

Find

$$\lim_{t \nearrow 1} (1-t) \sum_{n=1}^{\infty} \frac{t^n}{1+t^n},$$

where $t \nearrow 1$ means that t approaches 1 from below.