

Let  $n, k \leq 3$  be integers, and let  $S$  be a circle. Let  $n$  blue points and  $k$  red points be chosen uniformly and independently at random on the circle  $S$ . Denote by  $F$  the intersection of the convex hull of the red points and the convex hull of the blue points. Let  $m$  be the number of vertices of the convex polygon  $F$  (in particular,  $m = 0$  when  $F$  is empty). Find the expected value of  $m$ .