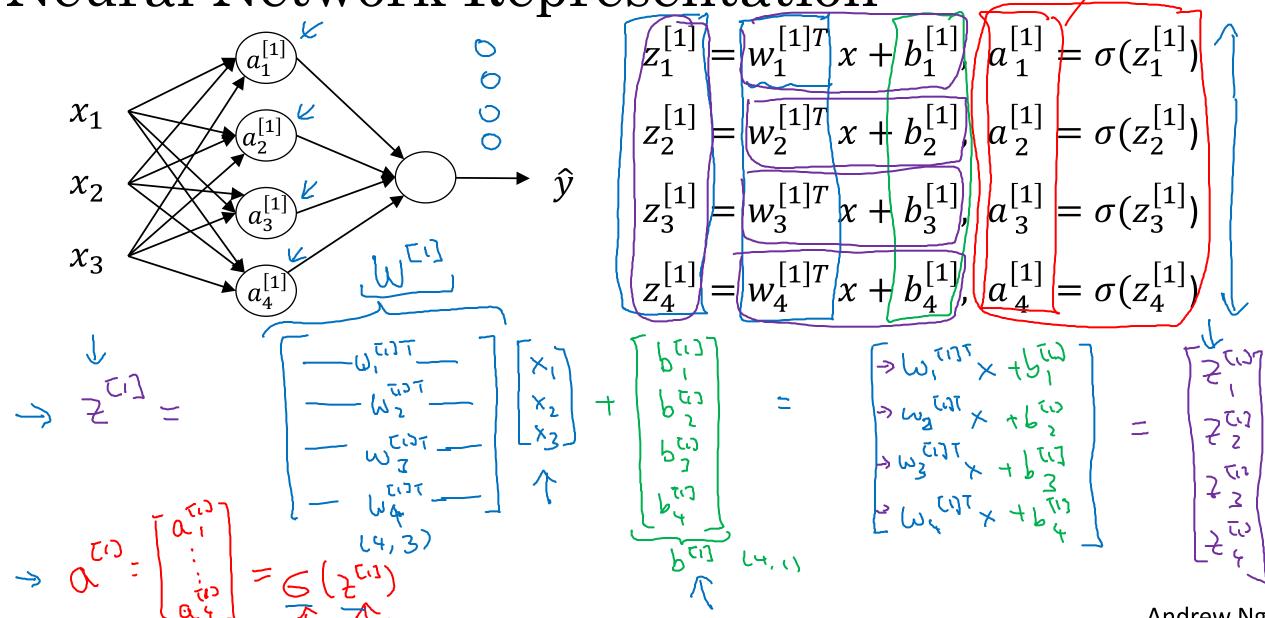
$$z = w^T x + b$$
$$a = \sigma(z)$$





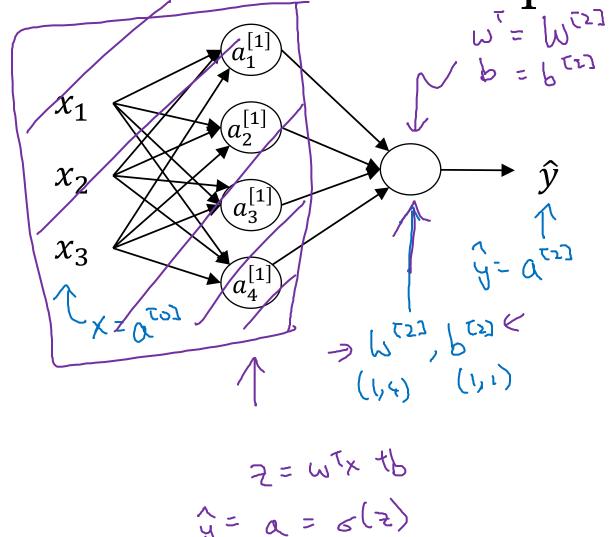
$$z = w^T x + b$$
$$a = \sigma(z)$$





 $(\omega_{i}^{(i)})^{T} \times 10^{T(i)}$ 

Neural Network Representation learning



Given input x:

$$z^{[1]} = W^{[1]} + b^{[1]}$$

$$(4,1) = \sigma(z^{[1]})$$

$$(4,1) = (4,1)$$

$$z^{[2]} = W^{[2]} a^{[1]} + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

$$(1,1) = (1,4) + b^{[2]}$$

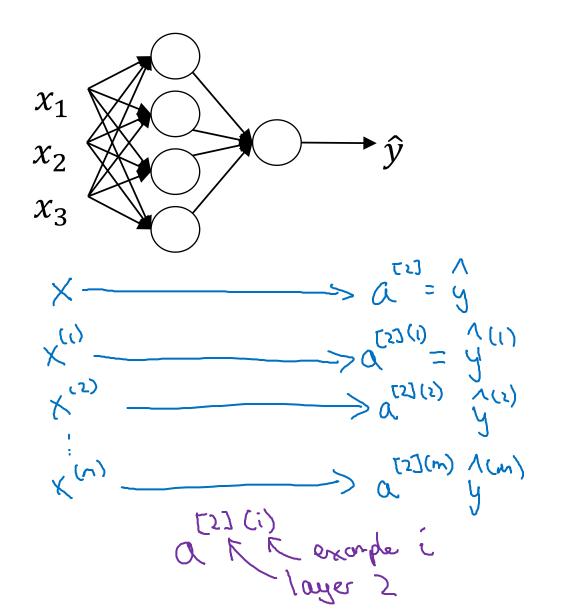
$$(1,1) = (1,1) + b^{[2]}$$

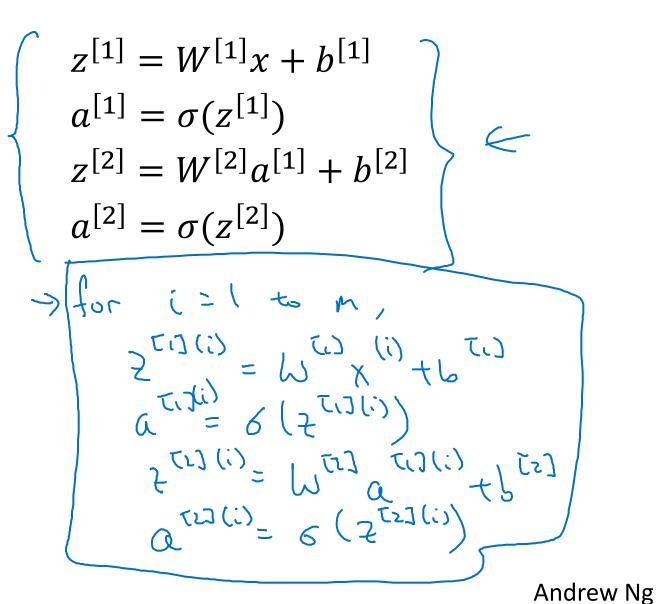


## One hidden layer Neural Network

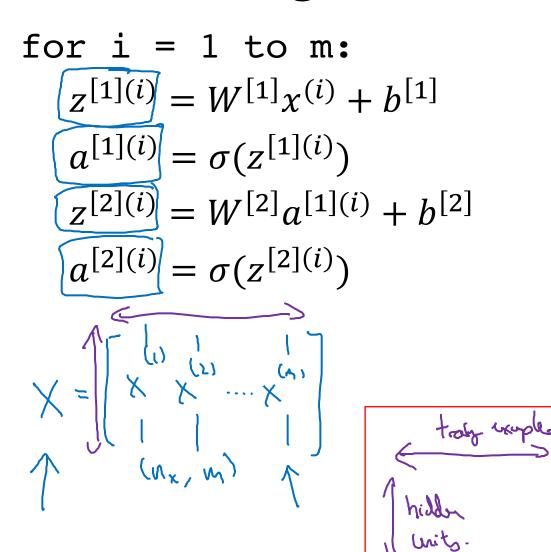
Vectorizing across multiple examples

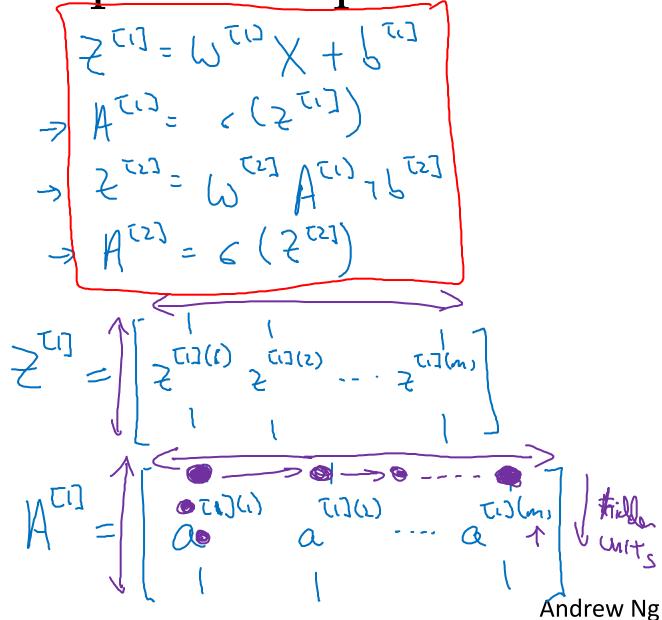
#### Vectorizing across multiple examples





Vectorizing across multiple examples



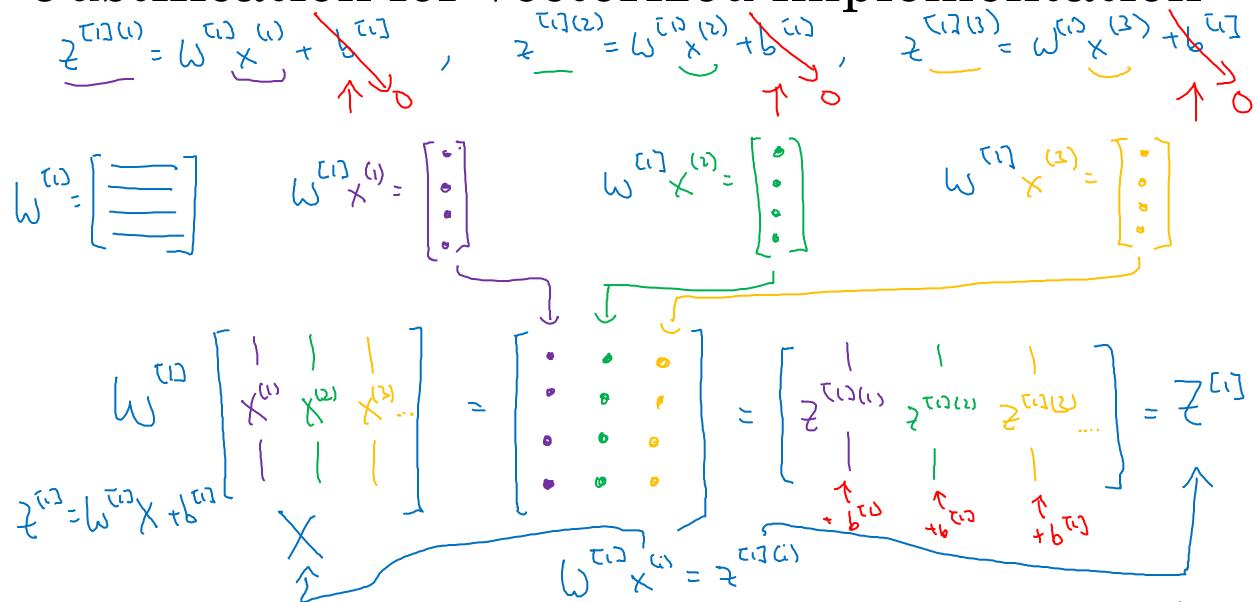




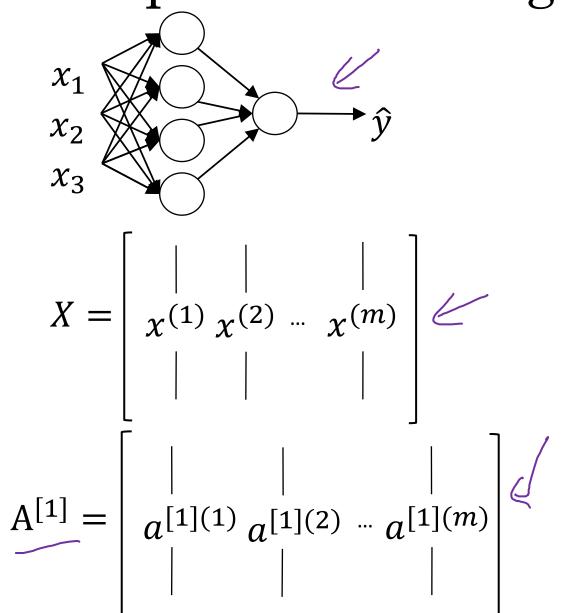
## One hidden layer Neural Network

Explanation for vectorized implementation

Justification for vectorized implementation



#### Recap of vectorizing across multiple examples



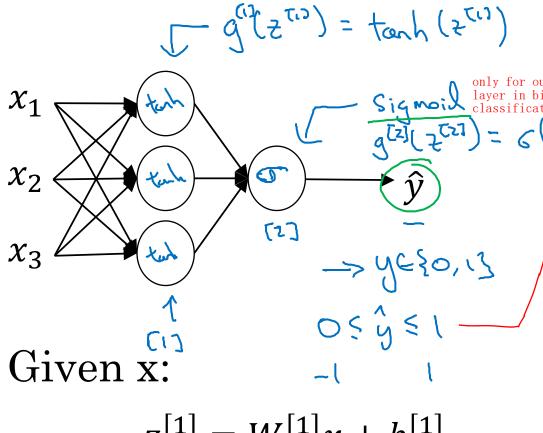
```
for i = 1 to m
                                     + z^{[1](i)} = W^{[1]}x^{(i)} + b^{[1]}
                                    \Rightarrow a^{[1](i)} = \sigma(z^{[1](i)})
                                  \Rightarrow z^{[2](i)} = W^{[2]}a^{[1](i)} + b^{[2]}
                            \Rightarrow a^{[2](i)} = \sigma(z^{[2](i)})
                                                                                                                                                                                                                      \chi = \alpha^{(0)} \quad \chi = \alpha^{(0)} \quad \chi^{(0)} = \alpha^{(0)
 Z^{[1]} = W^{[1]}X + b^{[1]} \leftarrow W^{[1]}X^{(0)} + b^{[1]}
         A^{[1]} = \sigma(Z^{[1]})
Z^{[2]} = W^{[2]}A^{[1]} + b^{[2]}
     A^{[2]} = \sigma(Z^{[2]})
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               Andrew Ng
```



## One hidden layer Neural Network

#### Activation functions

#### Activation functions

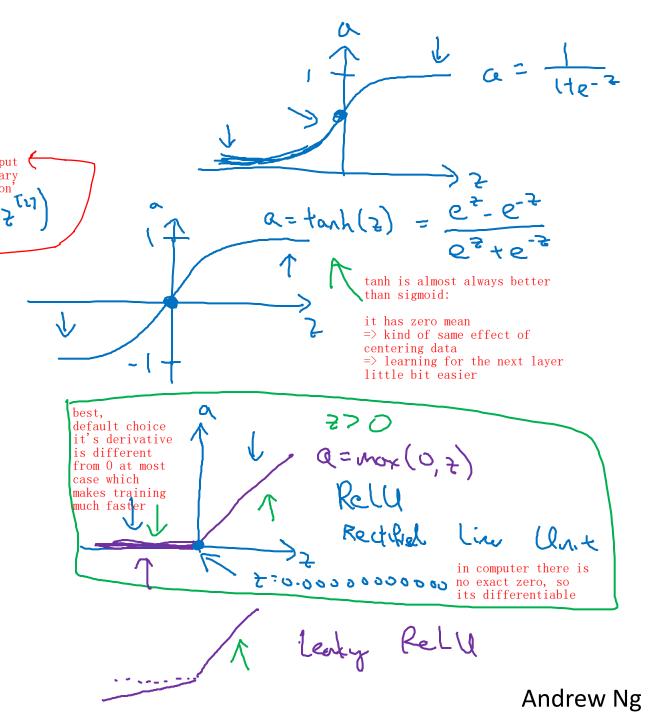


$$z^{[1]} = W^{[1]}x + b^{[1]}$$

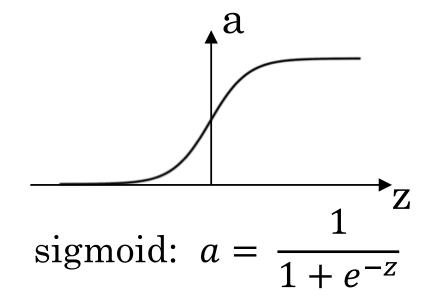
$$a^{[1]} = \sigma(z^{[1]}) \quad g^{(2]}(z^{(1)})$$

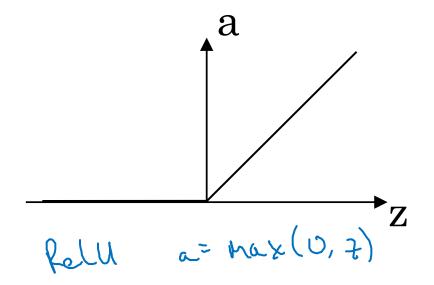
$$z^{[2]} = W^{[2]}a^{[1]} + b^{[2]}$$

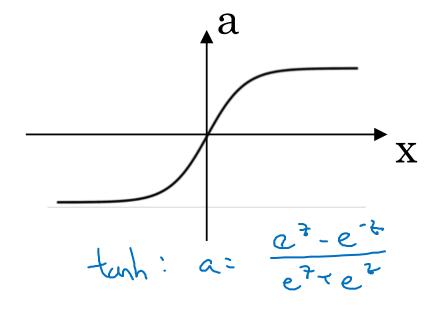
$$a^{[2]} = \sigma(z^{[2]}) \quad g^{(2)}(z^{(2)})$$

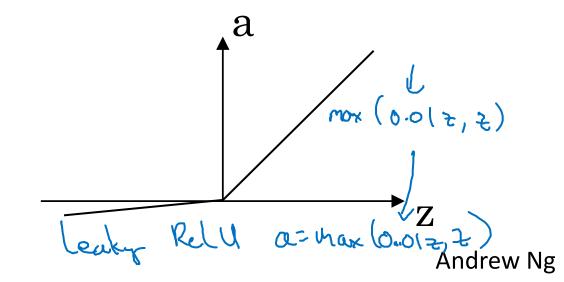


#### Pros and cons of activation functions







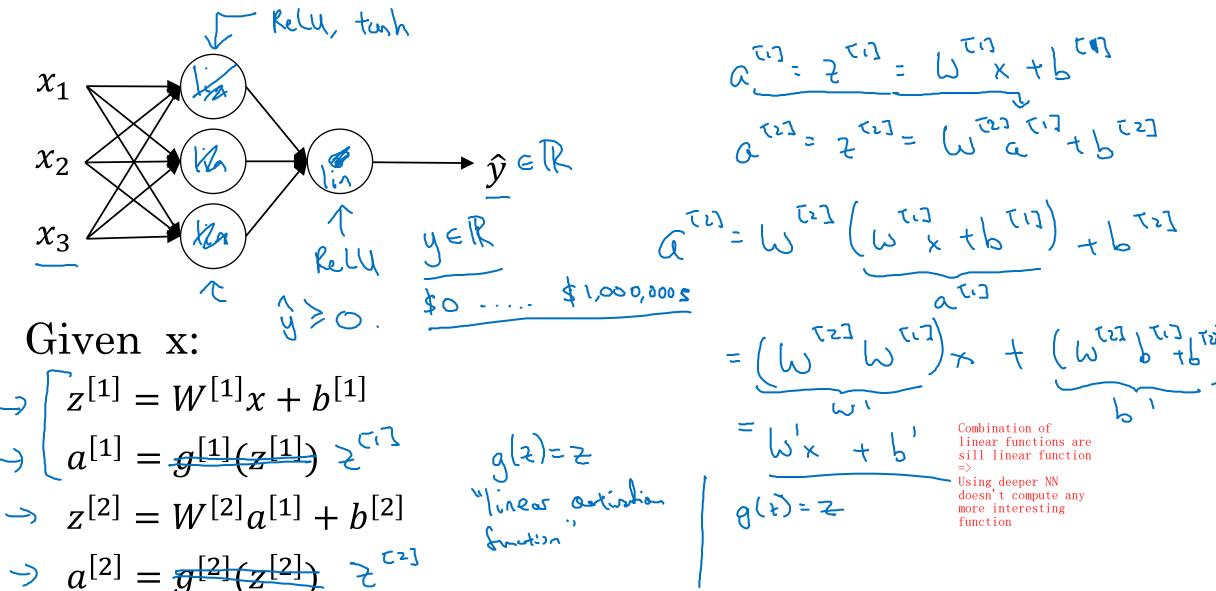




## One hidden layer Neural Network

Why do you need non-linear activation functions?

#### Activation function





## One hidden layer Neural Network

## Derivatives of activation functions

#### Sigmoid activation function

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$g(z) = \frac{1}{1 + e^{-z}}$$

$$a = g(z) = \frac{1}{1 + e^{-z}}$$

$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

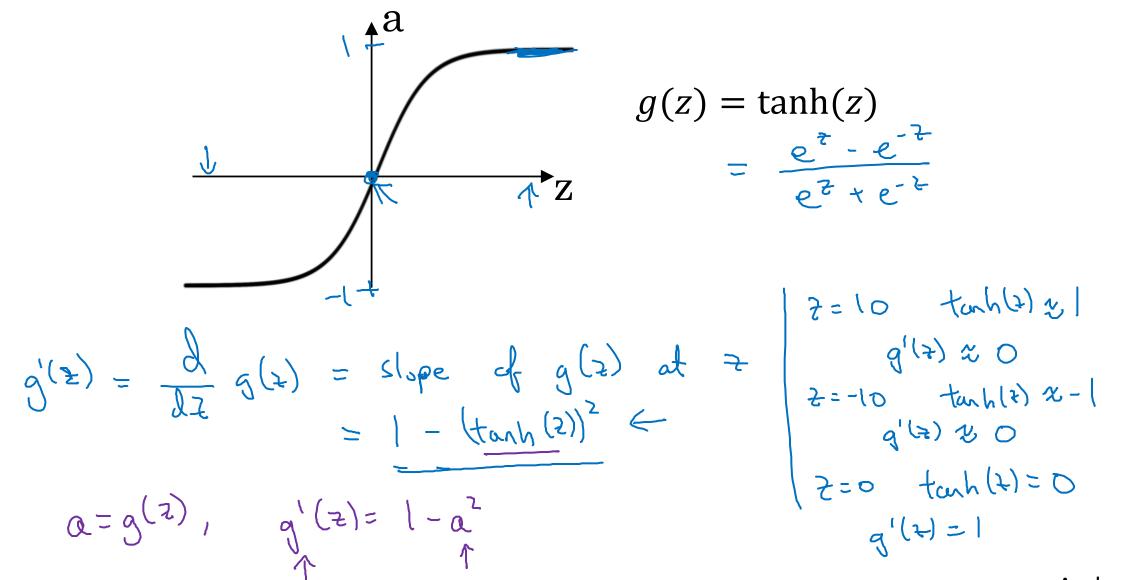
$$\frac{1}{1 + e^{-z}}$$

$$= \frac{1}{1 + e^{-z}}$$

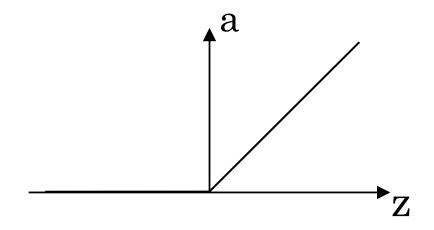
$$\frac{1}{1 + e^{-z}}$$

$$\frac$$

#### Tanh activation function



#### ReLU and Leaky ReLU

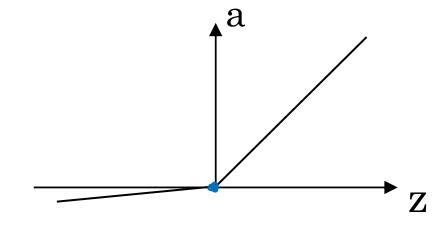


#### ReLU

$$g(t) = mox(0, 2)$$

$$\Rightarrow g'(t) = \begin{cases} 0 & \text{if } 2 < 0 \\ 1 & \text{if } t > 0 \end{cases}$$

$$\Rightarrow \frac{1}{2} = 0.0000...00$$



#### Leaky ReLU

$$g(z) = \max(0.01z, z)$$
 $g'(z) = \{0.01 \text{ if } z > 0\}$ 



## One hidden layer Neural Network

# Gradient descent for neural networks

#### Gradient descent for neural networks

Porometers: 
$$(D_1)$$
  $(D_2)$   $(D_3)$   $(D_4)$   $(D_4)$ 

#### Formulas for computing derivatives

Formal propagation!

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(1)} = U_{(1)}X + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}$$

$$Z^{(2)} = U_{(2)}Y + U_{(1)}Y + U_{(2)}Y + U_{($$

Back propagation:

$$Az^{[i]} = A^{[i]} = Y$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} A^{[i]} T$$

$$Ab^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = \frac{1}{m} np. Sum (Az^{[i]}, anais = 1, keepdans = 1 ne)$$

$$Az^{[i]} = U^{[i]} Az^{[i]} + g^{[i]} (Z^{[i]}) (n^{[i]}, m)$$

$$Az^{[i]} = \frac{1}{m} Az^{[i]} \times T$$

$$Az^{[i]} \times T$$

$$Ab^{[i]} = \frac{1}{m} np. sum (Az^{[i]}, ani = 1, keepdins = True)$$

$$Andrew Andrew Andrew$$

Andrew Ng



## One hidden layer Neural Network

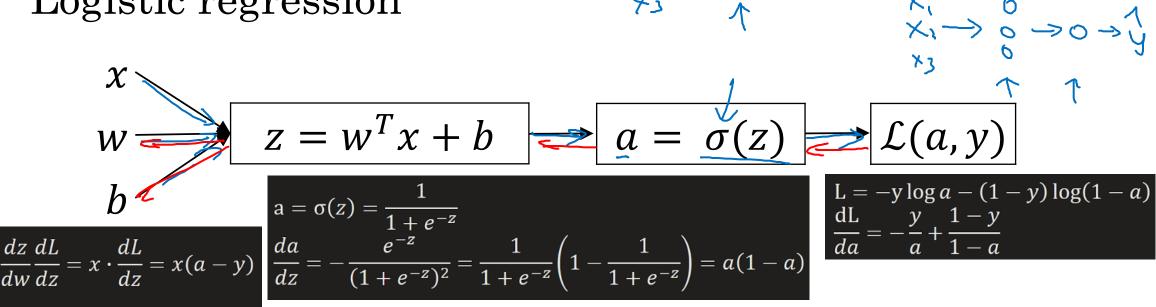
Backpropagation intuition (Optional)

#### Computing gradients

Logistic regression

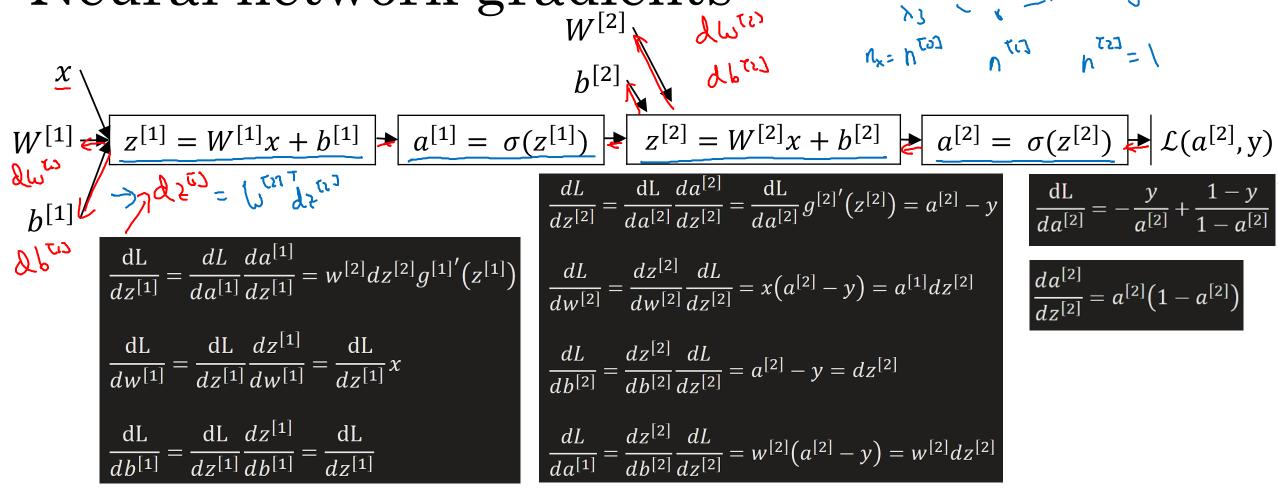
dw dz

 $\overline{db} \, \overline{dz}$ 



 $\frac{dL}{dz} = \frac{dL}{da}\frac{da}{dz} = \frac{dL}{da}g'(z) = (a-1)y + a(1-y) = a-y$ 

Neural network gradients



$$\sigma(z^{[2]}) = \mathcal{L}(a^{[2]}, y)$$

$$\frac{dL}{da^{[2]}} = -\frac{y}{a^{[2]}} + \frac{1-y}{1-a^{[2]}}$$

$$\frac{da^{[2]}}{dz^{[2]}} = a^{[2]}(1-a^{[2]})$$

#### Summary of gradient descent

$$dz^{[2]} = a^{[2]} - y$$
 $dW^{[2]} = dz^{[2]}a^{[1]^T}$ 
 $db^{[2]} = dz^{[2]}$ 
 $dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$ 
 $dW^{[1]} = dz^{[1]}x^T$ 
 $db^{[1]} = dz^{[1]}$ 

Vectorized Implementation:

$$z^{(1)} = \omega^{(1)} \times + b^{(1)}$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

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$$z^{(1)} = \left[z^{(1)}(z^{(1)})\right]$$

$$z^{(1)} = g^{(1)}(z^{(1)})$$

#### Summary of gradient descent

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$$dW^{[1]} = dz^{[1]}x^T$$

$$db^{[1]} = dz^{[1]}$$

$$dz^{[2]} = a^{[2]} - y$$

$$dW^{[2]} = dz^{[2]}a^{[1]^T}$$

$$db^{[2]} = dz^{[2]}$$

$$dz^{[2]} = \frac{1}{m}dz^{[2]}A^{[1]^T}$$

$$dz^{[2]} = \frac{1}{m}np. sum(dz^{[2]}, axis = 1, keepdims = True)$$

$$dz^{[1]} = W^{[2]T}dz^{[2]} * g^{[1]'}(z^{[1]})$$

$$dW^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = dz^{[1]}x^T$$

$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

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$$dy^{[1]} = \frac{1}{m}dz^{[1]}x^T$$

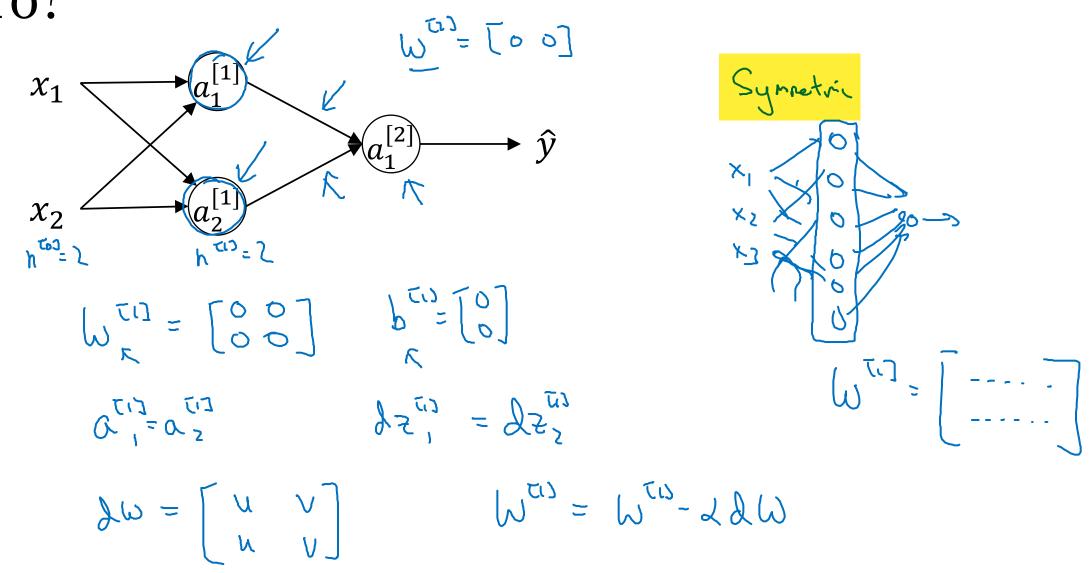
$$dy^{[1]} = \frac{1}{m}np. sum(dz^{[1]}, axis = 1, keepdims = True)$$



## One hidden layer Neural Network

#### Random Initialization

## What happens if you initialize weights to zero?



#### Random initialization

