

Let n be a positive integer, and denote by \mathbb{Z}_n the ring of integers modulo n . Suppose that there exists a function $f : \mathbb{Z}_n \rightarrow \mathbb{Z}_n$ satisfying the following three properties:

- (i) $f(x) \neq x$,
- (ii) $f(f(x)) = x$,
- (iii) $f(f(f(x+1)+1)+1) = x$ for all $x \in \mathbb{Z}_n$.

Prove that $n \equiv 2 \pmod{4}$.