PHY517 / AST443: Observational Techniques

Fall 2017

Homework 3

1. The Poisson distribution describes the probability to observe x events during a certain measurement interval, given a mean rate μ :

$$P_{\rm P}(x|\mu) = \frac{\mu^x}{x!}e^{-\mu}$$

Note that x has to be a positive integer.

- (a) Show that the mean of the Poisson distribution is μ .
- (b) Show that the variance of the Poisson distribution is μ .
- (c) Plot (on a single panel) the Poisson distribution for rates of $\mu = 1, 2, 4, 10$.
- (d) For $\mu = 30$, plot the Poisson distribution, as well as a Gaussian distribution of mean $\mu = 30$. Motivate your choice of standard deviation when plotting the Gaussian.
- 2. Write a (python) script that takes as input two FITS images, and outputs the difference of the images (in FITS format).

Hint: the following series identity is useful for Exercise (1):

$$\sum_{k=0}^{\infty} \frac{\lambda^k}{k!} e^{-\lambda} = e^{\lambda}$$