

Find

$$\lim_{N \rightarrow \infty} \frac{\ln^2 N}{N} \sum_{k=2}^{N-2} \frac{1}{\ln k \cdot \ln(N-k)}.$$

Note that  $\ln$  denotes the natural logarithm.