Let x, y, and z be integers such that $S = x^4 + y^4 + z^4$ is divisible by 29. Show that S is divisible by 29⁴.