

Research proposal - Tom George

Introduction

Intelligent agents must learn to represent the external world and themselves within it, then dynamically use these representations to solve tasks such as navigation, planning and decision making. Although biological and artificial intelligences do this for different reasons (e.g. survival vs. maximisation of an objective function) they often develop similar representations when trained on comparable tasks [1, 2], strongly indicating we can learn about one by studying the other. My research focuses on three fundamental questions; **how do neural systems learn, what representations do neural systems use, and how do neural dynamics and representations interact to enable flexible behaviour?** Using theoretical and data-driven approaches I study these in the context of the mammalian spatial-memory system where decades of research have revealed a rich landscape of learning phenomena [3–5], architectures [6], representations [7] and dynamics [4,8–10]. By building computational models I show how biology can be reconciled with statistical and machine learning models of artificial learning systems (NeuroAI [11]) providing novel interpretations for both. Along the way I have **developed popular open-source computational tools** to analyse neural data [12] and to build realistic models of spatial navigation [13].

Past work

(Work 1) Tooling for modelling navigation and neural representations in 2D spaces [13]. Studying the brain's role in spatial navigation often necessitates creating synthetic behaviour and/or neural data. After discovering that no single framework existed for this purpose I developed the RatInABox python toolkit [13] which generates realistic synthetic trajectories for agents exploring one- or two-dimensional environments along with associated neural data (place cells, grids cells etc.). I engaged and led a rapidly emerging open-source developer community whose contributions expanded RatInABox from a simple data generator into a comprehensive toolkit for navigational research, including features such as policy control, sensory inputs, multiagent interactions as well as representation and reinforcement learning capabilities. RatInABox jointly models navigation *and* neurons whilst remaining computationally lightweight. It has received over 40,000 downloads to date, and, in its first year, has already facilitated a promising new wave of hippocampal studies (as shown in [12, 14–24]) including my own on predictive representations [25, 26] (Work 2), hippocampal generative modelling [27] (Work 3) and neural data analysis (Aim 1).

(Work 2) Plausible mechanisms for learning predictive representations [25,26]. Predictive representations, specifically *successor features* (SRs) [28,29], enable agents to rapidly learn and transfer environmental structure. Previous studies have suggested that place cells [30] function like SRs for spatial navigation [31], however temporal difference (TD) learning [32] (the default learning rule) is not compatible with hippocampal biological constraints. I sought an alternative mechanism based on a spiking variant of Hebbian learning called STDP [3] and phase precession, a phenomenon which coordinates neural activity such that cells with potentially quite distant place fields spike in close and coordinated temporal proximity. This “compression” of behaviour down to short timescales enables STDP to bind place cells together in the order they are traversed, rapidly learning an SR-like representation for the current policy. This work provided one of the first biologically plausible mechanisms of how predictive maps can be learned [33,34] and bridged a fundamental mismatch between neural plasticity and behavioural timescales.

In a follow-up study [26], I sought a theoretical explanation for this result, deriving an equivalence between my phase-precession led STDP learning mechanism and $TD(\lambda)$ [32], an extension of the TD learning algorithm which accelerates learning with memory traces.

(Work 3) A generative model of the hippocampal formation [27]. The mammalian spatial-memory system possesses “generative” functionality [35], exemplified by various forms of *mind travel* [36] (the shift of an internal position encoding away from the true location to generate new trajectories) and *path integration* [37,38] (where self-location predictions can be generated in the absence of sensory input). Existing models which explain how the hippocampal formation path integrates use deep architectures trained with non-local learning rules [1, 2, 39, 40], leaving open the question of how this is learned in the brain. My NeurIPS paper [27] introduced a biologically plausible model of the hippocampal formation, demonstrating that local learning and message passing was sufficient. One important component was that fast theta-band oscillations (5-10 Hz) control the direction of information flow through a two-layer network, akin to a Helmholtz machine [41] trained using a high-frequency wake-sleep algorithm [42]. Local error-minimising learning rules yielded a ring-attractor in the hidden layer (closely matching that of entorhinal grid cells) capable of robust path integration. My work unified oscillations, Hebbian learning and the hippocampal “loop” under a single normative framework.

Ongoing and Future work

(Aim 1) I will develop efficient and scalable methods for neural latent discovery, enabling more accurate interpretation of neural tuning curves and dynamics. Latent variable models (LVMs) aim to find low-dimensional factors which explain high-dimensional neural data [43–57]. This contrasts a more traditional, but still widely used, approach where *tuning curves* are plotted to visualise each neurons activity as a function of a particular behavioural variable (e.g. the animal's location) [30, 58–60]. In an ongoing line of work I am developing a novel technique which blends these approaches by recursively fitting and optimizing tuning curves through a procedure related to expectation-maximisation [61]. This is fast (10 - 100x faster than comparable methods [55, 62–64]), performant, and conceptually simple but, like other modern LVM approaches, moves beyond the restrictive paradigm of explaining data exclusively in terms of behaviour. Early results are promising; optimized place fields are sharpened by my procedure and biases in their tuning curve shapes (e.g. that place fields close to walls are smaller [65]) are reduced implying space is encoded in a more uniform and precise manner than previously thought. Similar results apply to a motor-task dataset from somatosensory cortex [66]. I expect this tool to have impact in fields where disambiguating between theoretical hypotheses requires highly accurate characterisation of tuning curves and/or latent dynamics. It could also serve as a pre-processing step for neural datasets or for real-time latent decoding.

(Aim 2) I will apply latent variable methods to open neural datasets in order to disentangle the effect of synaptic structure and neural dynamics from representations. Latent variable models provide a means to reinterpret neural data in terms of the dynamics (the latent factors) and a mapping from these dynamics to spikes. Thus, there are two ways the brain can perform a task or adapt to new conditions; it can do so *dynamically* through its latent or *structurally* by synaptically adjusting its tuning curves. Consider the SR model of place fields discussed earlier: place fields can show SR-like skewing for structural reasons because their receptive fields are synaptically modified (e.g. see Work 1 [25] and [33, 34]) or for dynamical reasons [67] because the latent variable has a bias for exploring upcoming future locations causing place cells to fire early and thus skew backwards (e.g. due to theta sequences [68]). Disambiguating between these hypotheses is critical if we hope to truly understand how hippocampus supports spatial behaviour and memory. Building on my new latent variable methods (Aim 1) I will analyse new and existing neural dataset to explore which features of neural tuning curves can be attributed to synaptic learning and which to latent dynamics. This technique will be validated against carefully constructed synthetic datasets (Work 3) where the ground truth is known. This project will provide a new perspective on the role of dynamics in neural computation and will be a stepping stone towards a general theory of neural dynamics and structure (Aim 3).

(Aim 3) I will develop a general theory of when dynamics (i.e. “context”) and structure (“weights”) are used to solve cognitive tasks. The distinction between dynamics and structure is not restricted to spatial cognition. In machine learning, transformers-based architectures [69] are able to solve tasks either “in-weights” or “in-context” [70, 71]. In reinforcement learning, model-based methods find optimal actions at test-time through dynamical rollouts in contrast to model-free methods which learn policies “in weights” [32]. Recently, experimental [72] and theoretical [73] work has demonstrated that hippocampal episodic memory and prefrontal working memory store memories in synapses vs. in neural activity respectively. All in all, I see it as crucial for the field to move towards a unified understanding of why, and when, dynamics vs. structure is used to solve cognitive tasks. My research agenda will seek to answer this question at multiple levels, building upon Aims 1 and 2, while also embracing broader aspects beyond spatial cognition and the brain.

Summary

I have built tools for modelling spatial-memory and used these to study how/what neural systems learn. My works provide biologically plausible explanations of predictive representations and generative models in the hippocampus. My future research will focus on developing methods for neural latent discovery, disentangling latent dynamics from representations and moving towards a general theory of neural dynamics and structure.

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