Compute

$$\lim_{A \to +\infty} \frac{1}{A} \int_1^A A^{\frac{1}{x}} \mathrm{d}x.$$