Let f be a rational function (i.e. the quotient of two real polynomials) and suppose that f(n) is an integer for infinitely many integers n. Prove that f is a polynomial.