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Teammate first hand wrote some calculations for design0 (initial bridge design). The 2 other members (me included) also worked on it. We compared answers to make sure we did it right because these calculations are crucial for all the next steps.

The first thing we did when checking for correctness is inspecting the similarity of the shear force diagram.

$FOS_{tention} = 4.36$
 $FOS_{compression} = 1.038$
 $FOS_{flex.buck\ 1,top\ plate} = 0.619$
 $FOS_{flex.buck\ 2,flanges} = 3.59$
 $FOS_{flex.buck\ 3,webs} = 5.29$
 $FOS_{shear} = 2.86$
 $FOS_{glue} = 8.03$
 $FOS_{shear.buck} = 3.76$

5

Factor of safeties (FOSs) for design0. One of the FOSs is less than one, so requires optimization. Green text in the following modifications represents increase, red text decrease, and black text same.

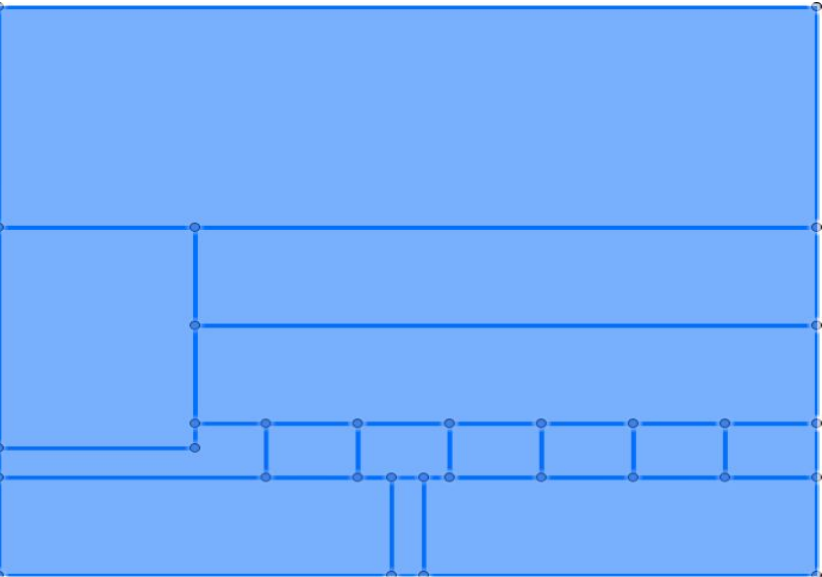
$FOS_{tention} = 4.53$
 $FOS_{compression} = 1.657$
 $FOS_{flex.buck\ 1,top\ plate} = 4.49$
 $FOS_{flex.buck\ 2,flanges} = 15.04$
 $FOS_{flex.buck\ 3,webs} = 15.56$
 $FOS_{shear} = 2.89$
 $FOS_{glue} = 6.60$
 $FOS_{shear.buck} = 3.78$

$FOS_{tention} = 8.21$
 $FOS_{compression} = 3.07$
 $FOS_{flex.buck\ 1,top\ plate} = 8.34$
 $FOS_{flex.buck\ 2,flanges} = 9.00$
 $FOS_{flex.buck\ 3,webs} = 11.92$
 $FOS_{shear} = 4.27$
 $FOS_{glue} = 10.05$
 $FOS_{shear.buck} = 2.47$

Attempt to even out the FOSs (maximize the minimum) by playing with parameters to weaken strong parts of the bridge to reinforce weak parts.

Additional tweaks to the bridge dimensions that brought the lowest FOS up to 3.02. Went through a total of three rounds of iteration.

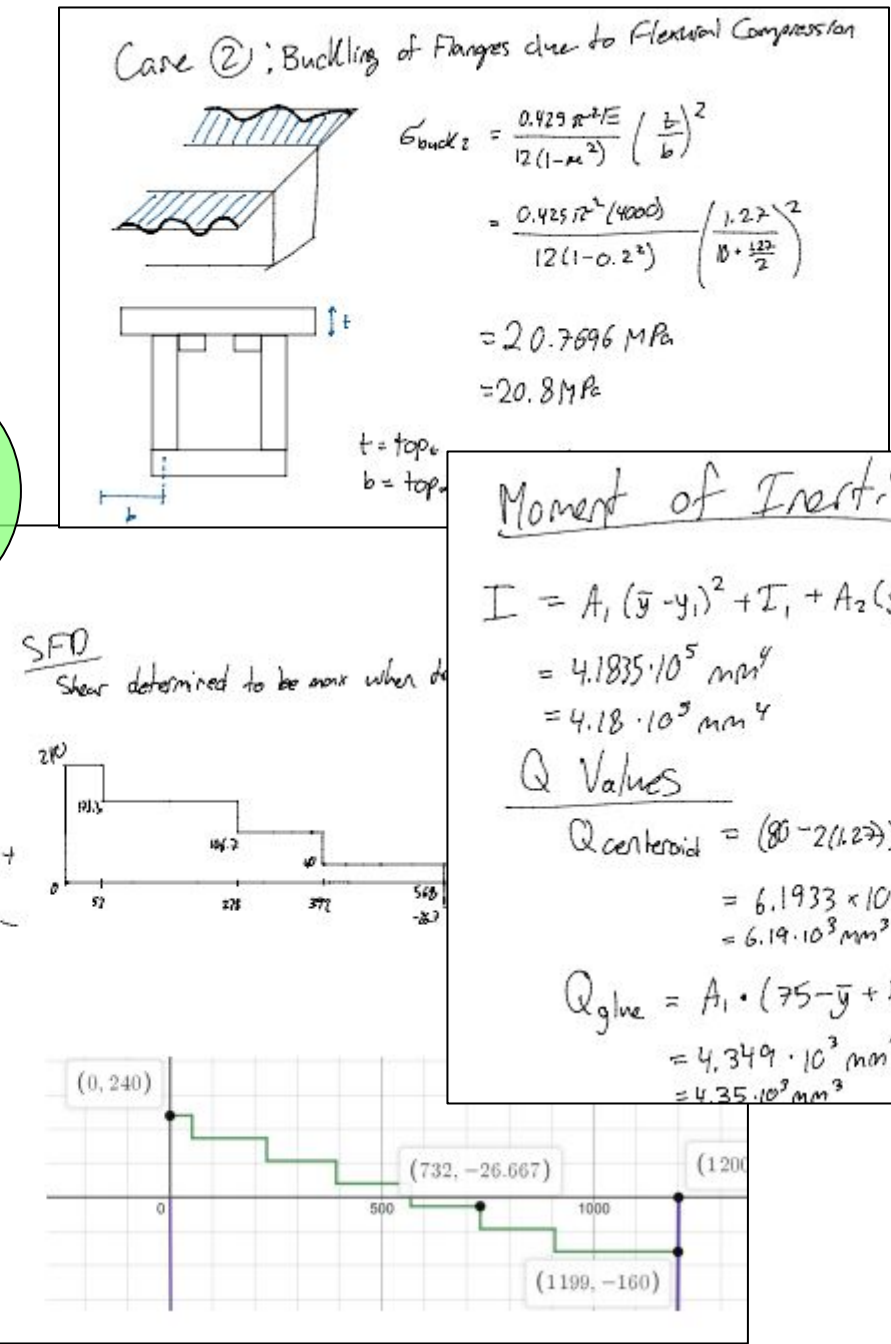
$FOS_{tention} = 8.21$
 $FOS_{compression} = 3.07$
 $FOS_{flex.buck\ 1,top\ plate} = 8.34$
 $FOS_{flex.buck\ 2,flanges} = 9.00$
 $FOS_{flex.buck\ 3,webs} = 11.92$
 $FOS_{shear} = 4.27$
 $FOS_{glue} = 10.05$
 $FOS_{shear.buck} = 3.02$



Version 1 of our matboard cutout, designed in Fusion 360. We realized that the space can be optimized, so we tried another cut

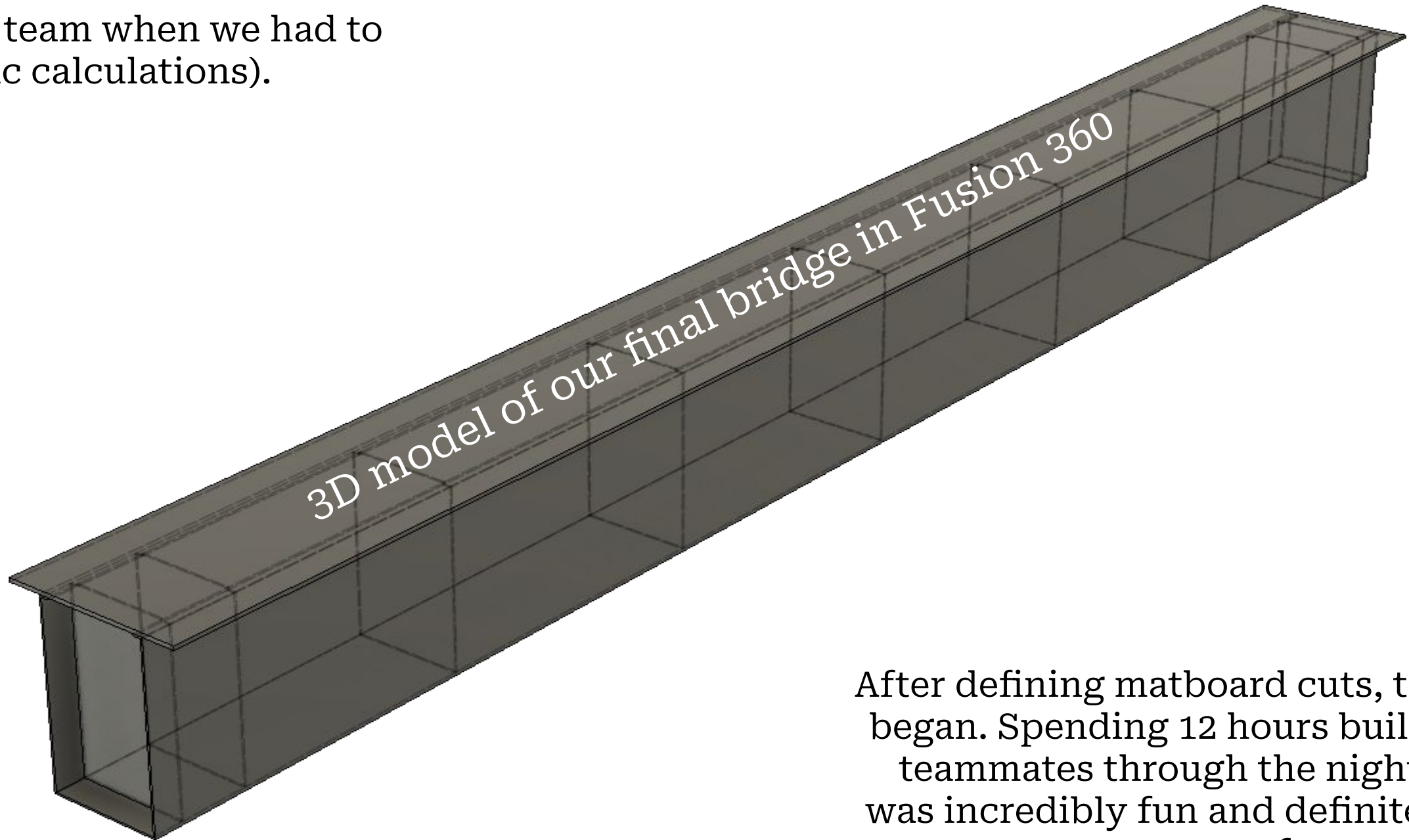
6

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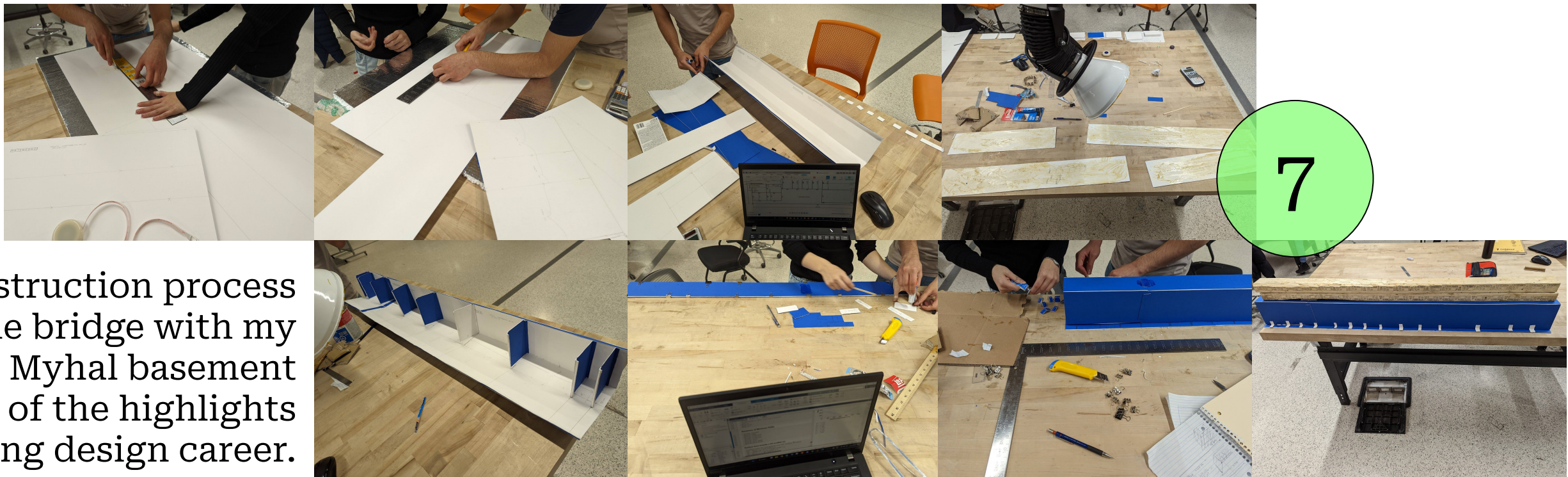


Various excerpts taken from sample calculations. The end calculations were to show different Factors of Safeties (FOSs) for various modes of failure. These Calculations were a good copy for the initial design0 calculations and included more details that what was expected for the team when we had to hand in the first deliverable (more basic calculations).

Moment of Inertia
 $I = A_1(\bar{y} - y_1)^2 + I_1 + A_2(\bar{y} - y_2)^2 + I_2 + A_3(\bar{y} - y_3)^2 + I_3 + A_4(\bar{y} - y_4)^2 + I_4$
 $= 4.185 \cdot 10^5 \text{ mm}^4$
 $= 4.18 \cdot 10^5 \text{ mm}^4$
Q Values
 $Q_{centeroid} = (80 - 2(1.23))(1.23)(\bar{y} - 1.23) + 2\bar{y}(1.23)(\frac{35}{2})$
 $= 6.1933 \cdot 10^3 \text{ mm}^3$
 $= 6.19 \cdot 10^3 \text{ mm}^3$
 $Q_{glue} = A_1 \cdot (\bar{y} - \bar{y} + 1.23^2)$
 $= 4.349 \cdot 10^3 \text{ mm}^3$
 $= 4.35 \cdot 10^3 \text{ mm}^3$



After defining matboard cuts, the construction process began. Spending 12 hours building the bridge with my teammates through the night in the Myhal basement was incredibly fun and definitely one of the highlights of my engineering design career.



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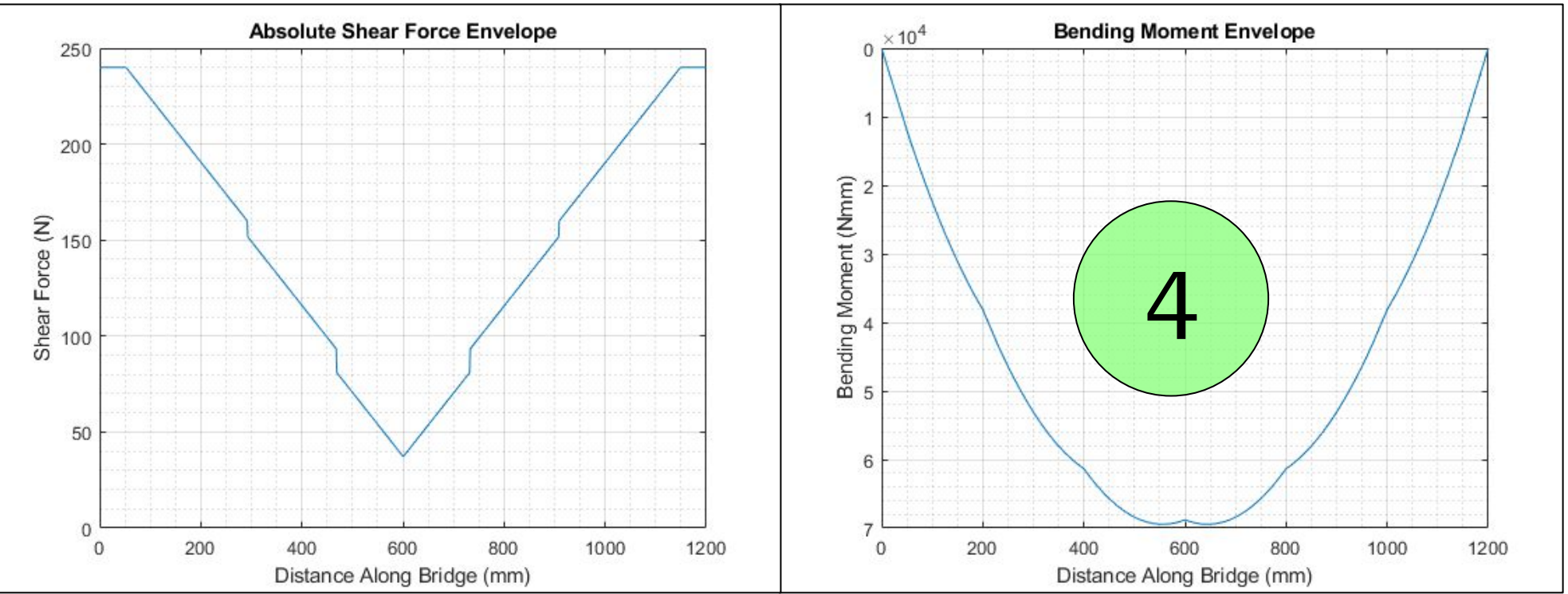
All hand calculations were ported over to a MATLAB script with modifiable parameters that are based on the draft of the bridge in the sketch.

The MATLAB script is able to output FOS values for all possible ways that the bridge could fail (assuming ideal conditions).

The script was crucial for us to play around with parameters and try to maximize the minimum FOS value.

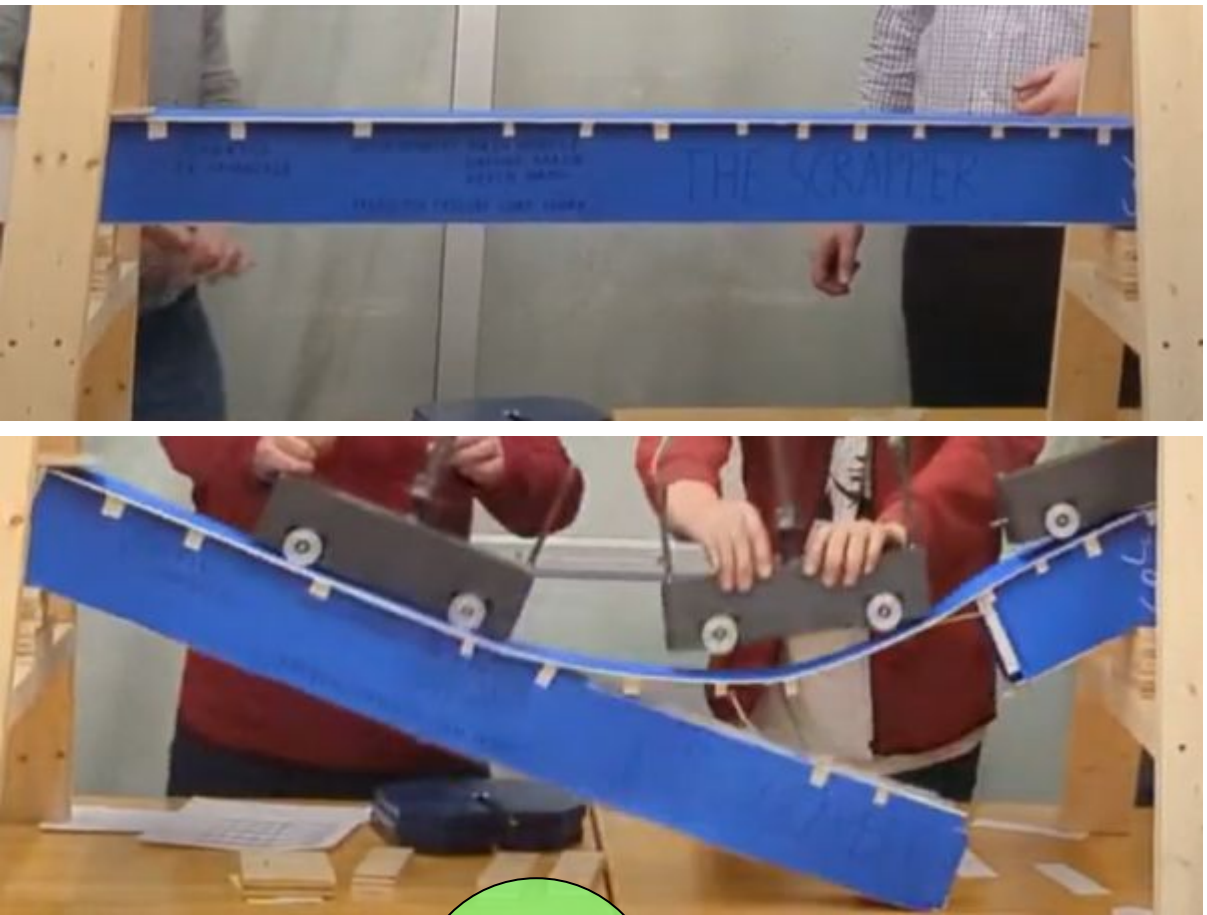
I used Git to track versions of our MATLAB code and made it open source.

```
333 lines (282 slots) 8.98 KB
1 %% Material Properties
2
3 close all;
4 clear;
5
6 %% Matboard dimensions (from in to mm)
7 matboard_w = 32 * 25.4;
8 matboard_h = 40 * 25.4;
9 matboard_t = 0.05 * 25.4;
10 SA_matboard = matboard_w * matboard_h;
11
12 %% Matboard properties
13 sigma_tens = 30;
14 sigma_comp = 6;
15 shear_strength = 4;
16 youngs_modulus = 4000;
17 poissons_ratio = 0.2;
18
19 %% Glue properties
20 shear_strength_glue = 2;
21 %% Moment and Shear Envelopes
22
23 L = 1200; % Length of bridge
24 n = 141; % Number of points
25 P = 400; % Total weight of train [N]
26 n_train = 1:900:1; % Number of train locations
27
28 lbs_dist = linspace(0, L, n);
29
30 % Offset by 1 because MATLAB indexes with 1
31 % Offset by 1 more to shift column one left
32 x_shear_start_locations = [52, 228, 392, 568, 732, 908] + 2;
33 x_train_loads = [-P/6, -P/6, -P/6, -P/6, -P/6, -P/6];
34 start_shear_all = (720 - (0:1:n_train-1))/3; % Column vector of all possible starting shears
35 all_train_locations = zeros(n_train, n);
```



Graphs generated with MATLAB code for the maximum values of shear force and bending moment for any given train location. These graphs are useful when comparing against FOSs because we are only concerned about the maximum possible shear force and bending at any moment.

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Unfortunately, our bridge did not pass the initial loading. As an engineer, it is always important to consider why something happens and learn from them. After (painfully) rewatching the fail a couple of times, I made several predictions:

- The way we cut and folded the matboard made the bridge fail by peeling, as seen in the thin slices of matboard
- The matboard bridge failed by shear in the splice connection. In the moment after failing, the bridge was completely straight, meaning it did not buckle.
- Despite theory, the glue joint was far too thin to have it covered entirely with glue so the actual FOS was lower.
- Our glue tab at the splice covered far too little surface area to account for vertical shear stresses