Let z be a complex number with $|z + 1| > 2$. Prove that $|z^3 + 1| > 1$.