

Let  $n \geq 2$  be an integer. What is the minimal and maximal possible rank of an  $n \times n$  matrix whose  $n^2$  entries are precisely the numbers  $1, 2, \dots, n^2$ ?