

$$\Downarrow F_{xy}(x, y) \stackrel{\text{DEF}}{=} P(X \leq x, Y \leq y)$$

Hence,

$$\begin{aligned} F_x(x) &= P(X \leq x) = P(X \leq x, Y \leq \infty) = F_{xy}(x, \infty) \\ &= \lim_{y \rightarrow \infty} F_{xy}(x, y) \end{aligned}$$

$$\begin{aligned} F_y(y) &= P(Y \leq y) = P(X \leq \infty, Y \leq y) = F_{xy}(\infty, y) = \\ &= \lim_{x \rightarrow \infty} F_{xy}(x, y) \end{aligned}$$

$x \rightarrow \infty$

$$P(X_1 \leq x < x_2, Y_1 \leq y < y_2) = ?$$

HOW TO  
CALCULATE

$$F_{xy}(x_1, y_1)$$

$$F_x(x_1)$$

$$F_y(y_1)$$

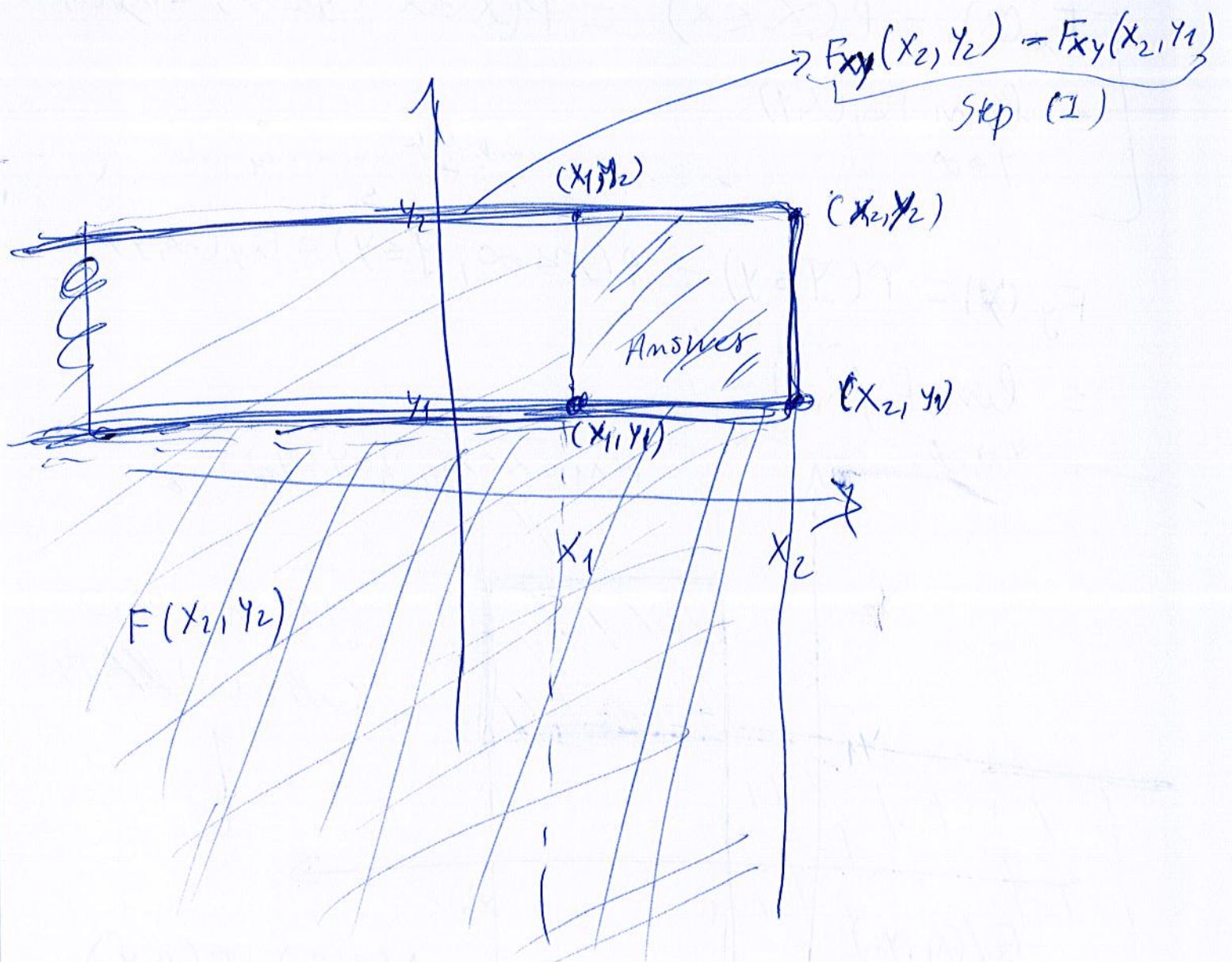
$$F_x(x_2) = F_{xy}(x_2, \infty)$$

$$F_{xy}(x_2, y_2) - F(x_1, y_2)$$

$$- F(x_2, y_1) + F(x_1, y_1)$$



$$P(X \leq x_2, y_1 \leq Y \leq y_2) = ?$$



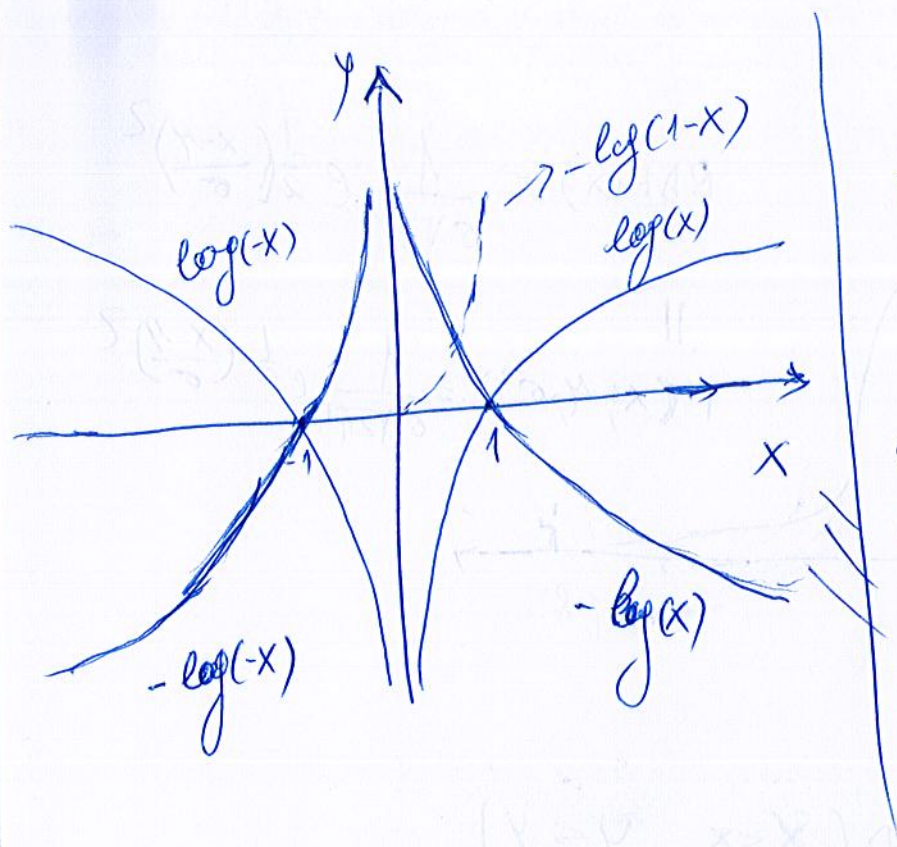
Step II  $F_{xy}(x_2, y_2) - F_{xy}(x_2, y_1) - F_{xy}(x_1, y_2)$

Step III  $F_{xy}(x_2, y_2) - F_{xy}(x_2, y_1) - F_{xy}(x_1, y_2) + F_{xy}(x_1, y_1)$

because ~~this~~  $\downarrow$  this part  
 was removed twice

$$P(X_1 \leq X \leq x_2, y_1 \leq Y \leq y_2)$$





$$f: [a, b] \rightarrow \mathbb{R} \quad f \in C^0[a, b]$$

$$\forall x_1, x_2 \in [a, b]$$

$$\forall \lambda \in [0, 1]$$

$$f(\lambda x_1 + (1-\lambda)x_2) \leq \lambda f(x_1) + (1-\lambda)f(x_2)$$

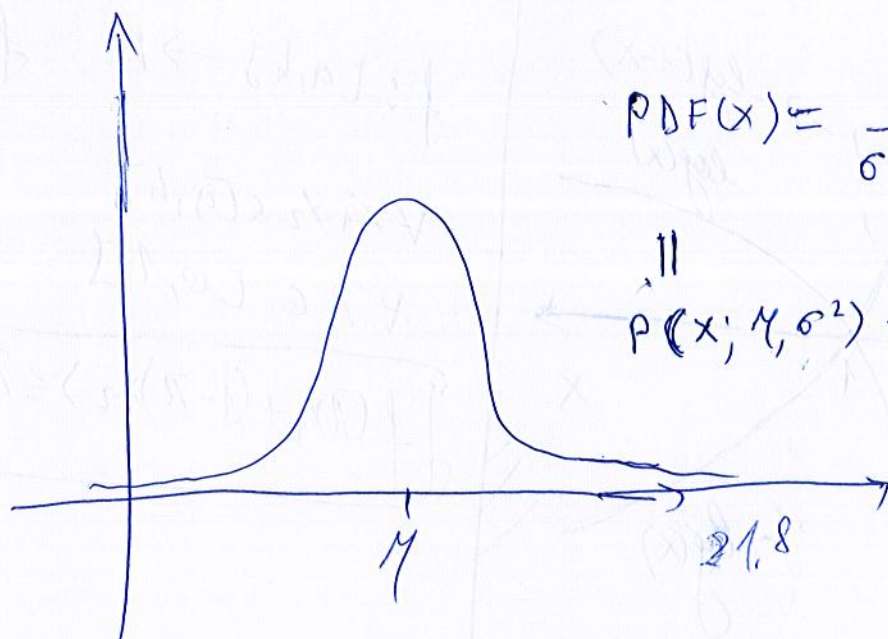
Convex function is a CONTINUOUS FUNCTION <sup>in its domain</sup> whose value at midpoint of every interval does not exceed the arithmetic mean of its values at the end of interval

$$f: [a, b] \rightarrow \mathbb{R}; f \in C^0; \lambda \in [0, 1] \quad \forall x_1, x_2 \in [a, b]$$

$$\forall \lambda \in [0, 1]$$

$$f(\lambda x_1 + (1-\lambda)x_2) \leq \lambda f(x_1) + (1-\lambda)f(x_2)$$





$$PDF(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

$$P(X; \mu, \sigma^2) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$$

$$F_{xy}(x, y) = P(X \leq x, Y \leq y)$$

~~$$P(X \leq x, Y \leq y)$$~~

$$F_X(x) = P(X \leq x, Y \leq \infty)$$

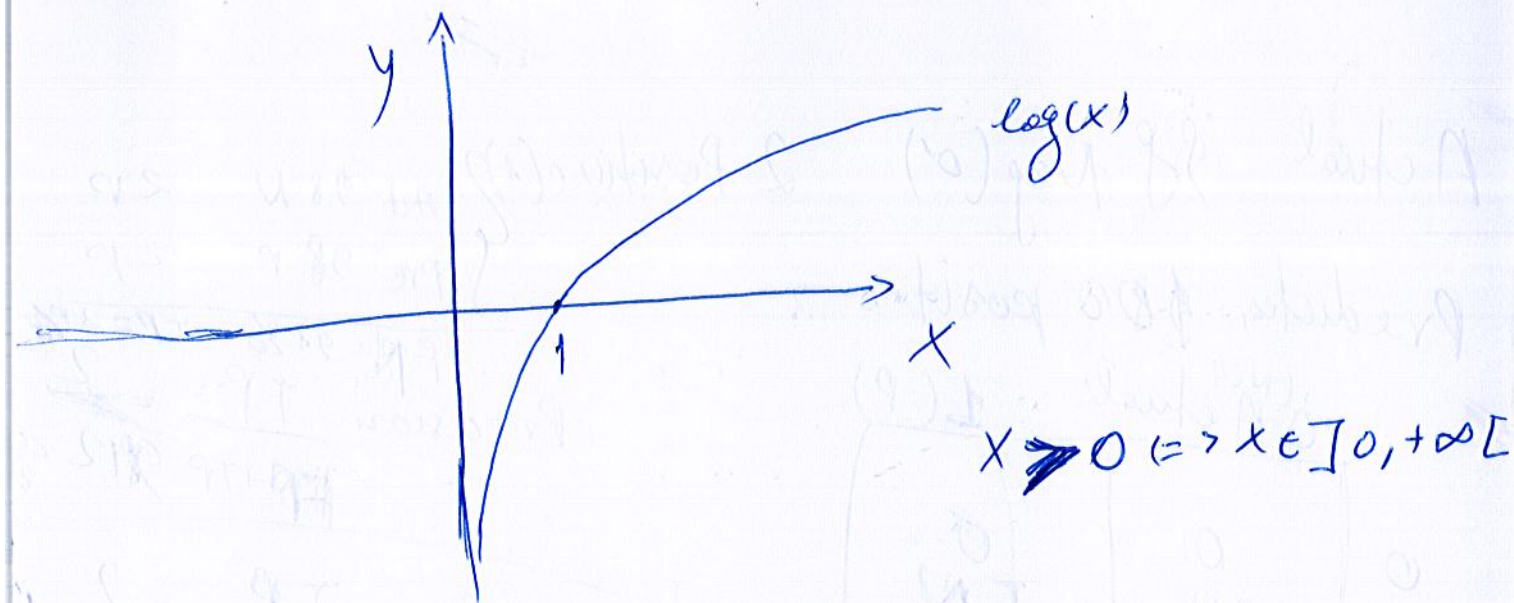
$$F_X(x) = P(X \leq x) = P(X \leq x \wedge Y \leq \infty)$$

$$= F_{xy}(x, \infty)$$

$$F_Y(y) = F_{xy}(\infty, y)$$

$$F_Y(y) = P(Y \leq y) = \cancel{P(Y \leq y)}$$

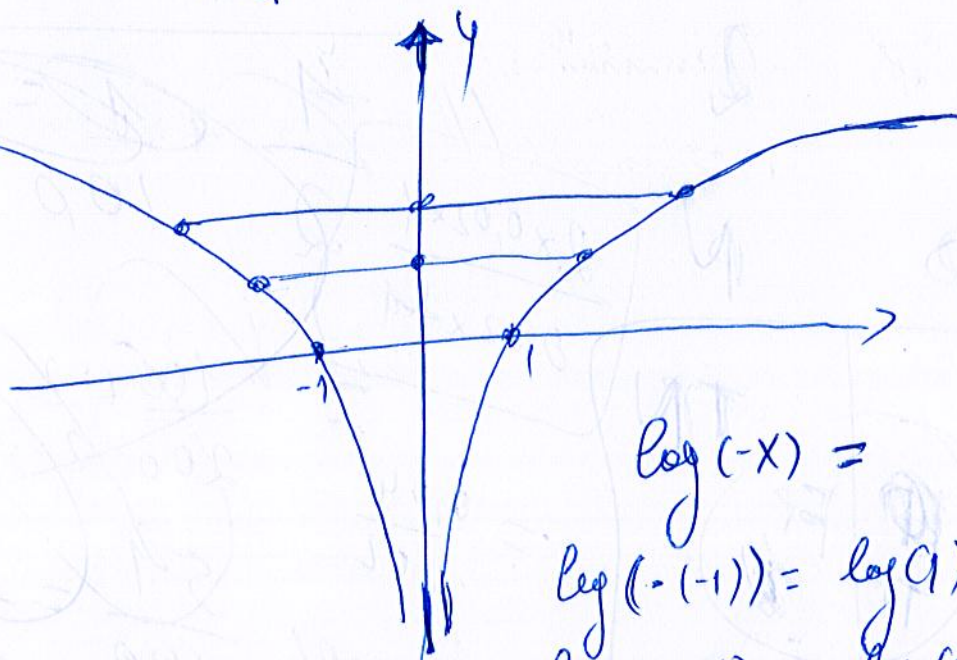
$$= P(Y \leq \infty, Y \leq y)$$



$\log(-x)$  ?

$-x$  must be  $> 0 \Leftrightarrow -x > 0 \Leftrightarrow x < 0$

Thus, if we have  $x < 0$  does exist  $\log(x)$



**AX of Symmetry**

$$\begin{aligned}\log(-x) &= \\ \log(-(-1)) &= \log(1) \\ \log(-(-2)) &= \log(2)\end{aligned}$$



Actual 98 Neg(0) 2 Positive(1)

Predicted 100 posit

(New)  
Actual

1(P)

0	0 TN	0 FN
1	98 FP	2 TP

Ad 98 N 2 P

pre 98 P 2 P

FP = 98% TP = 2%

$$\text{Precision} = \frac{TP}{FP + TP} = \frac{2}{98 + 2} = 2\%$$

$$\text{Recall} = \frac{TP}{TP + FN} = \frac{2}{2 + 0} = 100\%$$

$$F_1 = \frac{2 \times 2\% \times 100\%}{2\% + 100\%} = 1\%$$

98

2

FN	TP	FP	TN
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$$\frac{2 \times 0,02 \times 1}{0,02 \times 1} = 2$$

$$= \frac{0,04}{1,02}$$

FP = 98%

$$\frac{100 + 2 \times 100}{200} = \frac{100 + 200}{200} = \frac{300}{200} = 1,5$$

$$\frac{51}{100} = \frac{100}{51}$$

what is outside the eye is not seen  
pres  
over positiv



①

$$\sum_{k=1}^m 2k = 2 + 4 + 6 + \dots + 2m$$

↓  $\frac{2m}{2}$  terms  
↓  $\frac{2m}{2}$   
→  $m$  term

$$= \frac{(2+2m) \cdot m}{2} = \frac{2(m+1)m}{2} = (m+1)m$$

$$\sum_{k=1}^m k = 1 + 2 + 3 + \dots + m = \frac{1+m}{2} \cdot m = \frac{(1+m)m}{2}$$

Ex.  $2 + 4 + 6 + 8 = (1 + 2 + 3 + 4) \cdot 2$

$$\sum_{k=1}^m 2k = 2 \sum_{k=1}^m k$$

~~3+4~~  
 $1 + 2 + 3 + 4 + 5$   
6  
6

$$(1+5) \cdot \frac{5}{2}$$

$$(1+5) \cdot 2.5 = (1+5) \cdot 2 + \frac{1+5}{2} = 6 \cdot 2 + 3$$



1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12

$$1, 12 = 13 = 1+m$$

$$2, 11 = 13$$

$$3, 10 = 13$$

⋮

first 4 even numbers

$$2 + 4 + 6 + 8 = 20$$

$$1 + 2 + 3 + 4 + \dots = 10$$

2x4 number

$$2 + 4 + 6 + 8 = 2 \cdot (1 + 2 + 3 + 4)$$

$$2 = 1 + 1$$

$$4 = 1 + 3 = 2 + 2$$

$$6 = 2 + 4 = 3 + 3$$

$$8 = 3 + 5 = 4 + 4$$

$$\frac{2 + 4 + 6 + 8 + 10}{2} = \frac{2}{2} + \frac{4}{2} + \frac{6}{2} + \dots$$

$$\sum_{k=1}^n 2k = 2 \sum_{k=1}^n k$$

$$\frac{(1+m)m}{2}$$

$$\sum_{k=1}^m 2k = 2 \sum_{k=1}^m k$$

$$2, 4, 6, 8, \dots, m (=29)$$

$$S = \frac{(2+m) \cdot m}{2} \cdot \frac{1}{2}$$

$$\frac{m(m+1)}{2}$$

$$= \frac{(1+4) \cdot 4}{2} = 10$$

$$\sum_{k=1}^m k = \frac{1}{2} \sum_{k=1}^m 2k$$

$$\frac{m(m+1)}{2} = \frac{1}{2} \sum_{k=1}^m 2k$$

$$\sum_{k=1}^m k = \frac{1}{2} \sum_{k=1}^m 2k$$

$$\sum_{k=1}^m k = \sum_{k=1}^m k$$

$$\sum m \text{ first even} = 2 \sum \text{first } m$$



$$\cancel{p(z)} \quad p(z, \theta) = p(z|\theta) \cdot p(\theta) \\ = p(\theta|z) \cdot p(z)$$

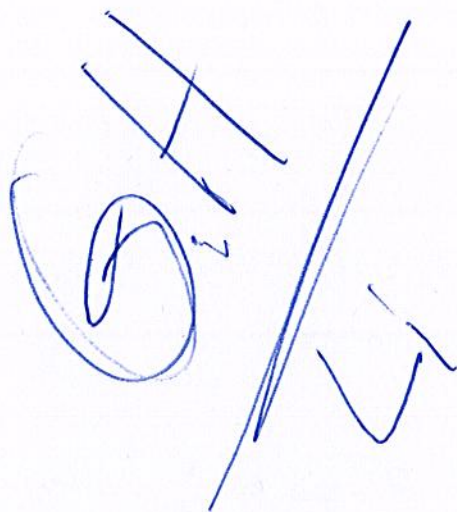
$$\text{mar}(z) = \sum_{\theta \in \Theta} p(z, \theta) = \sum_{\theta \in \Theta} p(\theta|z) p(z)$$

$$E_{z \sim p(z; \theta)} [z] = \sum_{z \in Z} z \cdot p(z; \theta) = \sum_{z \in Z} z \cdot p(z|\theta) \\ = \sum_{z \in Z} z \cdot p(z)$$

$$E[x] = \sum x \cdot p(x)$$

$$E[f(x)] = \sum f(x) \cdot p(x)$$


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$$(0)9 \cdot (0)59 = (0,5)9$$

$$(0)9 \cdot (0)59 =$$

$$(0)9 \cdot (0)59 \sum_{0 \leq n} = (0,5)9 \sum_{0 \leq n} = (5) \cdot 10/m$$

$$(0)59 \cdot 0,5 = (0,5)9 \cdot 5 = 1,5$$

$$(0)9 \cdot 0,5 = 0,5 \cdot 5 = 2,5$$

$$(0)9 \cdot 0,5 = 0,5 \cdot 5 = 2,5$$

$$(0)9 \cdot 0,5 = 0,5 \cdot 5 = 2,5$$

1/10