

Consider all 26^{26} words of length 26 in the Latin alphabet. Define the weight of a word as $1/(k+1)$, where k is the number of letters not used in this word. Prove that the sum of the weights of all words is 3^{75} .