Does there exist a real 3×3 matrix A such that $\mathrm{tr}(A) = 0$ and $A^2 + A^t = I$?
($\mathrm{tr}(A)$ denotes the trace of A, A^t is the transpose of A, and I is the identity matrix.)