Sample Quality

descriptive analysis of data

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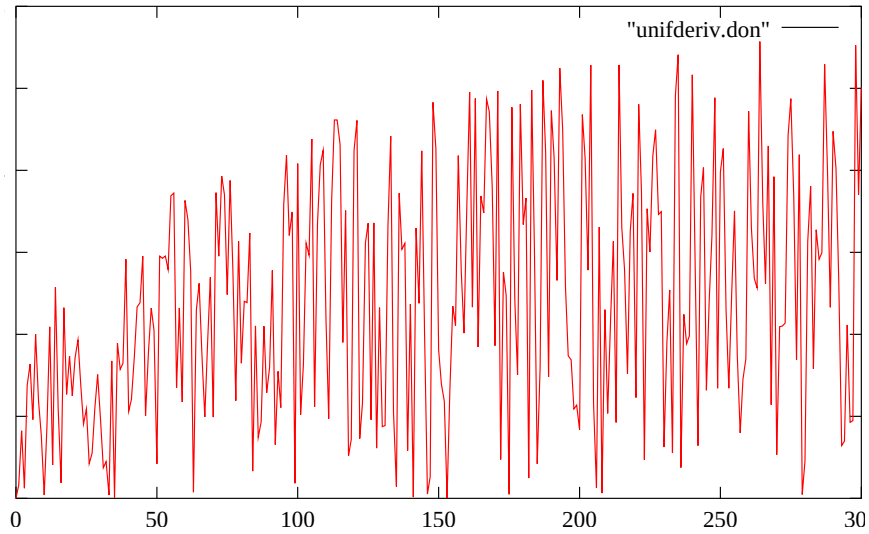
Porto Alegre, Brazil – October 2018

CONTROL OF EXPERIMENTS (1)



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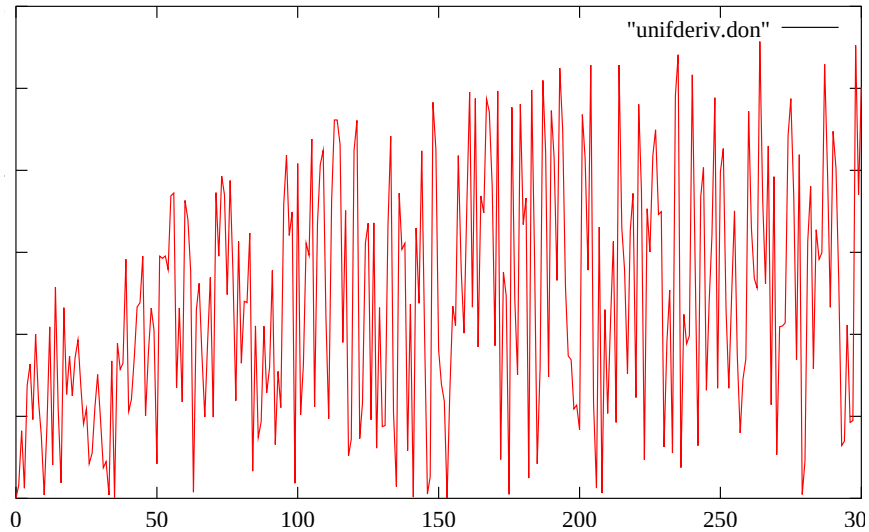
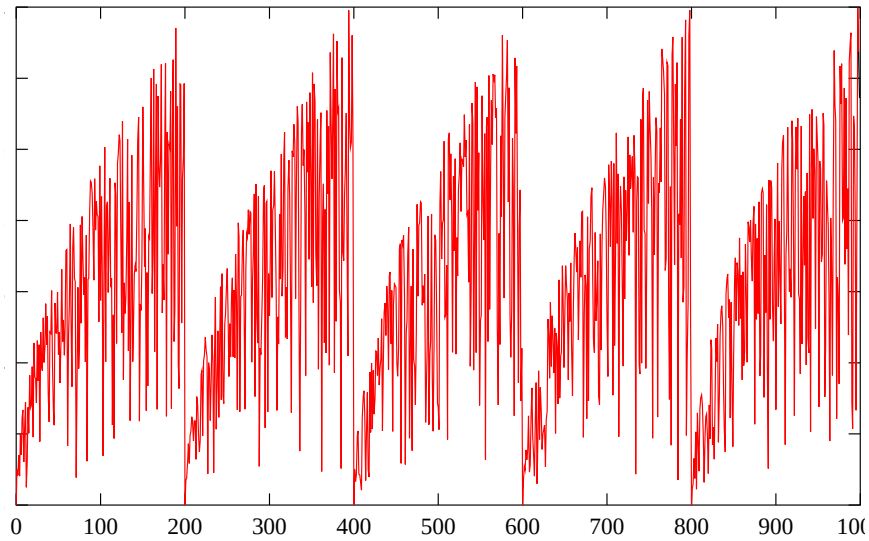


Tendency analysis

non homogeneous experiment
$\Rightarrow$ model the evolution of experiment
estimate and compensate tendency
explain why

CONTROL OF EXPERIMENTS (2)



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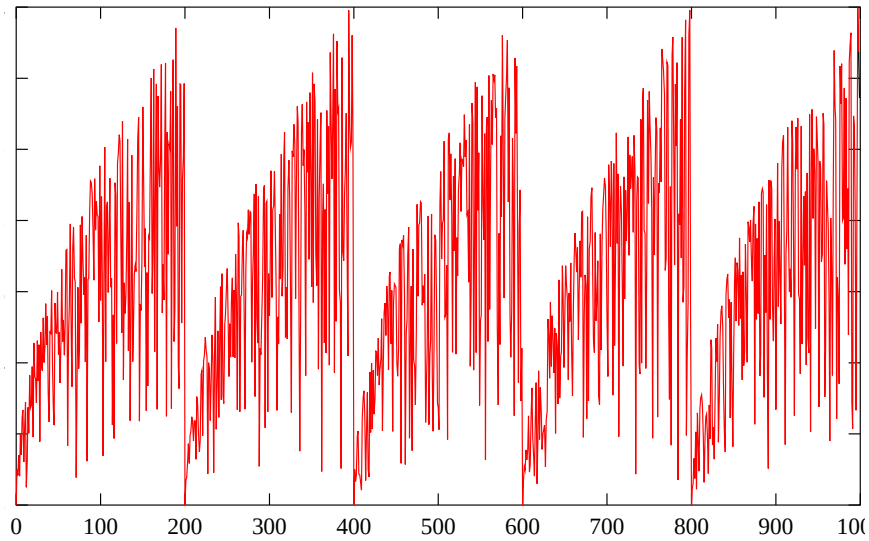


Periodicity analysis

periodic evolution of the experimental environment ?

$\Rightarrow$ model the evolution of experiment

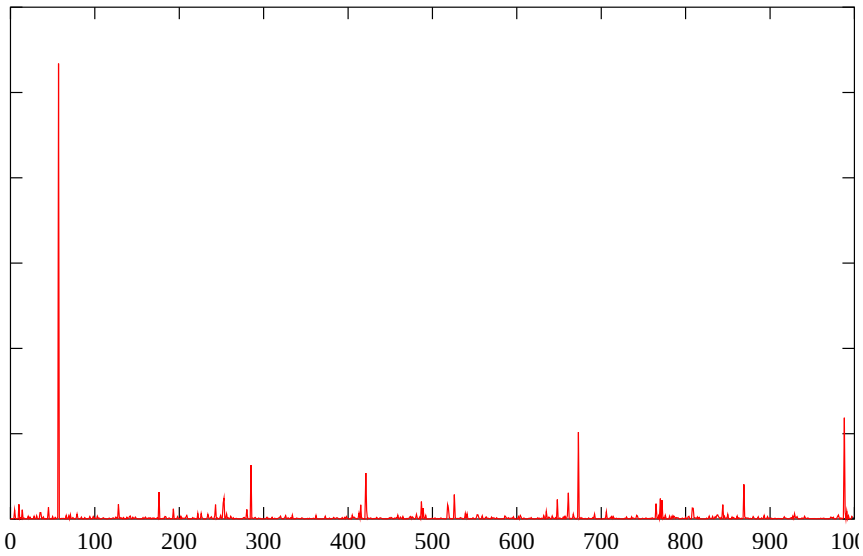
Fourier analysis of the sample

Integration on time (sliding window analysis) Danger : size of the window

Wavelet analysis

explain why

CONTROL OF EXPERIMENTS (3)



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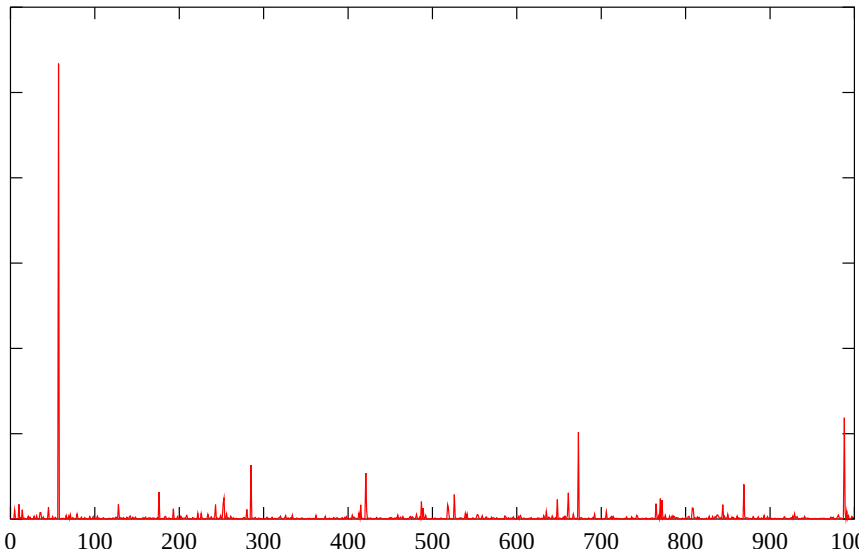

Non significant values

extraordinary behaviour of experimental environment
rare events with different orders of magnitude
$\Rightarrow$ threshold by value
Danger : choice of the threshold : indicate the rejection rate
$\Rightarrow$ threshold by quantile
Danger : choice of the percentage : indicate the rejection value
explain why

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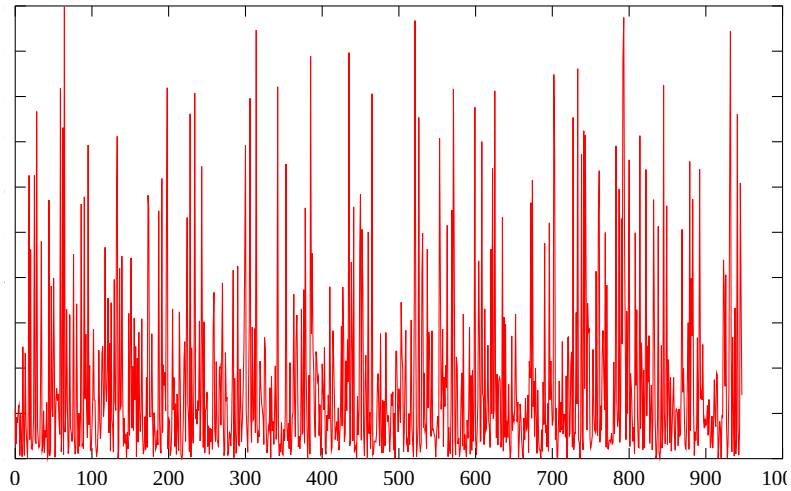
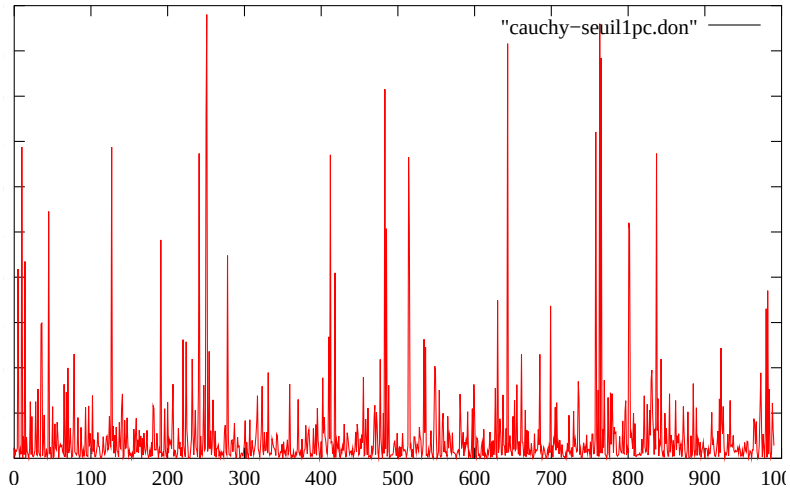
CONTROL OF EXPERIMENTS (4)

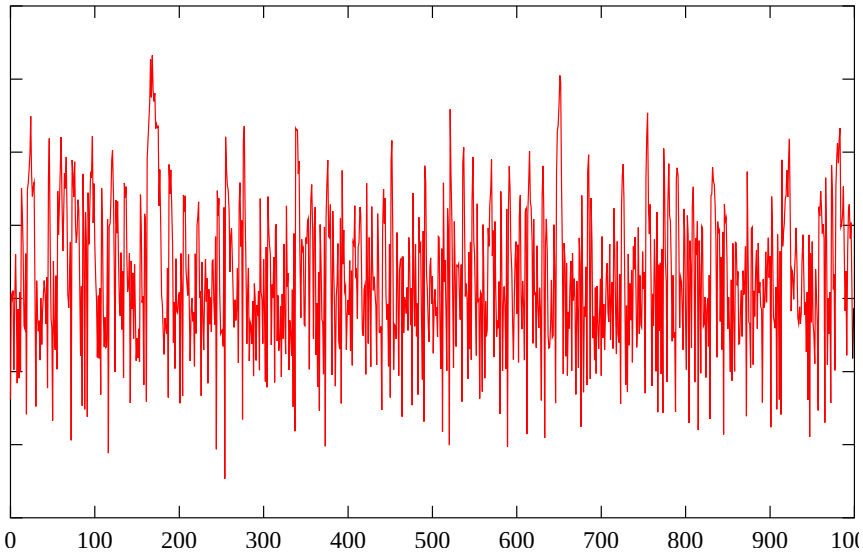
Threshold value : 10



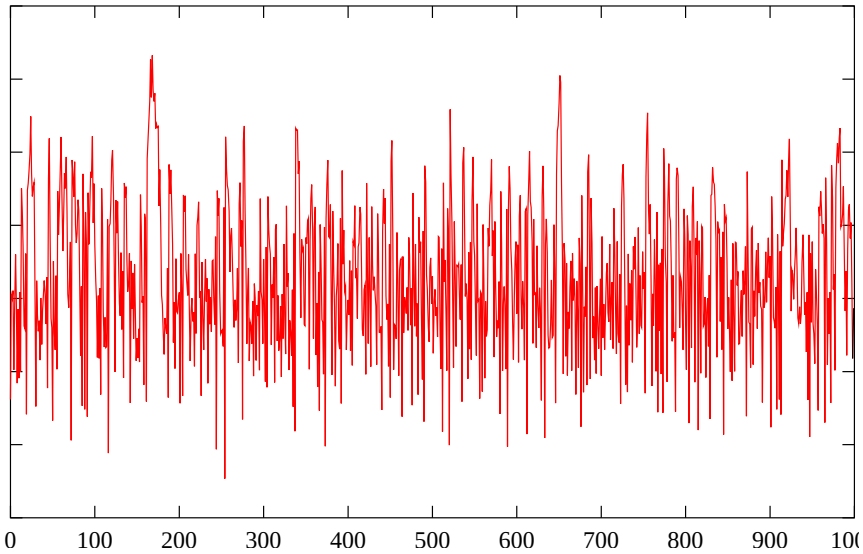
Threshold percentage : 1%



CONTROL OF EXPERIMENTS (5)



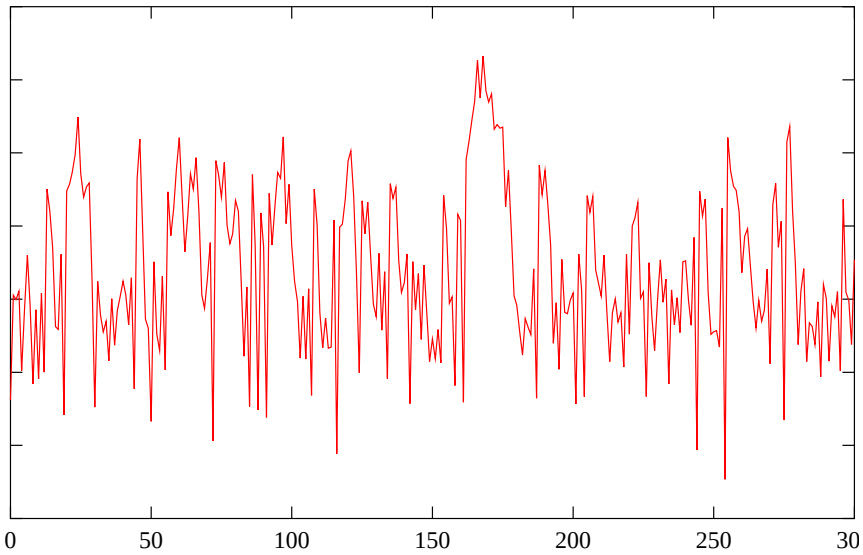
CONTROL OF EXPERIMENTS (5)



looks like correct experiments
Statistically independent
Statistically homogeneous

CONTROL OF EXPERIMENTS (5BIS)

Zooming



CONTROL OF EXPERIMENTS (5BIS)

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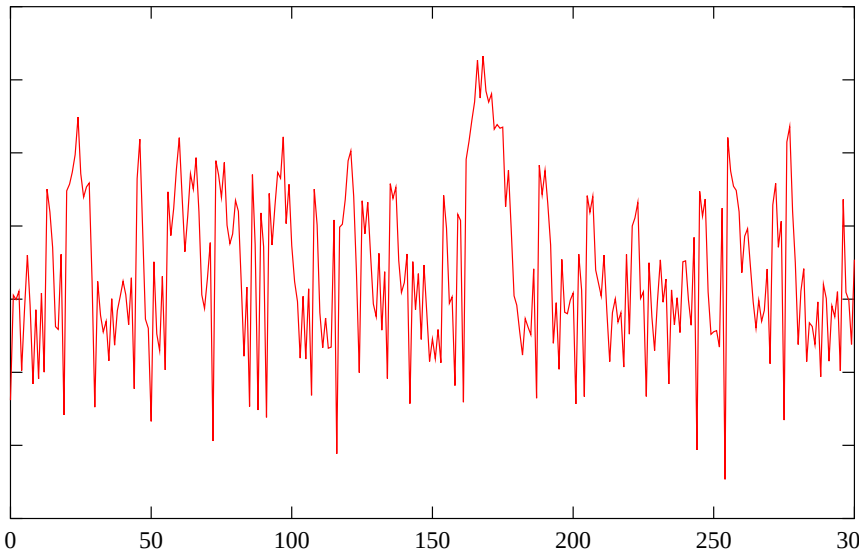


Autocorrelation

Danger time correlation among samples
experiments impact on experiments
$\Rightarrow$ stationarity analysis
autocorrelation estimation (ARMA)

EXPERIMENTAL RESULTS

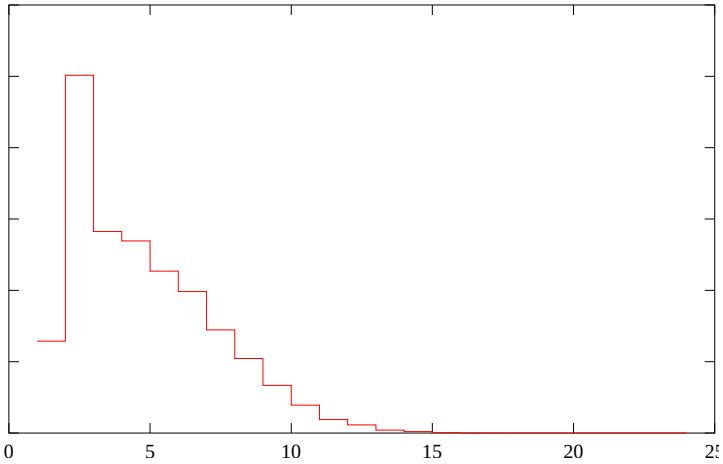
- Deterministic (controlled error non significant (white noise))
- Statistic (the system is non deterministic)

Sample analysis

- Identification of the response set
- Structure of the response set (measure)

DISTRIBUTION ANALYSIS

Summarize data in a **histogram**

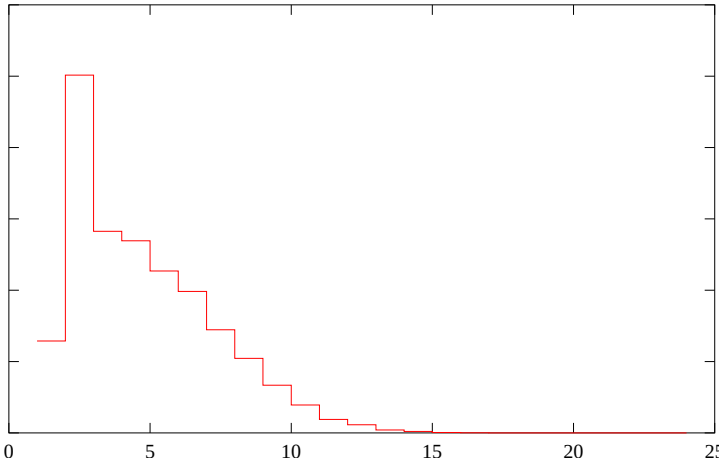


Shape analysis

- unimodal / multimodal
- variability
- symmetric / dissymmetric (skewness)
- flatness (kurtosis)

$\Longrightarrow$ **Central tendency analysis**
$\Longrightarrow$ **Variability analysis around the central tendency**

MODE VALUE



Mode

- **Categorical data**
- Most frequent value
- highly unstable value
- for continuous value distribution depends on the histogram step
- interpretation depends on the flatness of the histogram

$\Longrightarrow$ **Use it carefully**
$\Longrightarrow$ **Predictor function**

MEDIAN VALUE

Median

- **Ordered data**
- Split the sample in two equal parts

$$\sum_{i \leqslant Median} f_i \leqslant \frac{1}{2} \leqslant \sum_{i \leqslant Median+1} f_i .$$

- more stable value
- does not depends on the histogram step
- difficult to combine (two samples)

$\Longrightarrow$ **Randomized algorithms**

MEAN VALUE

Mean

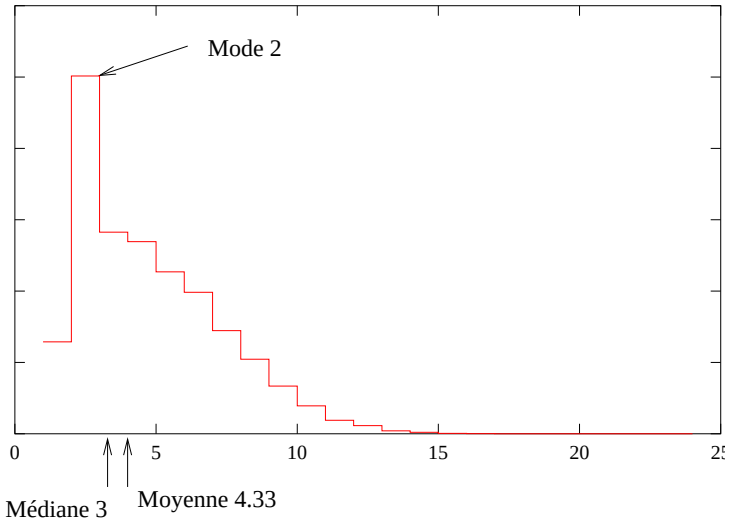
- **Vector space**
- Average of values

$$Mean = \frac{1}{Sample\_Size} \sum x_i = \sum_x x.f_x.$$

- stable value
- does not depends on the histogram step
- easy to combine (two samples $\Rightarrow$ weighted mean)

$\Longrightarrow$ **Additive problems (cost, durations, length,...)**

CENTRAL TENDENCY



Complementarity

- Valid if the sample is "Well-formed"
- **Semantic of the observation**
- Goal of analysis

$\Longrightarrow$ **Additive problems (cost, durations, length,...)**

CENTRAL TENDENCY (2)

Summary of Means

- Avoid means if possible
  Loses information
- Arithmetic mean
  When sum of raw values has physical meaning
  Use for summarizing times (not rates)
- Harmonic mean
  Use for summarizing rates (not times)
- Geometric mean
  Not useful when time is best measure of perf
  Useful when multiplicative effects are in play

VARIABILITY

Categorical data (finite set)

f_i : empirical frequency of element i
Empirical entropy

$$H(f) = -\sum_i f_i \log f_i.$$

Measure the empirical distance with the uniform distribution

- $H(f) \geqslant 0$
- $H(f) = 0$ iff the observations are reduced to a unique value
- $H(f)$ is maximal for the uniform distribution

VARIABILITY (2)

Ordered data

Quantiles : quartiles, deciles, etc
Sort the sample :

$$(x_1, x_2, \cdots, x_n) \longrightarrow (x_{(1)}, x_{(2)}, \cdots, x_{(n)});$$

$$Q_1 = x_{(n/4)};\ Q_2 = x_{(n/2)} = Median;\ Q_3 = x_{(3n/4)}.$$

For deciles

$$d_i = argmax_i\{\sum_{j \leqslant i} f_j \leqslant \frac{i}{10}\}.$$

Utilization as quantile/quantile plots to compare distributions

VARIABILITY (3)

Vectorial data

Quadratic error for the mean

$$Var(X) = \frac{1}{n}\sum_{1}^{n}(x_i - \bar{x}_n)^2.$$

Properties :

$$\begin{aligned} Var(X) &\geqslant 0; \\ Var(X) &= \overline{x^2} - (\bar{x})^2, \text{ where } \overline{x^2} = \frac{1}{n}\sum_{i=1}^{n} x_i^2. \\ Var(X + cste) &= Var(X); \\ Var(\lambda X) &= \lambda^2 Var(X). \end{aligned}$$