

Let  $\alpha \in \mathbb{R} \setminus \{0\}$  and suppose that  $F$  and  $G$  are linear maps (operators) from  $\mathbb{R}^n$  into  $\mathbb{R}^n$  satisfying  $F \circ G - G \circ F = \alpha F$ .

a) Show that for all  $k \in \mathbb{N}$  one has

$$F^k \circ G - G \circ F^k = \alpha k F^k.$$

b) Show that there exists  $k \geq 1$  such that  $F^k = 0$ .