Suppose that F is a family of finite subsets of $\mathbb N$ and for any two sets $A,B\in F$ we have $A\cap B\neq\emptyset$.

a) Is it true that there is a finite subset Y of $\mathbb N$ such that for any $A, B \in F$ we have $A \cap B \cap Y \neq \emptyset$?

b) Is the statement a) true if we suppose in addition that all of the members of F have the same size?

Justify your answers.