

Let P be an algebraic polynomial of degree n having only real zeros and real coefficients.

- a) Prove that for every real x the following inequality holds:

$$(n-1)(P'(x))^2 \geq nP(x)P''(x).$$

- b) Examine the case of equality.