

Given a group G , denote by $G(m)$ the subgroup generated by the m^{th} powers of elements of G . If $G(m)$ and $G(n)$ are commutative, prove that $G(\gcd(m, n))$ is also commutative.

($\gcd(m, n)$ denotes the greatest common divisor of m and n .)