(a) Let a_1, a_2, \ldots be a sequence of real numbers such that $a_1 = 1$ and $a_{n+1} > \frac{3}{2}a_n$ for all n. Prove that the sequence

$$\frac{a_n}{\left(\frac{3}{2}\right)^{n-1}}$$

has a finite limit or tends to infinity.

(b) Prove that for all $\alpha > 1$ there exists a sequence a_1, a_2, \ldots with the same properties such that

$$a_1, a_2, \ldots$$
 with the same properties such that
$$\lim_{n \to \infty} \frac{a_n}{\left(\frac{3}{2}\right)^{n-1}} = \alpha.$$