綠上,原方程的-般靜方:

 $X = \frac{1}{2} sin(t)$ 

七→∞们有界斜为

X· Cet·Dtet··sinit) (C.O为常教)

参照 (1), 斛得-般解

 $\sqrt{2} \quad w = X - y \qquad \frac{d^2w}{dt^2} + 2\frac{dw}{dt} + 2w = \cos(t)$ 

W= 
$$Ce^{-t} \sin(t) + De^{-t} \cos(t) + \frac{1}{5} \sin(t) + \frac{1}{5} \cos(t)$$
 (CD为常数)  
上 历古程的 - 解解为:

$$X = \frac{2+\omega}{2} = Ae^{-2t} + B + Ce^{-t} sin(t) + De^{-t} cos(t) + \frac{2}{5} sin(t)$$

$$\frac{2+\omega}{2} = Ae^{-2t} + B +$$

$$\frac{2-\omega}{2} = Ae^{-2t} + B$$

$$\frac{2-\omega}{2} = Ae^{-2t} + B$$

$$y = \frac{2-w}{2} = Ae^{-2t} + B - Ce^{-t} \sin(t) - De^{-t} \cos(t) - \frac{1}{5} \sin(t)$$

七→20的有界解为:

y = B - + cos(t)

$$\frac{2-\omega}{2} = Ae^{-2t} + B$$

$$\frac{2-\omega}{2} = Ae^{-2t} + B$$

X= B+亏 sin(t) (B为任意常款)

$$\sqrt{2} \ 2 = \chi + y \qquad \frac{d^2 t}{dt^2} + 2 \frac{dt}{dt} = cos(t)$$

 $\frac{1}{2}y = \frac{1}{x} \cdot y \cdot \frac{dy}{dt} = -\frac{1}{x^2} \cdot \frac{dx}{dt}$ 

代入y=fine 整理得:

一般 附为:

 $=\frac{1}{X^2}\frac{1}{2}(e^{-t}x^2+x)$ 

 $=-\frac{1}{2}(e^{-t}+\frac{1}{x})$ 

= - 1 (e-t + 4)

=> 2 ky + y = -e-t

⇒ f (t) = e<sup>-1t</sup>+ C ( L为常教)

= et + Cet (C为常教)

= et (L为常教)

 $\frac{4^{+}}{4^{+}} = -\frac{1}{2} e^{-\frac{1}{2}t}$ 

y (+) = (e-++ c) e-++

 $\Rightarrow \chi(t) = \frac{1}{e^{\tau} \cdot (e^{\tau}t)}$ 

代入X(0)=立, 斜得 C=1

 $\chi(t) = \frac{e^t}{1 + o^{\pm t}}$