

Let $F : (1, \infty) \rightarrow \mathbb{R}$ be the function defined by

$$F(x) := \int_x^{x^2} \frac{dt}{\ln t}.$$

Show that F is one-to-one (i.e. injective) and find the range (i.e. set of values) of F .