Find all twice continuously differentiable functions
$f : \mathbb{R} \to (0, +\infty)$ satisfying

$$f''(x)f(x) \geq 2(f'(x))^2$$

for all $x \in \mathbb{R}$.