

Let  $p(x) = x^5 + x$  and  $q(x) = x^5 + x^2$ .

Find all pairs  $(w, z)$  of complex numbers with  $w \neq z$  for which  $p(w) = p(z)$  and  $q(w) = q(z)$ .