Evolutionary Mechanics

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Abstract

We developed an application that is able to develop mechanical structures using an evolutionary algorithm. This approach can be scaled efficiently across many different nodes.

1 Method

Our project is divided in two sections and corresponding layers of parallelism. The first one is solving the mechanical equations to check if a mechanical structure can withstand a force. Figure 1 shows the result of such a simulation. The shape of a figure is approximated through squares. We used OpenMP for this part.

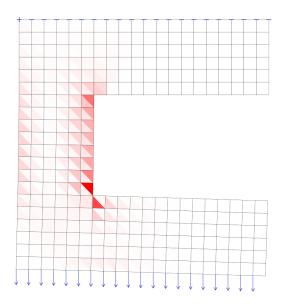


Figure 1: Result of a mechanical simulation

The second stage is the evolutionary algorithm. The best 10% survive in each round. The structures mutate and are simulated again. We used MPI for this part.

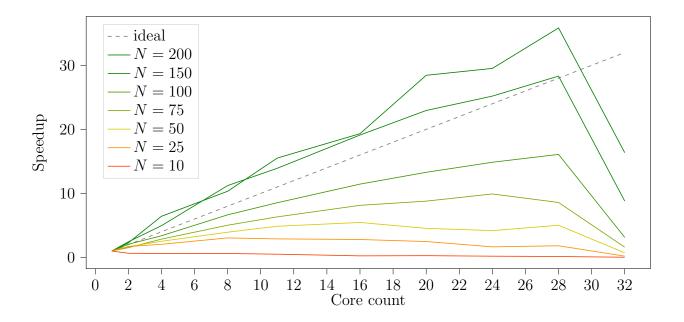


Figure 2: Speedup of the equation solver for different proplem sizes N.

	N = 10	N = 25	N = 50	N = 75	N = 100	N = 150	N = 200
Equations	230	1325	5150	11475	20300	45450	80600
C = 1	3	43	311	1153	3306	19869	97932
C = 2	4	25	185	754	1604	8149	42934
C = 4	5	21	123	403	976	4008	15251
C = 8	5	14	79	229	497	1771	9477
C = 11	6	15	64	182	387	1427	6311
C = 16	11	15	57	142	289	1040	5067
C = 20	10	17	69	131	249	866	3443
C = 24	14	26	74	116	222	789	3318
C = 28	19	24	62	134	205	702	2733
C = 32	91	209	432	718	1055	2257	5986

Table 1: Execution time for the equation solver for different field sizes N and cores C

1.1 Speeding up the equation solver

The reason for usign OpenMP is the tight coupeling between the data in the sparse matrix multiplication. gprof revealed that the equation solver spends most of it's time in the sparse matrix multiplication, however the whole equation solver class works parallelized.

- Threads are spawned at the highest level of the PerformanceEvaluator class. Subsequent calls to the equation setup, equation solver or linear algrabra operations will not spawn new threads. They require the threads to be set up already, and process only their chunk using the omp for directive.
- The equation setup process adds the local element striffness matrix into the global equation system. Depending on the mechanical structure, the position of different planes appears rather random. Therefore, a lock is needed to prevent a race condition. Because the matrix is sparse and each thread works on its own plane, that typically are not directly connected, it is unprobable that two threads operate on the same equation row at the same time. A global lock would introduce an unnecessary penalty, therefore each row uses it's own lock.
- All linear algebra operations of the **equation solver** work in parallel. There are two types of these operations. For addition, scalar multiplication, matrix multiplication or assigning a constant value, each thread processes its **own chunk of rows**. These operations do not require an implicit or explicit barrier. If for example, a vector addition follows a scalar multiplication, it is fine if the first thread begins with the scalar multiplication before the second thread has finished the vector addition, since each of them operates on its own set of rows.

However, in the conjugate gradient method there are also operations like the scalar product or the norm of the vector. These operations require a **reduction** and have an implicit barrier.

• In the beginning, a unique index has to be assigned to each Plane and corner. This is not parallelizable, as the total number of planes and corners is unknown and does not follow a predictable pattern.

The time complexity of the sequential equation solver is dominated by the sparse matrix multiplication, having a complexity of

$$O_{seqSolve}(N) = O(N^3) \tag{1}$$

as explained in the progress report. The sparse matrix multiplication is fully parallel. The indexing of the equation requires $O(N^2)$. Leaving the overhead for thread creation aside, the runtime complexity is

$$O_{parSolve}(N,C) = O\left(\frac{N^3}{C}\right) + O(N^2)$$
(2)

for a sufficiently large N. The efficiency is

$$E = \frac{O_{seqSolve}}{O_{parSolve}C} = O\left(\frac{N^3}{N^3 + C^2}\right) \tag{3}$$

The equation solver has weak scalability, because efficiency remains only at the same level if $N \propto C$. In practice however, there is a significant overhead in creating the threads. The speedup becomes only notable for problem sizes N > 50.

The Equation Solver is still a powerful solver. It is able to solve a mechanical structure with 80600 equations in 2.732 s using 28 cores on bridges. It also showcases OpenMP and locks well. The speedup of the execution time of table 3 are shown in figure 2.

1.2 Speeding up the evolutionary algorithm

Evolutionary algorithms are very parallel by nature. Each organism can be evaluated independent. Then they have to be sorted. We do the sorting on a node 0. Gather is used in that process. The best 10% get redistributed using Bcast.

A MPI Message for an evaluated board consisits of

- 1 float for the score
- $R \times C$ bytes, each containing the boolean value of the field.

We typically simulate grid sizes of 20, meaning the message has a size of 404 bytes. Since all processes will be initialized with the same field size it has not to be stored in the message. Our evolution works like shown in algorithm 1. The result of the finished evolution is shown on figure 4.

Algorithm 1 Evolute on node

Initialize all local fields fully set

for all epochs do

Mutate the fields

Evaluate the fields

Gather all fields into the master

Sort the fields on the master

Broadcast the best 10% to everyone

Replace local fields

end for

Cores	7	14	28	56	112	224
Cores per Task	1	1	1	1	1	2
Tasks	7	14	28	56	112	112
Nodes	1	1	1	2	4	8
N = 10	33.667	18.519	9,399	5.432	2.950	4.256
N = 20	296.997	164.875	91.958	43.114	25.199	29.429
N = 40	(2686.816)	(1343.408)	(671.704)	335.852	200.529	164.243

Table 2: Execution time in seconds for the evolution for different field sizes N and cores C. The generation size is set fixed to 112 and 1000 epochs are simulated.

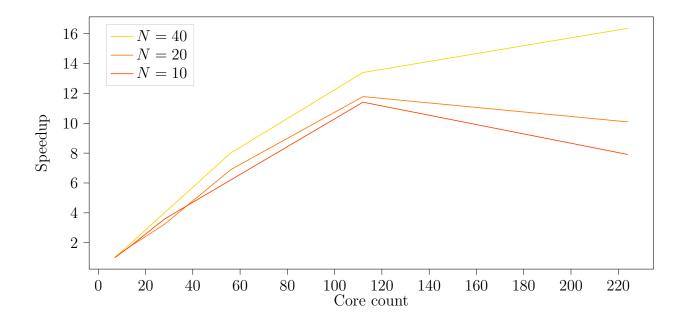


Figure 3: Speedup of the equation solver for different proplem sizes N.

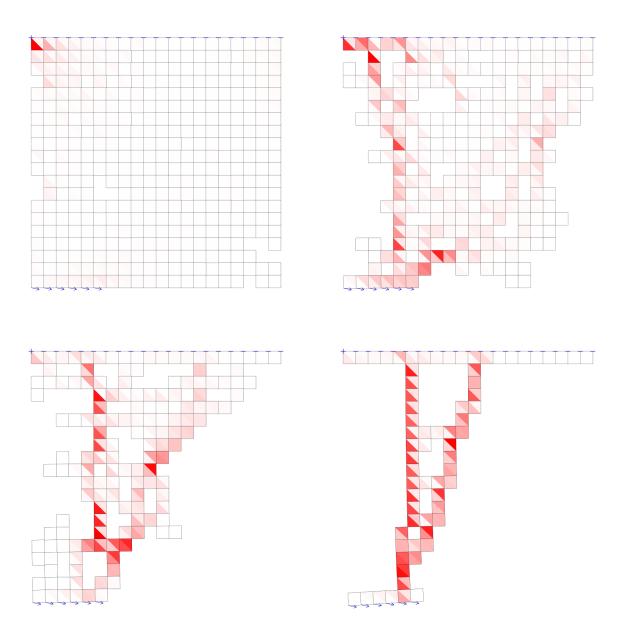


Figure 4: Result of a evoultion, using 20×20 gird, 100 organisms per epoch, 1000 epochs and a alterations decay of 0.995. Note, how the structure gets wider on the top to deal with the increased bending stress.