Finite Photon Packets, Overlap Criterion, and the Bell Threshold

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Emission takes time; therefore photons are finite spatiotemporal packets, not pointlike quanta. Let the packet length be

$$\ell \equiv c \,\tau_{\text{emit}} \,\kappa,\tag{1}$$

where $\tau_{\rm emit}$ is the emission (or coherence) time and $\kappa = \mathcal{O}(1)$ encodes lineshape. We prove and propose a decisive experimental test: in a loophole-free Bell experiment that (i) counts no-clicks via a CH/CH–Eberhard inequality and (ii) forbids post-selection, Bell violations vanish whenever the analyzer separation exceeds the photon packet length: $L > \ell$. Intuitively, nonclassical correlations require physical EM overlap of finite packets This is consistent with observations in long-distance fiber and free-space entanglement experiments once packets disengage (no overlap), spacelike-separated statistics revert to local bounds. We outline compact bench realizations using seeded vs. unseeded Nd:YAG/diode sources to vary ℓ by orders of magnitude, and provide visibility and Bell-parameter scaling vs. L/ℓ . The same overlap criterion explains laser coherence build-up as described in standard treatments of phase-locked cavity dynamics [1], and sets a gate-depth limit for photonic quantum computing as observed in recent photonic quantum circuit implementations: \sum (delays) $\ll \tau_{\rm emit}$.

INTRODUCTION (PROBLEM STATEMENT)

Standard treatments of quantum optics invoke point-like "photons" and wavefunction collapse at detection. See, for example, [2–6]. Lasers, interferometers, and detectors, however, are built from finite-time processes: an excited dipole relaxes over time; cavities store and release phase-coherent fields; detectors integrate EM energy over nonzero windows. A finite-time emission cannot produce a mathematical point. The physically faithful object is a finite photon packet with an envelope, phase, and polarization defined over a duration $\tau_{\rm emit}$.

The central claim here is operational: nonclassical two-photon correlations require spatiotemporal overlap of the packets. When overlap is absent, CH/CH–Eberhard tests that include no-clicks cannot violate local bounds. This yields a crisp, falsifiable prediction linking experiment geometry to source physics.

FINITE PHOTONS: DEFINITIONS AND BASIC RELATIONS

Let the complex field envelope of a single photon be E(t) with normalized first-order coherence $g^{(1)}(\tau)$. For a Lorentzian spectrum of FWHM $\Delta\nu$, the coherence time is approximately

$$\tau_c \approx \frac{1}{\pi \, \Delta \nu} \,,$$
(2)

(Gaussian differs by $\sqrt{2}$ under common conventions). We parameterize the packet length as

$$\ell \equiv c \, \tau_{\text{emit}} \, \kappa, \tag{3}$$

with $\tau_{\rm emit} \approx \tau_c$ in Fourier-limited cases; $\kappa \sim 1$ accounts for lineshape definitions. In pulsed sources, distinguish the *envelope duration* (pulse width) from the *coherence*

time; multi-longitudinal-mode pulses can have meterscale envelopes yet millimeter-scale ℓ .

Stimulated emission overlap. The probability amplitude to stimulate an inverted dipole with moment $\mu(t)$ is proportional to the overlap integral

$$\mathcal{A}_{\text{stim}} \propto \int_{-\infty}^{\infty} E(t) \, \mu(t) \, dt \,,$$
 (4)

so coherent build-up in a laser cavity requires finite-duration, phase-stable packets—impossible for pointlike quanta.

THE OVERLAP CRITERION AND BELL BOUND

Consider a biphoton source with packet length ℓ . Two analyzers (settings chosen via fast, independent RNGs) are separated by center-to-center distance L. Trials are pre-registered and evaluated with a CH/CH–Eberhard inequality that counts no-clicks; coincidence post-selection is forbidden.

Prediction (Overlap Criterion). If $L > \ell$, Bell violations vanish: $S(L) \leq 2$ under CH/CH-Eberhard evaluation without post-selection.

Mechanism sketch. Nonclassical correlations in this model are carried by EM overlap of finite packets. For separations $L \leq \ell$, the two packets share a common interaction domain, enabling phase-locked correlations across settings. As $L \to \infty$, overlap $\to 0$, so joint statistics reduce to local mixtures and the Bell functional saturates at the local bound.

A convenient visibility proxy is

$$V(\Delta L) \simeq \left| g^{(1)} \left(\frac{\Delta L}{c} \right) \right| ,$$
 (5)

so for a Lorentzian packet $V(\Delta L) \sim \exp(-|\Delta L|/\ell)$. The

Bell parameter obeys approximately

$$S(L) \approx 2 + \alpha V(L) \ (L \lesssim \ell), \qquad S(L) \to 2 \ (L \gtrsim \ell),$$
 (6)

with $\alpha \in [0,2]$ absorbing detection efficiencies and angle choices. The *threshold* $(L \approx \ell)$ is the key claim.

LASER COHERENCE AS MECHANISM, NOT METAPHOR

Laser build-up directly evidences finite, phase-bearing packets. In pointlike or instant-collapse ontologies, sequential stimulated emission lacks a coupling timescale and cannot select a cavity mode progressively. In contrast, the overlap relation above predicts gain proportional to packet—dipole overlap; narrowing the spectrum (increasing τ_c) extends ℓ , reducing threshold and enhancing phase locking—standard laser engineering outcomes, here elevated to the *ontology* of photons.

DECISIVE EXPERIMENTS (BENCH-TOP FEASIBLE)

- (A) Bell vs. packet length. Build two photonic Bell stations with independent RNGs and CH/CH–Eberhard evaluation. Use the same geometry while switching sources to vary ℓ : (i) unseeded Q-switched Nd:YAG (multi-mode; short ℓ), (ii) injection-seeded Q-switched Nd:YAG (single-mode; longer ℓ), (iii) single-frequency CW (very long ℓ). Prediction: violations only for $L \lesssim \ell$; none for $L \gg \ell$ without post-selection.
- (B) HOM/Interference envelope as ℓ ruler. Two identical packets on a 50/50 BS; visibility/HOM-dip depth vs relative delay follows $V(\Delta L)$.
- (C) Gate-depth cliff. Mach–Zehnder "circuit" with a Pockels phase gate. Process fidelity vs cumulative delay shows a cliff when $\sum \Delta T \approx \tau_{\rm emit}$. Repeating with different ℓ shifts the cliff in lockstep.
- (D) Pulse-envelope vs coherence. Demonstrate that long temporal pulses (ns) with multi-mode spectra yield short ℓ (mm–cm), whereas spectrally narrow fields (kHz) yield ℓ of km—even for short carved packets (cavity-dumped CW).

Anti–post-selection safeguards. Pre-register trial definitions; include no-clicks; fixed coincidence windows; publish full time tags; spacelike-separated settings.

IMPLICATIONS FOR QUANTUM COMPUTING

In this ontology, photonic operations require *continuous EM engagement*:

$$\sum_{\text{gates}} \Delta T \ll \tau_{\text{emit}} \quad \Rightarrow \quad \text{high-fidelity operations.} \quad (7)$$

With ns emitters ($\ell \sim 0.3\,\mathrm{m}$), multi-gate circuits outrun the packet. Long-lived transitions ($\mu\mathrm{s-ms}$) provide ℓ from 300 m to 300 km, enabling deep circuits. The same principle explains why lasers (engineered for long τ_c) readily achieve global phase coherence.

CONCLUSION

A finite-time emission produces a finite photon packet. Recognizing this yields a clean, falsifiable overlap criterion: Bell violations vanish without post-selection whenever $L > \ell = c\,\tau_{\rm emit}\,\kappa$. The same mechanism explains laser coherence and sets architectural limits for photonic quantum computing. The proposed experiments are compact and decisive. Either reality sides with finite packets—or collapse remains a story without a mechanism.

RELEVANT PRIOR WORK

This paper draws on experimental and theoretical foundations including the original Bell test formulations [5, 6], modern loophole-free demonstrations [2–4], and supporting work on entanglement swapping [7], long-range distribution [8], and photon indistinguishability [9]. Laser coherence mechanisms are rooted in [1, 10].

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