

Is it true that if $f : [0, 1] \rightarrow [0, 1]$ is

a) monotone increasing

b) monotone decreasing

then there exists an $x \in [0, 1]$ for which $f(x) = x$?