

Let $\{\varepsilon_n\}_{n=1}^\infty$ be a sequence of positive real numbers, such that $\lim_{n \rightarrow \infty} \varepsilon_n = 0$. Find

$$\lim_{n \rightarrow \infty} \frac{1}{n} \sum_{k=1}^n \ln \left(\frac{k}{n} + \varepsilon_n \right),$$

where \ln denotes the natural logarithm.