

For a permutation  $\sigma = (i_1, i_2, \dots, i_n)$  of  $(1, 2, \dots, n)$  define  $D(\sigma) = \sum_{k=1}^n |i_k - k|$ . Let  $Q(n, d)$  be the number of permutations  $\sigma$  of  $(1, 2, \dots, n)$  with  $d = D(\sigma)$ . Prove that  $Q(n, d)$  is even for  $d \geq 2n$ .