

Machine Learning 1: Foundations

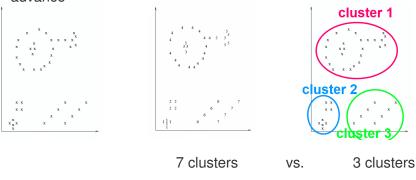
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Kaiserslautern, 16-23 June 2020

- Linear Clustering
- Non-linear Clustering
- 3 Hierarchical Clustering

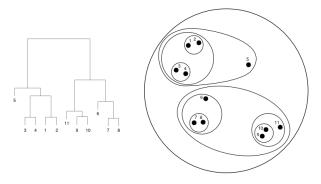
## Disadvantage

Big problem in *k*-means: do not know the number of clusters in advance



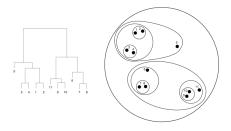
What to do?

► Generates a tree ("hierarchy") of clusters



do not need to specify number of clusters

- 1: **function** HIERARCHICALCLUSTERING(inputs  $\mathbf{x}_1, \dots, \mathbf{x}_n \in \mathbb{R}^d$ )
- 2: assign each input to a cluster
- 3: repeat
- 4: link the two clusters with minimal distance
- 5: until finished
- 6: **return** tree of cluster linkages
- 7: end function



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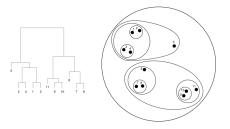
3: repeat

4: link the two clusters with minimal distance

5: until only a single root cluster left

6: **return** tree of cluster linkages

7: end function



How to measure distance between two clusters?

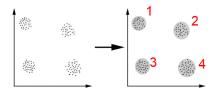
# Quiz: How to measure distance d(i,j) between two clusters i and j?

- Simple linkage Average linkage Complete linkage
- ▶ Let  $S_j \subseteq \{\mathbf{x}_1, \dots, \mathbf{x}_n\}$  be the set of inputs contained in the jth cluster
- ► Simple linkage:  $d(i,j) := \min_{\mathbf{x} \in S_i, \tilde{\mathbf{x}} \in S_j} \|\mathbf{x} \tilde{\mathbf{x}}\|$
- ► Average linkage:  $d(i,j) := \frac{\text{mean}}{\text{mean}}_{\mathbf{x} \in S_i, \tilde{\mathbf{x}} \in S_i} \|\mathbf{x} \tilde{\mathbf{x}}\|$
- ► Complete linkage:  $d(i,j) := \max_{\mathbf{x} \in S_i . \tilde{\mathbf{x}} \in S_i} \|\mathbf{x} \tilde{\mathbf{x}}\|$
- ► Note: again, all this can be kernelized...

### Conclusion

### Clustering:

Organizing data into groups



#### k-means:

- Alternatingly, assign inputs to closest cluster center and re-compute centers
- Can be kernelized
- Can be deepified using transfer learning

### Hierarchical clustering:

- Consider clusters at various scales
- ► Helpful when the number of clusters is unknown

## Refs I