

Let n be a positive integer and a_1, \dots, a_n be arbitrary integers. Suppose that a function $f : \mathbb{Z} \rightarrow \mathbb{R}$ satisfies $\sum_{i=1}^n f(k + a_i l) = 0$ whenever k and l are integers and $l \neq 0$. Prove that $f = 0$.