

Let \mathbb{R}^+ be the set of positive real numbers. Find all functions $f : \mathbb{R}^+ \rightarrow \mathbb{R}^+$ such that for all $x, y \in \mathbb{R}^+$

$$f(x)f(yf(x)) = f(x + y).$$