

The linear operator A on the vector space V is called an involution if $A^2 = E$ where E is the identity operator on V . Let $\dim V = n < \infty$.

- (i) Prove that for every involution A on V there exists a basis of V consisting of eigenvectors of A .
- (ii) Find the maximum number of distinct pairwise commuting involutions on V .