

# **Trajectory Pattern Mining in Social Media**

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# Outline

- **Introduction**
- **Research work**
  - Exploring Pattern-Aware Travel Routes for Trajectory Search
  - Constructing Popular Routes from Uncertain Trajectories
- **Conclusion**
- **Future work**

# Introduction (1/2)

- **Social media is everywhere**
  - E.g., GPS logs, geo-tagged photos, check-ins etc.
    - Spatial information
    - Temporal information



# Introduction (2/2)

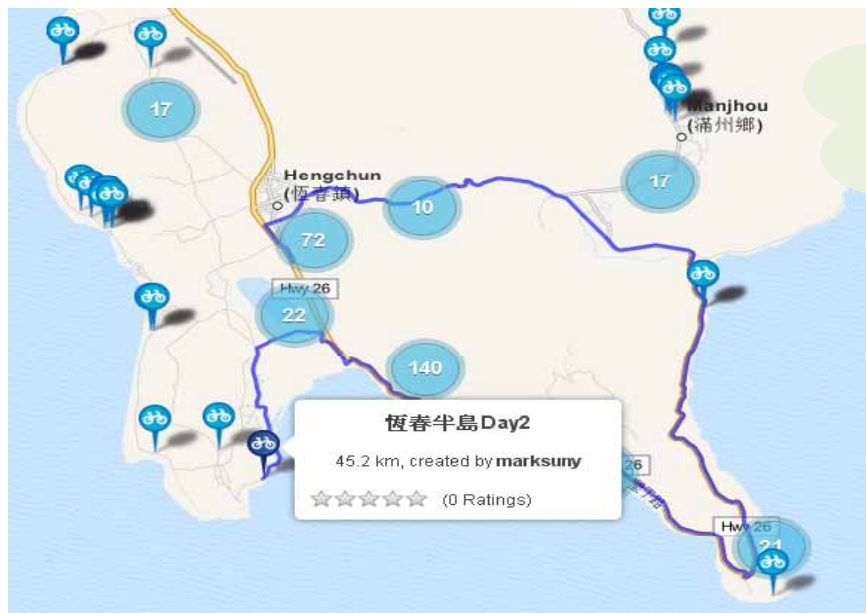
- **Trajectory**
  - A sequence of geo-locations



# **Work 1: Exploring Pattern-Aware Travel Routes for Trajectory Search**

# Introduction (1/3)

- **Existing GPS-related web services**
  - Query: a spatial range (e.g., Kenting)
  - Output: a set of trajectories



Which trajectories  
are interesting?



# Introduction (2/3)

- **Existing GPS-related web services**
  - Query: a spatial range (e.g., Kenting)
  - Output: a ranked list of trajectories

Manual  
Voting

Different user  
preferences?



**Trips** | Sort by: [All-time Popularity](#) | [Recent Popularity](#) | [Trip Date](#) | [Creation Date](#)

**All trips**

**20120204 Day5 墾丁\_滿州**  
by **alvinchao** on Feb 04, 2012  
★★★★★  
**Kending, Pingtung, Taiwan**  
Road biking | 24.4 miles

16min, Distance: 39.8 km, (自行車騎行時間)Moving Time: 3hr  
19 km/h, Avg Speed: 12.15 km/hTotal Ascent: 178270 m, Total  
Calories: 1,397 Weather : Sunny 5 days totalTime: 32hr 35min, (自  
Time: 21hrRest Time: 11hr 03min

**20101203-墾丁單車行day-3**  
by **undies** on Dec 04, 2010  
**Kending, Taiwan, Taiwan**  
Road biking | 24.1 miles

# Introduction (3/3)

- **User preferences**
  - In-breadth trip
    - Visit as many regions-of-interest (ROIs) as possible
  - In-depth trip
    - Stop a few ROIs for an in-depth visit





# Problem Definition

- **Data**

- Travel trajectory dataset

- E.g.,

tid	index	time	lon	lat
1	1	1269130206	120.910332	23.865391
1	2	1269130210	120.910332	23.865391
⋮				

- **Query**

- A spatial range
- A user-preference of depth/breadth

- **Output**

- Top K trajectories from historical data
  - Passed the query range



# Related Work

- **Trajectory search**

- Search by a trajectory [Chen et al. SIGMOD'05, Trajcevski et al. ACM GIS'07]
- Search by locations [Chen et al. SIGMOD'10]

- **Trip planning**

- Fastest/Popular routes from a source to a destination  
[Yuan et al. IEEE TKDE'12, Chen et al. ICDE'11]
- Visiting sequences of regions-of-interest (ROIs)  
[Zheng et al. WWW'09, Kurashima et al. CIKM'10, Arase et al. ACM MM'10, Yin et al. SDM'11]

# Issues (1/2)

- **How to formulate a trajectory score?**
- **Observation**
  - Trip planning
    - A travel route passes through some regions-of-interest (ROIs)



## Issues (2/2)

- **How to efficiently search top K trajectories from historical trajectories?**
- **Idea**
  - Only compute the scores of candidate trajectories
  - Iteratively reduce the searching space

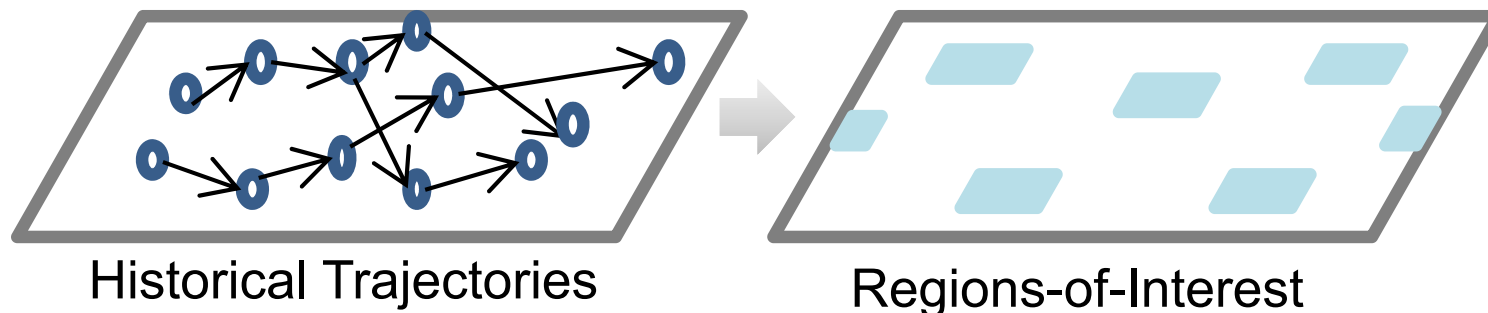
# Framework

- **Travel behavior exploration (off-line)**
  - Regions-of-interest (ROIs) discovery
  - ROIs scoring
    - User movement graph
- **Trajectory search (on-line)**
  - Trajectory score functions
    - Breadth-trip score
    - Depth-trip score
  - Bounded trajectory search algorithm

# Travel Behavior Exploration (1/4)

## Phase 1: ROIs discovery 從路徑建立ROI

- **Divide a 2D space into non-overlapping cells**
  - Uncertainty of GPS logs
    - Discover ROIs instead of points-of-interest (POIs)
- **Determine a set of ROIs**
  - A cell is a ROI if  
the number of distinct trajectories that **passed** the cell is  
greater than a user-specified threshold



# Travel Behavior Exploration (2/4)

## Phase 2: ROIs scoring

將路徑轉為ROI順序

- **Transform trajectories**

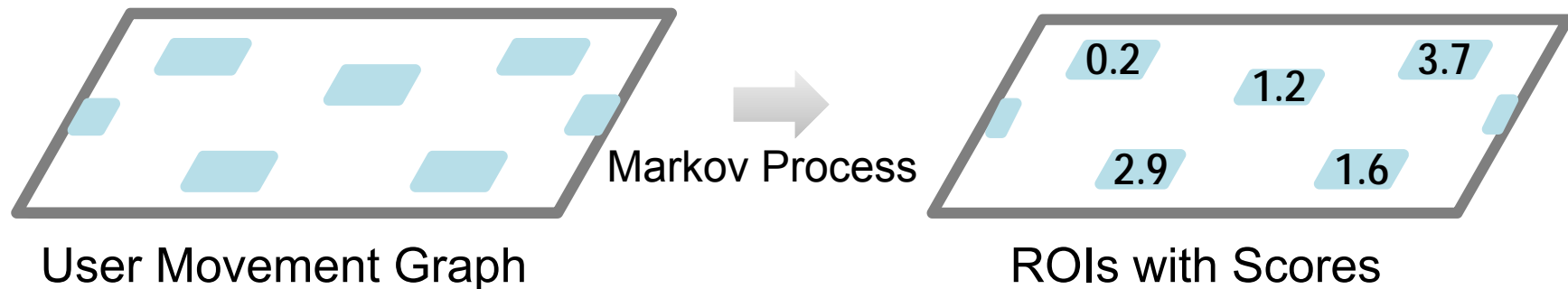
- Transform each trajectory into a sequence of ROIs

- E.g.,

Tid	Sequence of ROIs (Travel Route)
$Tr_1$	$R_1 \dashrightarrow R_4 \dashrightarrow R_7$
$Tr_2$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7 \dashrightarrow R_4 \dashrightarrow R_5 \dashrightarrow R_6$

- **Construct a user movement graph**

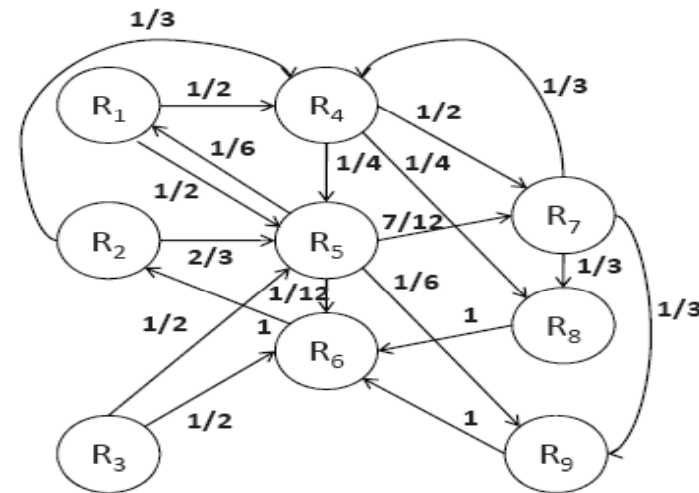
- Travel sequential relationships



# Travel Behavior Exploration (3/4)

- User movement graph**

Tid	Sequence of ROIs (Travel Route)
$Tr_1$	$R_1 \dashrightarrow R_4 \dashrightarrow R_7$
$Tr_2$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7 \dashrightarrow R_4 \dashrightarrow R_5 \dashrightarrow R_6$
$Tr_3$	$R_1 \dashrightarrow R_5 \dashrightarrow R_7$
$Tr_4$	$R_2 \dashrightarrow R_4 \dashrightarrow R_8$
$Tr_5$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7$
$Tr_6$	$R_5 \dashrightarrow R_7 \dashrightarrow R_8 \dashrightarrow R_6$
$Tr_7$	$R_3 \dashrightarrow R_5 \dashrightarrow R_1$
$Tr_8$	$R_3 \dashrightarrow R_6 \dashrightarrow R_2$
$Tr_9$	$R_5 \dashrightarrow R_9 \dashrightarrow R_6$
$Tr_{10}$	$R_4 \dashrightarrow R_7 \dashrightarrow R_9$



- Weight on edge  $\langle R_i, R_j \rangle$  is

$$w_{\langle R_i, R_j \rangle} = \frac{\sum_{Tr_h \in TRD, \langle R_i, R_j \rangle \subset Tr_h} \frac{1}{deg^+(R_i | Tr_h)}}{\left| \bigcup_{R_l \in \mathcal{R}, R_i \neq R_l} \{Tr_k | Tr_k \in TRD, \langle R_i, R_l \rangle \subset Tr_k\} \right|}$$

where  $deg^+(R_i | Tr) = |\{R_j | \langle R_i, R_j \rangle \subset Tr, R_i \neq R_j\}|$





# Travel Behavior Exploration (4/4)

- **Attractive scores of ROIs**

- Iteratively compute it until scores converge

- $$\begin{pmatrix} S^i(R_1) \\ S^i(R_2) \\ \vdots \\ S^i(R_m) \end{pmatrix} = M \cdot \begin{pmatrix} 1 \\ S^{i-1}(R_1) \\ \vdots \\ S^{i-1}(R_m) \end{pmatrix}$$
 Si(R1) = (1-a)\*1 + a\*w<R1,R1>\*Si-1(R1) + a\*w<R2,R1>\*Si-1(R2)...

where

- $$M = \begin{pmatrix} 1 - \alpha & \alpha \cdot w_{<R_1, R_1>} & \cdots & \alpha \cdot w_{<R_m, R_1>} \\ 1 - \alpha & \alpha \cdot w_{<R_1, R_2>} & \cdots & \alpha \cdot w_{<R_m, R_2>} \\ \vdots & & \ddots & \\ 1 - \alpha & \alpha \cdot w_{<R_1, R_m>} & \cdots & \alpha \cdot w_{<R_m, R_m>} \end{pmatrix}$$

- parameter  $\alpha \in [0, 1)$

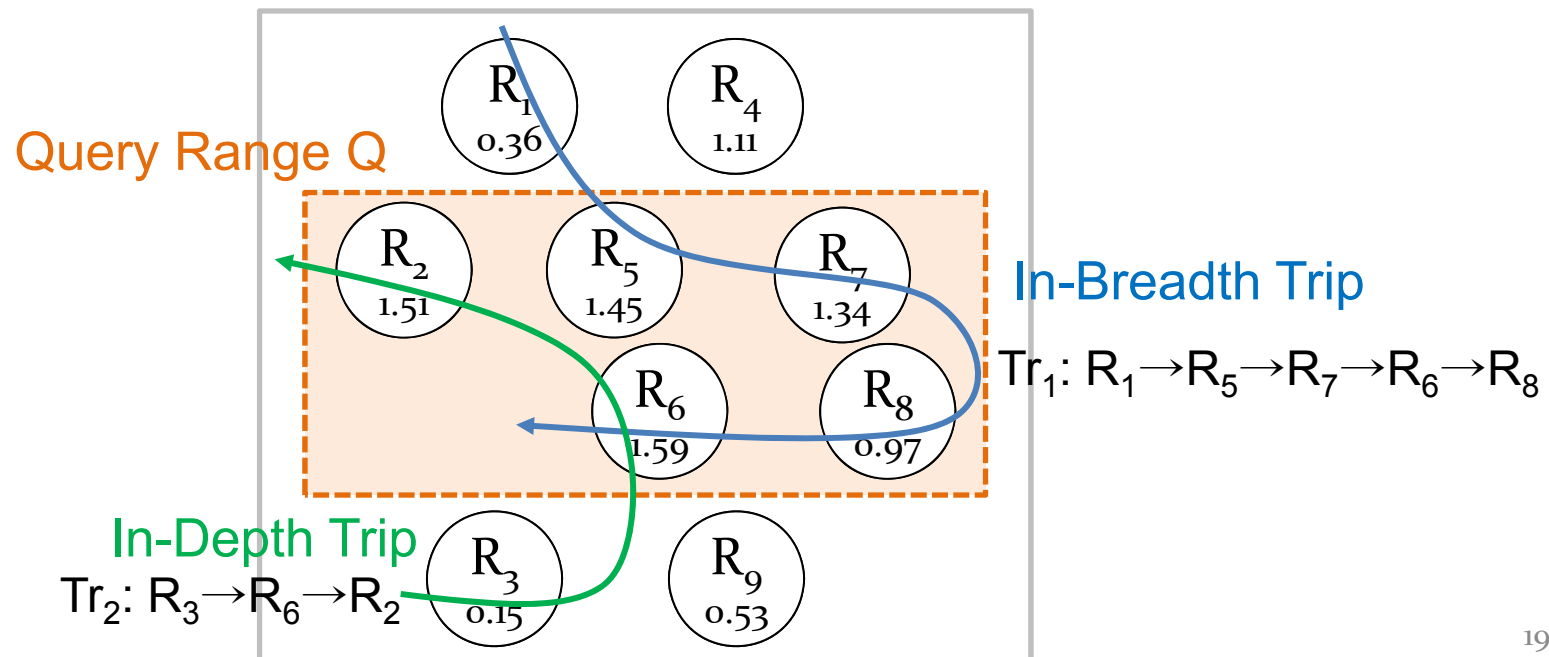
- $w_{<R_i, R_i>} = 0$

# Framework

- **Travel behavior exploration (off-line)**
  - Regions-of-interest (ROIs) discovery
  - ROIs scoring
    - User movement graph
- **Trajectory search (on-line)**
  - Trajectory score functions
    - Breadth-trip score
    - Depth-trip score
  - Bounded trajectory search (BTS) algorithm

# Trajectory Score Function (1/2)

- **In-breadth trip**
  - Visit as **many** ROIs as possible
- **In-depth trip**
  - Stop a **few** ROIs for an in-**depth** visit



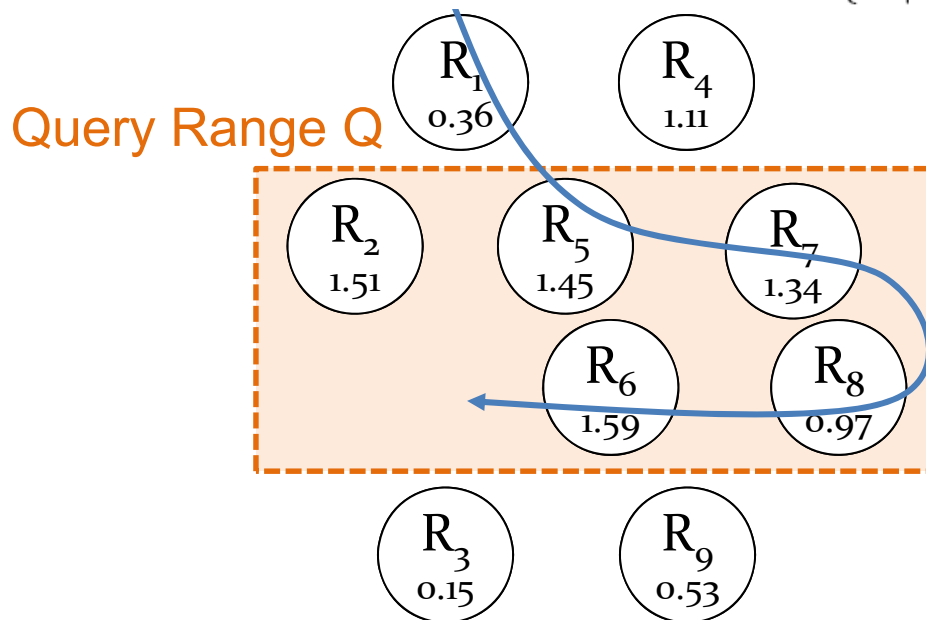
# Trajectory Score Function (2/2)

- **Breadth-trip score**

- $BT(Tr) = \sum_{\{R_i | R_i \in Tr.VS \cap R_Q\}} S(R_i)$

- **Depth-trip score**

- $DT(Tr) = \frac{1}{|\{R_i | R_i \in Tr.VS \cap R_Q\}|} \sum_{\{R_i | R_i \in Tr.VS \cap R_Q\}} S(R_i)$



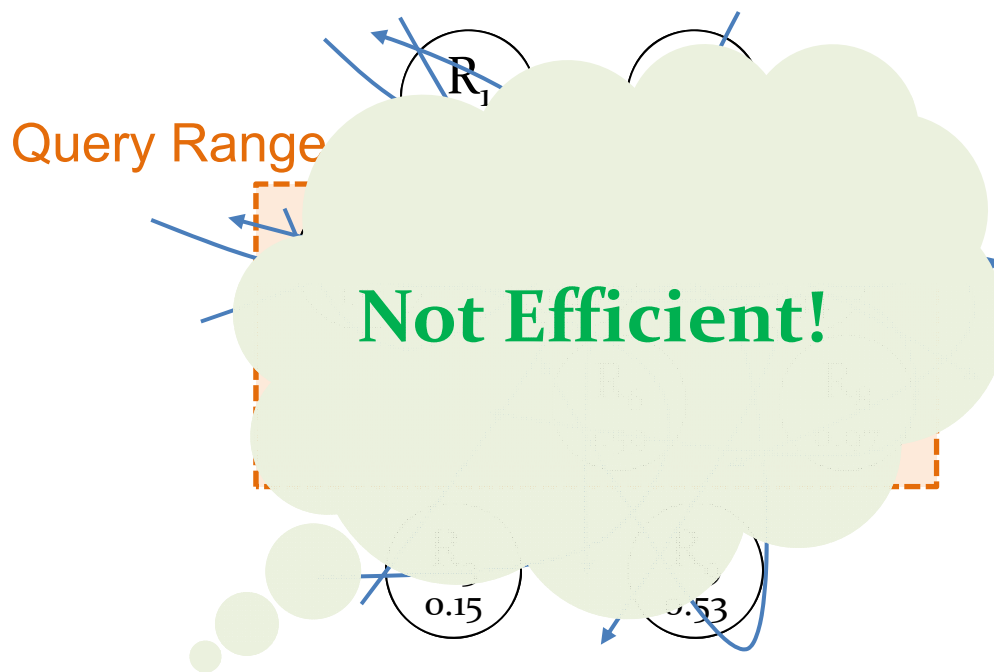
$$Tr_1: R_1 \rightarrow R_5 \rightarrow R_7 \rightarrow R_6 \rightarrow R_8$$

$$BT(Tr_1) = 1.45 + 1.34 + 1.59 + 0.97 = 5.35$$

$$DT(Tr_1) = (1.45 + 1.34 + 1.59 + 0.97) / 4 = 1.338$$

# Trajectory Search (1/2)

- **Naïve method**
  - Calculate the scores of the trajectories passing query range  $Q$  and then rank them



Tid	Sequence of ROIs (Travel Route)
$Tr_1$	$R_1 \dashrightarrow R_4 \dashrightarrow R_7$
$Tr_2$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7 \dashrightarrow R_4 \dashrightarrow R_5 \dashrightarrow R_6$
$Tr_3$	$R_1 \dashrightarrow R_5 \dashrightarrow R_7$
$Tr_4$	$R_2 \dashrightarrow R_4 \dashrightarrow R_8$
$Tr_5$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7$
$Tr_6$	$R_5 \dashrightarrow R_7 \dashrightarrow R_8 \dashrightarrow R_6$
$Tr_7$	$R_3 \dashrightarrow R_5 \dashrightarrow R_1$
$Tr_8$	$R_3 \dashrightarrow R_6 \dashrightarrow R_2$
$Tr_9$	$R_5 \dashrightarrow R_9 \dashrightarrow R_6$
$Tr_{10}$	$R_4 \dashrightarrow R_7 \dashrightarrow R_9$

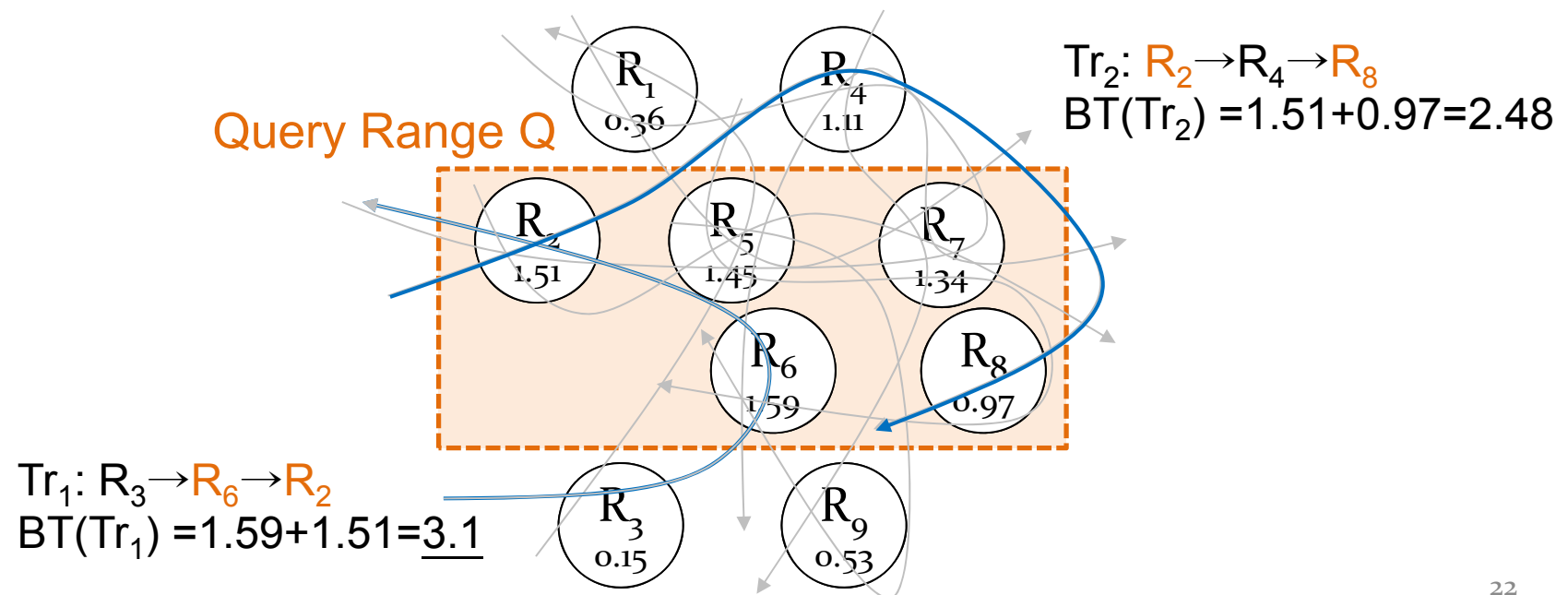
# Trajectory Search (2/2)

- **Idea**

- Only compute the scores of **candidate trajectories**

- **Observation**

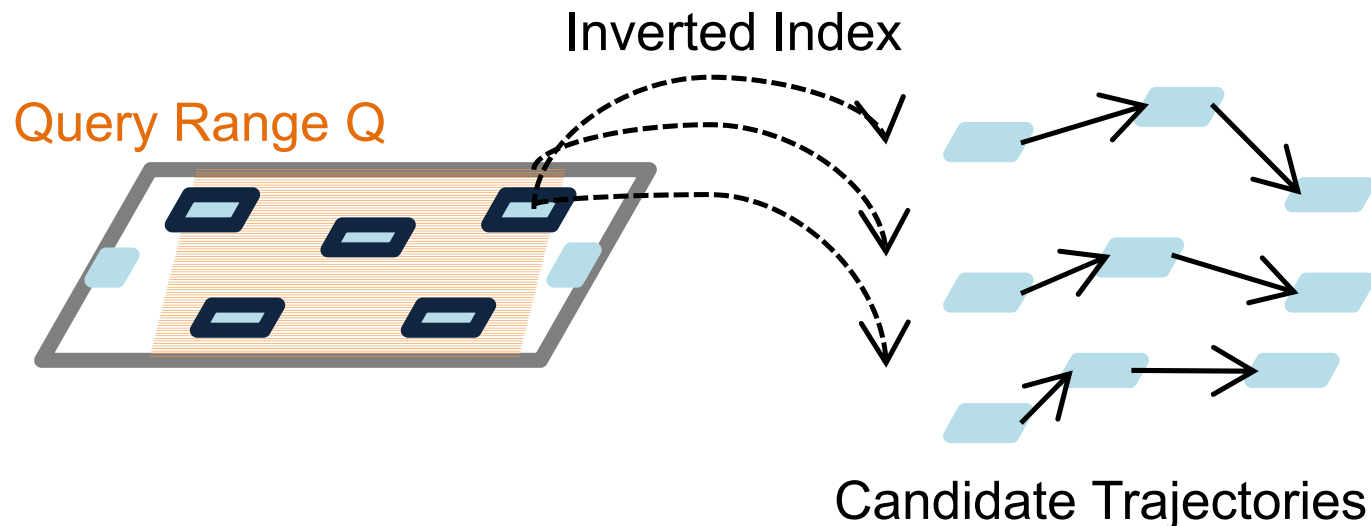
- A trajectory has a higher score if it passed **ROIs** having **higher attractive scores**



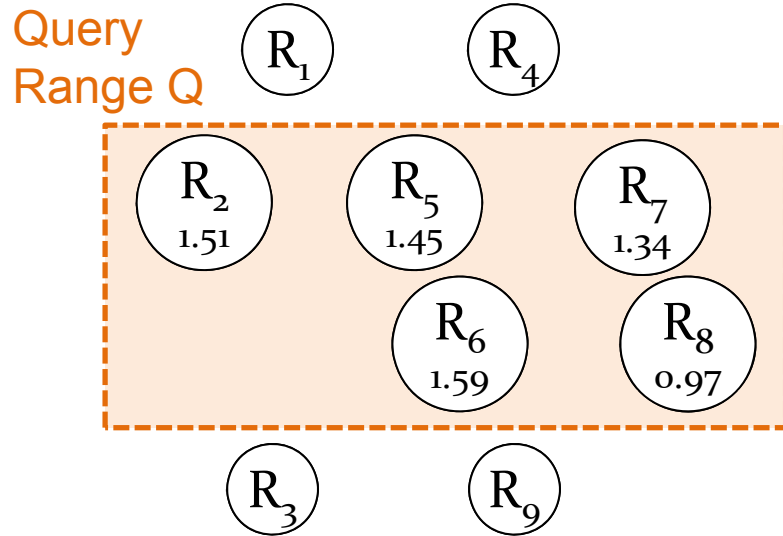
# Bounded Trajectory Search (1/3)

- **Idea**

- Scan ROIs in the query range to select candidate trajectories by ROIs' attractive scores
- Iteratively reduce the searching space by updating the score at rank K in the set of candidate trajectories



# Example: Top 5 Trajectories



Tid	Sequence of ROIs (Travel Route)	DT
$Tr_1$	$R_1 \dashrightarrow R_4 \dashrightarrow R_7$	
$Tr_2$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7 \dashrightarrow R_4 \dashrightarrow R_5 \dashrightarrow R_6$	1.48
$Tr_3$	$R_1 \dashrightarrow R_5 \dashrightarrow R_7$	1.395
$Tr_4$	$R_2 \dashrightarrow R_4 \dashrightarrow R_8$	1.24
$Tr_5$	$R_2 \dashrightarrow R_5 \dashrightarrow R_7$	1.433
$Tr_6$	$R_5 \dashrightarrow R_7 \dashrightarrow R_8 \dashrightarrow R_6$	1.338
$Tr_7$	$R_3 \dashrightarrow R_5 \dashrightarrow R_1$	1.45
$Tr_8$	$R_3 \dashrightarrow R_6 \dashrightarrow R_2$	1.55
$Tr_9$	$R_5 \dashrightarrow R_9 \dashrightarrow R_6$	1.52
$Tr_{10}$	$R_4 \dashrightarrow R_7 \dashrightarrow R_9$	

Scan ROIs in Q by attractive scores:

$S(R_6) = 1.59 \rightarrow \{Tr_2, Tr_6, Tr_8, Tr_9\}$   
 $S(R_2) = 1.51 \rightarrow \{Tr_4, Tr_5\}$   
 $S(R_5) = 1.45 \rightarrow \{Tr_3, Tr_7\}$   
 $S(R_7) = 1.34$   
 $S(R_8) = 0.97$

SBR<sub>T</sub> ↓

Round	$T$ (Candidate trajectories)	$LBS_T$	$SBR_T$
Initial	$\emptyset$	$\infty$	$R_8$

Top 5 trajectories:  $\{Tr_8, Tr_9, Tr_2, Tr_7, Tr_5\}$



# Bounded Trajectory Search (2/3)

- **Lower bound of the scores of candidate trajectories**
  - $LBS_T = DT(Tr)$  or  $BT(Tr)$   
where  $T$  is the candidate trajectories  
and  $DT(Tr)$  or  $BT(Tr)$  is the score at rank  $k$  in  $T$
- **Search bound for examining ROIs w.r.t.  $LBS_T$** 
  - $SBR_T = R_l^s$   
where for trajectory score function DT,  
$$l = \max\{i | S(R_i^s) \geq LBS_T, \forall i \in \mathbb{N}, 1 \leq i \leq |R_Q|\}.$$
  
and for trajectory score function BT,  
$$l = \max\{i | \sum_{i \leq j \leq |R_Q|} S(R_j^s) \geq LBS_T, \forall i \in \mathbb{N}, 1 \leq i \leq |R_Q|\}$$

# Bounded Trajectory Search (3/3)

- **Sort ROIs in decreasing order by attractive scores**
- **Scan ROIs from  $R^s_1$  to  $SBR_T = R^s_j$** 
  - The set of candidate trajectories,  $T$ 
    - Add the trajectories passed  $R^s_i$  into  $T$  and calculate their scores
  - Update  $LBS_T$  in  $T$  if  $|T| > k$
  - Update  $SBR_T$  w.r.t.  $LBS_T$
- **Thm: Correctness of algorithm BTS**
  - Proofs in Chap. 2.5.3.

# Experiments

- **Trajectory data**
  - Travel websites: EveryTrail, Bikemap
  - Taiwan
    - 6,548 trajectories
    - 1,301,192 GPS logs
- **Parameters**
  - Grid length: 300 meters
  - Minimum density threshold: 10
  - Rank-threshold K: 10



- **Query: Kenting**

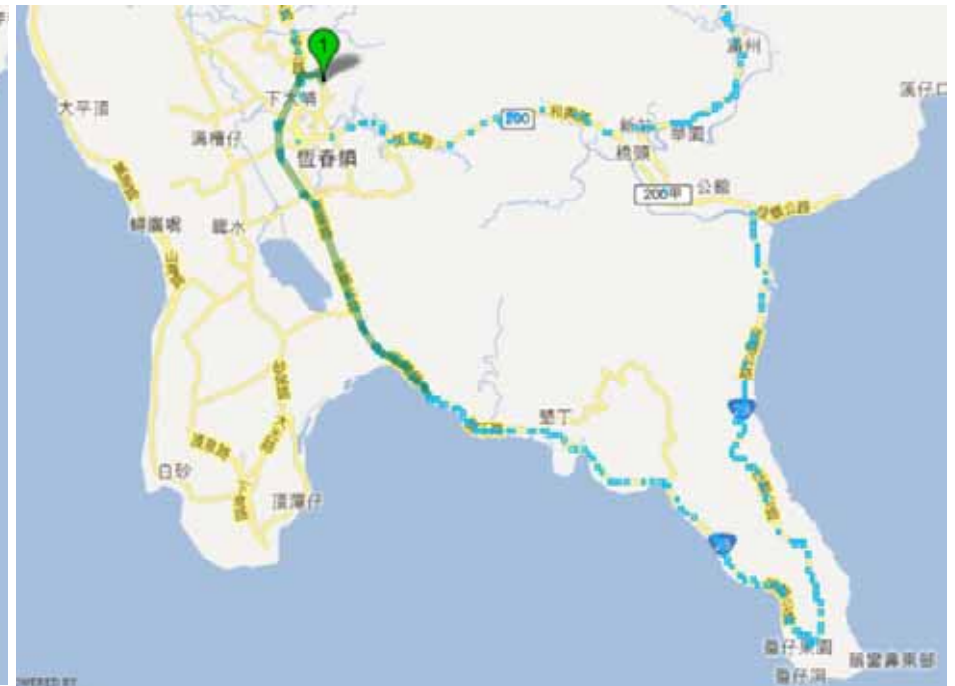


# Top 1 Trajectory in Kenting (2/2)

- In-Breadth Trip

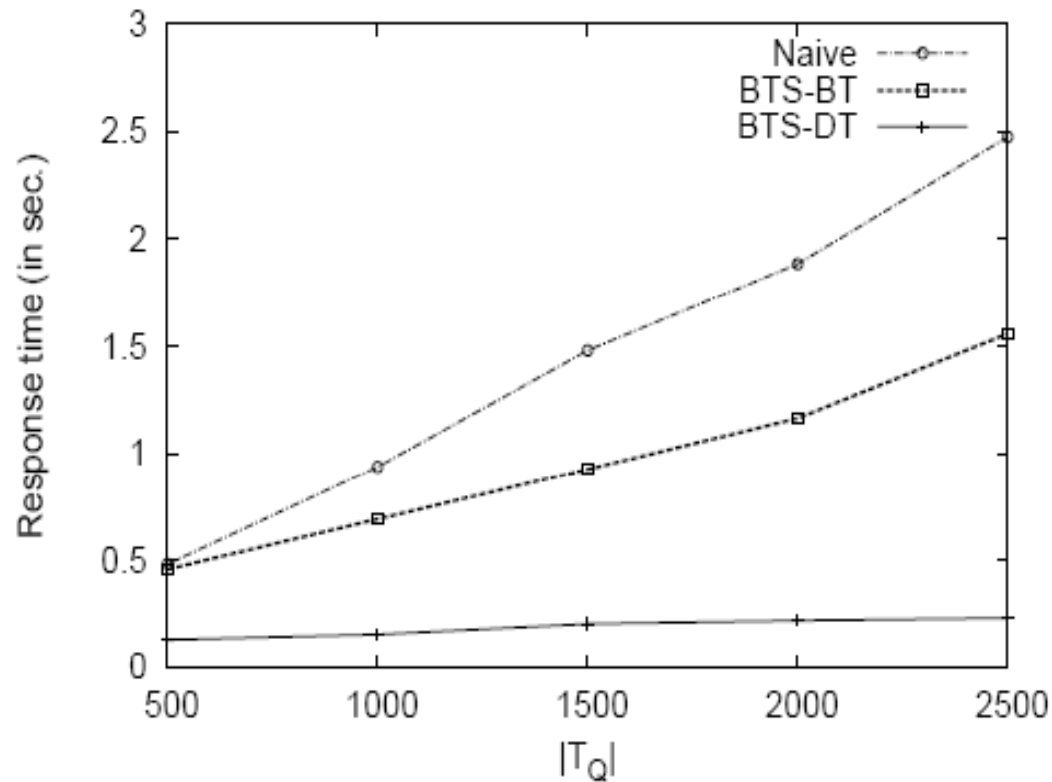


- In-Depth Trip



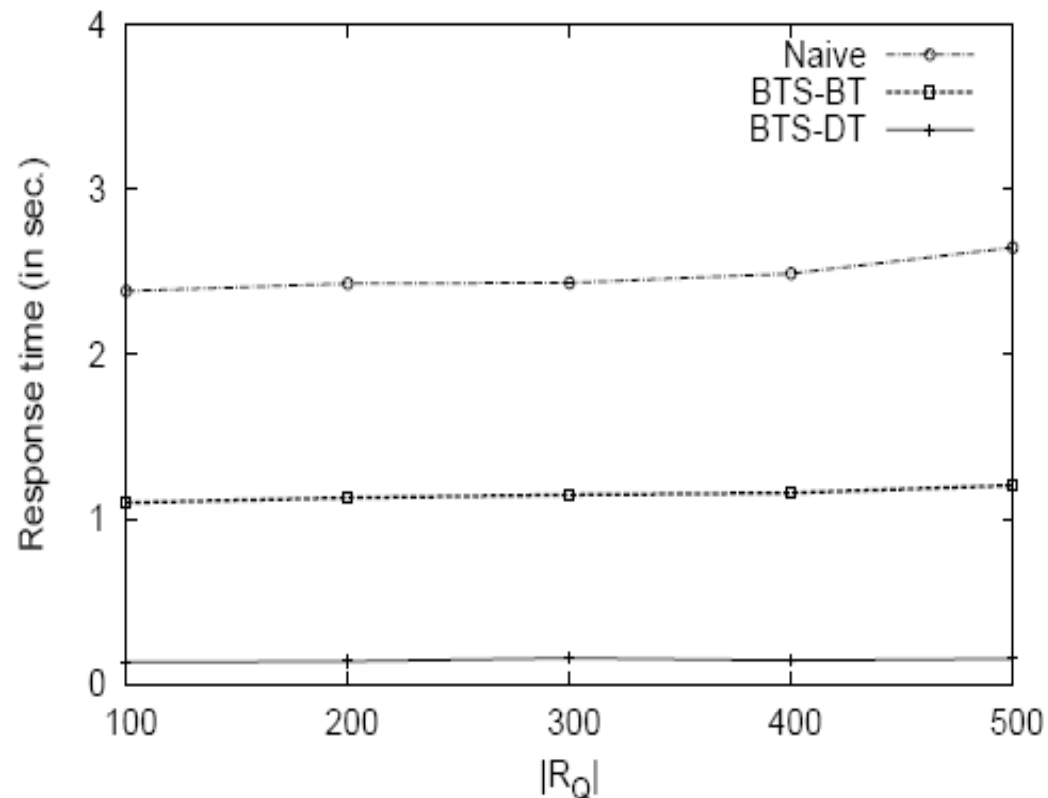
# Performance Evaluation (1/3)

- **Impact of the number of the trajectories crossing query range  $Q$ ,  $|T_Q|$** 
  - The number of ROIs in  $Q$ ,  $|R_Q|=500$



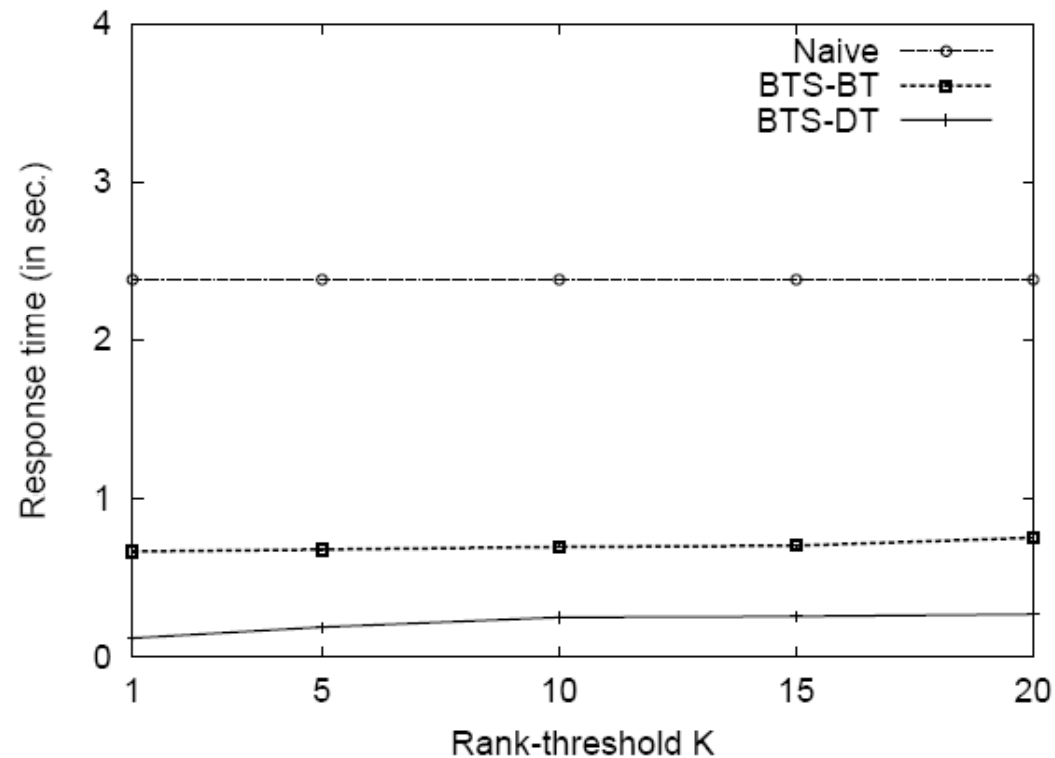
# Performance Evaluation (2/3)

- **Impact of the number of ROIs in query range  $Q$ ,  $|R_Q|$** 
  - $|T_Q|=3,892$



# Performance Evaluation (3/3)

- **Impact of the rank-threshold,  $K$** 
  - $|T_Q|=1,600$
  - $|R_Q|=100$





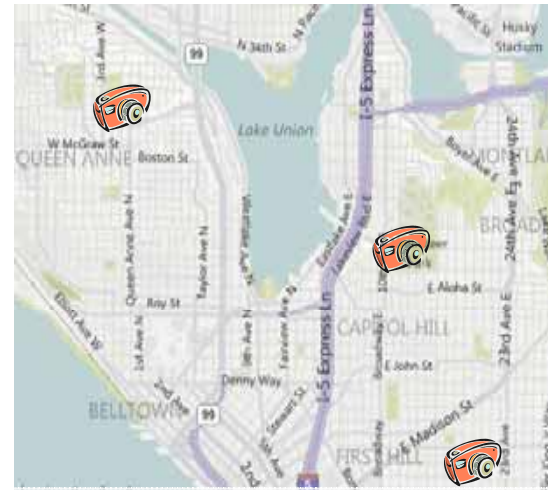
# Summary

- **Presented a novel trajectory search framework for trip planning by considering different user preferences**
- **Employed a user movement graph to capture travel patterns hidden in trajectory datasets and developed an algorithm to score ROIs**
- **Developed an algorithm BTS for efficiently retrieving the top K trajectories**

# **Work 2: Constructing Popular Routes from Uncertain Trajectories**

# Introduction (1/2)

- **Trajectory data**
  - Geo-tagged Flickr photo traces
  - Taxicabs' trajectories
  - Foursquare check-in sequences
- **Uncertainty of trajectories**
  - Energy saving
  - Features of applications



**Uncertain Trajectories**

# Introduction (2/2)

- **Question**

- What are popular routes between two consecutive geo-locations?

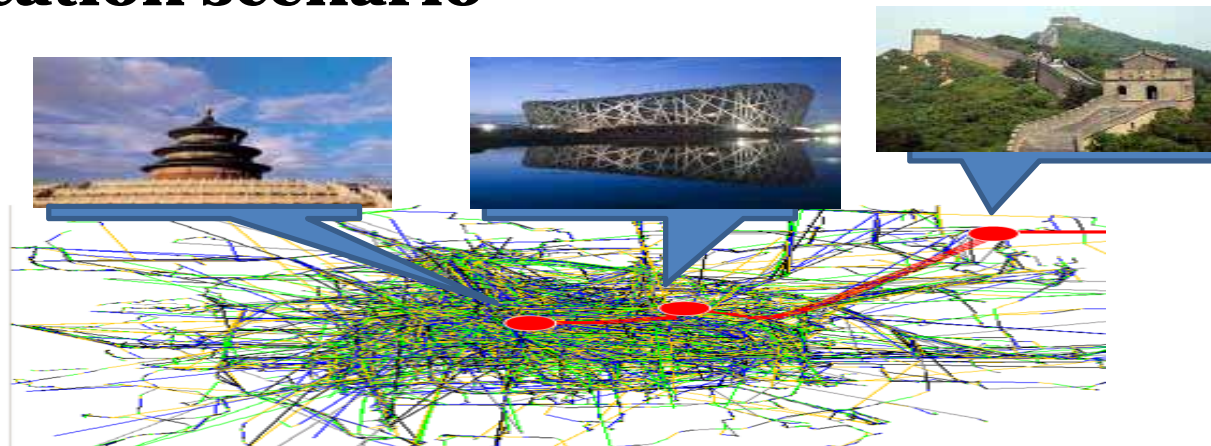


Road Network



2D Free Space

- **Application scenario**



# Problem Definition

- **Data**

- Uncertain trajectory dataset
- ~~Road networks~~

- **Query**

- A geo-location sequence  $q: q_1 \rightarrow \dots \rightarrow q_n$   
and  $q_{i+1}.t - q_i.t \leq \Delta t$  where  $\Delta t$  is a time span

- **Output**

- Top K popular routes
  - Sequentially traverse the geo-locations



# Challenges (1/2)

- **Road network information is not applicable or not available**

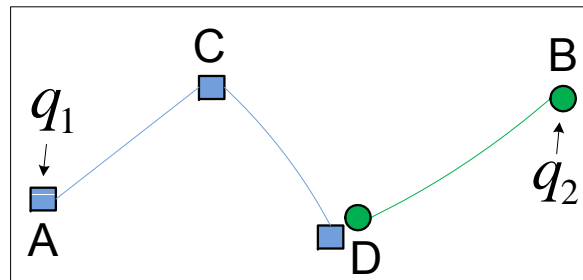


Road Network



2D Free Space

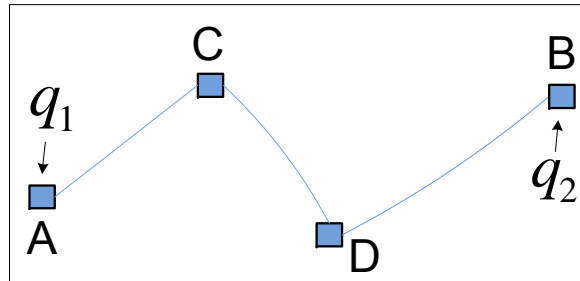
- **No historical trajectory passes through the given geo-location sequence**



■  $tra_1 : A \rightarrow C \rightarrow D$   
●  $tra_2 : D \rightarrow B$

# Challenges (2/2)

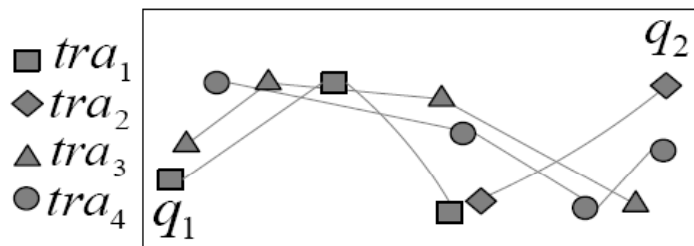
- **Uncertain trajectories passing through the given geo-location sequence are not detailed routes**



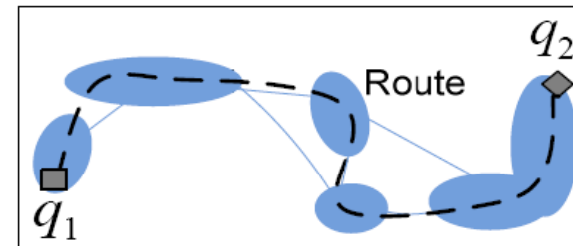
■  $tra_1: A \rightarrow C \rightarrow D \rightarrow B$

- **Which uncertain trajectories have similar movements?**

- Infer popular routes based on collective knowledge



Uncertain trajectories

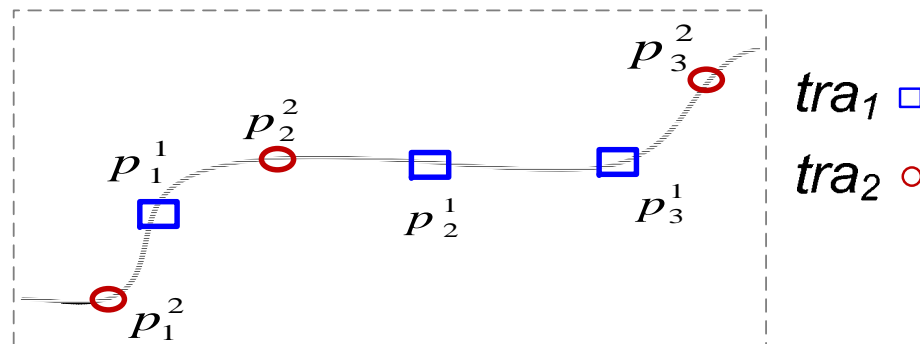


Mutual reinforcement

# Related Work (1/3)

- **Trajectory clustering**

- 2D free space [Lee et al. SIGMOD'07, Pelekis et al. ICDM'09]
  - Data: high-sampled trajectories
  - Issue for uncertain trajectories
    - Different geo-spatial representations of a route



- Road network [Kuijpers et al. SSTD'09]
  - Data: low-sampled trajectories
  - Disadvantage: do no detail routes



# Related Work (2/3)

- **Trip planning**
  - Data: high-sampled/low-sampled trajectories  
[Zheng et al. WWW'09/Kurashima et al. CIKM'10, Arase et al. MM'10, Yin et al. SDM'11]
  - Output: visiting sequences of ROIs
  - Disadvantage: do not detail routes

# Related Work (3/3)

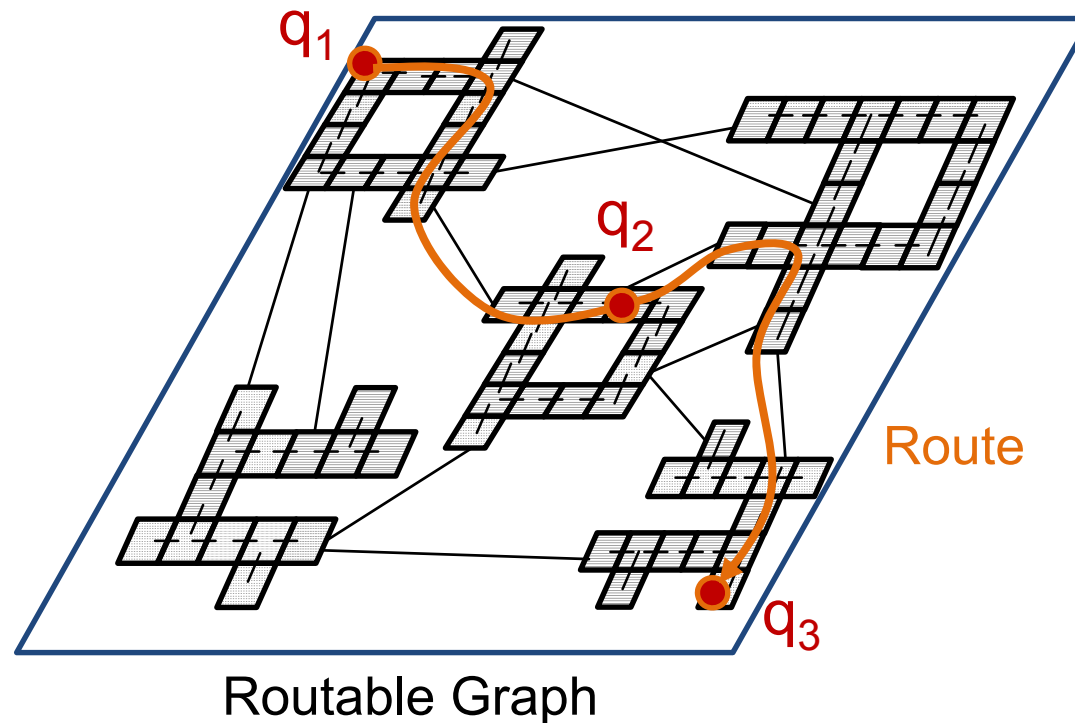
- **Route planning**

- Query: two or more geo-locations
- Output: Top K routes according to the geo-locations

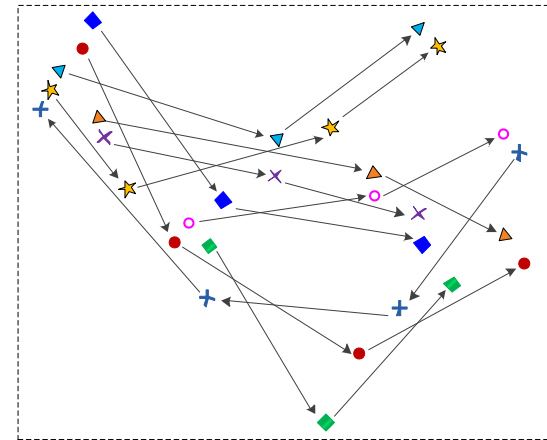
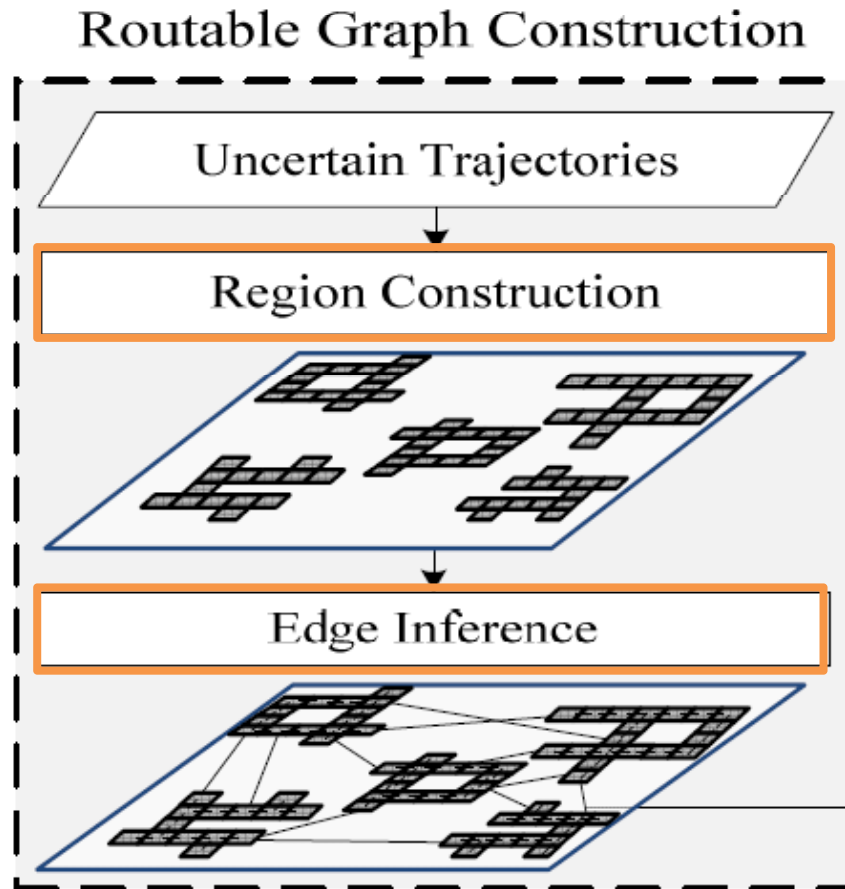
	Trajectory - Sampling Rate	Road Network	Ranking Criteria	Output
Chen et al. SIGMOD'10	High	V	Distance	Historical trajectories
Chen et al. ICDE'11	High		Popularity	Synthetic routes
Yuan et al. TKDE'12	Low	V	Fastest	Synthetic routes
Zheng et al. ICDE'12	Low	V	Popularity	Synthetic routes
Ours	Low		Popularity	Synthetic routes

# Framework

- **Routable graph construction (off-line)**
- **Route inference (on-line)**



# Framework Overview



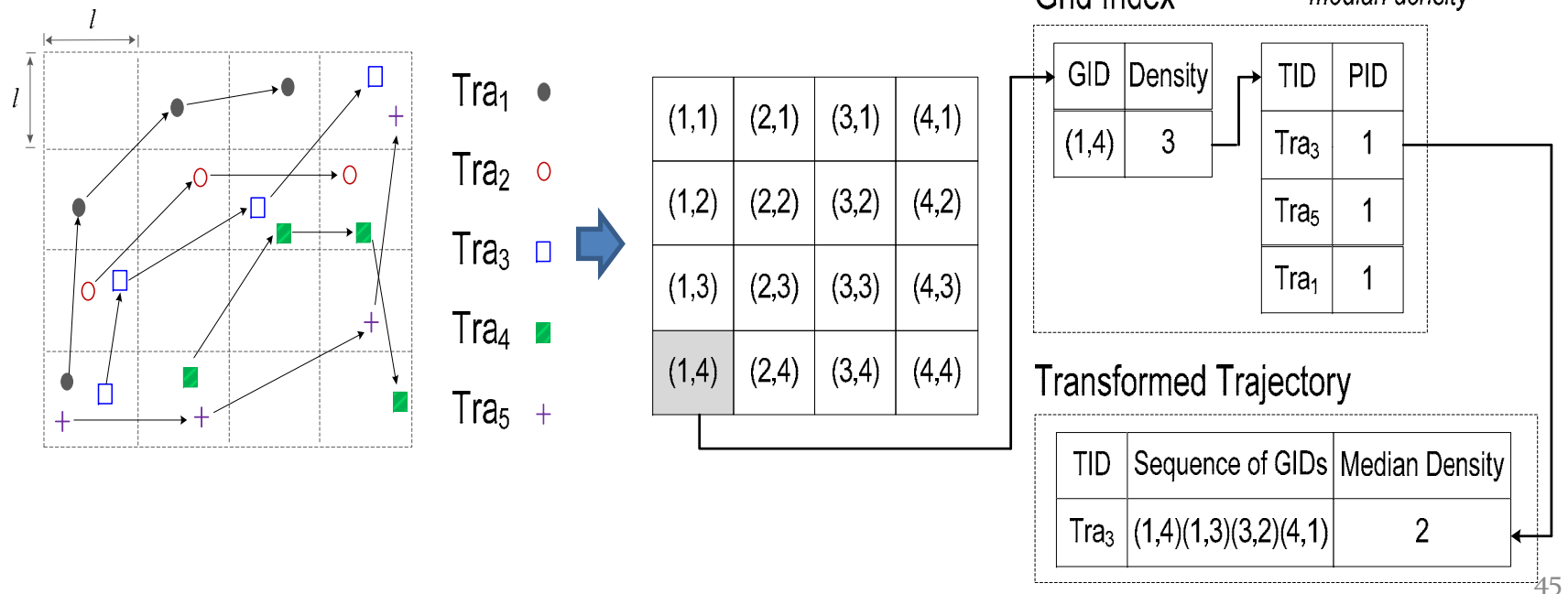
- Region: a connected geographical area
- Edges inside a region
- Edges between regions

# Routable Graph Construction (1/3)

- **Space partition**

- Divide a space into non-overlapping cells with a given cell length

- **Trajectory indexing**



# Routable Graph Construction (2/3)

- **Region**

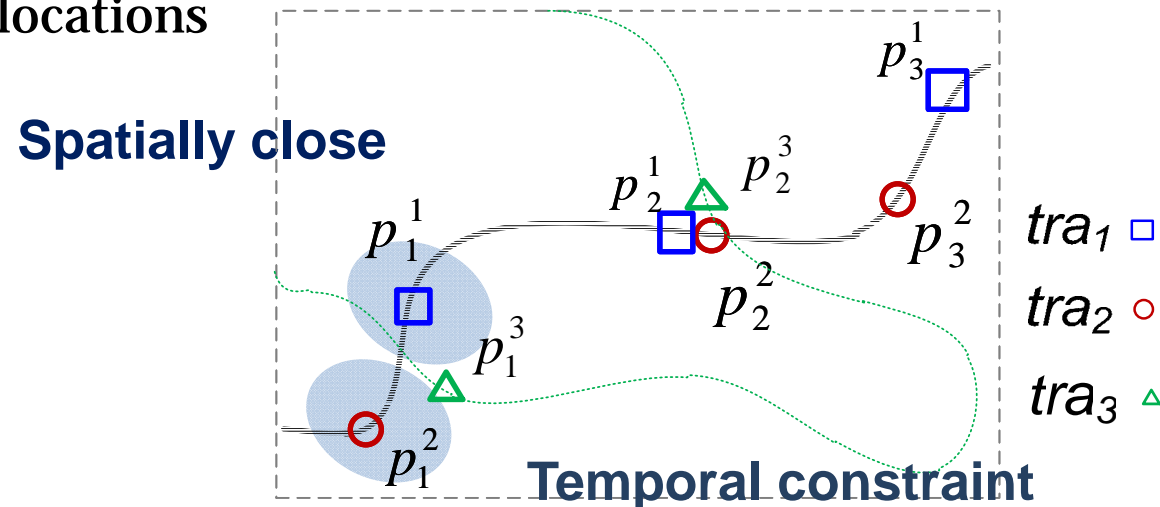
- A connected geographical area

- **Idea**

- Merge connected cells to form a region

- **Observation**

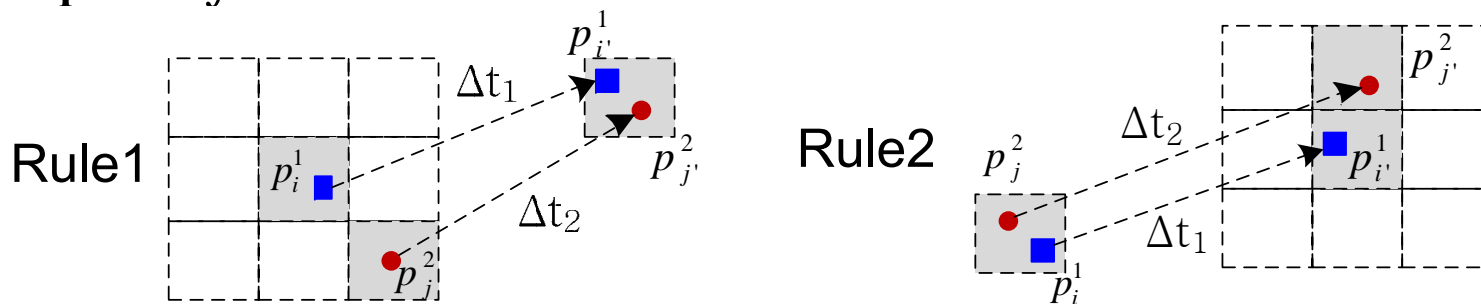
- $Tra_1$  and  $Tra_2$  follow the same route but have different sampled geo-locations



# Routable Graph Construction (3/3)

- **Spatio-temporally correlated relation between trajectories**

- Spatially close



- Temporal constraint  $\theta$

$$\cdot \frac{|\Delta t_1 - \Delta t_2|}{\max\{\Delta t_1, \Delta t_2\}} \leq \theta$$

- **Connection support of a cell pair**

- Minimum connection support  $C$

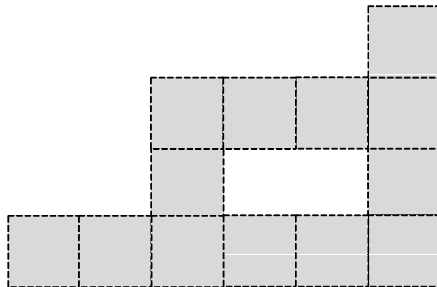
# Edge Inference (1/2)

## [Edges in a region]

Step 1: Let a region be a bidirectional graph first

Step 2: Infer the *direction*, *travel time* and *support* between each two consecutive cells

- Multiple shortest routes between consecutive points and then propagate the weight evenly
- Aggregate the weights
- Estimate the travel time of each edge





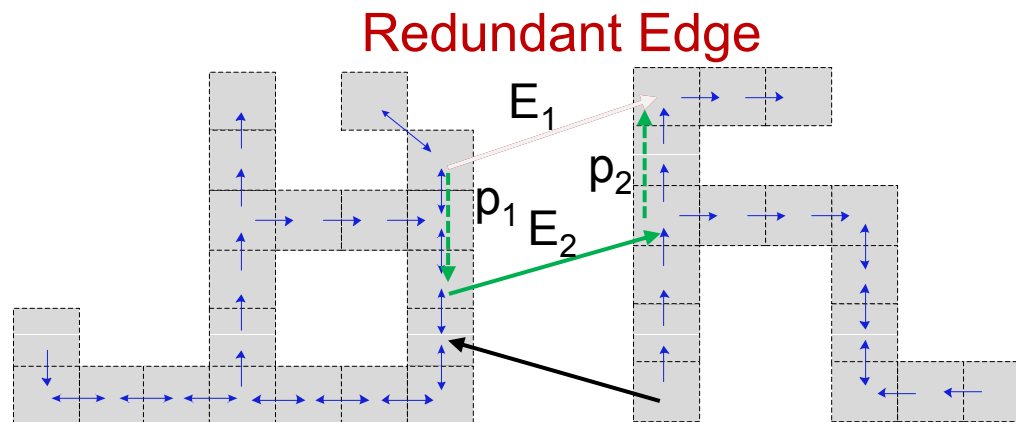
# Edge Inference (2/2)

## [Edges between regions]

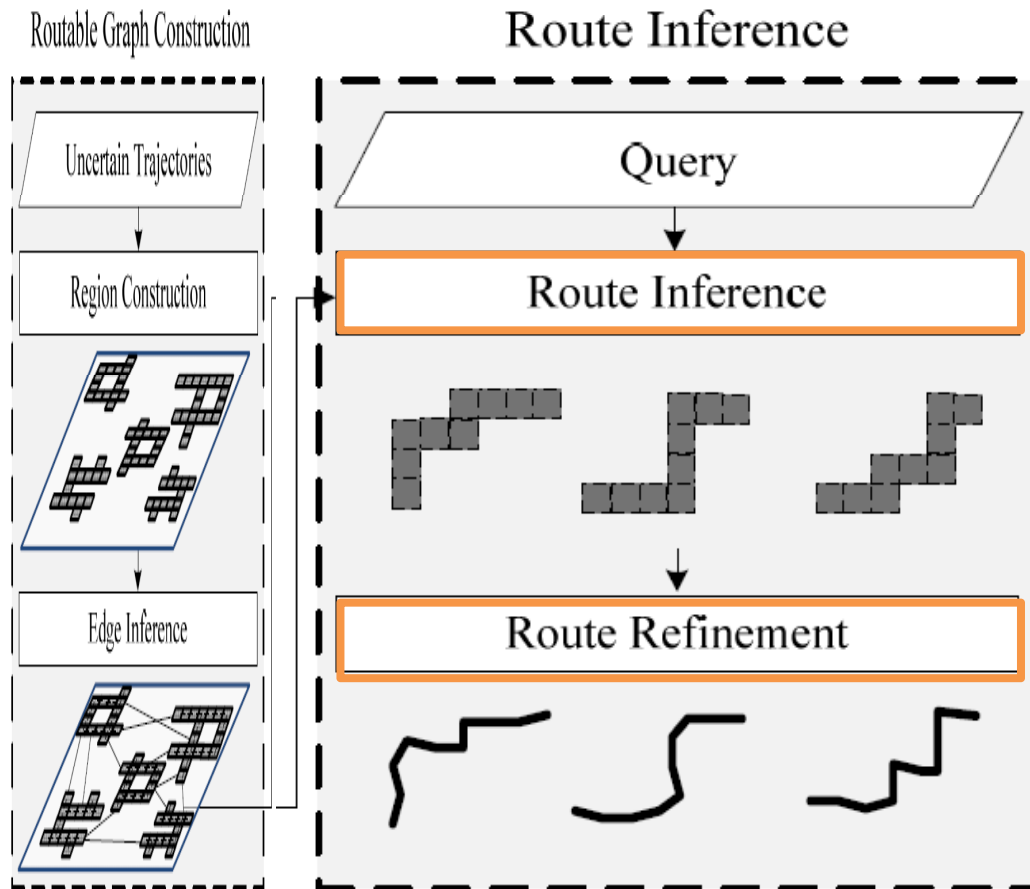
Step 1: Build edges between two cells in different regions by trajectories

Step 2: Replace the redundant edges by constructed edges

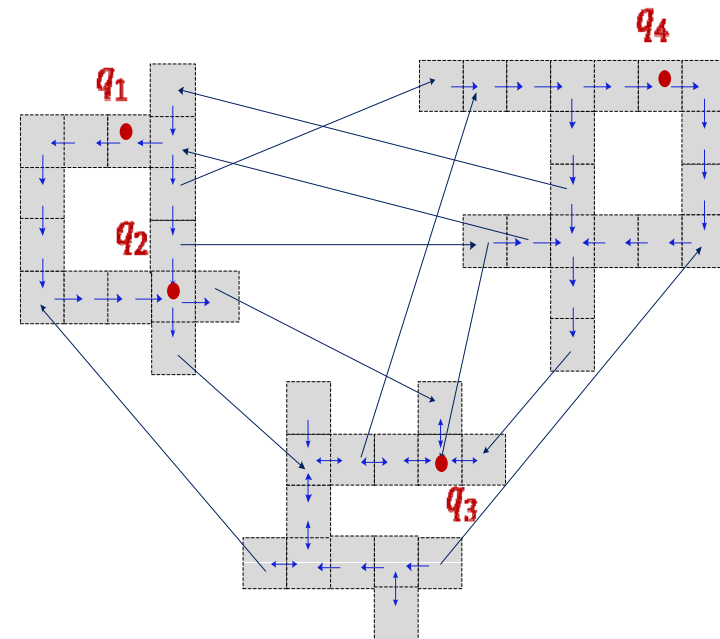
- Redundant edge
  - Exist at least one edge  $E_2$  s.t.  $E_2$ ' support  $>$   $E_1$ 's support
  - The travel time of the path  $p_1 \rightarrow E_2 \rightarrow p_2$  and the travel time of edge  $E_1$  are similar
- Propagate weights to multiple edges



# Route Inference (1/2)



- Local route search
- Global route search



# Route Inference (2/2)

- **Route score**

- Given a graph  $G = (V, E)$ , a route  $p: p_1 \rightarrow p_2 \rightarrow \dots \rightarrow p_m$ , the score of the route is

$$f(p) = \sum_{i=1}^m \rho(p_i)$$

where  $p_i: g_{i_1} \rightarrow g_{i_2} \rightarrow \dots \rightarrow g_{i_j}$

and  $\rho(p_i) = \frac{1}{j-1} | \cup_{k=1}^{j-1} \{tra | g_{i_k} \rightarrow g_{i_{k+1}} \in tra\} |$

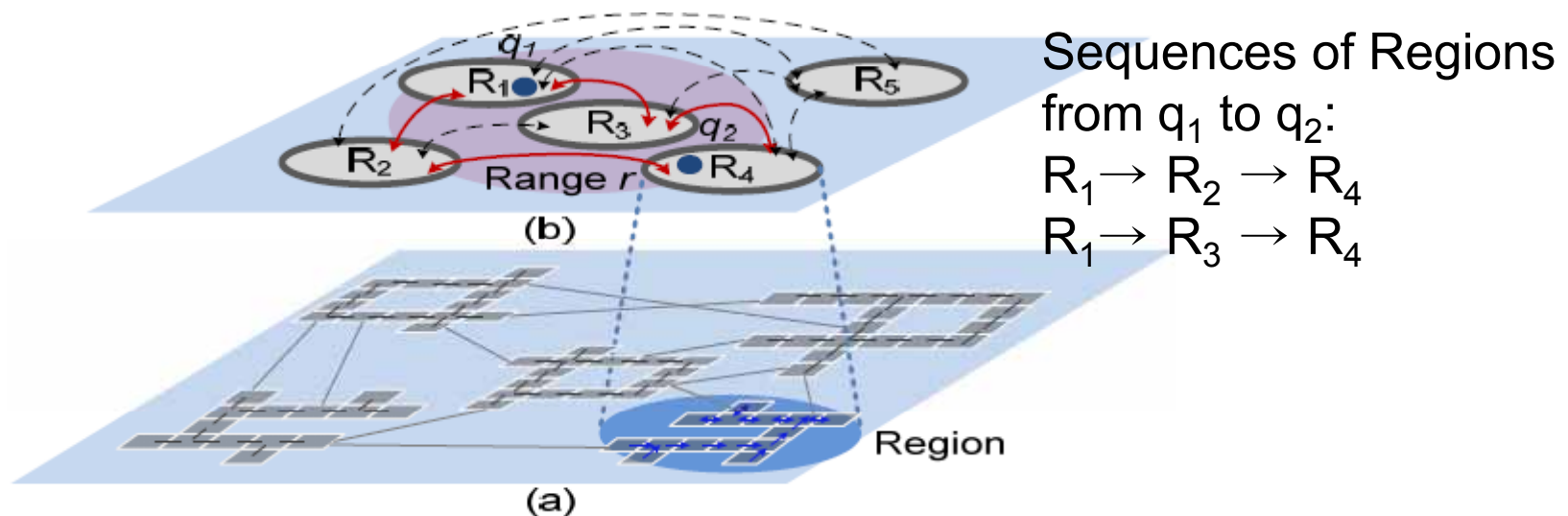
# Local Route Search

- **Goal**

- Top K local routes between two consecutive geo-locations  $q_i, q_{i+1}$

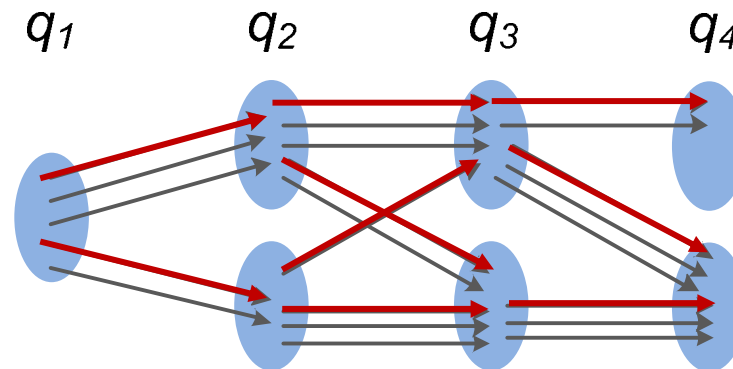
- **Approach**

- Determine qualified visiting sequences of regions by travel times
- A\*-like routing algorithm
  - $\hat{f}(p) = \rho(p_c) + h(p_f)$  where a route  $p: p_c \rightarrow p_f$



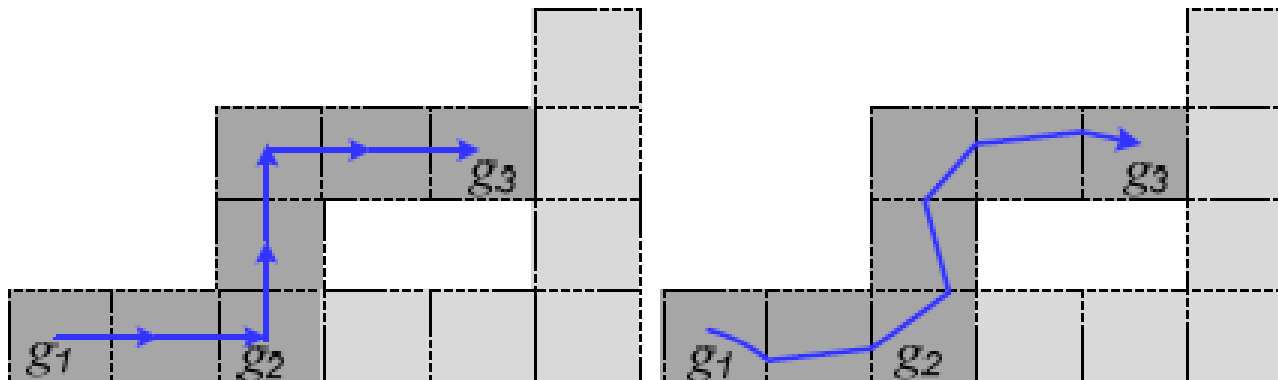
# Global Route Search

- **Input**
  - Local routes between any two consecutive geo-locations
- **Output**
  - Top K global routes
- **Branch-and-bound search approach**
  - E.g., Top 1 global route



# Route Refinement

- **Input**
  - Top K global routes: sequences of cells
- **Output**
  - Top K routes: sequences of segments
- **Approach**
  - Select GPS logs for each grid
  - Adopt linear regression to derive regression lines



# Experiments

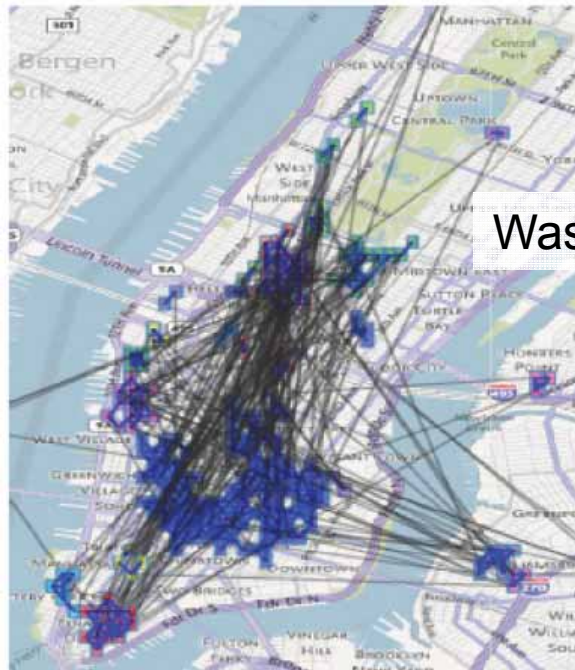
- **Real dataset**
  - Check-in records in Manhattan: 6,600 trajectories
  - GPS logs in Beijing: 15,000 trajectories
- **Effectiveness evaluation**
  - Inferred routes
    - Error:
      - T:  $\text{NDTW}(T, T') = \text{Avg}_{p_k \in T} \min_{tra \in T'} \text{NDTW}(p_k, tra)$
      - T': top K trajectories (ground truth)
- **Efficiency evaluation**
  - Query time
- **Competitor**
  - MPR [Chen et al. ICDE'11]



# Visualization in Manhattan

- Cell length: 500 m
- Minimum connection support: 3
- Temporal constraint: 0.2
- Time span  $\Delta t$ : 40 minutes

Routable Graph



Top 1 Popular Route



Union Square Park

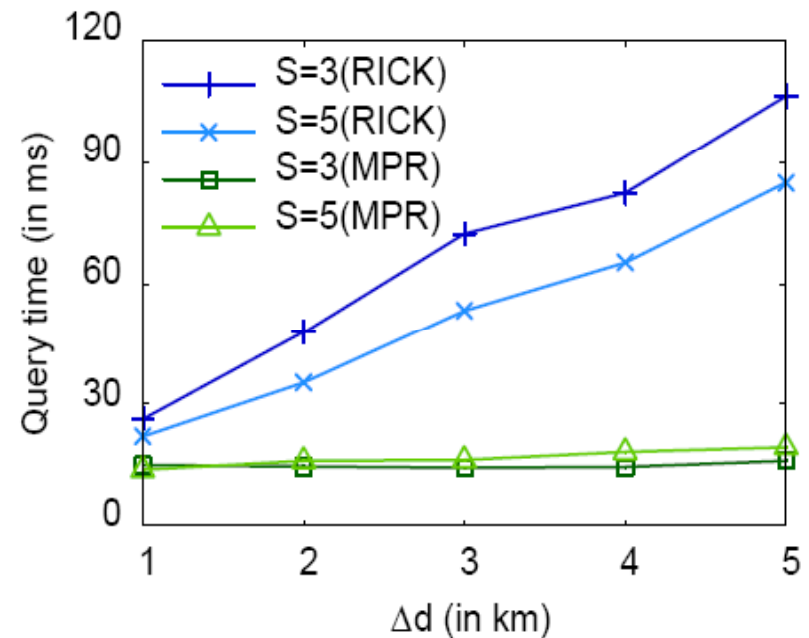
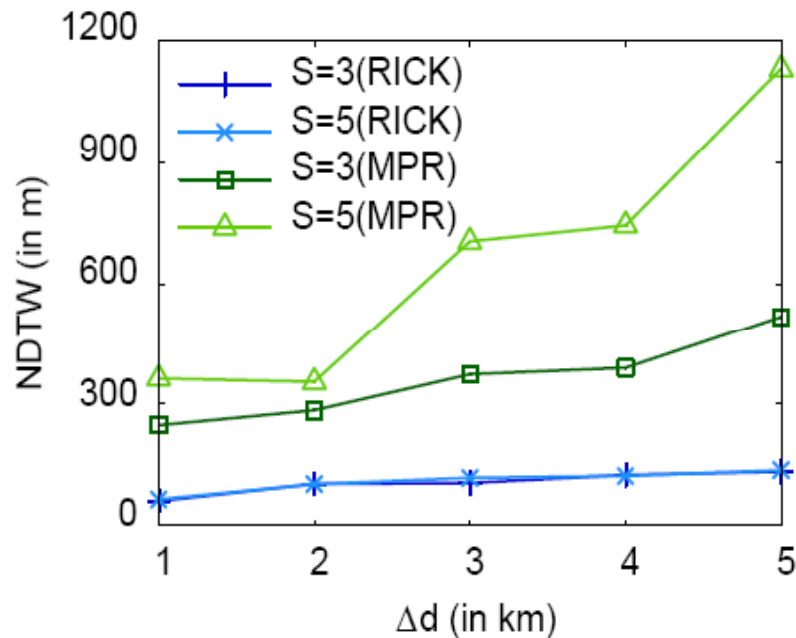
Washington Square Park

New Museum of Contemporary Art



# Performance Comparison

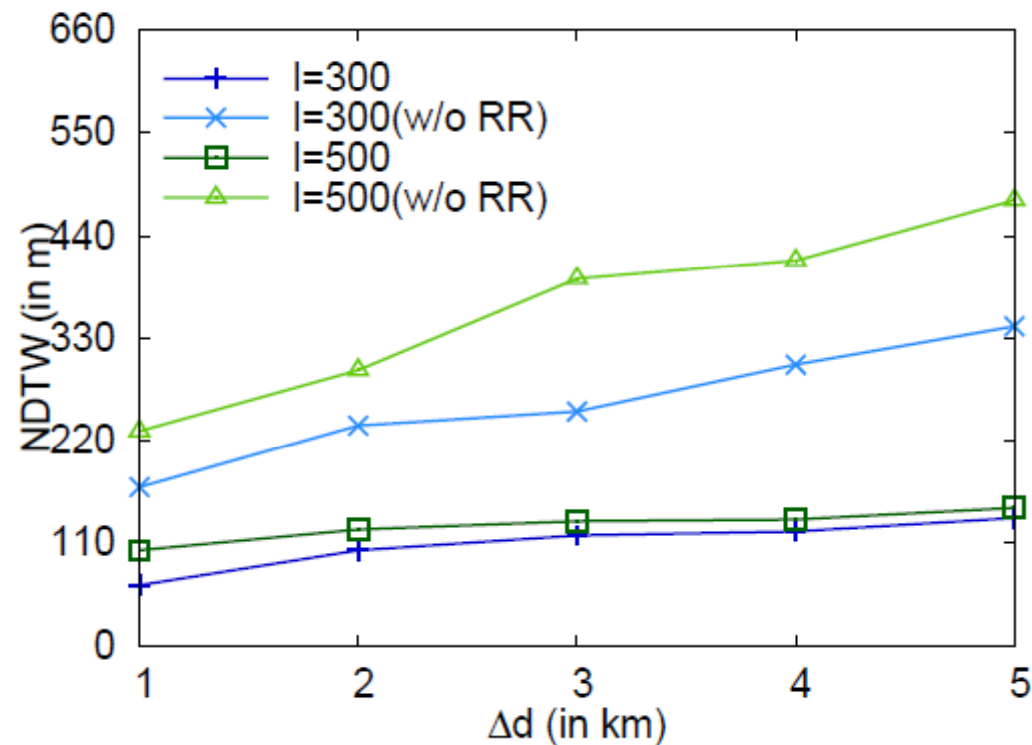
- **Competitor: MPR** [Chen et al. ICDE'11]
- **Parameters**
  - $|q|:2$ ,  $K:1$ , cell length: 300 m
- **Factors**
  - sampling rate (S), query distance ( $\Delta d$ )



# Effectiveness of Route Refinement

- **Parameters**

- $K:1$
- $|q|: 2$



# Summary

- **Developed a route inference framework without the aid of road networks**
- **Proposed a routable graph by exploring spatio-temporal correlations among uncertain trajectories**
- **Developed a routing algorithm to construct the top K popular routes**

# Conclusion

- **Proposed a novel trajectory search framework for trip planning**
  - Search pattern-aware travel routes from historical trajectories with considering a user-preference of depth/breadth
  - Developed an efficient bounded trajectory search algorithm
- **Proposed a route inference framework without the aid of road network information**
  - Infer popular routes from uncertain trajectories
  - Developed an effective approach to construct a routable graph
  - Developed efficient and effective approaches to infer popular routes