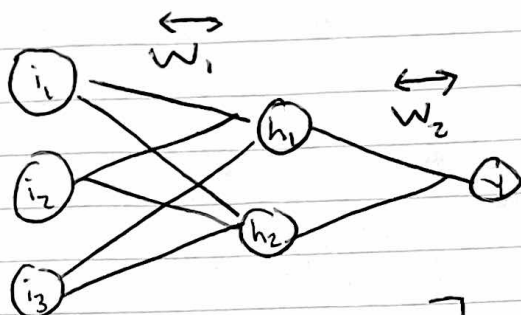


$$\vec{x}_1 = [2, 3, 4]$$

$$\vec{x}_2 = [6, 8, 3]$$

$$y_1 = 10$$

$$y_2 = 15$$



$$\vec{w}_1 = \begin{bmatrix} 0.1 & 0.4 \\ 0.2 & 0.5 \\ 0.3 & 0.6 \end{bmatrix}$$

$$\vec{w}_2 = \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

Activation: Hidden: $f_1(x) = \frac{1}{1 + e^{-x}}$

Output: $f_2(x) = x$

$$\eta = 0.1$$

$$\vec{x}_1 \cdot \vec{w}_1 = [2, 3, 4] \cdot \begin{bmatrix} 0.1 & 0.4 \\ 0.2 & 0.5 \\ 0.3 & 0.6 \end{bmatrix}$$

$$= [(0.2 + 0.6 + 1.2), (0.8 + 1.5 + 2.4)]$$

$$= [2, 4.7]$$

Hidden Activation: $f_1(\vec{x}_1 \cdot \vec{w}_1) = \left[\frac{1}{1 + e^{-2}}, \frac{1}{1 + e^{-4.7}} \right]$

$$= [0.88, 0.99]$$

$$f_1(\vec{x}_1 \cdot \vec{w}_1) \cdot \vec{w}_2 = [0.88, 0.99] \cdot \begin{bmatrix} 2 \\ 3 \end{bmatrix}$$

$$= 1.76 + 2.97$$

$$= 4.73$$

Output Activation: $f_2(f_1(\vec{x}_1 \cdot \vec{w}_1) \cdot \vec{w}_2) = 4.73$

Total Error: $\frac{1}{2}(10 - 4.73)^2$

$$= 13.89$$

$$\frac{\partial E_{\text{total}}}{\partial \vec{w}_{2(1,1)}} = \frac{\partial E_{\text{total}}}{\partial \text{out } y} \cdot \frac{\partial \text{out } y}{\partial y} \cdot \frac{\partial y}{\partial \vec{w}_{2(1,1)}}$$

$$\frac{\partial E_{\text{total}}}{\partial \text{out } y} = 2 * \frac{1}{2} (10 - 4.73) * (-1) = -5.27$$

$$\frac{\partial \text{out } y}{\partial y} = 1$$

$$\frac{\partial y}{\partial \vec{w}_{2(1,1)}} = 1.76$$

$$\Rightarrow \frac{\partial E_{\text{Total}}}{\partial \vec{w}_{2(1,1)}} = (-5.27)(1)(1.76) = -9.28$$

$$\begin{aligned} \vec{w}_{2(1,1)} &= \vec{w}_{2(1,1)} - \eta \frac{\partial E_{\text{Total}}}{\partial \vec{w}_{2(1,1)}} \\ &= 2 - 0.1 * (-9.28) \\ &= 2.93 \end{aligned}$$

$$\frac{\partial E_{\text{total}}}{\partial \vec{w}_{2(2,1)}} = (-5.27)(1)(2.97) = -15.65$$

$$\begin{aligned} \vec{w}_{2(2,1)} &= 3 - 0.1 * (-15.65) \\ &= 4.57 \end{aligned}$$

$$\vec{w}_2 = \begin{bmatrix} 2.93 \\ 4.57 \end{bmatrix}$$

$$\frac{\partial E_{total}}{\partial \overleftrightarrow{W_{1,(\dots)}}} = \frac{\partial E_{total}}{\partial out\ y} \cdot \frac{\partial out\ y}{\partial y} \cdot \frac{\partial y}{\partial out\ h_1} \cdot \frac{\partial out\ h_1}{\partial h_1} \cdot \frac{\partial h_1}{\partial \overleftrightarrow{W_{1,(\dots)}}}$$

($\overleftrightarrow{W_{2, \dots}}$)

$$\frac{\partial E_{total}}{\partial out\ y} = -5.27$$

$$\frac{\partial out\ y}{\partial y} = 1$$

$$\frac{\partial y}{\partial out\ h_1} = 2$$

$$\frac{\partial out\ h_1}{\partial h_1} = (out\ h_1)(1 - out\ h_1) = (0.88)(1 - 0.88) = 0.11$$

(i_1)

$$\frac{\partial h_1}{\partial \overleftrightarrow{W_{1,(\dots)}}} = 2$$

$$\frac{\partial E_{total}}{\partial \overleftrightarrow{W_{1,(\dots)}}} = (-5.27)(1)(2)(0.11)(2) = -2.32$$

$$\overleftrightarrow{W_{1, \dots}} = 0.1 - 0.1 * (-2.32)$$

$$= 0.33$$

$$\frac{\partial E_{total}}{\partial \overleftrightarrow{W_{1, (2,1)}}} = (-5.27)(1)(2)(0.11)(3)$$

$$= -3.48$$

$$\overleftrightarrow{W_{1, (2,1)}} = 0.2 - 0.1 * (-3.48)$$

$$= 0.55$$

$$\frac{\partial E_{total}}{\partial \overleftrightarrow{W_{1, (3,1)}}} = (-5.27)(1)(2)(0.11)(4)$$

$$= -4.64$$

$$\overleftrightarrow{W_{1, (3,1)}} = 0.3 - 0.1 * (-4.64) = 0.76$$

$$\frac{\partial E_{\text{total}}}{\partial W_1} = (-5.27)(1)(3)((0.99)(1-0.99))(2)$$

$$\frac{\partial E_{\text{total}}}{\partial W_1} = -0.31$$

$$\overleftrightarrow{W_1} = 0.4 - 0.1(-0.31)$$

$$= 0.43$$

$$\frac{\partial E_{\text{total}}}{\partial W_1} = (-5.27)(1)(3)(0.0099)(3)$$

$$= -0.47$$

$$\overleftrightarrow{W_1} = 0.5 - 0.1(-0.47)$$

$$= 0.55$$

$$\frac{\partial E_{\text{total}}}{\partial W_1} = (-5.27)(1)(3)(0.0099)(4)$$

$$= -0.63$$

$$\overleftrightarrow{W_1} = 0.6 - 0.1(-0.63)$$

$$= 0.66$$

$$\overleftrightarrow{W_1} = \begin{bmatrix} 0.33 & 0.43 \\ 0.55 & 0.55 \\ 0.76 & 0.66 \end{bmatrix}$$

$$\therefore \overleftrightarrow{W_1} = \begin{bmatrix} 0.33 & 0.43 \\ 0.55 & 0.55 \\ 0.76 & 0.66 \end{bmatrix}, \quad \overleftrightarrow{W_2} = \begin{bmatrix} 2.93 \\ 4.57 \end{bmatrix}$$