Let $f: \mathbb{R} \to \mathbb{R}$ be a continuously differentiable function that satisfies f'(t) > f(f(t)) for all $t \in \mathbb{R}$. Prove that $f(f(f(t))) \leq 0$ for all $t \geq 0$.