

Prove that if  $f : \mathbb{R} \rightarrow \mathbb{R}$  is three times differentiable, then there exists a real number  $\xi \in (-1, 1)$  such that

$$\frac{f'''(\xi)}{6} = \frac{f(1) - f(-1)}{2} - f'(0).$$