

Let  $S$  be an infinite set of real numbers such that  $|s_1 + s_2 + \cdots + s_k| < 1$  for every finite subset  $\{s_1, s_2, \dots, s_k\} \subset S$ . Show that  $S$  is countable.