

(a) Raising x to the power of n

1.  $5^3$ 
  - a.  $5 * 5 * 5 = 625$
2.  $6^{10}$ 
  - a.  $6 * 6 * 6 * 6 * 6 * 6 * 6 * 6 * 6 * 6 = 60466176$
3.  $2^5$ 
  - a.  $2 * 2 * 2 * 2 * 2 = 32$

(b) Polynomial Evaluation Using Horner's Rule

1.  $3x^4 - x^3 + 2x^2 - 5x + 1$  for  $x = 5$ 
  - a.  $((((3*5 - 1)*5 + 2)*5 - 5) * 5 + 1$
  - b.  $((((15 - 1)5 + 2) 5 - 5) * 5 + 1$
  - c.  $((14 * 5 + 2)5 - 5) * 5 + 1$
  - d.  $(72 * 5 - 5) * 5 + 1$
  - e.  $355 * 5 + 1$
  - f. 1776
2.  $2x^3 - x + 8$  for  $x = 3$ 
  - a.  $((2 * 3 + 0) * 3 - 1) * 3 + 8$
  - b.  $(6 * 3 - 1) * 3 + 8$
  - c.  $17 * 3 + 8$
  - d. 59
3.  $x^5 + 3x^3 - 6x^2 - 2x$  for  $x = 2$ 
  - a.  $((((2 + 0) * 2 + 3) * 2 - 6) * 2 - 2) * 2 + 0$
  - b.  $((((2 * 2 + 3) * 2 - 6) * 2 - 2) * 2$
  - c.  $((7 * 2 - 6) * 2 - 2) * 2$
  - d.  $(8 * 2 - 2) * 2$
  - e.  $14 * 2$
  - f. 28

(c) Euclid's algorithm

1. Find the greatest common denominator of 265, 175
  - a. GCD(265, 175)
    - i.  $265/175 = 1 \text{ R } 90$ ,  $\text{GCD}(175, 90) = \text{GCD}(265, 175)$
  - b. GCD(175, 90)
    - i.  $175/90 = 1 \text{ R } 85$   $\text{GCD}(175, 90) = \text{GCD}(90, 85)$
  - c. GCD(90, 80)
    - i.  $90/85 = 1 \text{ R } 5$   $\text{GCD}(90, 85) = \text{GCD}(80, 5)$
  - d. GCD(80, 5)
    - i.  $80/5 = 16 \text{ R } 0$
    - ii. **5** is the greatest common denominator
2. Find the greatest common denominator of 430, 113
  - a. GCD(430, 113)
    - i.  $430/113 = 3 \text{ R } 91$ ,  $\text{GCD}(430, 113) = \text{GCD}(113, 91)$
  - b. GCD(113, 91)

- i.  $113/91 = 1 \text{ R } 22$ ,  $\text{GCD}(113, 91) = \text{GCD}(91, 22)$
  - c.  $\text{GCD}(91, 22)$ 
    - i.  $91/22 = 4 \text{ R } 3$ ,  $\text{GCD}(91, 22) = \text{GCD}(22, 3)$
  - d.  $\text{GCD}(22, 3)$ 
    - i.  $22/3 = 7 \text{ R } 1$ ,  $\text{GCD}(22, 3) = \text{GCD}(3, 1)$
  - e.  $\text{GCD}(3, 1)$ 
    - i.  $3/1 = 3 \text{ R } 0$
    - ii. **1** is the greatest common denominator
- 3. Find the greatest common denominator of 510 , 255
  - a.  $\text{GCD}(510, 255)$ 
    - i.  $510/255 = 2 \text{ R } 0$
    - ii. **255** is the greatest common denominator

(d) Least Common Multiple

1. Solution: The Least Common Multiple (LCM) can be solved by  $(x * y)/\text{GCD}(x,y)$
2. Sample Problems
  - a.  $\text{LCM}(223, 32)$ 
    - i.  $223 * 32/\text{GCD}(223,32)$
    - ii.  $7136/\text{GCD}(223,32)$ 
      1.  $\text{GCD}(223,32)$ 
        - a.  $223/32 = 7 \text{ R } 31$ ,  $\text{GCD}(223,32) = \text{GCD}(32, 31)$
      2.  $\text{GCD}(32, 31)$ 
        - a.  $32/31 = 1 \text{ R } 1$ ,  $\text{GCD}(32, 31) = \text{GCD}(31, 1)$
      3.  $\text{GCD}(31,1)$ 
        - a.  $31/1 = 31 \text{ R } 0$
        - b.  $\text{GCD}(223, 32) = 1$
    - iii.  $7136/1$
    - iv.  $\text{LCM} = \mathbf{7136}$
  - b.  $\text{LCM}(50, 27)$ 
    - i.  $50 * 27/\text{GCD}(50,27)$
    - ii.  $1350/\text{GCD}(50,27)$ 
      1.  $\text{GCD}(50,27)$ 
        - a.  $50/27 = 1 \text{ R } 23$ ,  $\text{GCD}(50,27) = \text{GCD}(27,23)$
      2.  $\text{GCD}(27, 23)$ 
        - a.  $27/23 = 1 \text{ R } 4$ ,  $\text{GCD}(27,23) = \text{GCD}(23, 4)$
      3.  $\text{GCD}(23,4)$ 
        - a.  $23/4 = 5 \text{ R } 3$ ,  $\text{GCD}(23, 4) = \text{GCD}(4,3)$
      4.  $\text{GCD}(4,3)$ 
        - a.  $4/3 = 1 \text{ R } 1$ ,  $\text{GCD}(4,3) = \text{GCD}(3,1)$
      5.  $\text{GCD}(3,1)$ 
        - a.  $3/1 = 3 \text{ R } 0$
        - b.  $\text{GCD}(50,27) = 1$
    - iii.  $1350/1$
    - iv.  $\text{LCM}(50,27) = 1350$

- c.  $\text{LCM}(200, 15)$
- i.  $200 * 15 / \text{GCD}(200, 15)$
  - ii.  $3000 / \text{GCD}(200, 15)$ 
    - 1.  $\text{GCD}(200, 15)$ 
      - a.  $200/15 = 13 \text{ R } 5$ ,  $\text{GCD}(200, 15) = \text{GCD}(15, 5)$
    - 2.  $\text{GCD}(15, 5)$ 
      - a.  $15/5 = 3 \text{ R } 0$
      - b.  $\text{GCD}(200, 15) = 5$
  - iii.  $3000/5$
  - iv.  $\text{LCM}(200, 15) = 600$