For an  $n \times n$  matrix M with real entries let  $||M|| = \sup_{x \in \mathbb{R}^n \setminus \{0\}} \frac{||Mx||_2}{||x||_2}$ , where  $||\cdot||_2$  denotes the Euclidean norm on  $\mathbb{R}^n$ . Assume that an  $n \times n$  matrix A with real entries satisfies  $||A^k - A^{k-1}|| \leq \frac{1}{2002k}$  for all positive integers k.

Prove that  $||A^k|| \le 2002$  for all positive integers k.