

Prove that there exists no function

$f : (0, +\infty) \rightarrow (0, +\infty)$ such that

$f^2(x) \geq f(x+y)f(f(x)+y)$ for any $x, y > 0$.