

Prove that if  $f : [0, 1] \rightarrow [0, 1]$  is a continuous function, then the sequence of iterates  $x_{n+1} = f(x_n)$  converges if and only if

$$\lim_{n \rightarrow \infty} (x_{n+1} - x_n) = 0.$$