Find all differentiable functions $f : (0, \infty) \to \mathbb{R}$ such that

$$f(b) - f(a) = (b - a)f'\left(\sqrt{ab}\right) \quad \text{for all} \quad a, b > 0.$$