

Let  $p$  be a prime number. Call a positive integer  $n$  *interesting* if

$$x^n - 1 = (x^p - x + 1)f(x) + pg(x)$$

for some polynomials  $f$  and  $g$  with integer coefficients.

- a) Prove that the number  $p^p - 1$  is interesting.
- b) For which  $p$  is  $p^p - 1$  the minimal interesting number?