

Let $f(x)$ be a polynomial with real coefficients of degree n . Suppose that $\frac{f(k)-f(m)}{k-m}$ is an integer for all integers $0 \leq k < m \leq n$. Prove that $a-b$ divides $f(a) - f(b)$ for all pairs of distinct integers a and b .