Let A be  $3 \times 3$  real matrix such that the vectors Au and u are orthogonal for each column vector  $u \in \mathbb{R}^3$ . Prove that:

- a)  $A^T = -A$ , where  $A^T$  denotes the transpose of the matrix A;
  - b) there exists a vector  $v \in \mathbb{R}^3$  such that  $Au = v \times u$  for every  $u \in \mathbb{R}^3$ , where  $v \times u$  denotes the vector product in  $\mathbb{R}^3$ .