Find all polynomials P in two variables with real coefficients satisfying the identity

$$P(x,y)P(z,t) = P(xz - yt, xt + yz).$$