## Department of Industrial Engineering & Operations Research

## IEOR 162 Linear Programming & Network Flows (Spring 2022)

## Shortest paths application: Equipment replacement

A single machine is needed to perform a specified function for the next four years, after which the function and machine will no longer be needed. The purchase price of a machine varies over the next four years according to the following table.

|                |          | One Year | Two Years | Three Years |
|----------------|----------|----------|-----------|-------------|
| Year           | Now      | From now | From now  | From now    |
| Purchase price | \$25,000 | \$33,000 | \$38,000  | \$47,000    |

The salvage value of a machine depends only on its length of service and is given by the following table.

| Length of Service | One Year | Two Years | Three Years | Four Years |
|-------------------|----------|-----------|-------------|------------|
| Salvage Value     | \$17,000 | \$6,000   | \$3,000     | \$1,000    |

The annual operating cost varies with length of service, as follows.

| Length of Service     | New     | One Year | Two Years | Three Years |
|-----------------------|---------|----------|-----------|-------------|
| Annual operating cost | \$3,000 | \$5,000  | \$8,000   | \$18,000    |

Construct a network in which the shortest path will yield an optimal policy of purchasing, operating, and salvaging machines over the next four years if management wishes to minimize the total cost.

| Iteration | Node 1 | Node 2   | Node 3   | Node 4   | Node 5   |
|-----------|--------|----------|----------|----------|----------|
| 1         | 0      | $\infty$ | $\infty$ | $\infty$ | $\infty$ |
| 2         |        |          |          |          |          |
| 3         |        |          |          |          |          |
| 4         |        |          |          |          |          |
| 5         |        |          |          |          |          |