# Experimental Data Analysis in ©MATLAB

# Lecture 3:

Hypothesis testing, group differences, paired test, effect size

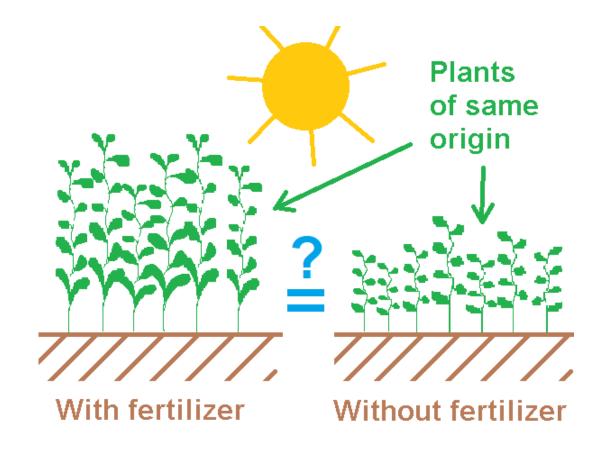
Jan Rusz Czech Technical University in Prague





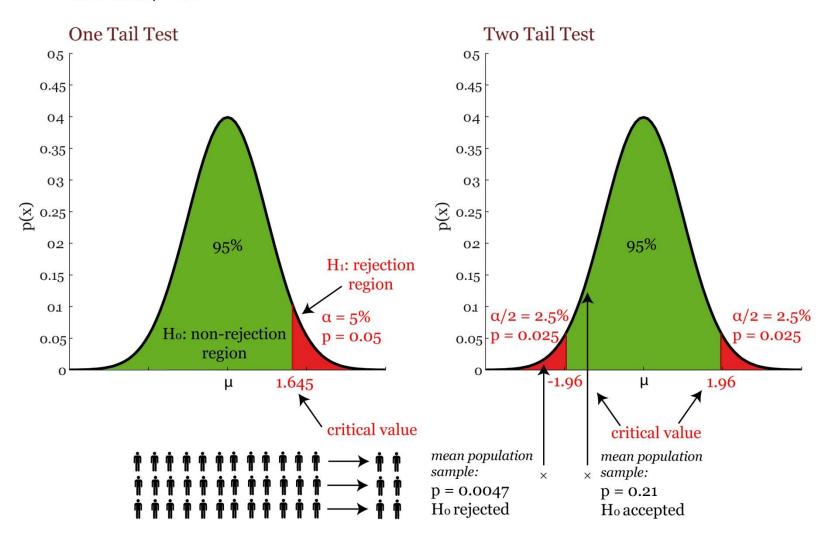
#### Motivation

- Do size of plants differ in dependence of fertilizer application?
- Obviously yes, but can you quantify the difference?
- Each plant has different size and there is different number of plants in groups.
- What is the probability of co-incidence?



## Hypothesis testing

distribution:  $\mu = 0$ ,  $\sigma = 1$ 



The average IQ for the adult population is defined to be 100 with standard deviation of 15. Researcher decided to reproduce this result and tested the IQ in 75 random adults. He obtained average IQ of 105 using this sample. Is there enough evidence to suggest that the average IQ has changed?

1. step: State null (H<sub>o</sub>) and alternative (H<sub>1</sub>) hypothesis

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1. step: State null (H<sub>o</sub>) and alternative (H<sub>1</sub>) hypothesis

$$H_o$$
:  $\mu = 100$ 

Two Tailed Test:  $H_1$ :  $\mu \neq 100$ 

One Tailed Test:  $H_1$ :  $\mu$  < 100

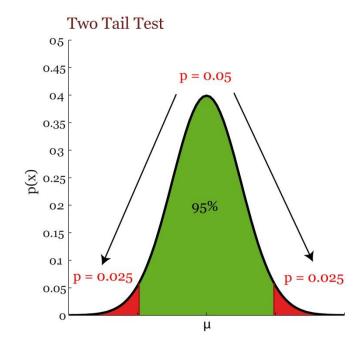
 $H_1$ :  $\mu > 100$ 

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#### 2. step: Choose level of significance (p)

$$H_o$$
:  $\mu = 100$ 

$$H_1$$
: µ ≠ 100

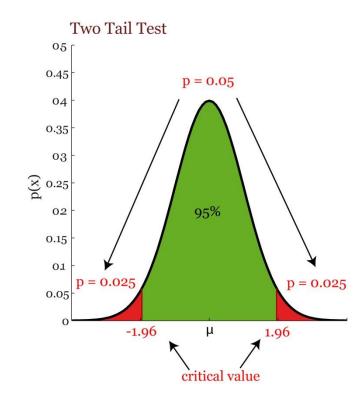


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#### 3. step: Find critical values

$$H_o$$
:  $\mu = 100$ 

$$H_1$$
: µ ≠ 100



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#### 4. step: Find test statistic

$$H_0$$
:  $\mu = 100$ ,  $\sigma = 15$ 

$$H_1$$
:  $\mu \neq 100$ 

$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{105 - 100}{\frac{15}{\sqrt{75}}}$$

z-test: We know standard deviation of the population

$$t = \frac{\bar{x} - \mu}{\frac{S}{\sqrt{n}}}$$

t-test: We calculate actual standard deviation (S) of the sample

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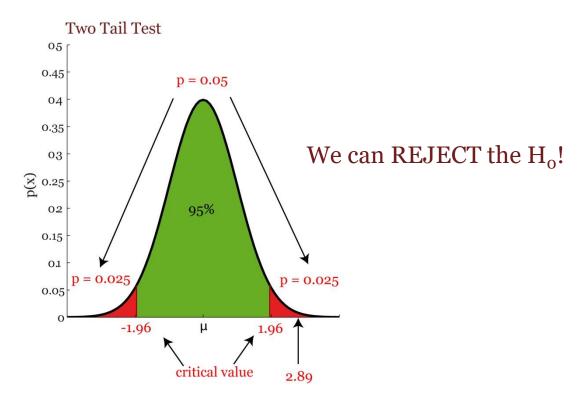
$$z = \frac{\bar{x} - \mu}{\frac{\sigma}{\sqrt{n}}} = \frac{105 - 100}{\frac{15}{\sqrt{75}}} = 2.89$$

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#### 5. step: Draw your conclusion

$$H_0$$
:  $\mu = 100$ ,  $\sigma = 15$ 

$$H_1$$
: µ ≠ 100



#### How to report *p* values?

The most common levels of significance reported with respect to research questions:

```
p < 0.05 * (minimal level of significance)

p < 0.01 ***

p < 0.001 *** (statistically highly significant – less than one in a thousand chance of being wrong)
```

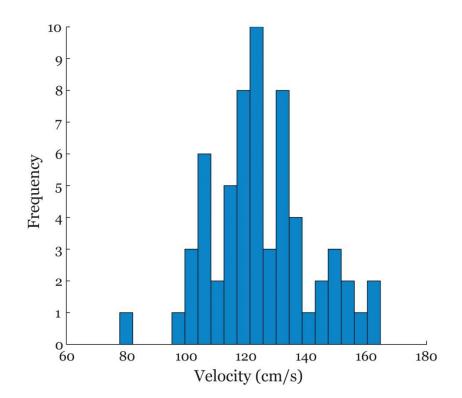
```
How to report them?
```

```
p < 1, 0.01>: 2 digits (p = 0.02, p = 0.51; 3 digits in special cases p = 0.049) p (0.01, 0.001>: 3 digits (p = 0.009, p = 0.001) p (0.001, 0>: always p < 0.001
```

#### Testing using the one-sample t-test

Researcher assumes that a number of patients with neurological disorders has problems with velocity of gait. Researcher wants to verify if a new patient has "normal" velocity of gait.

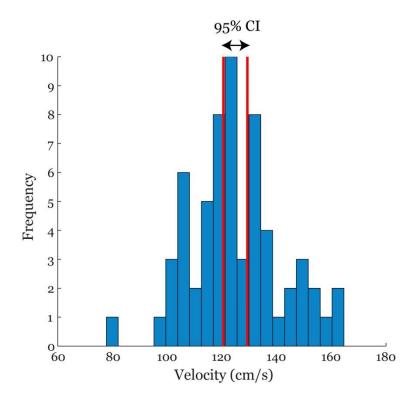
1) It is necessary to collect appropriate sample that would represent velocity of gait of normal population. In this case, the velocity of gait was collected from 62 normal healthy subjects.



#### Testing using the one-sample t-test

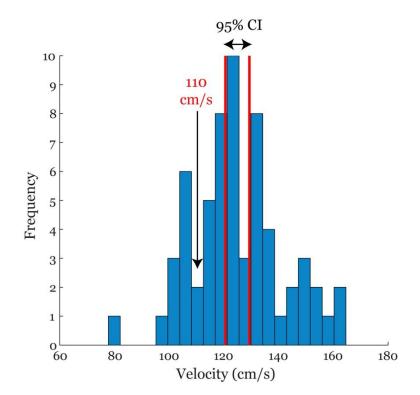
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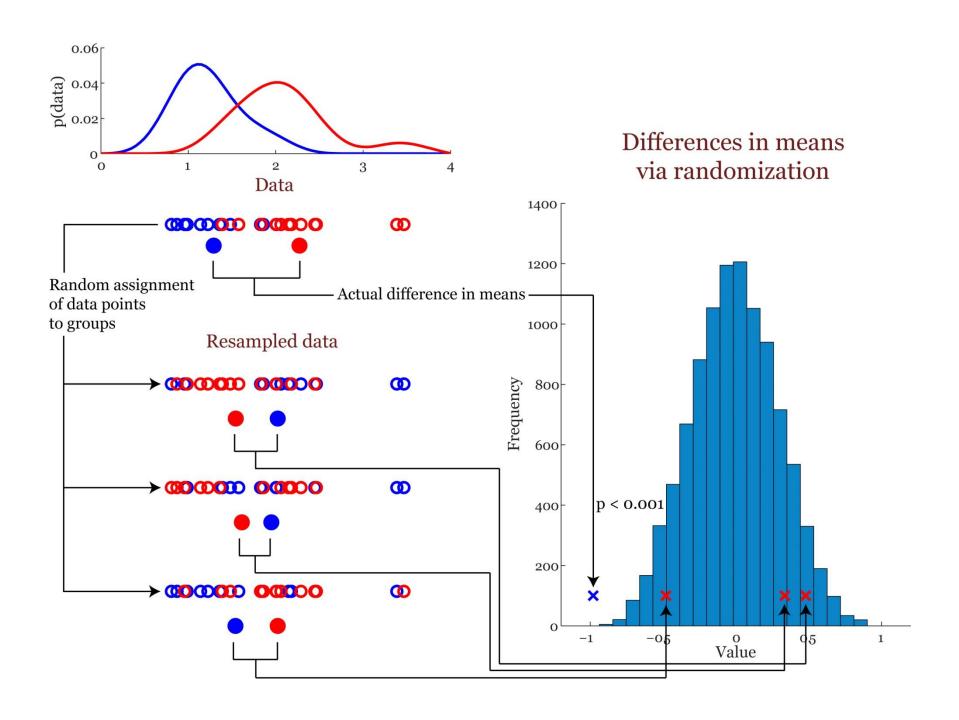
2) Using the t-test, we estimate the 95% confidence interval for velocity of gait in normal population  $(H_0)$ .



Researcher assumes that a number of patients with neurological disorders has problems with velocity of gait. Researcher wants to verify if a new patient has "normal" velocity of gait.

3) We can compare the actual researcher's gait velocity (H<sub>1</sub>) with estimated 95% confidence interval and reject the null hypothesis that his gait velocity performance belong to the normal population.

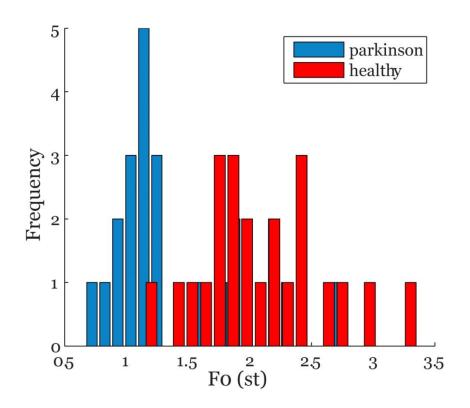




# Group differences for normally distributed data (t-test)

Researcher wants to verify if the intonation patterns differ between speakers with Parkinson's disease (PD) and healthy control speakers. He collected short reading texts from 23 speakers with PD and age- and 23 sexmatched controls, extracted fundamental frequency contour and converted it into semitone scale (st).

How to report the results? t(45) = -4.40, p < 0.001



# Group differences

#### for non-normally distributed data (Wilcoxon rank sum test)

Normal speaker is able to perform sustained vowel phonation without voice breaks that represent impaired function of vocal folds. To verify if vocal fold function differs in patients with Huntington's disease (HD), researcher collected sustained phonations from 34 speakers with HD and 34 age- and sex-matched controls and extracted analyzed number of voice breaks (nvb).

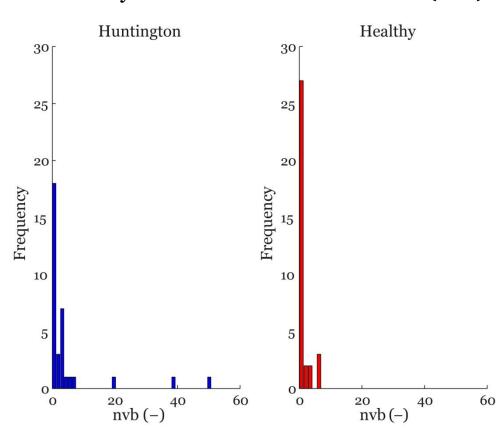
How to report the results? z(67) = 3.81, p < 0.001

What about t-test?

$$t(67) = 1.98, p = 0.051$$



Failed to found significant group differences



#### Independent samples





Scores are separate (e.g. testing the blood pressure of group of people on active drugs against group of people taking placebo)

#### Paired samples

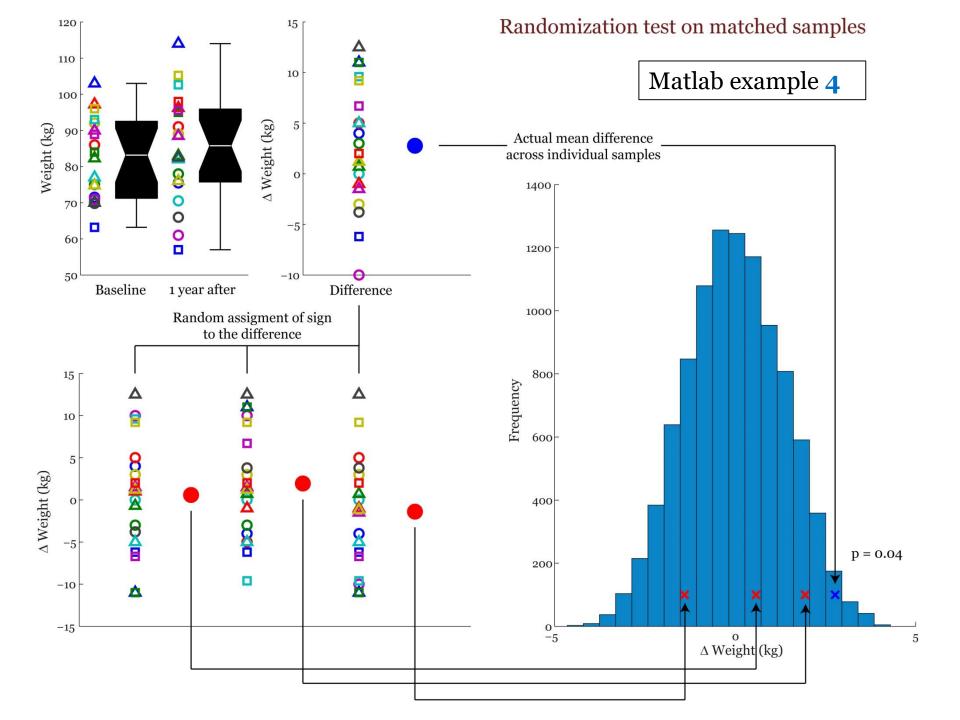




Scores are linked (e.g. measuring the blood pressures of the same people before and after they receive a dose)

## How to use paired test?

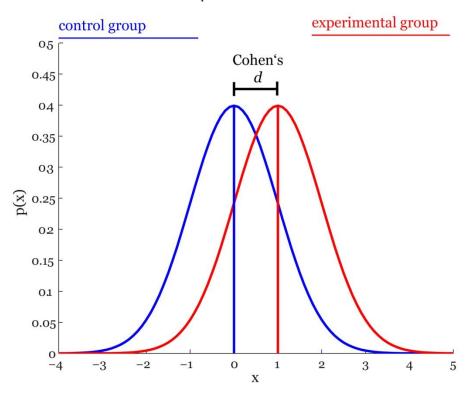
Is there any change in weight of 20 patients with Parkinson's disease one year after introduction of dopaminergic drugs?

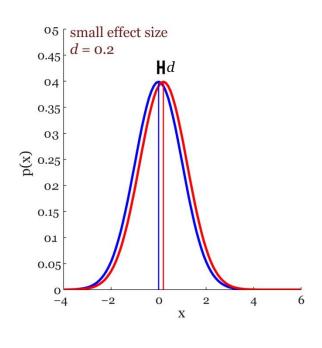


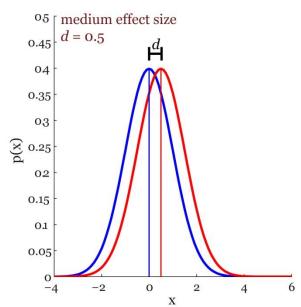
#### Cohen's effect size:

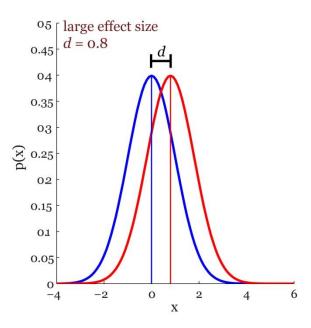
a quantitative measure of the strength of a phenomenon, independent of the measured units.

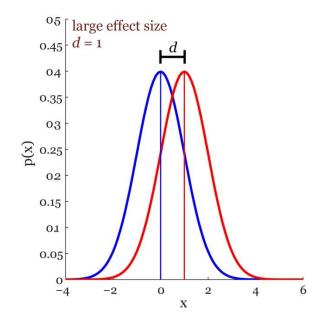
$$d = \frac{\mu_c - \mu_e}{\sigma} \qquad \sigma = \sqrt{\frac{\sigma_c^2 + \sigma_e^2}{2}}$$

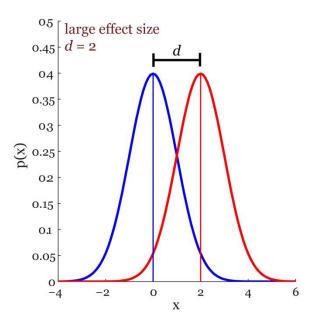


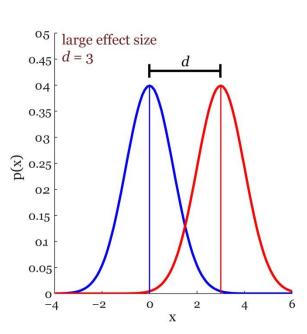












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a quantitative measure of the strength of a phenomenon, independent of the measured units.

