

Let n be a positive integer. Compute the number of words w (finite sequences of letters) that satisfy all the following three properties:

- (1) w consists of n letters, all of them are from the alphabet $\{\mathbf{a}, \mathbf{b}, \mathbf{c}, \mathbf{d}\}$;
- (2) w contains an even number of letters \mathbf{a} ;
- (3) w contains an even number of letters \mathbf{b} .

(For example, for $n = 2$ there are 6 such words: \mathbf{aa} , \mathbf{bb} , \mathbf{cc} , \mathbf{dd} , \mathbf{cd} and \mathbf{dc} .)