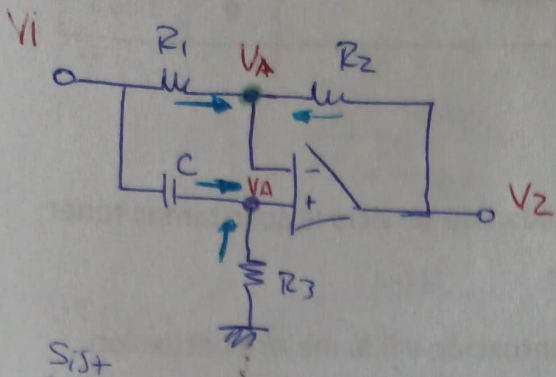


(7)

Guia

SISTEMATICO

#15



$$\bullet \quad V_A(s) \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - \frac{V_1(s)}{R_1} - \frac{V_2(s)}{R_2} = 0$$

$$\text{equação} \rightarrow \frac{V_1(s) - V_A(s)}{R_1} + \frac{V_2(s) - V_A(s)}{R_2} = 0$$

$$\frac{V_1(s)}{R_1} + \frac{V_2(s)}{R_2} = V_A(s) \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

(A)

$$\bullet \quad V_A(s) \left(sC + \frac{1}{R_3} \right) - V_1(s) sC = 0 \rightarrow$$

$$\text{equação} \rightarrow (V_1(s) - V_A(s)) sC - \frac{V_A(s)}{R_3} = 0$$

$$\frac{V_A(s)}{V_1(s)} = \frac{sC}{sC + \frac{1}{R_3}} = \frac{sC}{sCR_3 + 1}$$

(B)

$$\textcircled{A} \quad \frac{V_1(s)}{R_1} + \frac{V_2(s)}{R_2} = V_A(s) \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

(B)

$$\frac{V_1(s)}{R_1} + \frac{V_2(s)}{R_2} = \frac{V_1(s) sC R_3}{sC R_3 + 1} \left(\frac{1}{R_1} + \frac{1}{R_2} \right)$$

$$\frac{V_2(s)}{R_2} = V_1(s) \left[\frac{sC R_3}{sC R_3 + 1} \left(\frac{1}{R_1} + \frac{1}{R_2} \right) - \frac{1}{R_1} \right]$$

$$T(s) = \frac{V_2(s)}{V_1(s)} = R_2 \left[\frac{sC R_3}{sC R_3 + 1} \frac{R_2 + R_1}{R_1 R_2} - \frac{1}{R_1} \right]$$

$$T(s) = R_2 \frac{sC R_3 (R_2 + R_1) - (sC R_3 + 1) R_2}{(sC R_3 + 1) R_1 R_2}$$

$$T(s) = \frac{sC R_3 R_2 + sC R_3 R_1 - sC R_3 R_2 - R_2}{sC R_3 R_1 + R_1} = \frac{sC R_1 R_3 - R_2}{sC R_1 R_3 + R_1}$$

$$T(s) = \frac{C R_1 R_3}{C R_1 R_3} \frac{s - R_2 / C R_1 R_3}{s + 1 / C R_3} \Rightarrow T(s) = \frac{s - R_2 / C R_1 R_3}{s + 1 / C R_3}$$

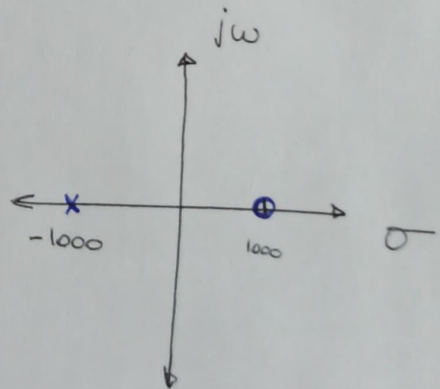
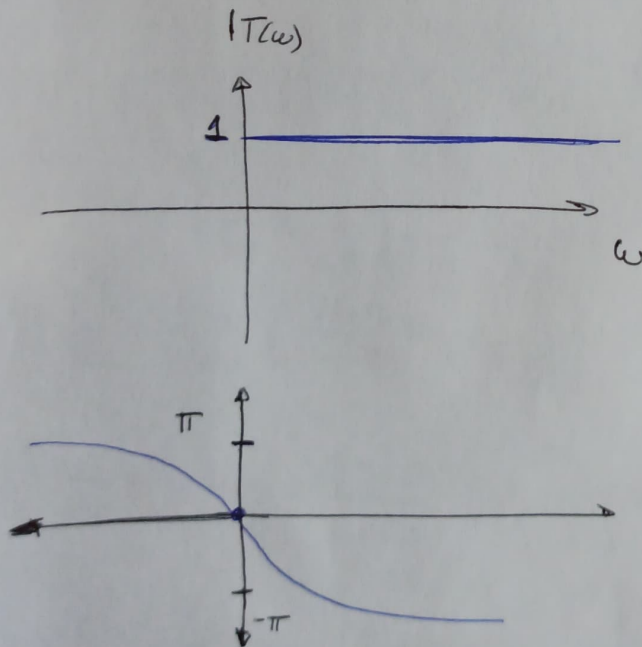
$$\frac{R_2}{R_1} = 1; R_3 = 1k; C = 1\mu F$$

#16

$$T(s) = \frac{s - 1000}{s + 1000} \Rightarrow T(s)|_{s=j\omega} = \frac{j\omega - 1000}{j\omega + 1000}$$

$$|T(\omega)| = \frac{\sqrt{\omega^2 + 1000^2}}{\sqrt{\omega^2 + 1000^2}} = 1; \quad \angle T(\omega) = \frac{e^{j \arctan(\omega/1000)}}{e^{j \arctan(\omega/1000)}}$$

$$\begin{aligned} T(\omega) &= |T(\omega)| e^{j\angle T(\omega)} = 1 e^{j(\arctan(\omega/1000) - \arctan(\omega/1000))} \\ &= 1 e^{j(-\arctan(\omega/1000) - \arctan(\omega/1000))} \\ &= 1 e^{j-2\arctan(\omega/1000)} \end{aligned}$$

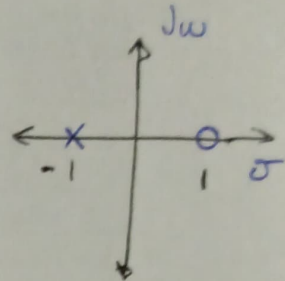


VERSIÓN NORMALIZADA

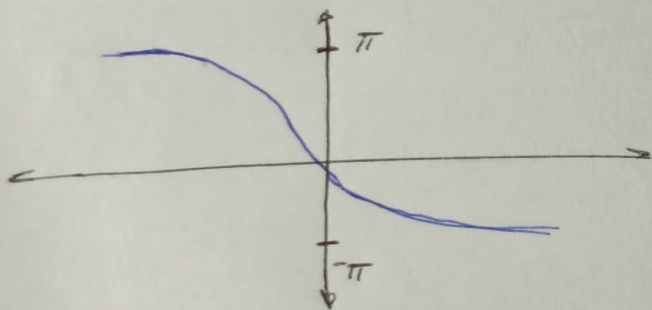
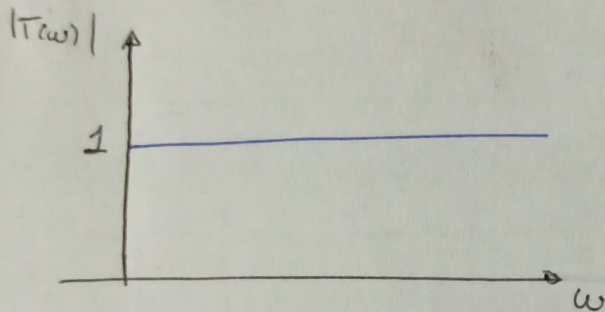
Retomando $T(s) = \frac{s - R_2 / C R_3}{s + 1 / C R_3}$; $R_2 = R_1$

$T(s) = \frac{s - 1 / C R_3}{s + 1 / C R_3} \equiv \frac{s - \omega_c}{s + \omega_p}$; $\omega_c = \omega_p$

\Rightarrow Normalizo tal que $T(s) = \frac{\omega_0 s - \omega_0}{\omega_0 s + \omega_0} = \frac{s - 1}{s + 1}$



\Rightarrow El Módulo sigue siendo 1, y la $\angle T(j\omega)$ no se modifica



Al normalizar sólo modifico el diagrama de polos y ceros

donde $\Rightarrow 1000 = \omega_0 = \frac{1}{C \cdot R_3 \cdot \omega} \equiv 1 \Rightarrow \boxed{\omega = 1000}$
 \downarrow \downarrow
 $1\mu F$ $1k$
 término de frecuencia

~~\Rightarrow Ver que si hubiera~~ \Rightarrow Ver que al normalizar no modifica la respuesta