

Let all roots of an  $n$ -th degree polynomial  $P(z)$  with complex coefficients lie on the unit circle in the complex plane. Prove that all roots of the polynomial

$$2zP'(z) - nP(z)$$

lie on the same circle.