

Let  $n$  be a positive integer. Prove that  $2^{n-1}$  divides

$$\sum_{0 \leq k < n/2} \binom{n}{2k+1} 5^k.$$