# Algorithms and Datastructures Runtime analysis Minsort / Heapsort, Induction

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Algorithms and Datastructures, October 2017

#### Structure

## Algorithms and Datastructures

Structure

Links

Organisation

Daphne

Forum

Checkstyle

Unit Tests

Version management

**Jenkins** 

## Sorting

Minsort

Heapsort

## Algorithms and Datastructures

Topics of this Lecture

#### Topics of the Lecture:

- Algorithms and Data Structures
   Efficient data handling and processing
   ... for problems that occur in practical any larger program / project
- ► **Algorithm** Solving of complex computional problems

# Example 1: Sorting

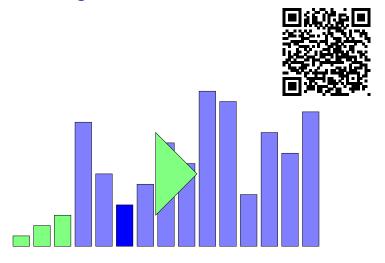


Figure: Sorting with Minsort

## Example 2: Navigation

- ▶ Datastructures: How to represent the map as data?
- Algorithms: How to find the shortest / fastest way?



Figure: Navigationplan © OpenStreetMap

## Content of the Lecture 1 / 2

#### **General:**

- ► Most of you had a lecture on basic progamming . . . performance was not an issue
- Here it is going to be:
  - 1. How fast is our program?
  - 2. How can I make it faster?
  - 3. How can I proof that it will always be that fast?
- Important issues:
  - Most of the time: application runtime
  - Sometimes also: resource / space consumption

## Content of the Lecture 2 / 2

## Algorithms:

- Sorting
- Dynamic Arrays
- Associative Arrays
- Hashing
- **Mathematics:**
- Runtime analysis
- ▶ O-Notation

- Priority Queue
- Linked Lists
- Pathfinding / Dijkstra Algorithm
- ► Search-Trees

Proof of correctness

## After the lecture . . .

... you should be able to understand the joke

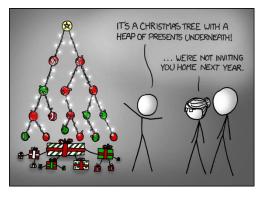


Figure: Comic © xkcd/835

Hopefully your parents will still invite you

## Links



## Homepage:

- Exercise sheets
- Lectures
- Materials

Link to Homepage

# Organisation 1 / 5

#### Lecture:

- ► Tuesday, 12:00 14:00, SR 00 010/014, Build. 101
- Recordings of the lecture will be uploaded to the webpage

#### **Exercises:**

- One exercise sheet per week
- Submission / Correction / Assistance online
- ► Tutorial: (if needed)
  Wednesday, 12:00-13:00 SR 00 010/014, Build. 101

#### Exam:

 Planned: Sa. 24th March 2018, 10:00-12:00, Build. 101, Lec. theater 026 & 036

# Organisation 2 / 5

#### **Exercises:**

- ▶ 80 % practical, 20 % theoretical
- We expect everyone to solve every exercise sheet

#### Exam:

- ▶ 50 % of all points from the exercise sheets are needed
- ▶ Content of exam: Whole lecture and all exercises

# Organisation - Exercises 3 / 5

#### **Exercises:**

- ► Tutors: Tim Maffenbeier, Abderrahmen Rakez, Tobias Faller
- Coordinators: Michael Uhl, Stefan Mautner,
   Florian Eggenhofer and Björn Grüning
- ▶ Deadline: ESE: 1 week, IEMS: none

# Organisation - Exercises 3 / 5

#### Exercises:

- Post questions into the forum (link later)
- Submission via "commit" through svn and Daphne
- ► Feedback one week after deadline through "update" (svn)
- Unit test / checkstyle via Jenkins

# Organisation - Exercises 4 / 5

#### **Exercises - Points:**

- Practical:
  - ► 60 % functionality
  - ▶ 20 % tests
  - 20 % documentation, Checkstyle, etc.
  - ▶ Program is not running ⇒ 0 points
- ► Theoretical (mathematical proof):
  - ▶ 40 % general idea / approach
  - ▶ 60 % clean / complete

# Organisation 5 / 5

#### **Effort:**

- ▶ 4 ECTS (ESE), 6 ECTS (IEMS)
- ▶ 120 / 180 working hours per semester
- ▶ 14 Lectures each 6 h / 8 h + exam
- ▶ 4 h / 6 h per exercise-sheet (one per week)

# Daphne

#### Daphne:

- Provides the following information:
  - Name / contact information of your tutor
  - Download of / info needed for exercise sheets
  - Collected points of all exercise sheets
  - Links to:
    - 1. Coding standards
    - 2. Build system
    - 3. The other systems
- ► Link: Daphne

#### Forum

#### Forum:

- Please don't hesitate to ask if something is unclear
- ► Ask in the forum and not separate. Others might also be interested in the answer
- ► I, Claudis Korzen or one of the tutors will reply as fast as possible
- ► Link: Forum

# Checkstyle flake8

## Checkstyle / Linting (flake8):

- ▶ Installation: python3 -m pip install flake8
- Check file: python3 -m flake8 path/to/files/\*.py
- ► Link: flake8

#### Unit Tests

#### Why unit tests?

- 1. A non-trivial method without an unit test is probably wrong
- 2. Simplifies debugging
- 3. We and you can automatic check correctness of code

#### What is a good unit test?

- Unit test checks desired output for a given input
- At least one typical input
- At least one **critical** case

  E.g. double occurrence of a value.

E.g. double occurrence of a value in sorting

#### Unit Tests

doctest

## **Testing (doctest):**

```
def subOne(n):
    """ Subtracts 1 from n
   >>> subOne(5)
   >>> subOne(3)
    return n-2
if __name__ == "__main__":
```

- Tests are contained in docstrings
- Module doctest runs them
- Run check with: python3 -m doctest path/to/files/\*.py -v

```
__name__ == __main__ :
print("2 minus 1: %d" % subOne(2))
```

# Version management

Subversion

## Version management (subversion):

- Keeps a history of code changes
- ▶ Initialize / update directory: **svn** checkout <URL>
- Add files / folders: svn add <file> --all
- Create snapshot: svn commit -m "<Your Message>" Data is uploaded to Jenkins automatically
- ► Link: Subversion

## **Jenkins**

#### Jenkins:

- Provides our build system
- You can check if your uploded code runs
  - Especially whether all unit test pass
  - ▶ And if **checkstyle** (flake8) is statisfied
- Will be shown in the first exercise
- ▶ Link: Jenkins

# Sorting 1 / 2

#### Problem:

- ▶ Input: n elements  $x_1, \ldots, x_n$
- ► Transitive operator "¡" which returns true if the left value is smaller than the right one
  - ▶ Transitivity: x < y,  $y < z \rightarrow x < z$
- ▶ Output:  $x_1, ..., x_n$  sorted with operator

## Example

Input: 14, 4, 32, 19, 8, 44, 65

Output:

# Sorting 2 / 2

#### Why do we need sorting?

- ► Nearly every program needs a sorting-algorithm
- Examples:
  - Index of a search engine
  - Listing filesystem in explorer / finder
  - ► (Music-) Library
  - ► Highscore list

## Minsort - Algorithm

#### Informal description:

- Find the minimum and switch the value with the first position
- Find the minimum and switch the value with the second position
- **.** . . .

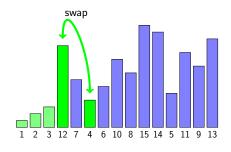


Figure: Minsort

## Minsort - Algorithm

## Minsort in Python:

```
def minsort(lst):
    for i in range (0, len(lst)-1):
        minimum = i
        for j in range(i+1, len(lst)):
             if lst[j] < lst[minimum]:</pre>
                 minimum = j
         if minimum != i:
             lst[i], lst[minimum] = \
                 Ist [minimum], Ist [i]
    return Ist
```

#### MinSort - Runtime

#### How long does our program run?

- We test it for different input sizes
- ► Observation:
  It is going to be
  "disproportional"
  slower the more
  numbers are being
  sorted

#### Table: Runtime for Minsort

n	Runtime / ms				
$2 \times 10^3$	5.24				
$4 \times 10^3$	16.92				
$6 \times 10^3$	39.11				
$8 \times 10^3$	67.80				
$10 \times 10^3$	105.50				
$12 \times 10^3$	150.38				
$14 \times 10^3$	204.00				
$16 \times 10^3$	265.98				
$18 \times 10^3$	334.94				

## MinSort - Runtime

#### How long does our program run?

- We test it for different input sizes
- Observation:

It is going to be "disproportional" slower the more numbers are being sorted

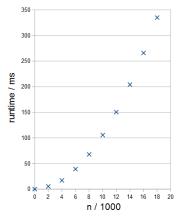


Figure: Runtime of Minsort

#### MinSort - Runtime

## Runtime analysis:

- As a first example serves this diagram for Minsort
  - Thats what you should do in the first exercise sheet

#### ▶ We observe:

- ► The runtime grows faster than linear
- With double the input size we need four times the time

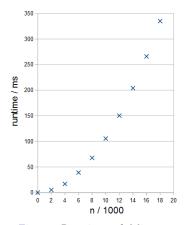


Figure: Runtime of Minsort

▶ Next lecture we will analyze deeper with other methods

# Heapsort - Algorithm 1 / 10

## **Heapsort:**

- The principle stays the same
- Better structure for finding the smallest element quicker

#### Binary heap:

- Preferably a complete binary tree
- ► **Heap property:** Each child is smaller (larger) than the parent element

## Heapsort - Algorithm 2 / 10

#### Min heap:

- ► **Heap property:** Each child is smaller (larger) than the parent element
- ▶ A valid heap fulfills the property at each node

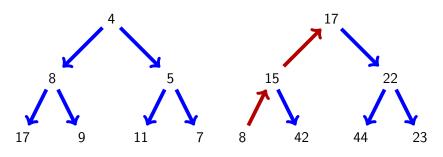


Figure: Valid min heap

Figure: Invalid min heap

## Heapsort - Algorithm 3 / 10

#### How to save the heap?

- We number all nodes from top to bottom and left to right starting at 0
  - ▶ The children of node i are 2i + 1 and 2i + 2
  - ▶ The parent node of node i is floor  $\left(\frac{i-1}{2}\right)$

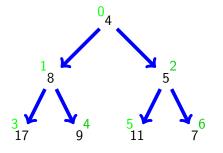


Table: Elements can be stored in array

0	1	2	3	4	5	6
4	8	5	17	9	11	7

Figure: Min heap

## Heapsort - Algorithm 4 / 10

## Repairing after taking the smallest element: heap.pop()

- Remove the smallest element (root node)
- Replace the root with the last node
- Sift the new root node down until the heap property is statisfied

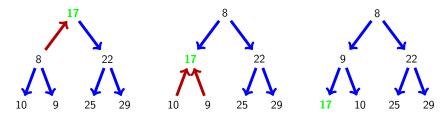


Figure: Repair of a min heap

# HeapSort - Algorithm 5 / 10

## **Heapsort:**

- Organize the *n* elements as heap
- ▶ While the heap still contains elements
  - Take the smallest element
  - Move the last node to the root
  - ▶ Repair the heap like previously described
- ▶ Output: 4, 5, ...

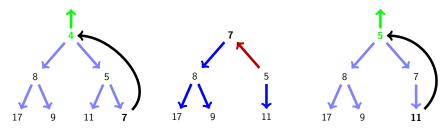


Figure: One iteration of Heapsort

# Heapsort - Algorithm 6 / 10

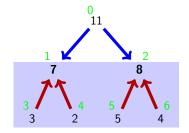
#### Creation of a heap:

- This operation is called heapify
- ▶ The *n* elements are already in the containing array
- ► Interpret this field als binary heap where the heap property is not yet statisfied
- We repair the heap from bottom up (in layers) with sift

# Heapsort - Algorithm 7 / 10

Table: Input in array

0	1	2	3	4	5	6
11	7	8	3	2	5	4



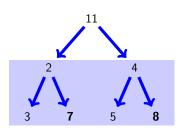
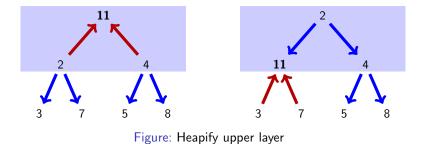


Figure: Heapify lower layer

# Heapsort - Algorithm 8 / 10



# Heapsort - Algorithm 9 / 10

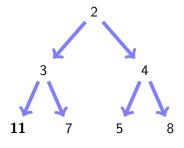


Figure: Resulting heap

# Heapsort - Algorithm 10 / 10

#### Finding the minimum is intuitive:

- ▶ Minsort: Iterate through all non-sorted elements
- ► **Heapsort:** Finding the minimum is trivial (concept)

  Just take the root of the heap

#### Removing the minimum in Heapsort:

- Repair the heap and restore the heap property
  - We don't have to repair the whole heap
- More of this in the next lecture

#### Further Literature

#### ► General for this Lecture

- [CRL01] Thomas H. Cormen, Ronald L. Rivest, and Charles E. Leiserson. Introduction to Algorithms. MIT Press, Cambridge, Mass, 2001.
- [MS08] Kurt Mehlhorn and Peter Sanders.
   Algorithms and Data Structures.
   Springer, Berlin, 2008.
   https://people.mpi-inf.mpg.de/~mehlhorn/
   ftp/Mehlhorn-Sanders-Toolbox.pdf.

#### Further Literature

#### Sorting

## Further Literature

#### Subversion

```
[Apa] Apache Subversion
https://subversion.apache.org/
```