

- a) Show that for any $m \in \mathbb{N}$ there exists a real $m \times m$ matrix A such that $A^3 = A + I$ where I is the $m \times m$ identity matrix.
- b) Show that $\det A > 0$ for every real $m \times m$ matrix satisfying $A^3 = A + I$.