# CIFAR-10 Image Recognition

# EE4305 Introduction to Fuzzy/Neural Systems

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# 1 Introduction

### T. HAYDEN & M. GINI

Machine learning has been the object of intense research over the last few decades. It has produced tangible useful results over many different fields from beating the best players at Go (see section 2.2) to allowing users to automatically tag their friends in uploaded photo albums (see section 3.3). Whilst the inner workings of machine learning are often

The object of this assignment is to give us some exposure into how machine learning can be applied to practical problems. This report will focus on how a multilayer perceptron can be trained on the CIFAR-10 data set to perform image recognition tasks. The CIFAR-10 data set contains  $60000~32\times32$  RGB images labeled into 10 classes. It is a popular benchmark used for image classification algorithms. It is useful because it is a relatively small data set and so training takes a relatively short amount of time.

In the following sections of the report, we give a brief overview of general applications of machine learning as well as some some notable recent accomplishments. The state-of-the-art algorithms

# 2 Literature Review on Artificial Neural Networks

### M. Gini

This section gives a literature review on the broad topic of artificial neural networks (ANN). A more specific review on ANN designed to classify the CIFAR-10 dataset is found in Section 3. The significance and applications of ANN will be reviewed in Section 2.1 while recent trends and accomplishments are discussed in Section 2.2.

# 2.1 Significance and Applications of Artificial Neural Networks

This subsection will illustrate the significance and applications of ANN. Increasing computer power shifted the focus of research towards deep ANN and similar architectures which are coined under the term "deep learning". These powerful deep ANN are nowadays used in a variety of applications<sup>[1][2]</sup>.

ANN are significant because they can work as a black box model. The performance can be improved by data preprocessing, augmentation and mainly by finding an appropriate network architecture and training process. No a-priori knowledge of the classification process itself is required. This makes deep ANN suited for applications where such knowledge is difficult to obtain. Character and speech recognition are such difficult problems, as well as image classification. In speech recognition, deep ANN have been shown to outperform other methods on a variety of speech recognition benchmarks, sometimes by a large margin [3]. In the field of image classification, the 2012 ILSVRC (ImageNet Large-Scale Visual Recognition Challenge) marks an important turning point because a convolutional neural network (CNN) architecture won the competition for the first time - by a large margin [4]. In both fields, ANN are now widely accepted as the most powerful approach.

However, the fact that ANN do not incorporate much a-priori knowledge can also backfire. In consequence, a trained model gives little insight into its inner workings and optimal network architectures are basically found through a trial-and-error process. Most design guidelines for deep learning methods are therefore rather based on empirical knowledge than on theoretical foundations.

New methods are developed to better understand the computations deep ANN perform at each layer. The resulting visualizations reveal the process of extracting high level features out of raw input data<sup>[5]</sup> [6]. In general, each layer extracts higher level features of the input the previous layer provides such that the features are highly abstract after a few layers. The last layer then classifies the input into one of the output categories.

# 2.2 Recent Trends and Accomplishments

Recent trends and accomplishments of ANN are described in this subsection. Two recent accomplishments are looked at in detail: The AlphaGo computer program and adversial examples. AlphaGo is a great example to illustrate the great capabilities of ANN. Adversial examples can easily fool very different kinds of neural networks which is a good way to exemplify the limitations the present ANN still possess.

The game Go is a complex board game with the impressive number of around  $10^{170}$  legal positions<sup>[7]</sup>. Due to its enormous search space and difficulty to evaluate board positions, it

is viewed as the most challenging of the classical games for artificial intelligence. A victory of a computer program over a professional human player has been considered to be at least a decade away. However, the computer program AlphaGo beat the European Go champion 5-0 in 2015<sup>[8]</sup>.

AlphaGo makes extensive use of ANN. It consists of a "value" and a "policy" network to separately evaluate the board position and select moves. It is trained in a combination of supervised learning from human expert games and reinforcement learning through self-play. The training of such big networks requires notable computation resources. In a recent trend, dedicated hardware to train deep ANN is developed. Besides other adaptions, it is designed to speed up matrix multiplications which are one of the main components of the training process. The most notable example is the Tensor Processing Unit which achieves a 15- to 30-fold performance compared to a contemporary GPU or CPU [9]. It is important to note that the development of deep learning is closely connected to the ever improving available computing power [10].

AlphaGo received considerable media coverage and is considered as one of the most impressive feats of deep learning. In a follow-up paper, a further improved version of AlphaGo is presented, AlphaZero<sup>[11]</sup>. It uses a single neural network and trains solely through reinforcement learning with self-play, starting with random play. It is only provided with the rules of Go. After only days of training, it defeated all previous versions of AlphaGo and achieved a never seen before playing strength. It is quite intriguing that even for such a complex task, the network can achieve superhuman performance without any provided knowledge besides the rules of the game.

As a second recent trend, adversarial examples recently surprised a lot of researches and became a hot topic of interest. To generate an adversarial example, a slight perturbation is applied to a correctly classified image. The classification process is then repeated and the perturbation is adapted such that the prediction error is *maximized*. A slight perturbation which is not recognizable by a human is already enough to let the neural network misclassify an image with a high confidence level<sup>[12]</sup>. It has been shown that adversarial examples trained on one model are likely to be misclassified by another model as well, i.e. they possess a transferability property<sup>[13]</sup>.

It is very likely that a randomly selected input to a neural network built from linear parts is processed incorrectly and the models only behave reasonably on a very thin manifold encompassing the training data<sup>[14]</sup>. This result questions the generalization abilities of ANN. Furthermore, the transferability property allows potential attacks on systems using ANN <sup>[15][16]</sup>. For example, stop signs could be slightly modified with stickers such that they are misclassified by autonomous vehicles which then behave unexpectedly. Further research is required to develop defense strategies against such attacks. Only then, ANN can deployed in safety critical applications.

# 3 Literature Review on the CIFAR-10 dataset

### T. M. HAYDEN

The CIFAR-10 dataset [17] is a well established dataset in the machine learning community. It is challenging because it is a relatively small dataset. Even so, excellent results, even exceeding human performance, have been obtained using a variety of CNN architectures<sup>1</sup>. At the time of writing, the highest published result on the CIFAR-10 dataset was achieved in 2015 with accuracy of 96.53%. This is considerably better than human performance which has an accuracy

<sup>&</sup>lt;sup>1</sup>http://rodrigob.github.io/are\_we\_there\_yet/build/classification\_datasets\_results.html

of around  $94\%^{[18]}$ .

# 3.1 Data Augmentation

Like many other machine learning problems, image classification will almost always benefit from additional data<sup>[19]</sup>. However, even when restricted to a particular dataset such as CIFAR-10 it is possible to generate more data using a technique called data augmentation<sup>[20]</sup>. Data augmentation manipulates existing images to create 'new' data for use in training.

Common methods to augment images for use in machine learning include mirroring, rotation and image translation<sup>[4]</sup>. Using these techniques it is possible to train on a dataset that can be several times larger than the original dataset. The leading architectures all made heavy use of data augmentation<sup>[21] [22] [23]</sup>.

# 3.2 State of the art architectures for classifying the CIFAR-10 dataset

In this section, the results of several different CNN architectures are presented. It should be noted that these architectures were not designed specifically to perform on the CIFAR-10 dataset. As such, they may not be fully optimised and it is likely that they could be improved slightly.

### 3.2.1 Fractional max-pooling

In a standard CNN, convolutional layers are often interspaced with 2x2 max-pooling layers. These max-pooling layers serve to downsample the data. This allows the CNN to be somewhat spatially invariant to the locations of the features and improve accuracy. However each max pooling layer also removes 75% of the data<sup>[21]</sup>. This in effect reduces the maximum depth of the CNN due to the disjoint nature of the max-pooling regions.

By using a new approach known as fractional max-pooling, it is possible to max-pool using a non-integer mask size. In this manner, the size of the hidden layers is reduced by a lesser amount and it is possible to create deeper networks without having to add consecutive convolutional layers. This is important as generally deeper networks will lead to stronger classifiers <sup>[24]</sup>. However, deeper networks are also in general more expensive to train.

An architecture based on fractional max-pooling currently has the highest published classification accuracy on the CIFAR-10 dataset at 96.53%. This architecture also made heavy use of data augmentation. Additionally, the model was 'fine-tuned' after initial training by re-training on the original dataset for a few epochs using a low learning.

### 3.2.2 The All Convolutional Net(ALL-CNN)

In this architecture <sup>[23]</sup> a CNN consisting entirely of convolutional layers is proposed. Max-pooling layers are instead replaced with convolutional layers with increased stride. These increased stride layers act in a similar way to max-pool layers in that they downsample the data and allow the CNN somewhat invariant feature location. This architecture has an accuracy of 95.59% which is the 2nd highest published result. This architecture also makes heavy use of data augmentation.

#### 3.2.3 Layer-sequential unit-variance (LSUV) initialization

LSUV initialisation provides a method to initialise deep CNN. This produces networks with better accuracy than uninitialised networks. In addition LSUV greatly accelerates the training

of CNNs. An architecture based on the LSUV method machine managed to achieve an accuracy of 94.16%. Note that this only used a moderate amount of data augmentation.

It is important to stress the use of data augmentation when looking at these results. Table shows the results of the three leading architectures along with the amount of data augmentation. Moderate data augmentation consists of mirroring in the horizontal axis and small translations in each axis. Extreme data augmentation involves upscaling the images to  $126 \times 126$  pixel images and performing a variety of operations such as shearing, colour augmentation, rotation, translation and scaling. It may be the case that with additional data augmentation, LSUV outperforms the max-Pooling approach.

Data Augmentation	Fractional Max-Pooling	ALL-CNN	LSUV
None	-	90.92%	-
Moderate	-	92.75%	93.94%
Extreme	96.53%	95.59%	-

Table 1: Table showing the results of the leading CIFAR-10 architectures.

## 3.3 Application areas of image recognition algorithms

There are numerous applications of image recognition algorithms across many different fields. However in order for neural networks to be effective, large amounts of labeled data must first be collected. In practice labelling and uploading of images is mostly done by users of the application by 'tagging' images. For example in a stock image database such as Shutterstock<sup>2</sup>, users would be prompted to tag uploaded images with the image contents. This provides Shutterstock with an enormous amount of data perfect for machine learning. This has allowed Shutterstock to develop powerful new tools to label images using machine learning. For example the newly released compositionally aware search which allows users to serarch for images with specific objects in different locations of the image<sup>[25]</sup>.

Another application of image recognition is to automatically tag recognised faces when uploading photos onto social media websites. This is useful as it is often tedious to tag each image in large albums. Automatic tagging algorithms have been developed using machine learning to automatically tag faces with accuracy as high 99% [26]. This allows users to upload entire albums without having to tag each photo individually.

# 4 Multi-Layer Perceptron Classifier

### M. GINI & T. M. HAYDEN

This section presents the multi-layer perceptron (MLP) classifier designed to classify the CIFAR-10 dataset. It is organized as follows: Section 4.1 introduces the software setup used to implement the MLP classifier. Section 4.2 discusses the data preprocessing and augmentation. Section 4.3 analyzes the effect of different network structures on performance. Section 4.4 analyzes the effect of different hyperparameters.

<sup>&</sup>lt;sup>2</sup>https://www.shutterstock.com/

### 4.1 Software Setup

MATLAB's Neural Networks toolbox is employed to implement the MLP classifier. The toolbox provides convenient algorithms and applications to design the MLP. A network training function with a convenient graphical user interface (GUI) to observe the progress is included as well. Figure 1 shows the GUI.

Since this is a classification problem, parts of the network structure are given. The output of the MLP should be a prediction of to which class the input belongs to. This is accomplished with the help of the softmax function, also called normalized exponential function. Equation 4.1 shows the formula of such a function. A softmax layer is then used as the last layer. It gets a K-dimensional input vector z of arbitrary real values and "squashes" it into a K-dimensional output vector  $\sigma(z)$  of real values in the range [0,1]. In our case, K=10 and the output values represent the probabilities that the input belongs to the respective class. The class with the highest probability then constitutes the predicition of the MLP.

$$\sigma(\mathbf{z})_j = \frac{e^{z_j}}{\sum_{k=1}^K e^{z_k}} \quad \text{for} \quad j = 1, \dots K.$$
 (4.1)

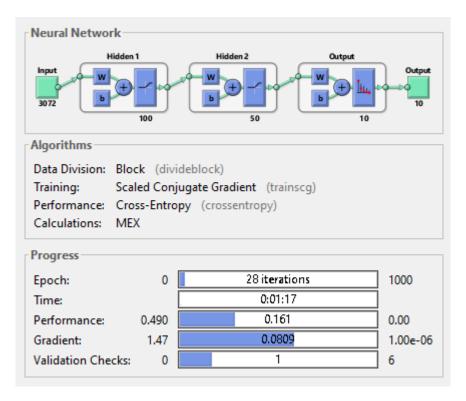


Figure 1: Screenshot of MATLAB's nntraintool.

The other hidden layers consist of standard MLP. The input to the MLP are the pixel values of the image. Preprocessing and augmentation as described in the next section is also done before the pixel values are fed into the network.

MATLAB offers lots of adjustable settings for the MLP. Unless mentioned otherwise, the following settings are employed as default settings:

- Training function: 'trainscg' which is the scaled conjugate gradient method.
- Loss function: 'crossentropy' which penalizes
- Activation function: 'tansig' which is the hyperbolic tangent sigmoid activation function

- The training batch size is set to 20000 images. This constitutes a compromise between a good performance and a reasonable training time.
- As a default network structure, two hidden layers are employed with 100 and 50 neurons.
- Dataset structure: 80% are used for the training and 20% are used for validation. For the testing, the dedicated testing batch provided in the dataset is utilized.
- Weight initialization: The weights of the neurons are randmoly initialized. Since this leads to slightly different performances for each run, for the performance analysis each configuration is run five times and then the test accuracy is averaged.

### 4.2 Data Preprocessing and Augmentation

Data preprocessing and augmentation take place before the data is fed into the network. In the preprocessing step, the data is normalized and centered around the mean. In the augmentation step, the amount of data is augmented through operations like image flipping.

### 4.2.1 Data Preprocessing

Each image of the dataset is represented by a 32\*32\*3 array, which results in 1024 pixel values per color channel. To be processed by the MLP, it is transformed into a 1\*3072 array. The pixel values are integers in the range [0,255]. For normalization, the data is divided by 255 to lie within the range [0,1]. Accordingly, the datatype changes from the integer type to double. In a second step, the mean per pixel over the whole training set is subtracted. This centers the data per channel.

Data preprocessing also includes the division of the complete dataset into appropriate training, validation and test data batches. There are 50000 images available for training. With the default splitting into training and validation dataset (80% for training and 20% for validation), Figure 2 shows the effect of increasing the training batch size as well as employing data preprocessing.

As intuitively expected, the test accuracy increases for an increasing training batch size. However, the data preprocessing does not lead to a significant increase of performance. The normalization and mean subtraction do not have a big influence in that specific case since the input values already lie in a well defined range and the mean per pixel is also a almost constant value over all pixels. The errorbars show that the different accuracies are most likely due to the random weight initialization.

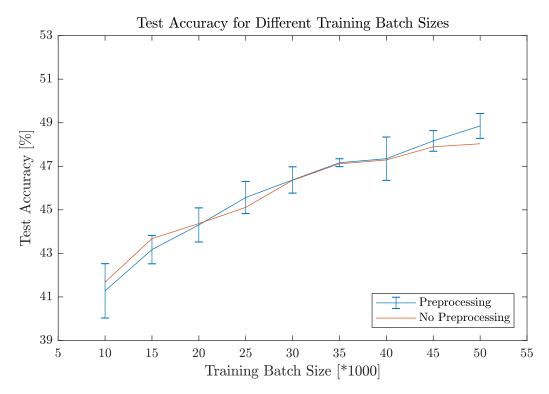


Figure 2: Comparison of network performance with and without data preprocessing. The errorbars represent one standard deviation.

### 4.2.2 Data Augmentation

Figure 2 above shows that a larger training batch size leads to an increased performance. A natural approach is therefore to artificially increase the training batch size. Image flipping and image rotation are used. Figure 3 illustrates the performance gain from vertical image mirroring. The test accuracy is significantly increased for all training batch sizes by around 3%.

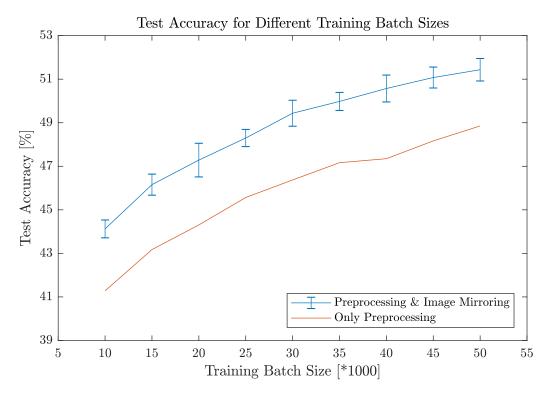


Figure 3: Comparison of network performance with and without data augmentation. The errorbars represent one standard deviation.

### 4.3 Optimization of Network Structure

Choosing the correct architecture of a neural network remains a complicated area of study which is still not fully understood <sup>[27]</sup>. For any given problem there are essentially an infinite number of valid MLP architectures. There are many different approaches to architecture selection but none are foolproof <sup>[27]</sup>.

### 4.3.1 Layers of the MLP

Every neural network, including MLPs, will have at the very least one input layer and one output layer. The size of the input layer simply depends on the size of the input data. In the case of CIFAR-10 the input size is  $32 \times 32 \times 3$ , the size of the input image data.

In addition to the input layer, each network will also have an output layer. The size of the output layer is also defined by the format of the data. In the the case of CIFAR-10, the output layer is a softmax layer with 10 nodes corresponding to each class label.

There can be an arbitrarily large number of hidden layers. However performance gains from addition additional layers beyond the first are very small or even negligible. Additionally adding more layers increases the chance that the classifier finds a local minima <sup>[28]</sup>. Figure 4 shows the effect of adding additional layers to our MLP classifier. Note that adding additional layers after the 2nd has almost no impact on the test accuracy.

c)on the training of the MLP

- Varying the number of neurons
- Varying the number of layers

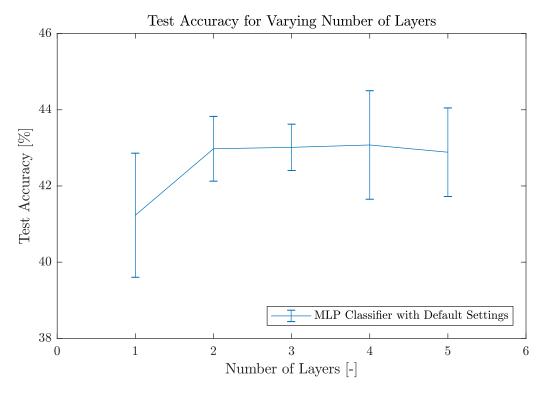


Figure 4: Effect of adding additional layers to the MLP classifier

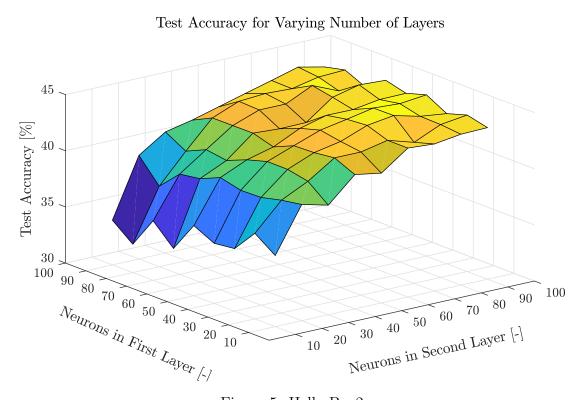


Figure 5: Hello Boy2

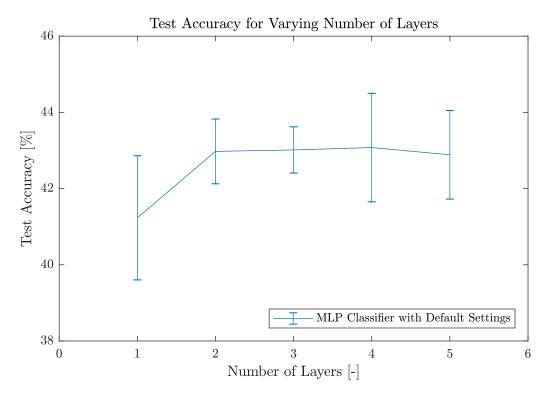


Figure 6: Hello Boy2

M. Gini 5. CNN NETWORK

# 4.4 Optimization of Network Hyperparameters

Hyperparameter selection for neural networks such as MLPs has become an interesting field of research with many interesting algorithms being used to estimate good parameters to use<sup>[29]</sup>. However, since these algorithms rely on performing many trials and updating the parameters accordingly, they proved unsuitable for our purposes due to our limited resources. Our approach instead relied on performing a limited number of trails to find trends. From these general trends and our knowledge of MLP classifiers, we then estimated good parameters to use.

d) on the performance of the MLP with different objective functions and optimization methods

#### Some pic of the confusion matrix

- Different learning rates
- Different optimization methods
- Different performance functions There are six different performance functions available in the MATLAB environment:

e) any other interesting observation that you think are pertinent (e.g. effect of learning rate on convergence speed).

### 4.4.1 Learning Rate

Choosing the learning rate for a MLP classifier can be a challenging process. There is no approach that will work optimally for every dataset. A learning rate that is too high can overshoot the solution and become unstable. However low learning rates can become stuck in local minima or take a long time to train. A good solution is to pick a high learning rate that can pass over local minima and to gradually decrease the learning rate so that the classifier does not become unstable. This will result in a classifier which initially follows general trends and 'explores' a large portion of the parameter space. Later on the smaller learning rate will allow for the model to be fine tuned into a particular solution.

The effects of changing the learning rate in our model can be seen in figure 7. The figure shows that increased learning rates, in general, had a positive effect on model accuracy.

- 4.4.2 Performance function
- 4.4.3 Activation function
- 4.4.4 Training fucntion

### 5 CNN Network

M. GINI & T. M. HAYDEN

### 6 Conclusion

M. GINI & T. HAYDEN

Long story short: we completely aced our project BOOM 2+2=4 -1 = 3 quick maths

M. Gini 6. CONCLUSION

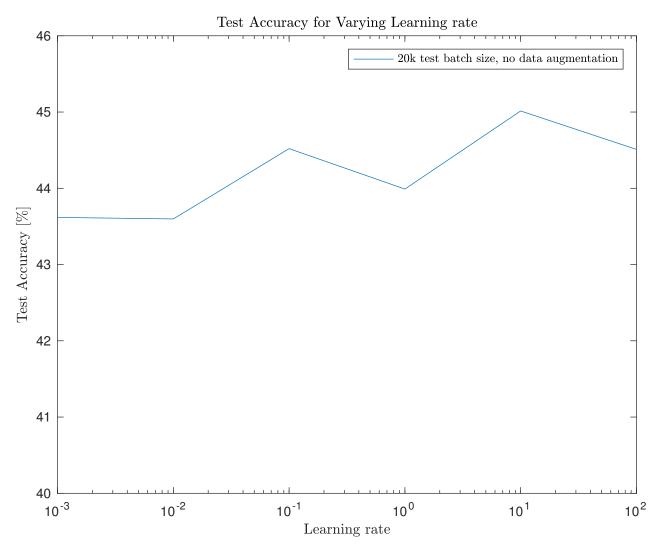


Figure 7: 2+2=

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