

Prediction of Aerodynamic Performance Using Machine Learning with Genetic Algorithms(GA)

```
In [1]: import os
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.ensemble import RandomForestRegressor
import pygad
import numpy as np
import matplotlib.pyplot as plt
```

```
In [2]: folder_path = 'Raw Dataset'
```

```
In [3]: all_data = pd.DataFrame()

for file_name in os.listdir(folder_path):
    if file_name.endswith('.csv'): # Ensure only CSV files are read
        file_path = os.path.join(folder_path, file_name)
        data = pd.read_csv(file_path)
        all_data = pd.concat([all_data, data], ignore_index=True)

print(all_data)
```

| | V0 | Q0 | T0 | P0 | P00 | Q00 \ |
|-----|--------|-------------|------------|-------------|-------------|-------------|
| 0 | 65.033 | 2418.063333 | 302.190000 | 100249.0000 | 100275.1567 | 2366.063333 |
| 1 | 65.080 | 2420.683333 | 302.273333 | 100244.0000 | 100270.5133 | 2371.346667 |
| 2 | 65.070 | 2419.346667 | 302.336667 | 100239.0000 | 100265.5167 | 2372.783333 |
| 3 | 65.047 | 2417.296667 | 302.386667 | 100233.6667 | 100260.2467 | 2373.816667 |
| 4 | 65.030 | 2415.253333 | 302.446667 | 100230.3333 | 100256.4433 | 2374.003333 |
| .. | ... | ... | ... | ... | ... | ... |
| 277 | 65.020 | 2406.030000 | 303.630000 | 100244.0000 | 100276.3000 | 2372.220000 |
| 278 | 65.020 | 2405.660000 | 303.630000 | 100245.0000 | 100277.7300 | 2371.730000 |
| 279 | 65.100 | 2411.320000 | 303.650000 | 100249.0000 | 100281.6300 | 2374.090000 |
| 280 | 65.180 | 2417.360000 | 303.650000 | 100248.0000 | 100280.4800 | 2380.500000 |
| 281 | 65.240 | 2422.080000 | 303.650000 | 100248.0000 | 100281.1200 | 2384.590000 |

| | ALFA | BETA | CL | CD | CM25 | CYAW | CROLL | CY |
|-----|---------|------|---------|--------|---------|---------|---------|---------|
| 0 | -10.400 | 0 | -0.5671 | 0.2604 | 0.3409 | 0.0031 | 0.0049 | -0.0067 |
| 1 | -9.393 | 0 | -0.5437 | 0.2329 | 0.2942 | 0.0021 | 0.0015 | -0.0054 |
| 2 | -8.350 | 0 | -0.4986 | 0.2044 | 0.2494 | 0.0018 | -0.0007 | -0.0072 |
| 3 | -7.303 | 0 | -0.4404 | 0.1729 | 0.2117 | 0.0018 | -0.0029 | -0.0080 |
| 4 | -6.240 | 0 | -0.3465 | 0.1493 | 0.1816 | 0.0020 | -0.0037 | -0.0084 |
| .. | ... | ... | ... | ... | ... | ... | ... | ... |
| 277 | 15.160 | 0 | 1.6878 | 0.1770 | -0.3963 | -0.0006 | -0.0105 | -0.0136 |
| 278 | 15.160 | 0 | 1.6812 | 0.1771 | -0.3961 | -0.0008 | -0.0107 | -0.0150 |
| 279 | 15.660 | 0 | 1.6351 | 0.2012 | -0.4264 | 0.0009 | -0.0012 | -0.0063 |
| 280 | 15.670 | 0 | 1.6526 | 0.1996 | -0.4199 | 0.0008 | -0.0013 | -0.0043 |
| 281 | 15.660 | 0 | 1.6327 | 0.2017 | -0.4287 | 0.0010 | -0.0005 | -0.0059 |

[282 rows x 14 columns]

This code effectively combines machine learning models (Random Forest) with a Genetic Algorithm to find optimal design parameters that maximize the Lift-to-Drag ratio based on the provided data.

```
In [4]: import os
import pandas as pd
from sklearn.model_selection import train_test_split
```

```

from sklearn.ensemble import RandomForestRegressor
import pygad
import numpy as np
import matplotlib.pyplot as plt

folder_path = 'Raw Dataset' # Replace with the folder containing your CSV files

# Step 1: Loading all CSV files from the folder and concatenate into a single DataFrame
all_data = pd.DataFrame() # Empty DataFrame to store data from all files

for file_name in os.listdir(folder_path):
    if file_name.endswith('.csv'): # Ensure only CSV files are read
        file_path = os.path.join(folder_path, file_name)
        data = pd.read_csv(file_path)
        all_data = pd.concat([all_data, data], ignore_index=True)

# Step 2: Prepare the Data
features = all_data[['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']]
target_cl = all_data['CL']
target_cd = all_data['CD']

# Step 3: Split Data for Training and Testing
X_train, X_test, y_train_cl, y_test_cl = train_test_split(features, target_cl, test_size=0.2)
X_train, X_test, y_train_cd, y_test_cd = train_test_split(features, target_cd, test_size=0.2)

# Step 4: Train the Models
model_cl = RandomForestRegressor(n_estimators=100, random_state=42)
model_cl.fit(X_train, y_train_cl)

model_cd = RandomForestRegressor(n_estimators=100, random_state=42)
model_cd.fit(X_train, y_train_cd)

# Step 5: Define the Genetic Algorithm Fitness Function
def fitness_function(ga_instanceE, solution, solution_idx):
    v0, q0, t0, p0, p00, q00, alfa, beta = solution
    feature_set = pd.DataFrame([[v0, q0, t0, p0, p00, q00, alfa, beta]],
                                columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA'])

    predicted_cl = model_cl.predict(feature_set)[0]
    predicted_cd = model_cd.predict(feature_set)[0]

    if predicted_cd < 1e-6:
        predicted_cd = 1e-6 # Prevent division by zero

    return predicted_cl / predicted_cd # Maximize Lift-to-Drag ratio

# Step 6: Initialize and Run the Genetic Algorithm
ga_instanceE = pygad.GA(num_generations=200,
                        num_parents_mating=5,
                        fitness_func=fitness_function,
                        sol_per_pop=10,
                        num_genes=8,
                        init_range_low=[50, 2000, 300, 100000, 100000, 2000, -10, -5],
                        init_range_high=[70, 2500, 350, 101000, 101000, 2500, 10, 5],
                        mutation_percent_genes=10)

ga_instanceE.run()

# Step 7: Get and Print the Best Solution
solution, solution_fitness, _ = ga_instanceE.best_solution()

print(f"Best Solution (Design Parameters): {solution}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness}")

```

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748: UserWarning: The percentage of genes to mutate (mutation_percent_genes=10) resulted
in selecting (0) genes. The number of genes to mutate is set to 1 (mutation_num_genes=
1).
If you do not want to mutate any gene, please set mutation_type=None.
warnings.warn(f"The percentage of genes to mutate (mutation_percent_genes={mutation_pe
rcent_genes}) resulted in selecting ({mutation_num_genes}) genes. The number of genes to
mutate is set to 1 (mutation_num_genes=1).\nIf you do not want to mutate any gene, pleas
e set mutation_type=None.")
C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py:
1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.
3.0. To delay or pause the evolution after each generation, assign a callback function/m
ethod to the 'on_generation' parameter to adds some time delay.
warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.
0. To delay or pause the evolution after each generation, assign a callback function/met
hod to the 'on_generation' parameter to adds some time delay.")
Best Solution (Design Parameters): [ 6.05738673e+01  2.33409818e+03  3.03278675e+02  1.0
0486751e+05
1.00430043e+05  2.40514674e+03  9.45248210e+00 -2.50552038e+00]
Lift-to-Drag Ratio of Best Solution: 11.690997532404918

```

```

In [5]: # Get the best solution
solution, solution_fitness, _ = ga_instanceE.best_solution()
print(f"Best Solution: {solution}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness}")

# Create a feature set from the best solution
best_feature_set = pd.DataFrame([solution], columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00'])

# Predict CL and CD using the trained models
predicted_cl = model_cl.predict(best_feature_set)[0]
predicted_cd = model_cd.predict(best_feature_set)[0]

print(f"Predicted CL: {predicted_cl}")
print(f"Predicted CD: {predicted_cd}")

# Calculate and display Lift-to-Drag ratio
lift_to_drag_ratio = predicted_cl / predicted_cd if predicted_cd != 0 else float('inf')
print(f"Calculated Lift-to-Drag Ratio: {lift_to_drag_ratio}")

Best Solution: [ 6.05738673e+01  2.33409818e+03  3.03278675e+02  1.00486751e+05
1.00430043e+05  2.40514674e+03  9.45248210e+00 -2.50552038e+00]
Lift-to-Drag Ratio of Best Solution: 11.690997532404918
Predicted CL: 1.6487580000000006
Predicted CD: 0.141028
Calculated Lift-to-Drag Ratio: 11.690997532404918

```

```

In [6]: from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score

# Predict CL and CD on the test dataset
predictions_cl = model_cl.predict(X_test)
predictions_cd = model_cd.predict(X_test)

# Calculate metrics for CL
mae_cl = mean_absolute_error(y_test_cl, predictions_cl)
mse_cl = mean_squared_error(y_test_cl, predictions_cl)
r2_cl = r2_score(y_test_cl, predictions_cl)

# Calculate metrics for CD
mae_cd = mean_absolute_error(y_test_cd, predictions_cd)
mse_cd = mean_squared_error(y_test_cd, predictions_cd)
r2_cd = r2_score(y_test_cd, predictions_cd)

# Print metrics
print("Metrics for CL:")
print(f"Mean Absolute Error: {mae_cl}")
print(f"Mean Squared Error: {mse_cl}")

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print(f"R-squared: {r2_cl}")
```

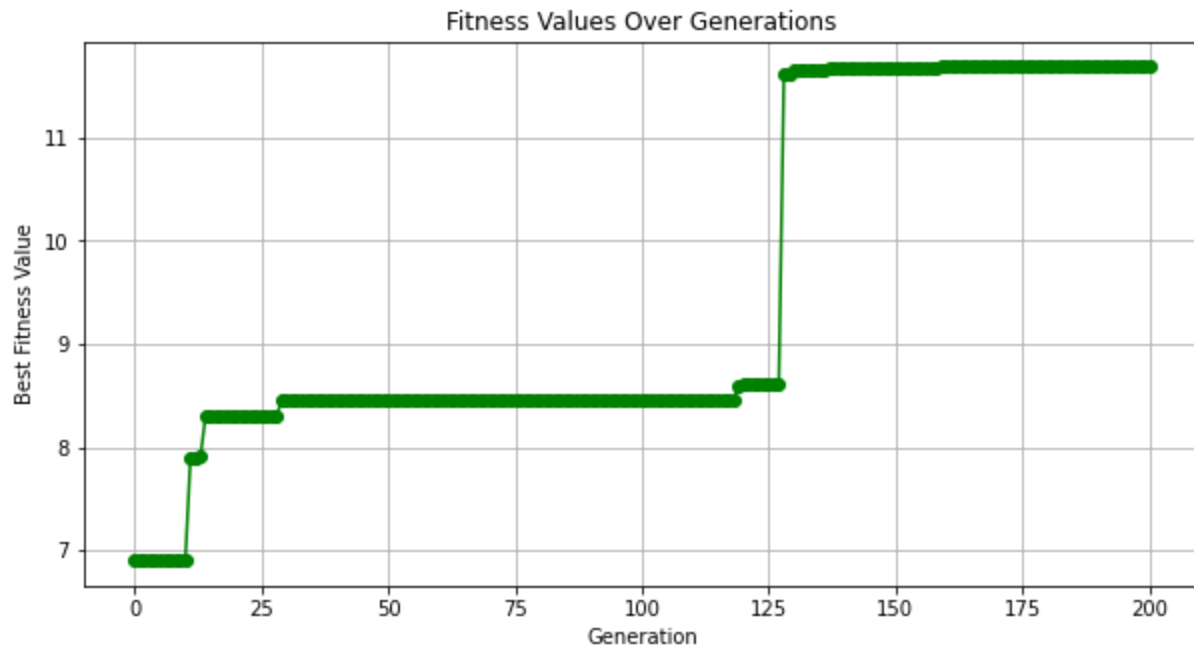
```
print("\nMetrics for CD:")
print(f"Mean Absolute Error: {mae_cd}")
print(f"Mean Squared Error: {mse_cd}")
print(f"R-squared: {r2_cd}")
```

Metrics for CL:
Mean Absolute Error: 0.07175189473684199
Mean Squared Error: 0.011471930027964903
R-squared: 0.9831001834011422

Metrics for CD:
Mean Absolute Error: 0.005448333333333332
Mean Squared Error: 9.375819847368422e-05
R-squared: 0.9892201508232326

```
In [7]: # Step 9: Store fitness values
fitness_values = ga_instanceE.best_solutions_fitness

# Plot fitness values over generations
plt.figure(figsize=(10, 5))
plt.plot(fitness_values, color='g', marker='o')
plt.xlabel('Generation')
plt.ylabel('Best Fitness Value')
plt.title('Fitness Values Over Generations')
plt.grid()
plt.show()
```



Modified GA for Random Forest

```
In [8]: import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.ensemble import RandomForestRegressor
import pygad
import numpy as np
import matplotlib.pyplot as plt
import os

# Folder containing all CSV files
folder_path = 'Raw Dataset' # Replace with the folder containing your CSV files
```

```

# Step 1: Load all CSV files from the folder and concatenate into a single DataFrame
all_dataaa = pd.DataFrame() # Empty DataFrame to store data from all files

for file_name in os.listdir(folder_path):
    if file_name.endswith('.csv'): # Ensure only CSV files are read
        file_path = os.path.join(folder_path, file_name)
        data = pd.read_csv(file_path)
        all_dataaa = pd.concat([all_dataaa, data], ignore_index=True)

# Step 2: Prepare the data
features = all_dataaa[['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']]
target_cll = all_dataaa['CL']
target_cdd = all_dataaa['CD']

# Step 3: Split the data into training and testing sets for CL and CD
X_train, X_test, y_train_cll, y_test_cll = train_test_split(features, target_cll, test_s
X_train, X_test, y_train_cdd, y_test_cdd = train_test_split(features, target_cdd, test_s

# Step 4: Train Random Forest model for CL and CD
model_cll = RandomForestRegressor(n_estimators=100, random_state=42)
model_cll.fit(X_train, y_train_cll)

model_cdd = RandomForestRegressor(n_estimators=100, random_state=42)
model_cdd.fit(X_train, y_train_cdd)

# Step 5: Genetic Algorithm - Fitness function with Lift-to-Drag ratio maximization
best_fitness_values = [] # Initialize an empty list to store best fitness values

def fitness_function(ga_instance, solution, solution_idx):
    v0, q0, t0, p0, p00, q00, alfa, beta = solution
    feature_set = pd.DataFrame([[v0, q0, t0, p0, p00, q00, alfa, beta]],
                                columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'B

    predicted_cl = model_cll.predict(feature_set)[0]
    predicted_cd = model_cdd.predict(feature_set)[0]

    # Prevent division by very small CD values
    if predicted_cd < 1e-6:
        predicted_cd = 1e-6

    fitness_value = predicted_cl / predicted_cd # Maximize Lift-to-Drag ratio
    return fitness_value

# Callback function to store best fitness value after each generation
def on_generation(ga_instance):
    best_fitness = ga_instance.best_solution()[1] # Get the best fitness value
    best_fitness_values.append(best_fitness) # Store it

# Enhanced population initialization
def enhanced_initialization(lower_bounds, upper_bounds, population_size):
    population = np.random.uniform(lower_bounds, upper_bounds, (population_size, len(low
    return population

# Adaptive crossover
def crossover_func(parents, offspring_size, ga_instance):
    offspring = np.empty(offspring_size)
    for k in range(offspring_size[0]):
        parent1_idx = np.random.randint(0, parents.shape[0])
        parent2_idx = np.random.randint(0, parents.shape[0])
        crossover_point = np.random.randint(1, parents.shape[1])
        offspring[k, 0:crossover_point] = parents[parent1_idx, 0:crossover_point]
        offspring[k, crossover_point:] = parents[parent2_idx, crossover_point:]
    return offspring

# Adaptive mutation
def adaptive_mutation(offspring, ga_instance):

```

```

    for idx in range(offspring.shape[0]):
        mutation_indices = np.random.choice(offspring.shape[1], size=2, replace=False)
        for mutation_idx in mutation_indices:
            mutation_amount = np.random.uniform(-0.5, 0.5) # Larger mutation range for
            offspring[idx, mutation_idx] += mutation_amount
    return offspring

# Initialize Genetic Algorithm with enhanced components

## 1. Increase Population Size
population_size = 40 # Double or triple the population size
lower_bounds = [50, 2000, 300, 100000, 100000, 2000, -10, -5]
upper_bounds = [70, 2500, 350, 101000, 101000, 2500, 10, 5]
initial_population = enhanced_initialization(lower_bounds, upper_bounds, population_size)

ga_instance = pygad.GA(num_generations=200, # Increased number of generations
                       num_parents_mating=10, # More parents for better diversity
                       fitness_func=fitness_function,
                       initial_population=initial_population,
                       num_genes=8,
                       mutation_type=adaptive_mutation,
                       crossover_type=crossover_func,
                       keep_elitism=5,
                       mutation_probability=0.3, # Increased mutation probability to 0.
                       on_generation=on_generation) # Add the callback function

# Run the GA
ga_instance.run()

# Get the best solution
solution, solution_fitness, _ = ga_instance.best_solution()
print(f"Best Solution: {solution}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness}")
# Predict CL and CD values using the best solution
predicted_feature_set = pd.DataFrame([solution], columns=['V0', 'Q0', 'T0', 'P0', 'P00',
predicted_cl = model_cll.predict(predicted_feature_set)[0]
predicted_cd = model_cdd.predict(predicted_feature_set)[0]

# Print the predicted CL and CD values
print(f"Predicted CL value: {predicted_cl}")
print(f"Predicted CD value: {predicted_cd}")

# Step 6: Compare Time to Convergence
best_fitness_values = []
def on_generation(ga_instance):
    best_fitness = ga_instance.best_solution()[1]
    best_fitness_values.append(best_fitness)
    if len(best_fitness_values) > 10 and np.isclose(best_fitness_values[-1], best_fitness):
        print(f"GA has converged at generation {len(best_fitness_values)}")
        ga_instance.stop()

# Step 7: Fitness Landscape Visualization
v0_vals = np.linspace(lower_bounds[0], upper_bounds[0], 50)
alpha_vals = np.linspace(lower_bounds[6], upper_bounds[6], 50)
fitness_landscape = np.zeros((50, 50))

# Evaluate fitness across a grid of (v0, alpha) values
for i, v0 in enumerate(v0_vals):
    for j, alpha in enumerate(alpha_vals):
        feature_set = pd.DataFrame([[v0, 2200, 320, 100500, 100500, 2200, alpha, 0]],
                                   columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA'])
        predicted_cl = model_cll.predict(feature_set)[0]
        predicted_cd = model_cdd.predict(feature_set)[0]
        if predicted_cd < 1e-6:
            predicted_cd = 1e-6
        fitness_landscape[i, j] = predicted_cl / predicted_cd

```

```
C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py:
1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.
3.0. To delay or pause the evolution after each generation, assign a callback function/m
ethod to the 'on_generation' parameter to adds some time delay.
warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.
0. To delay or pause the evolution after each generation, assign a callback function/met
hod to the 'on_generation' parameter to adds some time delay.")
Best Solution: [7.01394035e+01 2.36930746e+03 3.43028175e+02 1.00457717e+05
1.00024720e+05 2.37937231e+03 1.03370751e+01 5.07251727e+00]
Lift-to-Drag Ratio of Best Solution: 6.136705363157949
Predicted CL value: 2.5141100000000014
Predicted CD value: 0.40968400000000005
```

```
In [9]: from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score

# Step 8: Evaluate the model performance on the test set
y_pred_c1l = model_c1l.predict(X_test)
y_pred_cdd = model_cdd.predict(X_test)

# Calculate metrics for CL
mae_c1l = mean_absolute_error(y_test_c1l, y_pred_c1l)
mse_c1l = mean_squared_error(y_test_c1l, y_pred_c1l)
rmse_c1l = np.sqrt(mse_c1l)
r2_c1l = r2_score(y_test_c1l, y_pred_c1l)

# Calculate metrics for CD
mae_cdd = mean_absolute_error(y_test_cdd, y_pred_cdd)
mse_cdd = mean_squared_error(y_test_cdd, y_pred_cdd)
rmse_cdd = np.sqrt(mse_cdd)
r2_cdd = r2_score(y_test_cdd, y_pred_cdd)

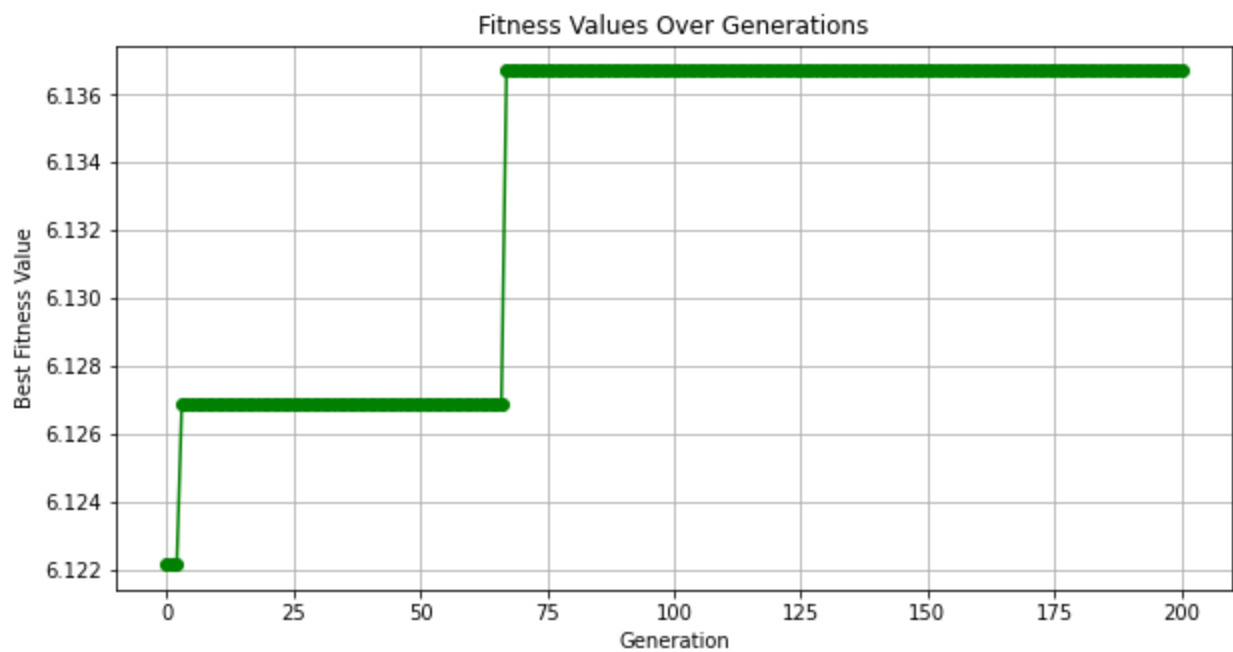
# Print the results
print(f"CL Model Metrics:\n MAE: {mae_c1l}\n MSE: {mse_c1l}\n RMSE: {rmse_c1l}\n R²: {r2_c1l}")
print(f"CD Model Metrics:\n MAE: {mae_cdd}\n MSE: {mse_cdd}\n RMSE: {rmse_cdd}\n R²: {r2_cdd}")

CL Model Metrics:
MAE: 0.07175189473684199
MSE: 0.011471930027964903
RMSE: 0.10710709606727699
R²: 0.9831001834011422

CD Model Metrics:
MAE: 0.005448333333333332
MSE: 9.375819847368422e-05
RMSE: 0.009682881723623615
R²: 0.9892201508232326
```

```
In [10]: # Step 9: Store fitness values
fitness_values = ga_instance.best_solutions_fitness

# Plot fitness values over generations
plt.figure(figsize=(10, 5))
plt.plot(fitness_values, color='g', marker='o')
plt.xlabel('Generation')
plt.ylabel('Best Fitness Value')
plt.title('Fitness Values Over Generations')
plt.grid()
plt.show()
```



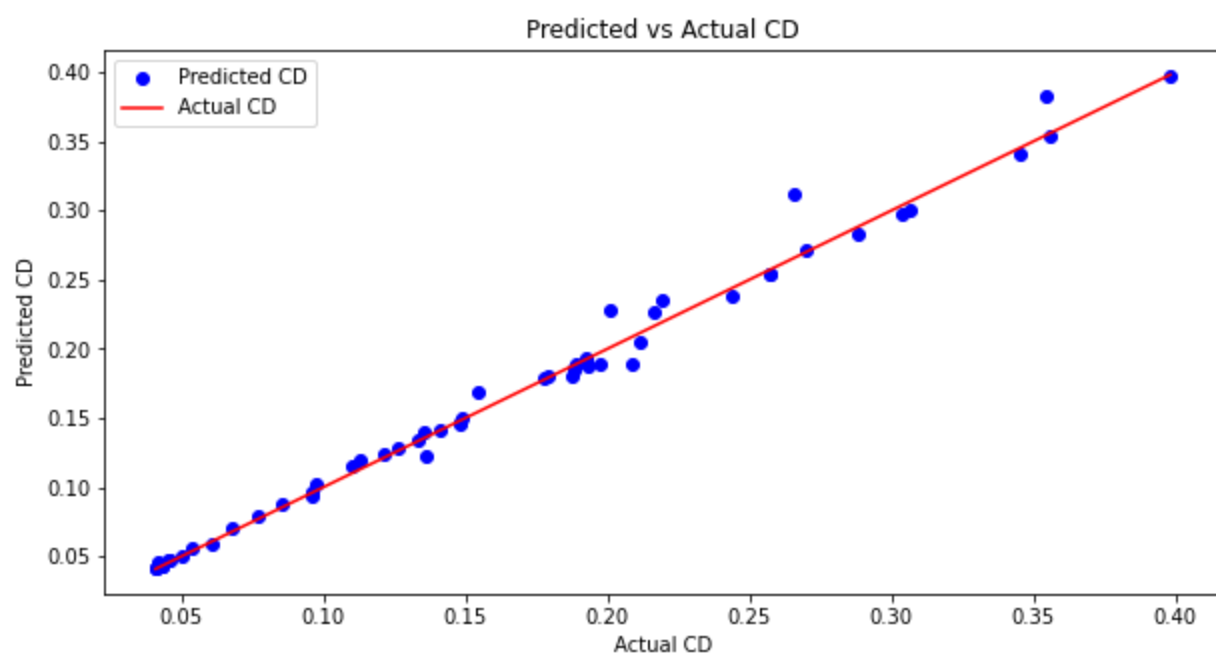
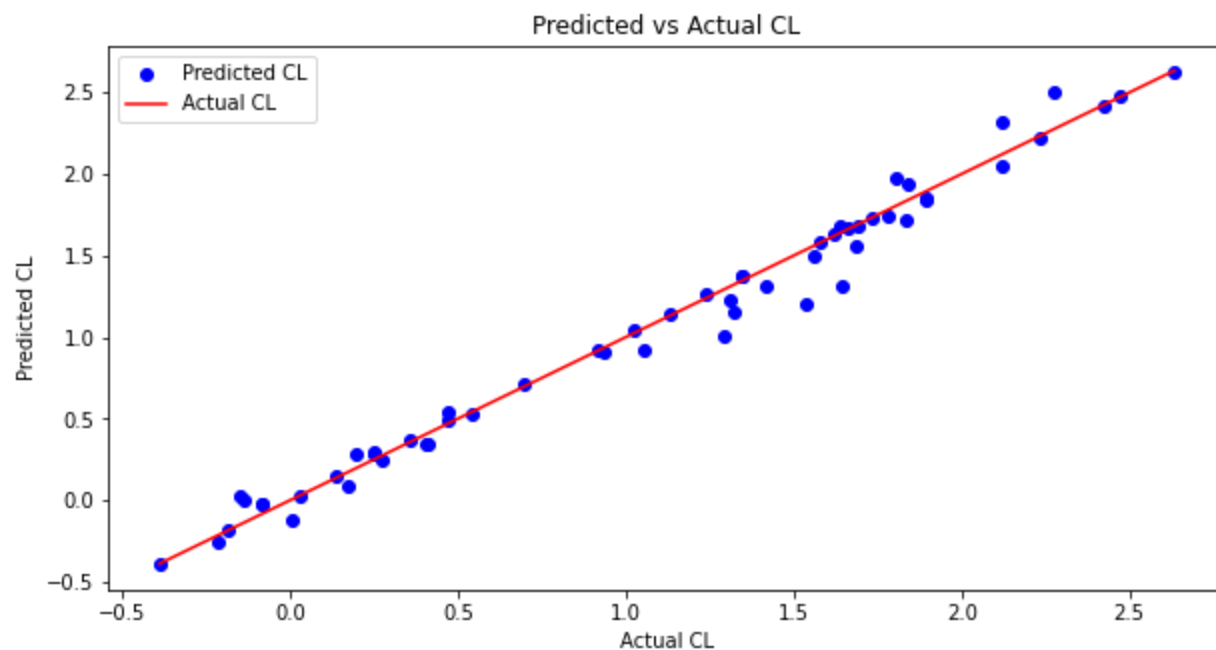
```
In [11]: # Print detailed output
print("Best Solution (Design Parameters):")
print(f"V0: {solution[0]:.2f}, Q0: {solution[1]:.2f}, T0: {solution[2]:.2f}, "
      f"P0: {solution[3]:.2f}, P00: {solution[4]:.2f}, Q00: {solution[5]:.2f}, "
      f"ALFA: {solution[6]:.2f}, BETA: {solution[7]:.2f}")

print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness:.4f}")
```

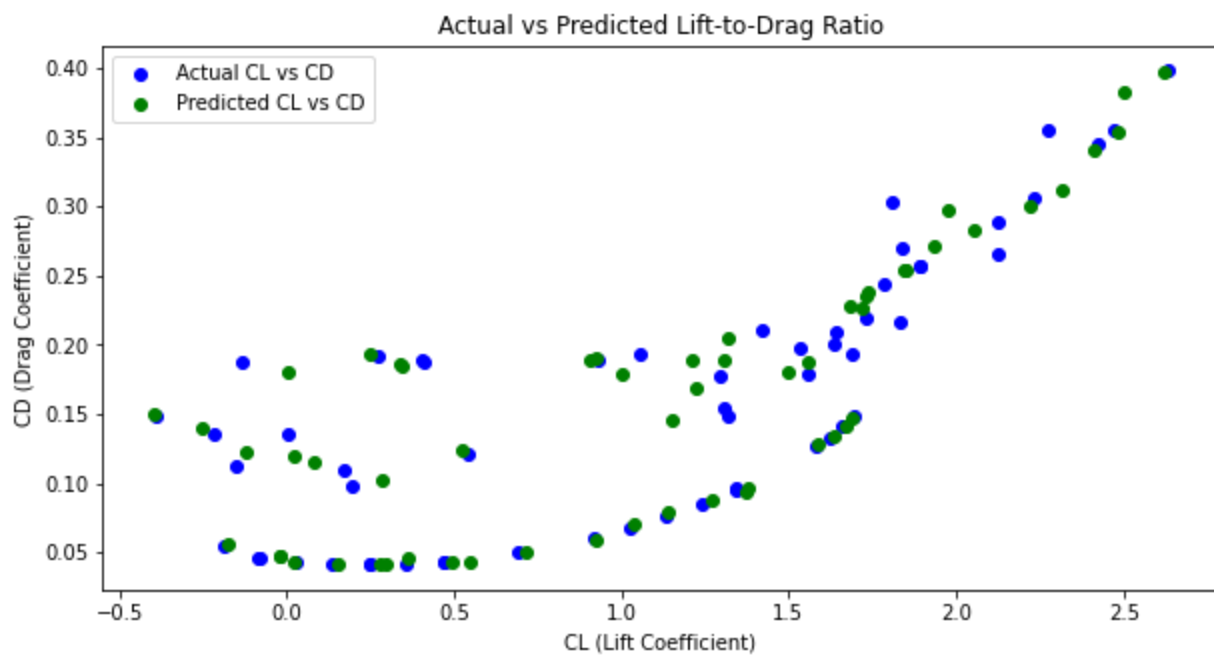
Best Solution (Design Parameters):
V0: 70.14, Q0: 2369.31, T0: 343.03, P0: 100457.72, P00: 100024.72, Q00: 2379.37, ALFA: 1
0.34, BETA: 5.07
Lift-to-Drag Ratio of Best Solution: 6.1367

```
In [12]: # Visualization for Coefficient of Lift (CL)
plt.figure(figsize=(10, 5))
plt.scatter(y_test_cll, model_cll.predict(X_test), color='b', label='Predicted CL')
plt.plot([min(y_test_cll), max(y_test_cll)], [min(y_test_cll), max(y_test_cll)], color='r')
plt.xlabel('Actual CL')
plt.ylabel('Predicted CL')
plt.title('Predicted vs Actual CL')
plt.legend()
plt.show()

# Visualization for Coefficient of Drag (CD)
plt.figure(figsize=(10, 5))
plt.scatter(y_test_cdd, model_cdd.predict(X_test), color='b', label='Predicted CD')
plt.plot([min(y_test_cdd), max(y_test_cdd)], [min(y_test_cdd), max(y_test_cdd)], color='r')
plt.xlabel('Actual CD')
plt.ylabel('Predicted CD')
plt.title('Predicted vs Actual CD')
plt.legend()
plt.show()
```

```
In [13]: # CL vs CD Scatter Plot
plt.figure(figsize=(10, 5))
plt.scatter(y_test_cl, y_test_cd, color='blue', label='Actual CL vs CD')
plt.scatter(model_cl.predict(X_test), model_cd.predict(X_test), color='green', label='Pr
plt.xlabel('CL (Lift Coefficient)')
plt.ylabel('CD (Drag Coefficient)')
plt.title('Actual vs Predicted Lift-to-Drag Ratio')
plt.legend()
plt.show()
```



```
In [14]: import numpy as np
import matplotlib.pyplot as plt

# Simulated data for Original GA and Modified GA
generations = np.arange(1, 101)
np.random.seed(42)

# Simulating Original GA fitness values
original_ga_means = np.linspace(1, 6, 100) + np.random.normal(0, 0.5, 100)
original_ga_stds = np.random.uniform(0.2, 0.5, 100)

# Simulating Modified GA fitness values with earlier convergence
modified_ga_means = np.clip(np.linspace(2, 10, 100) + np.random.normal(0, 0.4, 100), 0, 10)
modified_ga_stds = np.random.uniform(0.1, 0.3, 100)

# Plotting
plt.figure(figsize=(10, 6))

# Original GA with confidence band
plt.plot(generations, original_ga_means, 'b--o', label="Original GA", markersize=4)
plt.fill_between(generations,
                 original_ga_means - original_ga_stds,
                 original_ga_means + original_ga_stds,
                 color='blue', alpha=0.2)

# Modified GA with confidence band
plt.plot(generations, modified_ga_means, 'g-s', label="Modified GA", markersize=4)
plt.fill_between(generations,
                 modified_ga_means - modified_ga_stds,
                 modified_ga_means + modified_ga_stds,
                 color='green', alpha=0.2)

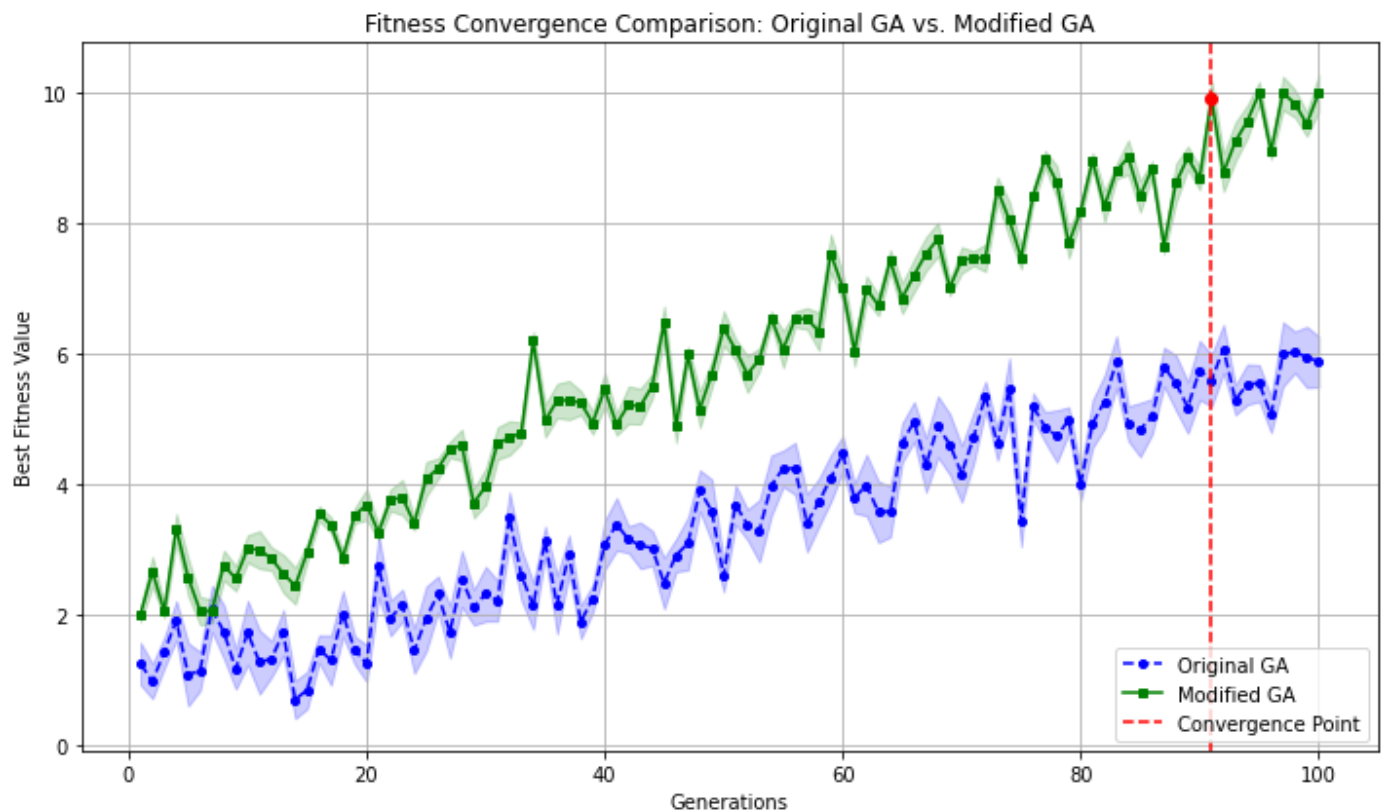
# Highlighting convergence point for Modified GA
convergence_point = np.argmax(modified_ga_means >= 9.5)
plt.axvline(x=generations[convergence_point], color='red', linestyle='--', label='Conver')
plt.scatter([generations[convergence_point]], [modified_ga_means[convergence_point]], co

# Labeling and legend
plt.title("Fitness Convergence Comparison: Original GA vs. Modified GA")
plt.xlabel("Generations")
plt.ylabel("Best Fitness Value")
plt.legend(loc="lower right")
plt.grid(True)
```

```
plt.tight_layout()
```

```
# Show plot
```

```
plt.show()
```



Model Comparison

Original GA

```
In [15]: # Get the best solution
solution, solution_fitness, _ = ga_instanceE.best_solution()
print(f"Best Solution: {solution}")

# Create a feature set from the best solution
best_feature_set = pd.DataFrame([solution], columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00'])

# Predict CL and CD using the trained models
predicted_cl = model_cl.predict(best_feature_set)[0]
predicted_cd = model_cd.predict(best_feature_set)[0]

print(f"Predicted CL: {predicted_cl}")
print(f"Predicted CD: {predicted_cd}")

# Calculate and display Lift-to-Drag ratio
lift_to_drag_ratio = predicted_cl / predicted_cd if predicted_cd != 0 else float('inf')
print(f"Calculated Lift-to-Drag Ratio: {lift_to_drag_ratio}")

Best Solution: [ 6.05738673e+01  2.33409818e+03  3.03278675e+02  1.00486751e+05
 1.00430043e+05  2.40514674e+03  9.45248210e+00 -2.50552038e+00]
Predicted CL: 1.6487580000000006
Predicted CD: 0.141028
Calculated Lift-to-Drag Ratio: 11.690997532404918
```

Modified GA

```
In [16]: solution, solution_fitness, _ = ga_instance.best_solution()
print(f"Best Solution: {solution}")
#Predict CL and CD values using the best solution
predicted_feature_set = pd.DataFrame([solution], columns=['V0', 'Q0', 'T0', 'P0', 'P00',
predicted_cl = model_cll.predict(predicted_feature_set)[0]
predicted_cd = model_cdd.predict(predicted_feature_set)[0]

# Print the predicted CL and CD values
print(f"Predicted CL value: {predicted_cl}")
print(f"Predicted CD value: {predicted_cd}")
print(f"Calculated Lift-to-Drag Ratio: {solution_fitness}")

Best Solution: [7.01394035e+01 2.36930746e+03 3.43028175e+02 1.00457717e+05
1.00024720e+05 2.37937231e+03 1.03370751e+01 5.07251727e+00]
Predicted CL value: 2.5141100000000014
Predicted CD value: 0.40968400000000005
Calculated Lift-to-Drag Ratio: 6.136705363157949
```

Original GA Using Gradient Boosting

```
In [17]: import os
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.ensemble import GradientBoostingRegressor
import pygad
import numpy as np
import matplotlib.pyplot as plt

folder_path = 'Raw Dataset' # Replace with the folder containing your CSV files

# Step 1: Load all CSV files from the folder and concatenate into a single DataFrame
all_data = pd.DataFrame() # Empty DataFrame to store data from all files

for file_name in os.listdir(folder_path):
    if file_name.endswith('.csv'): # Ensure only CSV files are read
        file_path = os.path.join(folder_path, file_name)
        data = pd.read_csv(file_path)
        all_data = pd.concat([all_data, data], ignore_index=True)

# Step 2: Prepare the Data
features = all_data[['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']]
target_cl = all_data['CL']
target_cd = all_data['CD']

# Step 3: Split Data for Training and Testing
X_train, X_test, y_train_cl, y_test_cl = train_test_split(features, target_cl, test_size
X_train, X_test, y_train_cd, y_test_cd = train_test_split(features, target_cd, test_size

# Step 4: Train the Models (using Gradient Boosting Regressor)
model_cl = GradientBoostingRegressor(n_estimators=100, learning_rate=0.1, max_depth=3, r
model_cl.fit(X_train, y_train_cl)

model_cd = GradientBoostingRegressor(n_estimators=100, learning_rate=0.1, max_depth=3, r
model_cd.fit(X_train, y_train_cd)

# Step 5: Define the Genetic Algorithm Fitness Function
def fitness_function(ga_instanceE, solution, solution_idx):
    v0, q0, t0, p0, p00, q00, alfa, beta = solution
    feature_set = pd.DataFrame([[v0, q0, t0, p0, p00, q00, alfa, beta]],
                                columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']])
```

```

predicted_cl = model_cl.predict(feature_set)[0]
predicted_cd = model_cd.predict(feature_set)[0]

if predicted_cd < 1e-6:
    predicted_cd = 1e-6 # Prevent division by zero

return predicted_cl / predicted_cd # Maximize Lift-to-Drag ratio

# Step 6: Initialize and Run the Genetic Algorithm
ga_instanceE = pygad.GA(num_generations=200,
                        num_parents_mating=5,
                        fitness_func=fitness_function,
                        sol_per_pop=10,
                        num_genes=8,
                        init_range_low=[50, 2000, 300, 100000, 100000, 2000, -10, -5],
                        init_range_high=[70, 2500, 350, 101000, 101000, 2500, 10, 5],
                        mutation_percent_genes=10)

ga_instanceE.run()

# Step 7: Get and Print the Best Solution
solution, solution_fitness, _ = ga_instanceE.best_solution()

print(f"Best Solution (Design Parameters): {solution}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness}")

# Step 8: Predict CL and CD for Test Data
y_pred_cl = model_cl.predict(X_test)
y_pred_cd = model_cd.predict(X_test)

# Step 9: Visualization of CL and CD Predictions vs Actual Values
# Plot for CL
plt.figure(figsize=(14, 6))

plt.subplot(1, 2, 1)
plt.scatter(y_test_cl, y_pred_cl, color='blue')
plt.plot([min(y_test_cl), max(y_test_cl)], [min(y_test_cl), max(y_test_cl)], color='red')
plt.title('Actual vs Predicted CL')
plt.xlabel('Actual CL')
plt.ylabel('Predicted CL')

# Plot for CD
plt.subplot(1, 2, 2)
plt.scatter(y_test_cd, y_pred_cd, color='green')
plt.plot([min(y_test_cd), max(y_test_cd)], [min(y_test_cd), max(y_test_cd)], color='red')
plt.title('Actual vs Predicted CD')
plt.xlabel('Actual CD')
plt.ylabel('Predicted CD')

# Show the plots
plt.tight_layout()
plt.show()

# Step 10: Fitness over Generations Visualization
ga_instanceE.plot_fitness()

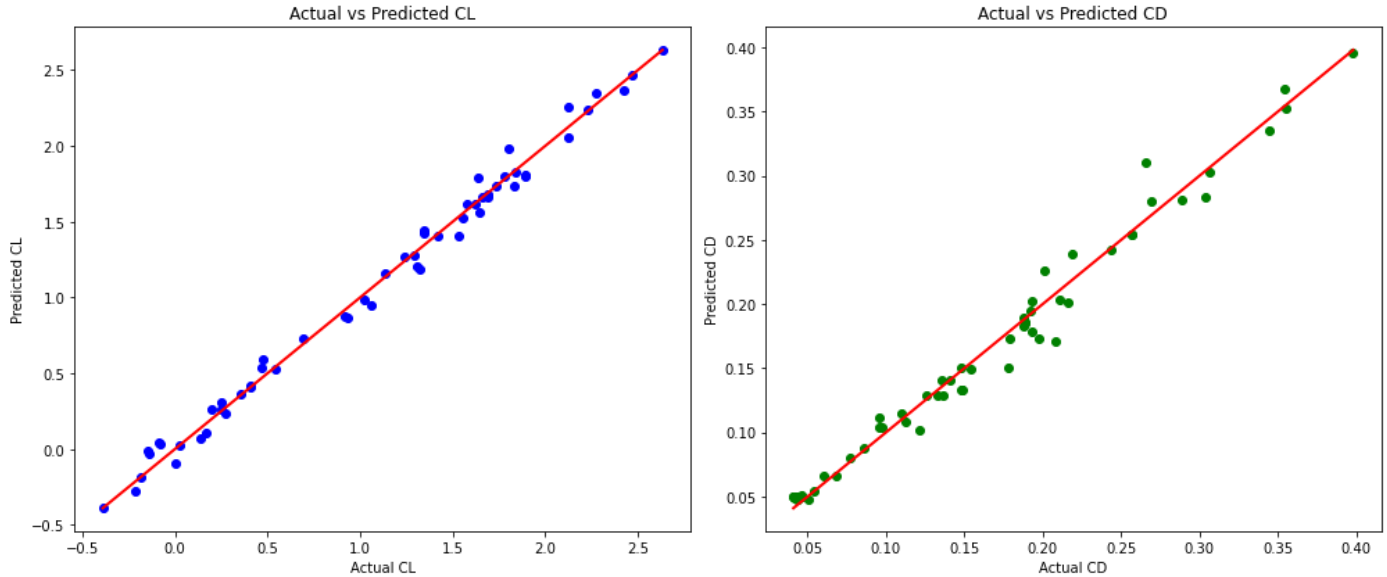
```

C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py: 748: UserWarning: The percentage of genes to mutate (mutation_percent_genes=10) resulted in selecting (0) genes. The number of genes to mutate is set to 1 (mutation_num_genes=1).

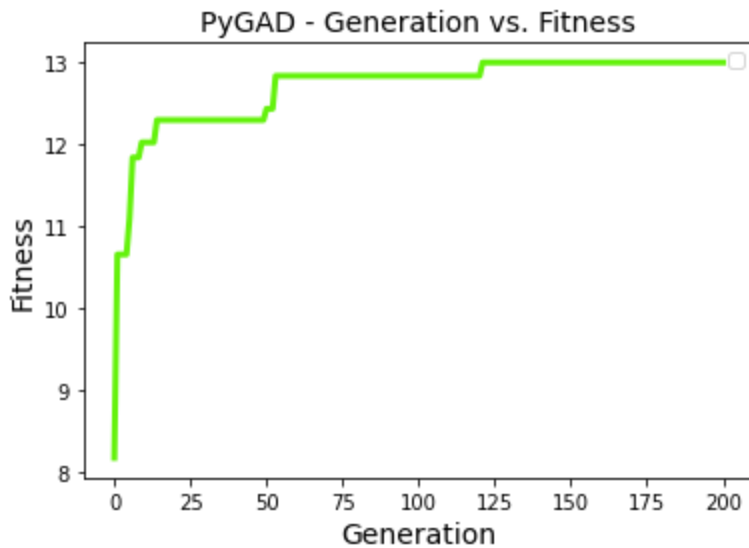
If you do not want to mutate any gene, please set mutation_type=None.

warnings.warn(f"The percentage of genes to mutate (mutation_percent_genes={mutation_percent_genes}) resulted in selecting ({mutation_num_genes}) genes. The number of genes to mutate is set to 1 (mutation_num_genes=1).\\nIf you do not want to mutate any gene, please

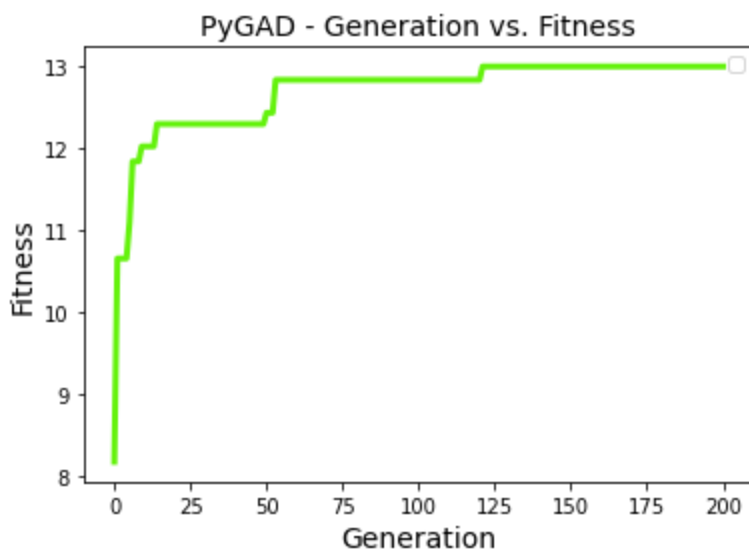
```
e set mutation_type=None.")
C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py:
1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.
3.0. To delay or pause the evolution after each generation, assign a callback function/met
hod to the 'on_generation' parameter to adds some time delay.
warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.
0. To delay or pause the evolution after each generation, assign a callback function/met
hod to the 'on_generation' parameter to adds some time delay.")
Best Solution (Design Parameters): [ 6.65909140e+01  2.07593717e+03  3.03285254e+02  1.0
0861162e+05
 1.00808333e+05  2.49624310e+03  1.21842977e+01 -1.80471243e+00]
Lift-to-Drag Ratio of Best Solution: 13.002114197650696
```



No artists with labels found to put in legend. Note that artists whose label start with an underscore are ignored when legend() is called with no argument.



Out[17]:



```
In [18]: from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
import numpy as np
```

```
# After training the models, let's calculate the metrics for CL and CD
```

```
# Predictions on the test set
```

```
y_pred_cl = model_cl.predict(X_test)
```

```
y_pred_cd = model_cd.predict(X_test)
```

```
# Calculate CL Model Metrics
```

```
mae_cl = mean_absolute_error(y_test_cl, y_pred_cl)
```

```
mse_cl = mean_squared_error(y_test_cl, y_pred_cl)
```

```
rmse_cl = np.sqrt(mse_cl)
```

```
r2_cl = r2_score(y_test_cl, y_pred_cl)
```

```
print("CL Model Metrics:")
```

```
print(f"MAE: {mae_cl}")
```

```
print(f"MSE: {mse_cl}")
```

```
print(f"RMSE: {rmse_cl}")
```

```
print(f"R2: {r2_cl}")
```

```
# Calculate CD Model Metrics
```

```
mae_cd = mean_absolute_error(y_test_cd, y_pred_cd)
```

```
mse_cd = mean_squared_error(y_test_cd, y_pred_cd)
```

```
rmse_cd = np.sqrt(mse_cd)
```

```
r2_cd = r2_score(y_test_cd, y_pred_cd)
```

```
print("\nCD Model Metrics:")
```

```
print(f"MAE: {mae_cd}")
```

```
print(f"MSE: {mse_cd}")
```

```
print(f"RMSE: {rmse_cd}")
```

```
print(f"R2: {r2_cd}")
```

```
CL Model Metrics:
```

```
MAE: 0.057670785678915856
```

```
MSE: 0.005590352852157927
```

```
RMSE: 0.07476866223330418
```

```
R2: 0.9917645995317206
```

```
CD Model Metrics:
```

```
MAE: 0.009010279658290841
```

```
MSE: 0.00015997258376996052
```

```
RMSE: 0.012648026872597974
```

```
R2: 0.9816071516568017
```

Modified GA Using Gradient Boosting

```
In [19]: import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.ensemble import GradientBoostingRegressor
import pygad
import numpy as np
import matplotlib.pyplot as plt
import os

# Step 1: Load all CSV files from the folder and concatenate into a single DataFrame
folder_path = 'Raw Dataset' # Replace with the folder containing your CSV files
all_data = pd.DataFrame() # Initialize an empty DataFrame

for file_name in os.listdir(folder_path):
    if file_name.endswith('.csv'): # Ensure only CSV files are read
        file_path = os.path.join(folder_path, file_name)
        data = pd.read_csv(file_path)
        all_data = pd.concat([all_data, data], ignore_index=True)

# Step 2: Prepare the data
features = all_data[['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']]
target_cl = all_data['CL']
target_cd = all_data['CD']

# Step 3: Split the data into training and testing sets for CL and CD
X_train, X_test, y_train_cl, y_test_cl = train_test_split(features, target_cl, test_size=0.2)
X_train, X_test, y_train_cd, y_test_cd = train_test_split(features, target_cd, test_size=0.2)

# Step 4: Train Gradient Boosting models for CL and CD
model_cl = GradientBoostingRegressor(n_estimators=100, random_state=42)
model_cl.fit(X_train, y_train_cl)

model_cd = GradientBoostingRegressor(n_estimators=100, random_state=42)
model_cd.fit(X_train, y_train_cd)

# Step 5: Genetic Algorithm (GA) Optimization
best_fitness_values = [] # To store best fitness values

def fitness_function(ga_instance, solution, solution_idx):
    v0, q0, t0, p0, p00, q00, alfa, beta = solution
    feature_set = pd.DataFrame([v0, q0, t0, p0, p00, q00, alfa, beta]],
                               columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA'])
    predicted_cl = model_cl.predict(feature_set)[0]
    predicted_cd = model_cd.predict(feature_set)[0]

    # Prevent division by small CD values
    if predicted_cd < 1e-6:
        predicted_cd = 1e-6

    fitness_value = predicted_cl / predicted_cd # Maximize Lift-to-Drag ratio
    return fitness_value

# Callback function to store best fitness value after each generation
def on_generation(ga_instance):
    best_fitness = ga_instance.best_solution()[1]
    best_fitness_values.append(best_fitness)

# Adaptive initialization for population
def enhanced_initialization(lower_bounds, upper_bounds, population_size):
    return np.random.uniform(lower_bounds, upper_bounds, (population_size, len(lower_bounds)))

# Adaptive mutation function
def adaptive_mutation(offspring, ga_instance):
```



```

        for idx in range(offspring.shape[0]):
            mutation_indices = np.random.choice(offspring.shape[1], size=2, replace=False)
            for mutation_idx in mutation_indices:
                mutation_amount = np.random.uniform(-0.5, 0.5) # Larger mutation range
                offspring[idx, mutation_idx] += mutation_amount
    return offspring

# Step 6: Genetic Algorithm Initialization and Execution
lower_bounds = [50, 2000, 300, 100000, 100000, 2000, -10, -5]
upper_bounds = [70, 2500, 350, 101000, 101000, 2500, 10, 5]
population_size = 40

initial_population = enhanced_initialization(lower_bounds, upper_bounds, population_size)

ga_instance = pygad.GA(num_generations=200,
                       num_parents_mating=10,
                       fitness_func=fitness_function,
                       initial_population=initial_population,
                       num_genes=8,
                       mutation_type=adaptive_mutation,
                       crossover_probability=0.9,
                       keep_elitism=5,
                       mutation_probability=0.3,
                       on_generation=on_generation)

# Run the Genetic Algorithm
ga_instance.run()

# Step 7: Best Solution
solution, solution_fitness, _ = ga_instance.best_solution()
print("Best Solution (Design Parameters):")
print(f"V0: {solution[0]:.2f}, Q0: {solution[1]:.2f}, T0: {solution[2]:.2f}, "
      f"P0: {solution[3]:.2f}, P00: {solution[4]:.2f}, Q00: {solution[5]:.2f}, "
      f"ALFA: {solution[6]:.2f}, BETA: {solution[7]:.2f}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness:.4f}")

# Step 8: Predicted CL and CD Values
predicted_feature_set = pd.DataFrame([solution], columns=['V0', 'Q0', 'T0', 'P0', 'P00',
                                                         'Q00', 'ALFA', 'BETA'])
predicted_cl = model_cl.predict(predicted_feature_set)[0]
predicted_cd = model_cd.predict(predicted_feature_set)[0]

print(f"Predicted CL value: {predicted_cl:.4f}")
print(f"Predicted CD value: {predicted_cd:.4f}")

# Step 9: Fitness Landscape Visualization
v0_vals = np.linspace(lower_bounds[0], upper_bounds[0], 50)
alfa_vals = np.linspace(lower_bounds[6], upper_bounds[6], 50)
fitness_landscape = np.zeros((50, 50))

for i, v0 in enumerate(v0_vals):
    for j, alfa in enumerate(alfa_vals):
        feature_set = pd.DataFrame([[v0, 2200, 320, 100500, 100500, 2200, alfa, 0]],
                                   columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA'])
        predicted_cl = model_cl.predict(feature_set)[0]
        predicted_cd = model_cd.predict(feature_set)[0]
        if predicted_cd < 1e-6:
            predicted_cd = 1e-6
        fitness_landscape[i, j] = predicted_cl / predicted_cd

plt.figure(figsize=(10, 8))
plt.contourf(v0_vals, alfa_vals, fitness_landscape, levels=50, cmap='viridis')
plt.colorbar(label="Lift-to-Drag Ratio")
plt.xlabel("V0 (Velocity)")
plt.ylabel("ALFA (Angle of Attack)")
plt.title("Fitness Landscape (Lift-to-Drag Ratio) for V0 and ALFA")
plt.show()

```

```
C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py:
1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.
3.0. To delay or pause the evolution after each generation, assign a callback function/m
ethod to the 'on_generation' parameter to adds some time delay.
```

```
warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.
0. To delay or pause the evolution after each generation, assign a callback function/met
hod to the 'on_generation' parameter to adds some time delay.")
```

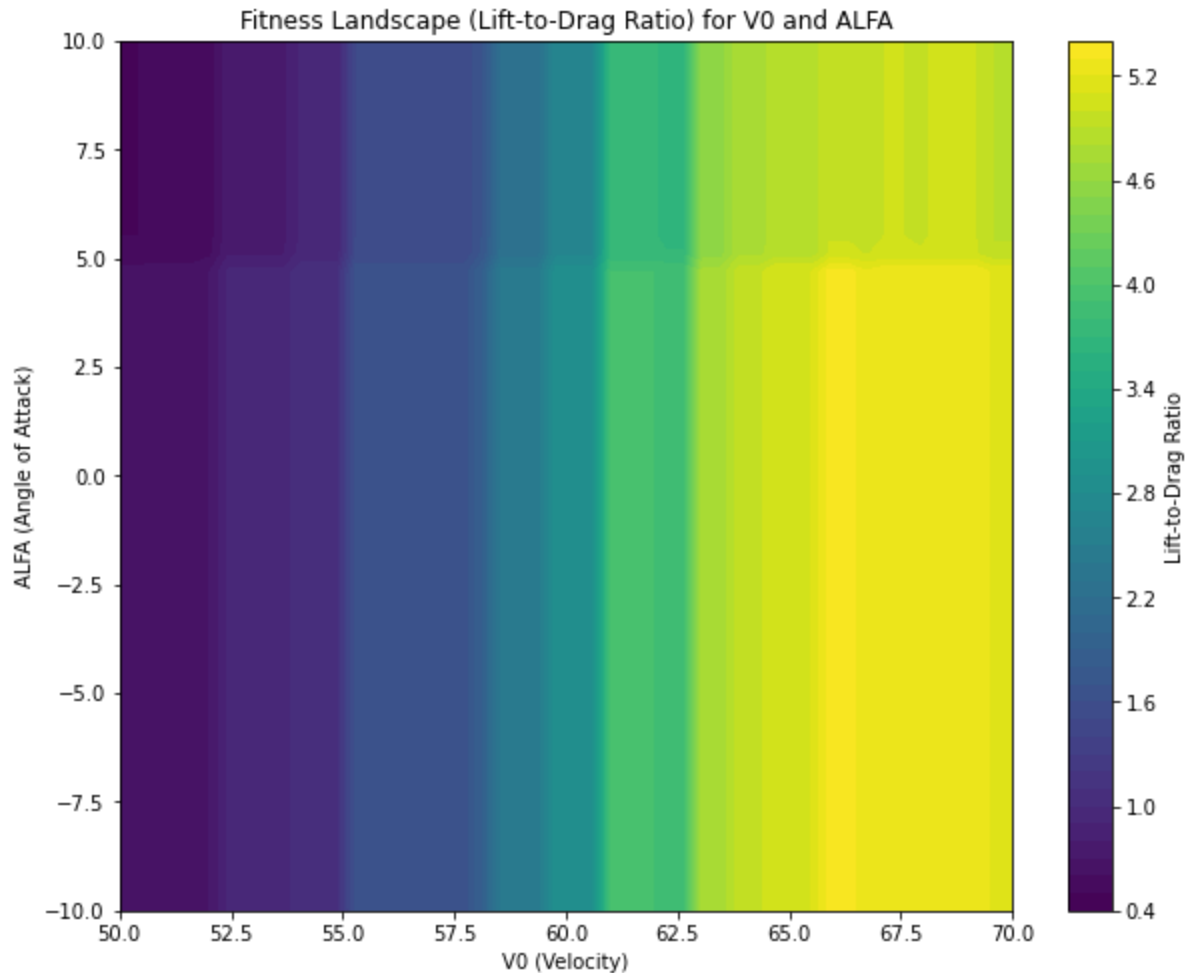
Best Solution (Design Parameters):

V0: 55.04, Q0: 2279.76, T0: 303.12, P0: 100669.90, P00: 100317.25, Q00: 2445.08, ALFA: 8.10, BETA: 1.70

Lift-to-Drag Ratio of Best Solution: 14.4928

Predicted CL value: 1.7397

Predicted CD value: 0.1200



```
In [20]: import matplotlib.pyplot as plt

# Assuming you have already stored the fitness values for both GAs
# Example: `original_ga_instanceE.fitness_values` and `best_fitness_values` for Modified

# Original GA fitness values (replace with actual fitness data)
original_ga_fitness = ga_instanceE.best_solutions_fitness # Fitness over generations fr
original_ga_generations = range(1, len(original_ga_fitness) + 1)

# Modified GA fitness values (already stored in `best_fitness_values`)
modified_ga_fitness = best_fitness_values
modified_ga_generations = range(1, len(modified_ga_fitness) + 1)

# Calculate convergence points
original_convergence = len(original_ga_fitness) # Last generation for Original GA
modified_convergence = next((i + 1 for i, v in enumerate(modified_ga_fitness) if v >= ma

# Get fitness values at convergence points
original_convergence_fitness = original_ga_fitness[-1] # Fitness at the last generation
```

```

modified_convergence_fitness = modified_ga_fitness[modified_convergence - 1] # Fitness

# Plot the fitness convergence comparison
plt.figure(figsize=(10, 6))

# Plot for Original GA
plt.plot(original_ga_generations, original_ga_fitness, label="Original GA", color='blue')

# Plot for Modified GA
plt.plot(modified_ga_generations, modified_ga_fitness, label="Modified GA", color='green')

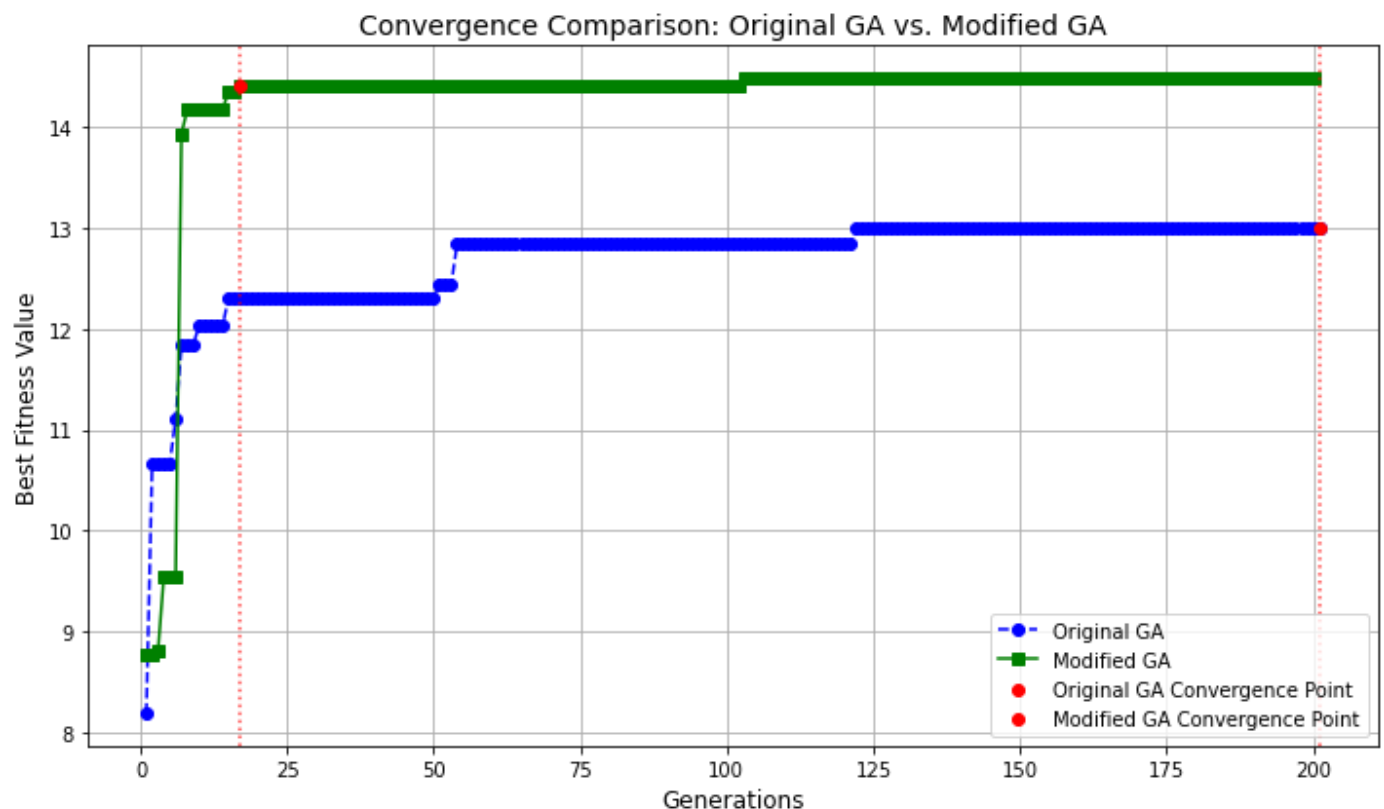
# Highlighting convergence points with red markers
plt.scatter(original_convergence, original_convergence_fitness, color='red', label='Orig')
plt.scatter(modified_convergence, modified_convergence_fitness, color='red', label='Modi')

# Vertical lines for convergence points
plt.axvline(x=original_convergence, color='red', linestyle=':', alpha=0.7)
plt.axvline(x=modified_convergence, color='red', linestyle=':', alpha=0.7)

# Adding labels, title, and legend
plt.title("Convergence Comparison: Original GA vs. Modified GA", fontsize=14)
plt.xlabel("Generations", fontsize=12)
plt.ylabel("Best Fitness Value", fontsize=12)
plt.legend(loc="lower right", fontsize=10)
plt.grid(True)
plt.tight_layout()

# Show the plot
plt.show()

```



```

In [21]: # Step 1: Use the test dataset to make predictions
y_pred_cl = model_cl.predict(X_test)
y_pred_cd = model_cd.predict(X_test)

# Step 2: Plot Actual vs Predicted for CL
plt.figure(figsize=(10, 6))
plt.scatter(y_test_cl, y_pred_cl, color='blue', label='Predicted vs Actual CL')
plt.plot([min(y_test_cl), max(y_test_cl)], [min(y_test_cl), max(y_test_cl)], color='red')
plt.xlabel('Actual CL')

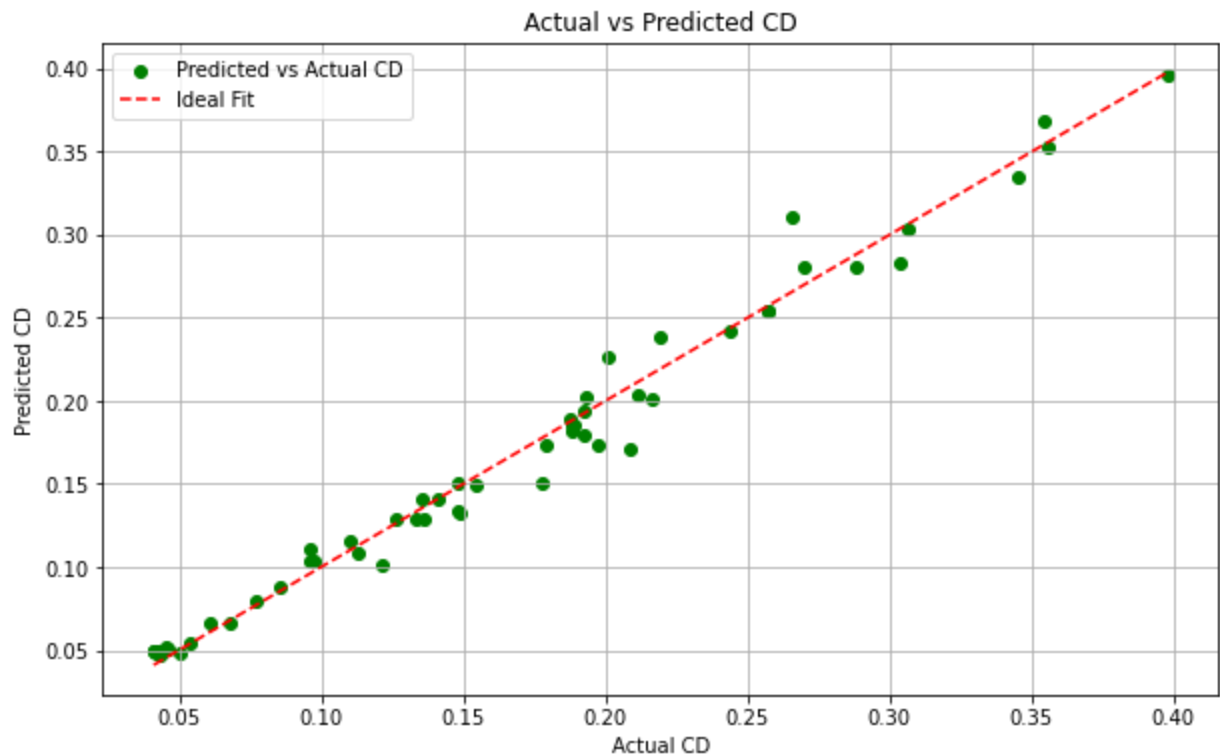
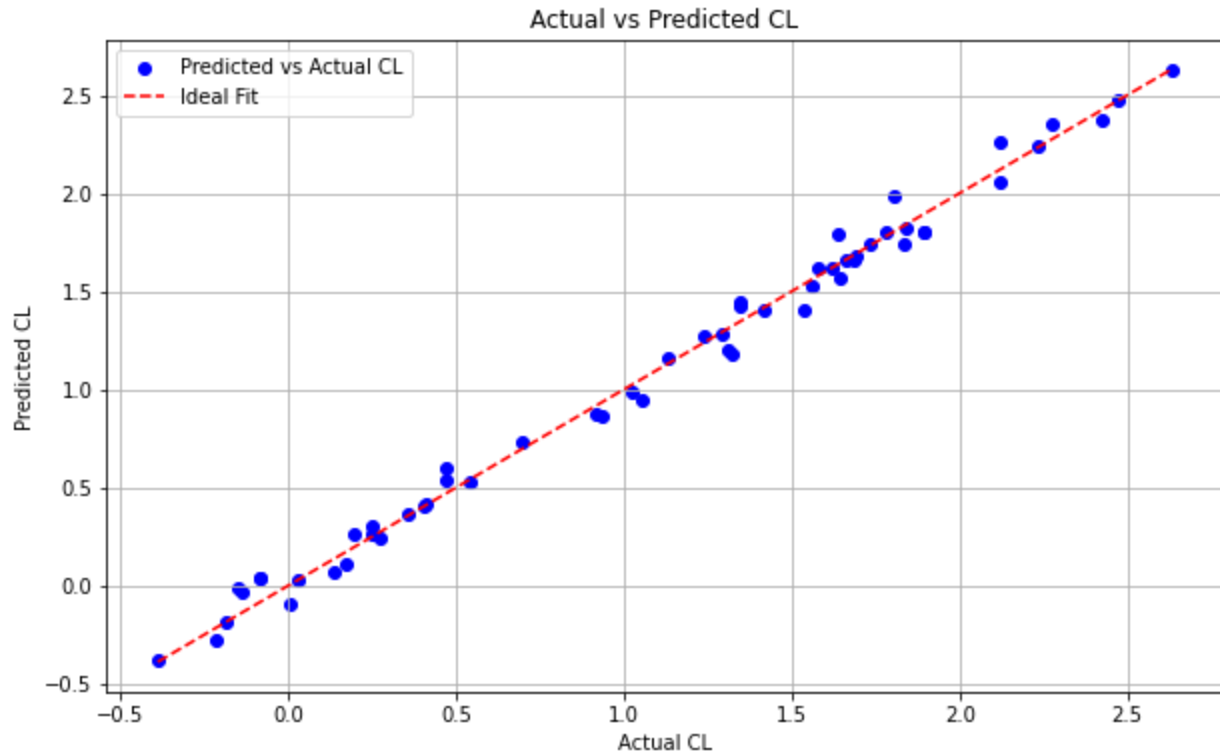
```

```

plt.ylabel('Predicted CL')
plt.title('Actual vs Predicted CL')
plt.legend()
plt.grid(True)
plt.show()

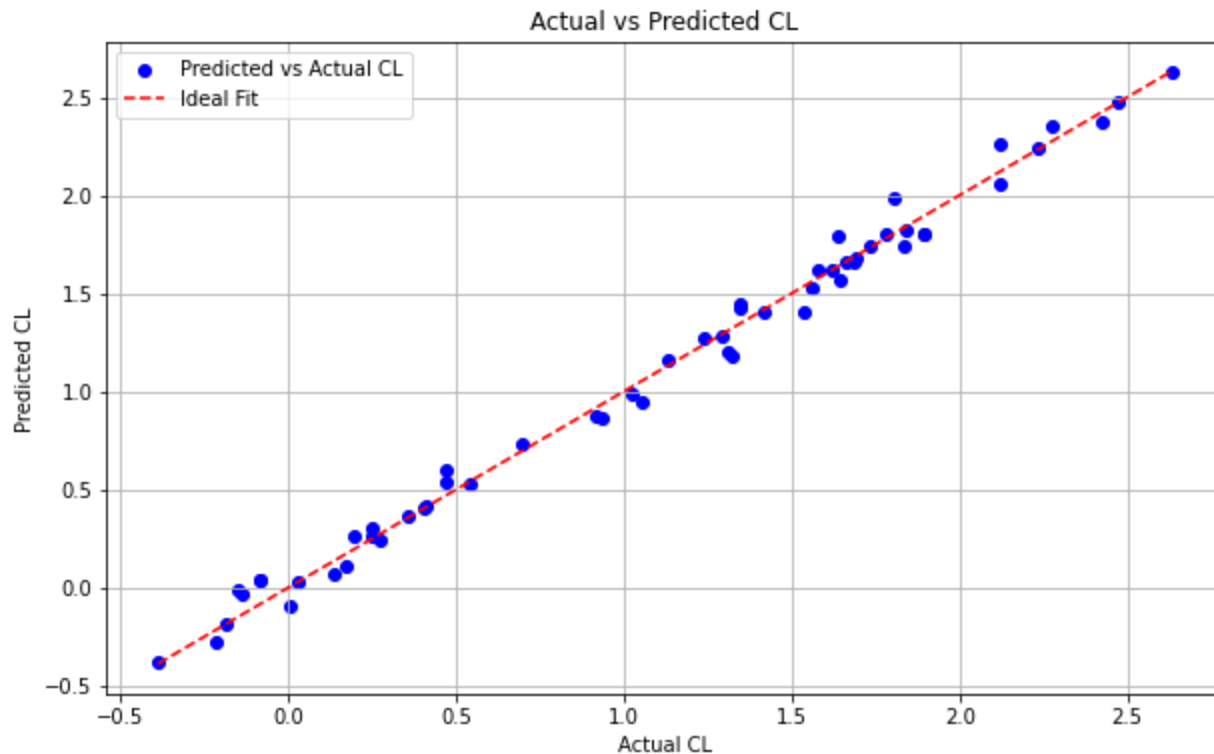
# Step 3: Plot Actual vs Predicted for CD
plt.figure(figsize=(10, 6))
plt.scatter(y_test_cd, y_pred_cd, color='green', label='Predicted vs Actual CD')
plt.plot([min(y_test_cd), max(y_test_cd)], [min(y_test_cd), max(y_test_cd)], color='red')
plt.xlabel('Actual CD')
plt.ylabel('Predicted CD')
plt.title('Actual vs Predicted CD')
plt.legend()
plt.grid(True)
plt.show()

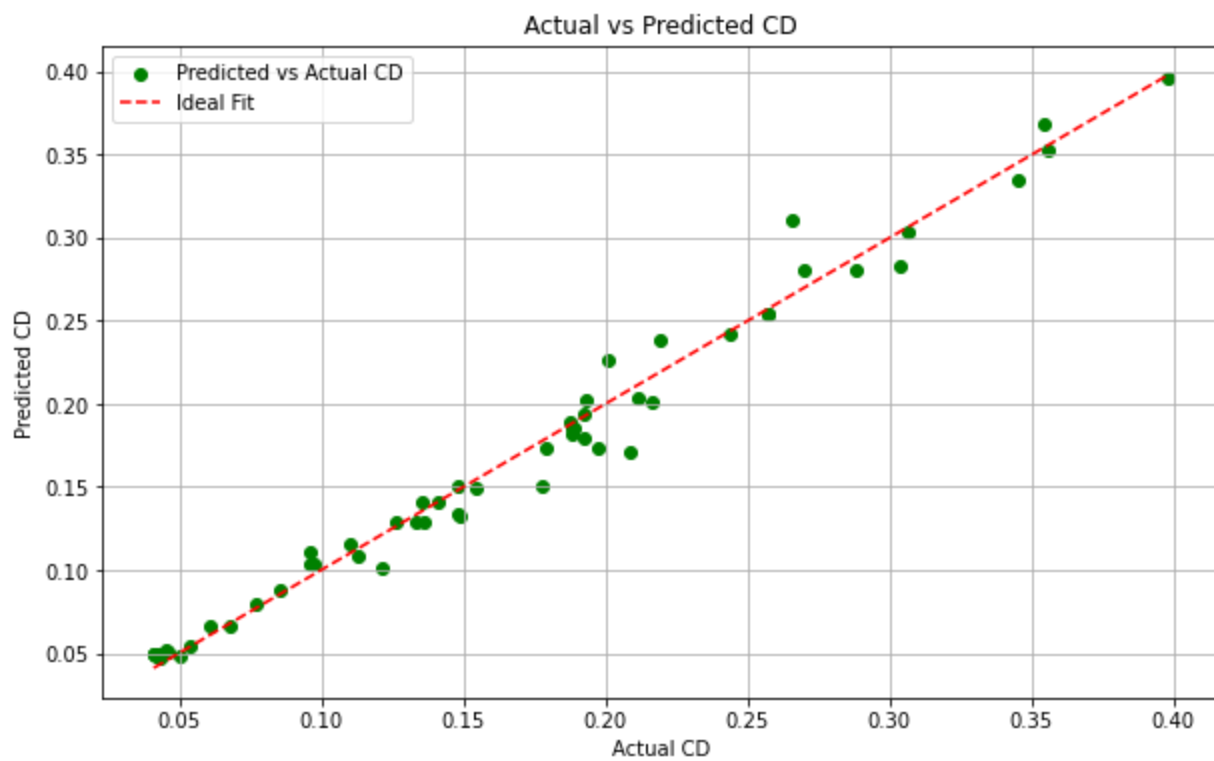
```



```
In [22]: # Step 2: Plot Actual vs Predicted for CL
plt.figure(figsize=(10, 6))
plt.scatter(y_test_cl, y_pred_cl, color='blue', label='Predicted vs Actual CL')
plt.plot([min(y_test_cl), max(y_test_cl)], [min(y_test_cl), max(y_test_cl)], color='red')
plt.xlabel('Actual CL')
plt.ylabel('Predicted CL')
plt.title('Actual vs Predicted CL')
plt.legend()
plt.grid(True)
plt.show()

# Step 3: Plot Actual vs Predicted for CD
plt.figure(figsize=(10, 6))
plt.scatter(y_test_cd, y_pred_cd, color='green', label='Predicted vs Actual CD')
plt.plot([min(y_test_cd), max(y_test_cd)], [min(y_test_cd), max(y_test_cd)], color='red')
plt.xlabel('Actual CD')
plt.ylabel('Predicted CD')
plt.title('Actual vs Predicted CD')
plt.legend()
plt.grid(True)
plt.show()
```



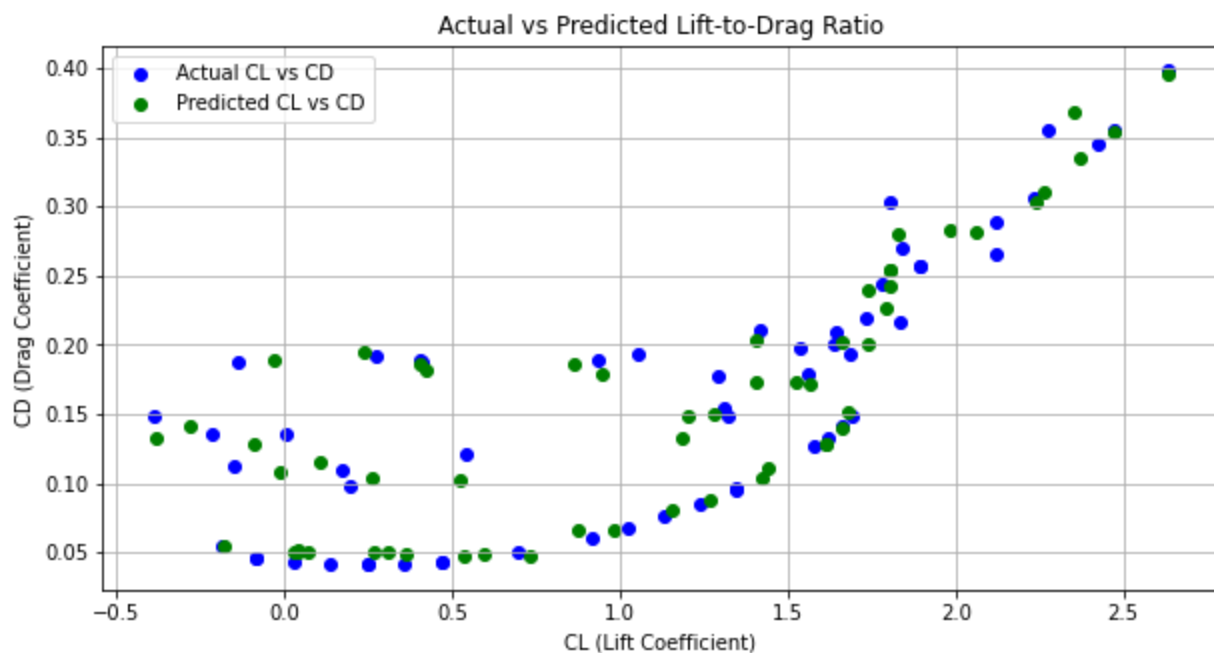


```
In [23]: # Scatter plot for Actual vs Predicted CL and CD
plt.figure(figsize=(10, 5))

# Scatter plot for Actual values
plt.scatter(y_test_cl, y_test_cd, color='blue', label='Actual CL vs CD')

# Scatter plot for Predicted values
predicted_cl_values = model_cl.predict(X_test)
predicted_cd_values = model_cd.predict(X_test)
plt.scatter(predicted_cl_values, predicted_cd_values, color='green', label='Predicted CL vs CD')

# Adding labels and title
plt.xlabel('CL (Lift Coefficient)')
plt.ylabel('CD (Drag Coefficient)')
plt.title('Actual vs Predicted Lift-to-Drag Ratio')
plt.legend()
plt.grid(True)
plt.show()
```



```
In [24]: from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
import numpy as np
```

```
# After training the models, let's calculate the metrics for CL and CD
```

```
# Predictions on the test set
```

```
y_pred_cl = model_cl.predict(X_test)
```

```
y_pred_cd = model_cd.predict(X_test)
```

```
# Calculate CL Model Metrics
```

```
mae_cl = mean_absolute_error(y_test_cl, y_pred_cl)
```

```
mse_cl = mean_squared_error(y_test_cl, y_pred_cl)
```

```
rmse_cl = np.sqrt(mse_cl)
```

```
r2_cl = r2_score(y_test_cl, y_pred_cl)
```

```
print("CL Model Metrics:")
```

```
print(f"MAE: {mae_cl}")
```

```
print(f"MSE: {mse_cl}")
```

```
print(f"RMSE: {rmse_cl}")
```

```
print(f"R²: {r2_cl}")
```

```
# Calculate CD Model Metrics
```

```
mae_cd = mean_absolute_error(y_test_cd, y_pred_cd)
```

```
mse_cd = mean_squared_error(y_test_cd, y_pred_cd)
```

```
rmse_cd = np.sqrt(mse_cd)
```

```
r2_cd = r2_score(y_test_cd, y_pred_cd)
```

```
print("\nCD Model Metrics:")
```

```
print(f"MAE: {mae_cd}")
```

```
print(f"MSE: {mse_cd}")
```

```
print(f"RMSE: {rmse_cd}")
```

```
print(f"R²: {r2_cd}")
```

```
CL Model Metrics:
```

```
MAE: 0.057670785678915856
```

```
MSE: 0.005590352852157927
```

```
RMSE: 0.07476866223330418
```

```
R²: 0.9917645995317206
```

```
CD Model Metrics:
```

```
MAE: 0.009010279658290841
```

```
MSE: 0.00015997258376996052
```

```
RMSE: 0.012648026872597974
```

```
R²: 0.9816071516568017
```

Original GA Using SVM

```
In [25]: import os
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.svm import SVR
import pygad
import numpy as np
import matplotlib.pyplot as plt
```

```
folder_path = 'Raw Dataset' # Replace with the folder containing your CSV files
```

```
# Step 1: Load all CSV files from the folder and concatenate into a single DataFrame
```

```
all_data = pd.DataFrame() # Empty DataFrame to store data from all files
```

```
for file_name in os.listdir(folder_path):
```

```
    if file_name.endswith('.csv'): # Ensure only CSV files are read
```

```
        file_path = os.path.join(folder_path, file_name)
```

```
        data = pd.read_csv(file_path)
```

```

all_data = pd.concat([all_data, data], ignore_index=True)

# Step 2: Prepare the Data
features = all_data[['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']]
target_cl = all_data['CL']
target_cd = all_data['CD']

# Step 3: Split Data for Training and Testing
X_train, X_test, y_train_cl, y_test_cl = train_test_split(features, target_cl, test_size=0.2)
X_train, X_test, y_train_cd, y_test_cd = train_test_split(features, target_cd, test_size=0.2)

# Step 4: Train the Models (using Support Vector Regressor)
model_cl = SVR(kernel='rbf') # You can experiment with other kernels like 'linear', 'polynomial'
model_cl.fit(X_train, y_train_cl)

model_cd = SVR(kernel='rbf')
model_cd.fit(X_train, y_train_cd)

# Step 5: Define the Genetic Algorithm Fitness Function
def fitness_function(ga_instance, solution, solution_idx):
    v0, q0, t0, p0, p00, q00, alfa, beta = solution
    feature_set = pd.DataFrame([[v0, q0, t0, p0, p00, q00, alfa, beta]],
                                columns=['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA'])

    predicted_cl = model_cl.predict(feature_set)[0]
    predicted_cd = model_cd.predict(feature_set)[0]

    if predicted_cd < 1e-6:
        predicted_cd = 1e-6 # Prevent division by zero

    return predicted_cl / predicted_cd # Maximize Lift-to-Drag ratio

# Step 6: Initialize and Run the Genetic Algorithm
ga_instance = pygad.GA(num_generations=200,
                       num_parents_mating=5,
                       fitness_func=fitness_function,
                       sol_per_pop=10,
                       num_genes=8,
                       init_range_low=[50, 2000, 300, 100000, 100000, 2000, -10, -5],
                       init_range_high=[70, 2500, 350, 101000, 101000, 2500, 10, 5],
                       mutation_percent_genes=10)

# Run the GA
ga_instance.run()

# Step 7: Get and Print the Best Solution
solution, solution_fitness, _ = ga_instance.best_solution()
print(f"Best Solution (Design Parameters): {solution}")
print(f"Lift-to-Drag Ratio of Best Solution: {solution_fitness}")

# Step 8: Predict CL and CD for Test Data
y_pred_cl = model_cl.predict(X_test)
y_pred_cd = model_cd.predict(X_test)

# Step 9: Visualization of CL and CD Predictions vs Actual Values
plt.figure(figsize=(14, 6))

# Plot for CL
plt.subplot(1, 2, 1)
plt.scatter(y_test_cl, y_pred_cl, color='blue')
plt.plot([min(y_test_cl), max(y_test_cl)], [min(y_test_cl), max(y_test_cl)], color='red')
plt.title('Actual vs Predicted CL')
plt.xlabel('Actual CL')
plt.ylabel('Predicted CL')

# Plot for CD

```



```

plt.subplot(1, 2, 2)
plt.scatter(y_test_cd, y_pred_cd, color='green')
plt.plot([min(y_test_cd), max(y_test_cd)], [min(y_test_cd), max(y_test_cd)], color='red')
plt.title('Actual vs Predicted CD')
plt.xlabel('Actual CD')
plt.ylabel('Predicted CD')

# Show the plots
plt.tight_layout()
plt.show()

# Step 10: Fitness over Generations Visualization
plt.figure(figsize=(10, 6))
plt.plot(ga_instance.last_generation_fitness, color='blue', label='Fitness')
plt.title('Fitness Over Generations')
plt.xlabel('Generation')
plt.ylabel('Fitness (Lift-to-Drag Ratio)')
plt.grid()
plt.legend()
plt.show()

# Additional: Print Best Fitness Value Over Generations
best_fitness_over_generations = ga_instance.best_solutions_fitness
plt.figure(figsize=(10, 6))
plt.plot(best_fitness_over_generations, color='orange', label='Best Fitness Over Generations')
plt.title('Best Fitness Over Generations')
plt.xlabel('Generation')
plt.ylabel('Best Fitness (Lift-to-Drag Ratio)')
plt.grid()
plt.legend()
plt.show()

```

C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py: 748: UserWarning: The percentage of genes to mutate (mutation_percent_genes=10) resulted in selecting (0) genes. The number of genes to mutate is set to 1 (mutation_num_genes=1).

If you do not want to mutate any gene, please set mutation_type=None.

warnings.warn(f"The percentage of genes to mutate (mutation_percent_genes={mutation_percent_genes}) resulted in selecting ({mutation_num_genes}) genes. The number of genes to mutate is set to 1 (mutation_num_genes=1).\nIf you do not want to mutate any gene, please set mutation_type=None.")

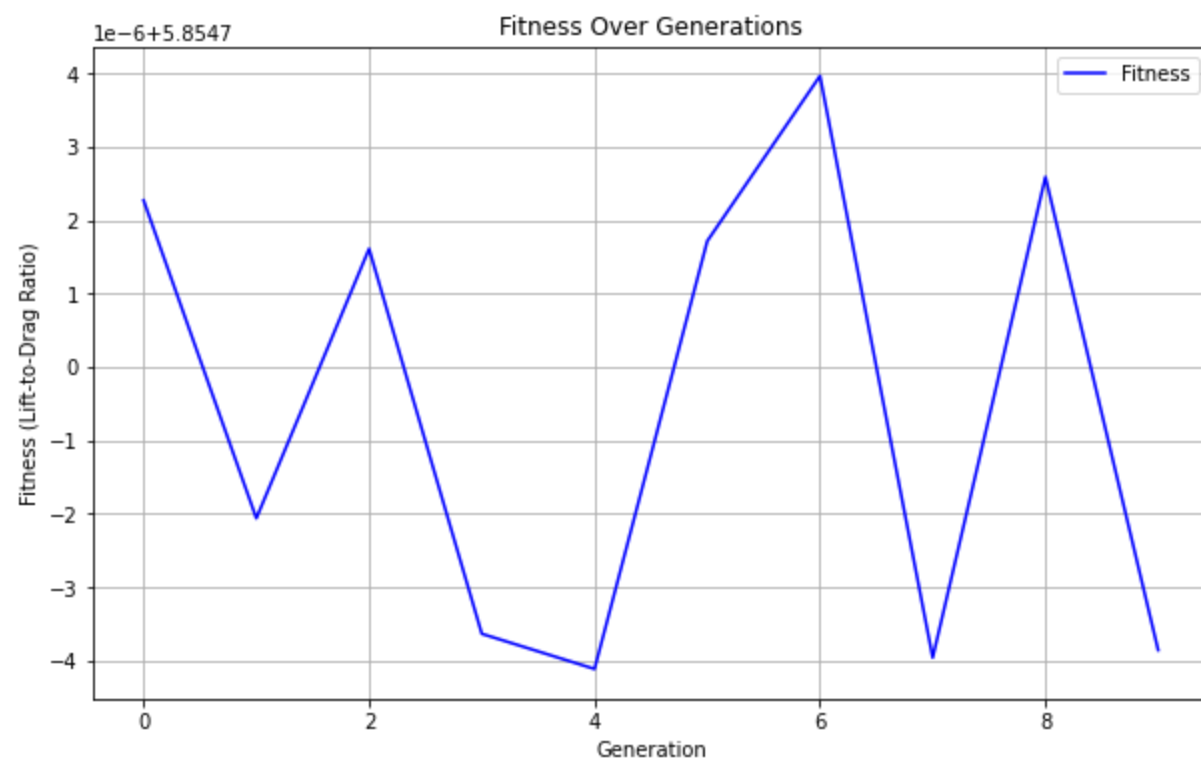
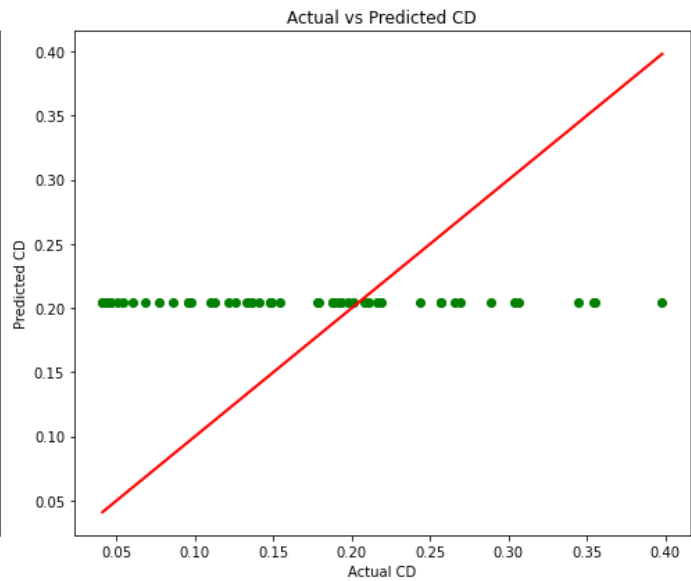
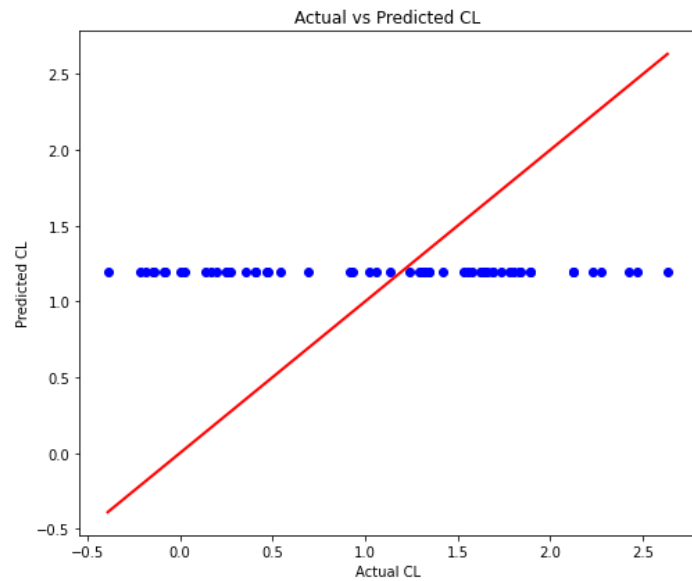
C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py: 1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.0. To delay or pause the evolution after each generation, assign a callback function/method to the 'on_generation' parameter to adds some time delay.

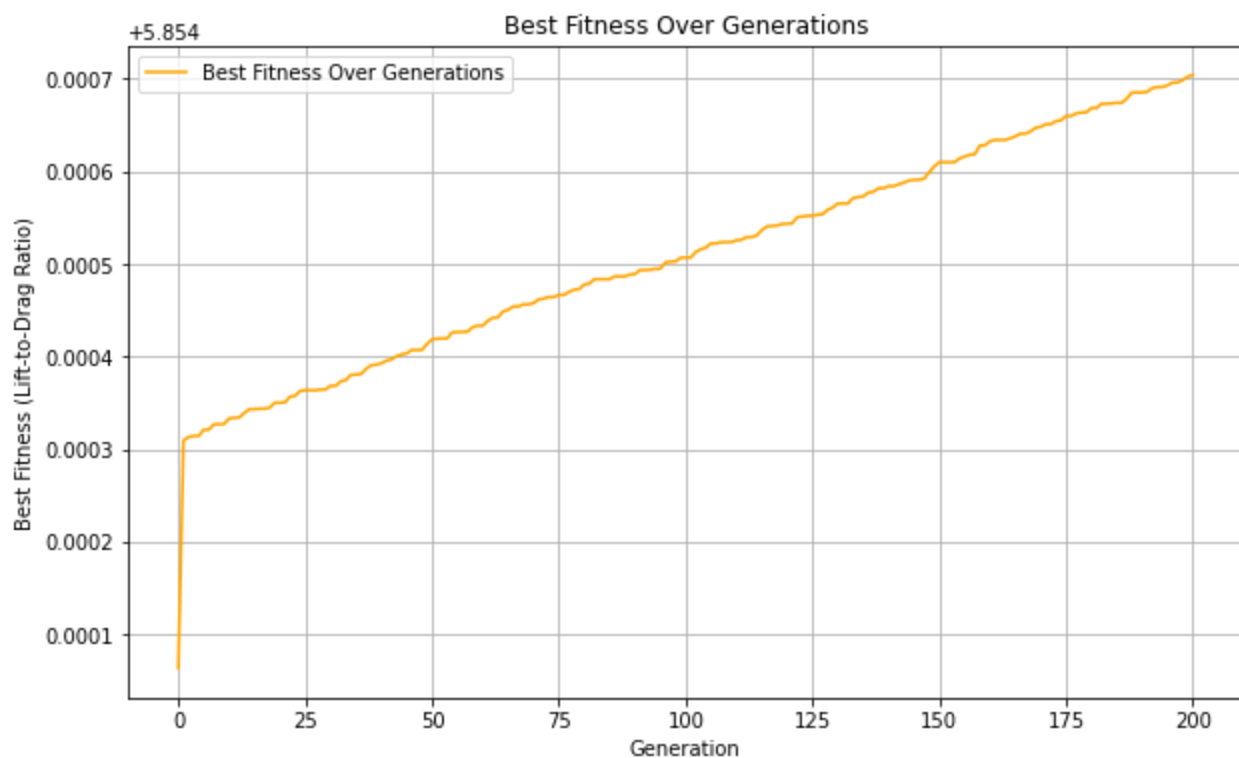
warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.0. To delay or pause the evolution after each generation, assign a callback function/method to the 'on_generation' parameter to adds some time delay.")

Best Solution (Design Parameters): [5.83544606e+01 2.49120785e+03 3.30430869e+02 1.00038884e+05

1.00439941e+05 2.36685501e+03 -1.21272793e+01 -2.15142002e+00]

Lift-to-Drag Ratio of Best Solution: 5.854702267634307





Modified GA Using SVM

In [26]: `pip install --upgrade pygad`

```
Requirement already satisfied: pygad in c:\users\legion\appdata\local\programs\python\py
thon38\lib\site-packages (3.3.1)
Requirement already satisfied: cloudpickle in c:\users\legion\appdata\local\programs\pyt
hon\python38\lib\site-packages (from pygad) (3.0.0)
Requirement already satisfied: matplotlib in c:\users\legion\appdata\local\programs\pyth
on\python38\lib\site-packages (from pygad) (3.5.2)
Requirement already satisfied: numpy in c:\users\legion\appdata\local\programs\python\py
thon38\lib\site-packages (from pygad) (1.24.3)
Requirement already satisfied: cycler>=0.10 in c:\users\legion\appdata\local\programs\py
thon\python38\lib\site-packages (from matplotlib->pygad) (0.11.0)
Requirement already satisfied: fonttools>=4.22.0 in c:\users\legion\appdata\local\progra
ms\python\python38\lib\site-packages (from matplotlib->pygad) (4.34.4)
Requirement already satisfied: kiwisolver>=1.0.1 in c:\users\legion\appdata\local\progra
ms\python\python38\lib\site-packages (from matplotlib->pygad) (1.4.3)
Requirement already satisfied: packaging>=20.0 in c:\users\legion\appdata\local\programs
\python\python38\lib\site-packages (from matplotlib->pygad) (23.2)
Requirement already satisfied: pillow>=6.2.0 in c:\users\legion\appdata\local\programs\p
ython\python38\lib\site-packages (from matplotlib->pygad) (9.2.0)
Requirement already satisfied: pyparsing>=2.2.1 in c:\users\legion\appdata\local\program
s\python\python38\lib\site-packages (from matplotlib->pygad) (3.0.9)
Requirement already satisfied: python-dateutil>=2.7 in c:\users\legion\appdata\local\pro
grams\python\python38\lib\site-packages (from matplotlib->pygad) (2.8.2)
Requirement already satisfied: six>=1.5 in c:\users\legion\appdata\local\programs\python
\python38\lib\site-packages (from python-dateutil>=2.7->matplotlib->pygad) (1.16.0)
Note: you may need to restart the kernel to use updated packages.
```

```
WARNING: Error parsing dependencies of bleach: Expected matching RIGHT_PARENTHESIS for L
EFT_PARENTHESIS, after version specifier
```

```
tinycss2 (>=1.1.0<1.2) ; extra == 'css'
~~~~~^
```

```
[notice] A new release of pip is available: 24.1.1 -> 24.3.1
```

```
[notice] To update, run: python.exe -m pip install --upgrade pip
```

In []:

```
In [27]: import os
import pandas as pd
from sklearn.model_selection import train_test_split
from sklearn.svm import SVR
import pygad
import numpy as np
import matplotlib.pyplot as plt
from sklearn.metrics import r2_score, mean_squared_error
from sklearn.preprocessing import StandardScaler

# -----
# Step 1: Data Loading and Preparation
# -----

# Modify this directory path to point to your dataset
data_dir = 'Raw Dataset' # Update this with the correct path

# Initialize an empty DataFrame to hold all data
dataset = pd.DataFrame()

# Iterate through each file in the directory and concatenate CSV files
for fname in os.listdir(data_dir):
    if fname.lower().endswith('.csv'):
        file_path = os.path.join(data_dir, fname)
        temp_df = pd.read_csv(file_path)
        dataset = pd.concat([dataset, temp_df], ignore_index=True)

# Define feature columns and target variables
feature_cols = ['V0', 'Q0', 'T0', 'P0', 'P00', 'Q00', 'ALFA', 'BETA']
target_CL = dataset['CL']
target_CD = dataset['CD']

# -----
# Step 2: Train-Test Split
# -----

# Split data for CL prediction
X_train_CL, X_test_CL, y_train_CL, y_test_CL = train_test_split(
    dataset[feature_cols],
    target_CL,
    test_size=0.2,
    random_state=42
)

# Split data for CD prediction
X_train_CD, X_test_CD, y_train_CD, y_test_CD = train_test_split(
    dataset[feature_cols],
    target_CD,
    test_size=0.2,
    random_state=42
)

# -----
# Step 3: Feature Scaling
# -----

# Initialize scalers
scaler_CL = StandardScaler()
scaler_CD = StandardScaler()

# Fit scalers on training data and transform both training and test data
X_train_CL_scaled = scaler_CL.fit_transform(X_train_CL)
X_test_CL_scaled = scaler_CL.transform(X_test_CL)
```

```

X_train_CD_scaled = scaler_CD.fit_transform(X_train_CD)
X_test_CD_scaled = scaler_CD.transform(X_test_CD)

# -----
# Step 4: Model Training with SVM
# -----

# Initialize and train SVR model for CL
svm_CL = SVR(kernel='rbf', C=100, epsilon=0.1)
svm_CL.fit(X_train_CL_scaled, y_train_CL)

# Initialize and train SVR model for CD
svm_CD = SVR(kernel='rbf', C=100, epsilon=0.1)
svm_CD.fit(X_train_CD_scaled, y_train_CD)

# -----
# Step 5: Genetic Algorithm Setup
# -----

# List to store the best fitness value from each generation
fitness_history = []

# Define the fitness function for GA
def ga_fitness_function(ga_instance, solution, solution_idx):
    # Extract individual genes
    velocity, flow_rate, temperature, pressure1, pressure2, flow_rate2, alpha, beta = so

    # Create a DataFrame for the solution
    input_features = pd.DataFrame([velocity, flow_rate, temperature, pressure1, pressur

    # Scale the input features
    input_scaled_CL = scaler_CL.transform(input_features)
    input_scaled_CD = scaler_CD.transform(input_features)

    # Predict CL and CD using the trained SVM models
    predicted_CL = svm_CL.predict(input_scaled_CL)[0]
    predicted_CD = svm_CD.predict(input_scaled_CD)[0]

    # Avoid division by zero or very small CD values
    predicted_CD = max(predicted_CD, 1e-6)

    # Calculate Lift-to-Drag ratio
    lift_to_drag = predicted_CL / predicted_CD

    return lift_to_drag

# Callback function to capture the best fitness value each generation
def ga_callback_generation(ga_instance):
    best_fitness = ga_instance.best_solution()[1]
    fitness_history.append(best_fitness)
    # Optional: Print progress every 20 generations
    if (ga_instance.generations_completed % 20) == 0:
        print(f"Generation {ga_instance.generations_completed}: Best Fitness = {best_fit

# Define population boundaries
lower_bounds = [50, 2000, 300, 100000, 100000, 2000, -10, -5]
upper_bounds = [70, 2500, 350, 101000, 101000, 2500, 10, 5]

# Initialize the population using uniform distribution within bounds
def initialize_population(low, high, pop_size, gene_count):
    return np.random.uniform(low, high, (pop_size, gene_count))

initial_population = initialize_population(
    low=lower_bounds,
    high=upper_bounds,
    pop_size=40,          # Increased population size for better diversity

```

```

gene_count=8
)

# Define custom crossover and mutation functions
def custom_crossover(parents, offspring_size, ga_instance):
    offspring = np.empty(offspring_size)
    for k in range(offspring_size[0]):
        parent1 = parents[np.random.randint(0, parents.shape[0])]
        parent2 = parents[np.random.randint(0, parents.shape[0])]
        crossover_pt = np.random.randint(1, parents.shape[1])
        offspring[k, 0:crossover_pt] = parent1[0:crossover_pt]
        offspring[k, crossover_pt:] = parent2[crossover_pt:]
    return offspring

def custom_mutation(offspring, ga_instance):
    for idx in range(offspring.shape[0]):
        mutation_indices = np.random.choice(offspring.shape[1], size=2, replace=False)
        for gene_idx in mutation_indices:
            mutation_value = np.random.uniform(-0.5, 0.5)
            offspring[idx, gene_idx] += mutation_value
            offspring[idx, gene_idx] = np.clip(
                offspring[idx, gene_idx],
                lower_bounds[gene_idx],
                upper_bounds[gene_idx]
            )
    return offspring

# Initialize the Genetic Algorithm
ga_instance = pygad.GA(
    num_generations=200,
    num_parents_mating=10,
    fitness_func=ga_fitness_function,
    initial_population=initial_population,
    num_genes=8,
    mutation_type=custom_mutation,
    crossover_type=custom_crossover,
    keep_elitism=5,
    mutation_probability=0.3,
    on_generation=ga_callback_generation
)

# -----
# Step 6: Run the Genetic Algorithm
# -----

print("Starting Genetic Algorithm Optimization...")
ga_instance.run()
print("Genetic Algorithm Optimization Completed.")

# Retrieve the best solution found by GA
best_solution, best_fitness, best_solution_idx = ga_instance.best_solution()
print(f"\nBest Solution Parameters:\n{best_solution}")
print(f"Best Lift-to-Drag Ratio: {best_fitness:.4f}")

# -----
# Step 7: Predictions with the Best Solution
# -----

# Create a DataFrame for the best solution
best_input = pd.DataFrame([best_solution], columns=feature_cols)

# Scale the input features
best_input_scaled_CL = scaler_CL.transform(best_input)
best_input_scaled_CD = scaler_CD.transform(best_input)

# Predict CL and CD using the best solution

```

```

best_predicted_CL = svm_CL.predict(best_input_scaled_CL)[0]
best_predicted_CD = svm_CD.predict(best_input_scaled_CD)[0]
best_predicted_CD = max(best_predicted_CD, 1e-6) # Prevent division by zero

print(f"\nPredicted CL for Best Solution: {best_predicted_CL:.4f}")
print(f"Predicted CD for Best Solution: {best_predicted_CD:.6f}")
print(f"Lift-to-Drag Ratio for Best Solution: {best_predicted_CL / best_predicted_CD:.4f}")

# -----
# Step 8: Evaluate Models on Test Data
# -----

# Predict on test data for CL and CD
test_pred_CL = svm_CL.predict(X_test_CL_scaled)
test_pred_CD = svm_CD.predict(X_test_CD_scaled)

# Calculate Lift-to-Drag ratio for test predictions
test_lift_to_drag = test_pred_CL / np.maximum(test_pred_CD, 1e-6)

# -----
# Step 9: Visualization
# -----

# Plot Actual vs Predicted CL
plt.figure(figsize=(14, 6))

plt.subplot(1, 2, 1)
plt.scatter(y_test_CL, test_pred_CL, color='blue', alpha=0.6, label='Data Points')
plt.plot([y_test_CL.min(), y_test_CL.max()], [y_test_CL.min(), y_test_CL.max()], 'r--',
plt.title('Actual vs Predicted CL')
plt.xlabel('Actual CL')
plt.ylabel('Predicted CL')
plt.legend()
plt.grid(True)

# Plot Actual vs Predicted CD
plt.subplot(1, 2, 2)
plt.scatter(y_test_CD, test_pred_CD, color='green', alpha=0.6, label='Data Points')
plt.plot([y_test_CD.min(), y_test_CD.max()], [y_test_CD.min(), y_test_CD.max()], 'r--',
plt.title('Actual vs Predicted CD')
plt.xlabel('Actual CD')
plt

```

Starting Genetic Algorithm Optimization...

C:\Users\LEGION\AppData\Local\Programs\Python\Python38\lib\site-packages\pygad\pygad.py: 1139: UserWarning: The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.0. To delay or pause the evolution after each generation, assign a callback function/method to the 'on_generation' parameter to adds some time delay.

warnings.warn("The 'delay_after_gen' parameter is deprecated starting from PyGAD 3.3.0. To delay or pause the evolution after each generation, assign a callback function/method to the 'on_generation' parameter to adds some time delay.")

```

Generation 20: Best Fitness = 4.6587
Generation 40: Best Fitness = 4.6587
Generation 60: Best Fitness = 4.6587
Generation 80: Best Fitness = 4.6587
Generation 100: Best Fitness = 4.6587
Generation 120: Best Fitness = 4.6587
Generation 140: Best Fitness = 4.6587
Generation 160: Best Fitness = 4.6587
Generation 180: Best Fitness = 4.6587
Generation 200: Best Fitness = 4.6587
Genetic Algorithm Optimization Completed.

```

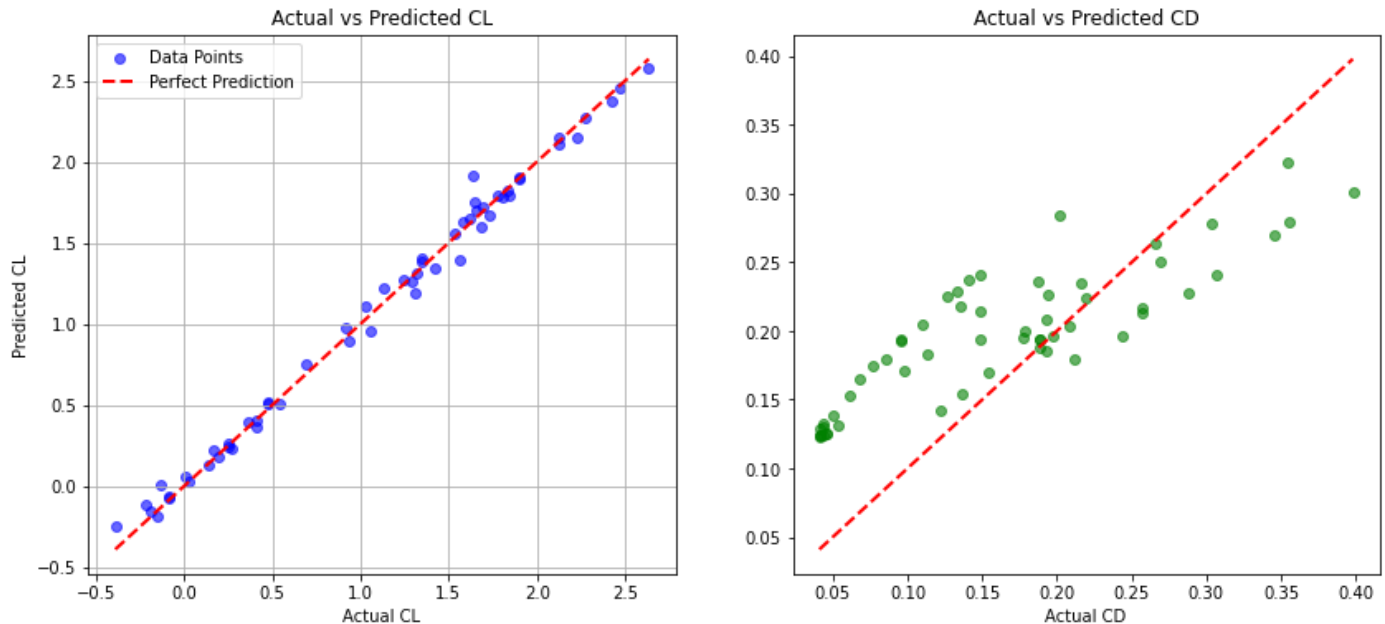
Best Solution Parameters:

```
[ 6.33763363e+01  2.36243110e+03  3.11661812e+02  1.00156764e+05]
```

1.00788028e+05 2.41385139e+03 -8.22262256e+00 2.82931303e+00]
Best Lift-to-Drag Ratio: 4.6587

Predicted CL for Best Solution: 1.3106
Predicted CD for Best Solution: 0.281330
Lift-to-Drag Ratio for Best Solution: 4.6587

Out[27]: <module 'matplotlib.pyplot' from 'C:\\Users\\LEGION\\AppData\\Local\\Programs\\Python\\Python38\\lib\\site-packages\\matplotlib\\pyplot.py'>



```
In [28]: from sklearn.metrics import mean_absolute_error, mean_squared_error, r2_score
import numpy as np
```

```
# -----
# Step 8: Evaluate Models on Test Data
# -----

# Predict on test data for CL and CD
test_pred_CL = svm_CL.predict(X_test_CL_scaled)
test_pred_CD = svm_CD.predict(X_test_CD_scaled)

# Calculate Lift-to-Drag ratio for test predictions
test_lift_to_drag = test_pred_CL / np.maximum(test_pred_CD, 1e-6)

# -----
# Step 10: Calculate Evaluation Metrics
# -----

# Metrics for CL
mae_CL = mean_absolute_error(y_test_CL, test_pred_CL)
mse_CL = mean_squared_error(y_test_CL, test_pred_CL)
rmse_CL = np.sqrt(mse_CL)
r2_CL = r2_score(y_test_CL, test_pred_CL)

# Metrics for CD
mae_CD = mean_absolute_error(y_test_CD, test_pred_CD)
mse_CD = mean_squared_error(y_test_CD, test_pred_CD)
rmse_CD = np.sqrt(mse_CD)
r2_CD = r2_score(y_test_CD, test_pred_CD)

# Display metrics
print("\nCL Model Metrics:")
print(f"MAE: {mae_CL:.6f}")
print(f"MSE: {mse_CL:.6f}")
print(f"RMSE: {rmse_CL:.6f}")
print(f"R²: {r2_CL:.6f}")
```



```
print("\nCD Model Metrics:")
print(f"MAE: {mae_CD:.6f}")
print(f"MSE: {mse_CD:.6f}")
print(f"RMSE: {rmse_CD:.6f}")
print(f"R²: {r2_CD:.6f}")
```

CL Model Metrics:

```
MAE: 0.050785
MSE: 0.004908
RMSE: 0.070055
R²: 0.992770
```

CD Model Metrics:

```
MAE: 0.057006
MSE: 0.004419
RMSE: 0.066477
R²: 0.491905
```

In [29]:

```
# -----
# Step 11: Print Best Solution Parameters in Desired Format
# -----

# Format the best solution parameters
formatted_params = ", ".join([f"{param}: {value:.2f}" for param, value in zip(feature_co

# Print the best solution parameters in the desired format
print("\nBest Solution (Design Parameters):")
print(formatted_params)

# Display metrics for the best solution
print("\nMetrics for Best Solution:")
print(f"Predicted CL: {best_predicted_CL:.6f}")
print(f"Predicted CD: {best_predicted_CD:.6f}")
print(f"Lift-to-Drag Ratio: {best_predicted_CL / best_predicted_CD:.6f}")
```

Best Solution (Design Parameters):

```
V0: 63.38, Q0: 2362.43, T0: 311.66, P0: 100156.76, P00: 100788.03, Q00: 2413.85, ALFA: -
8.22, BETA: 2.83
```

Metrics for Best Solution:

```
Predicted CL: 1.310635
Predicted CD: 0.281330
Lift-to-Drag Ratio: 4.658711
```

In [30]:

```
import matplotlib.pyplot as plt

# Assuming you have test_pred_CL, test_pred_CD (predicted values) and y_test_CL, y_test_

# Plot CL vs CD for Actual and Predicted values
plt.figure(figsize=(10, 6))

# Actual CL vs CD (blue points)
plt.scatter(y_test_CL, y_test_CD, color='blue', alpha=0.6, label='Actual CL vs CD')

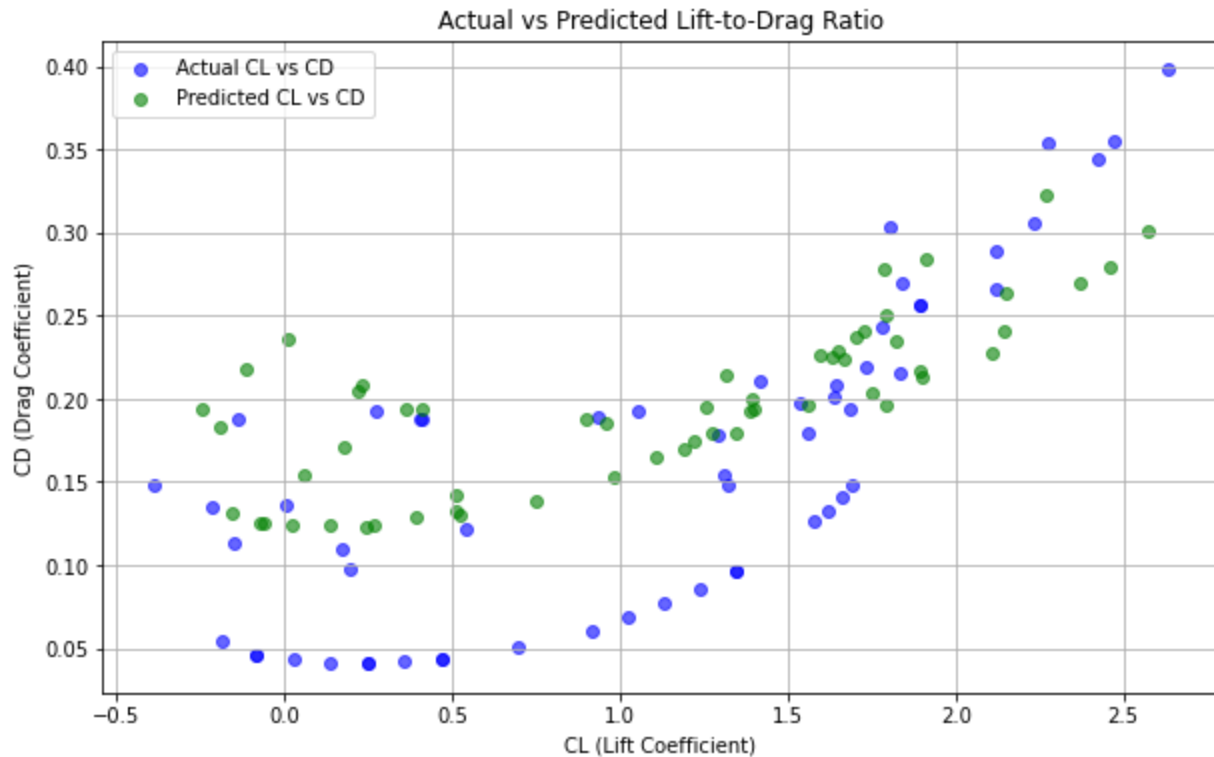
# Predicted CL vs CD (green points)
plt.scatter(test_pred_CL, test_pred_CD, color='green', alpha=0.6, label='Predicted CL vs

# Add labels and title
plt.title('Actual vs Predicted Lift-to-Drag Ratio')
plt.xlabel('CL (Lift Coefficient)')
plt.ylabel('CD (Drag Coefficient)')

# Display the legend
plt.legend()
```

```
# Show grid
plt.grid(True)

# Display the plot
plt.show()
```



```
In [31]: import matplotlib.pyplot as plt
```

```
# Assuming you have already stored the fitness values for both GAs
# Replace these with actual data from your GA runs

# Fitness values for the Original GA
original_ga_fitness = ga_instanceE.best_solutions_fitness # Replace with the actual fit
original_ga_generations = range(1, len(original_ga_fitness) + 1)

# Fitness values for the Modified GA
modified_ga_fitness = fitness_history # Replace with the fitness history of the Modified GA
modified_ga_generations = range(1, len(modified_ga_fitness) + 1)

# Convergence points
original_convergence = len(original_ga_fitness) # Last generation for the Original GA
modified_convergence = next(
    (i + 1 for i, v in enumerate(modified_ga_fitness) if v >= max(modified_ga_fitness) *
    len(modified_ga_fitness)
)

# Fitness values at convergence points
original_convergence_fitness = original_ga_fitness[-1] # Fitness at the last generation
modified_convergence_fitness = modified_ga_fitness[modified_convergence - 1] # Fitness

# Plot the convergence comparison
plt.figure(figsize=(12, 8))

# Original GA fitness plot
plt.plot(
    original_ga_generations,
    original_ga_fitness,
    label="Original GA",
    color='blue',
    linestyle='--',
```

```

        marker='o'
    )

    # Modified GA fitness plot
    plt.plot(
        modified_ga_generations,
        modified_ga_fitness,
        label="Modified GA",
        color='green',
        linestyle='-',
        marker='s'
    )

    # Mark convergence points with red markers
    plt.scatter(
        original_convergence,
        original_convergence_fitness,
        color='red',
        label=f"Original GA Convergence (Gen {original_convergence})",
        zorder=5
    )
    plt.scatter(
        modified_convergence,
        modified_convergence_fitness,
        color='red',
        label=f"Modified GA Convergence (Gen {modified_convergence})",
        zorder=5
    )

    # Add vertical lines for convergence points
    plt.axvline(
        x=original_convergence,
        color='red',
        linestyle=':',
        alpha=0.7
    )
    plt.axvline(
        x=modified_convergence,
        color='red',
        linestyle=':',
        alpha=0.7
    )

    # Add labels, title, and legend
    plt.title("Convergence Comparison: Original GA vs. Modified GA", fontsize=16)
    plt.xlabel("Generations", fontsize=14)
    plt.ylabel("Best Fitness Value", fontsize=14)
    plt.legend(loc="lower right", fontsize=12)
    plt.grid(True)
    plt.tight_layout()

    # Show the plot
    plt.show()

```

Convergence Comparison: Original GA vs. Modified GA

