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Presentation · September 2001

DOI: 10.13140/RG.2.1.1774.7605

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LOW-POWER HIGH-PRECISION CRYSTAL OSCILLATORS

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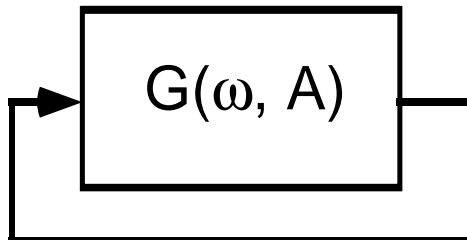
- Crystal resonator.
- General theory of crystal oscillators
 - splitting for analysis
 - oscillation: condition and frequency
 - amplitude limitation
 - start-up time.
- Theory of the 3-point oscillator
 - linear analysis with and without losses
 - nonlinear behaviour
 - amplitude and energy of oscillation
 - frequency stability, frequency tuning
 - phase noise
 - elimination of unwanted modes
 - loading by amplifier.
- Practical implementations
 - grounded drain oscillator
 - grounded source oscillators
 - amplitude regulator
 - circuit examples.

APPLICATIONS OF CRYSTAL OSCILLATORS

- Time-keeping (real-time clocks, RTC)
 - precision and stability: 10^{-6}
($\cong 30\text{s/year}$)
 - low power
watches: $\leq 0.5 \mu\text{W}$
- Radio communication
 - precision and stability: 10^{-6} to 10^{-5}
(1 to 10kHz at 1GHz)
 - low power ($\ll 1\text{mW}$)
 - phase noise if :
 - no VCO (direct RF generation)
 - injection synchronized VCO
 - wide-band PLL loopotherwise negligible ($\sim 1/Q^2$)
- Clock of analog systems (filters)
 - precision and stability : 10^{-4}
(better than component mismatch)
- Clock of digital systems
 - no high precision required
 - beware of overtone oscillation!

BASICS ON OSCILLATORS

- Frequency-dependent nonlinear loop.



ω = (angular) frequency
 A = amplitude

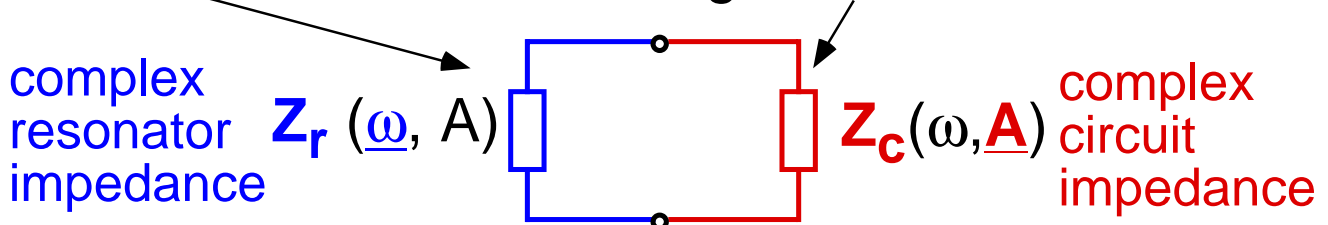
- strongly nonlinear: relaxation oscillator
- weakly nonlinear: harmonic oscillator
- Stable oscillation at frequency ω_0 : $G(\omega_0, A_0) = 1$

with: $\left. \frac{d(\text{Arg}(G))}{d\omega} \right|_{\omega=\omega_0, A=A_0} < 0$ (phase stability)

and: $\left. \frac{d|G|}{dA} \right|_{\omega=\omega_0, A=A_0} < 0$ (amplitude stability)

Alternative representation:

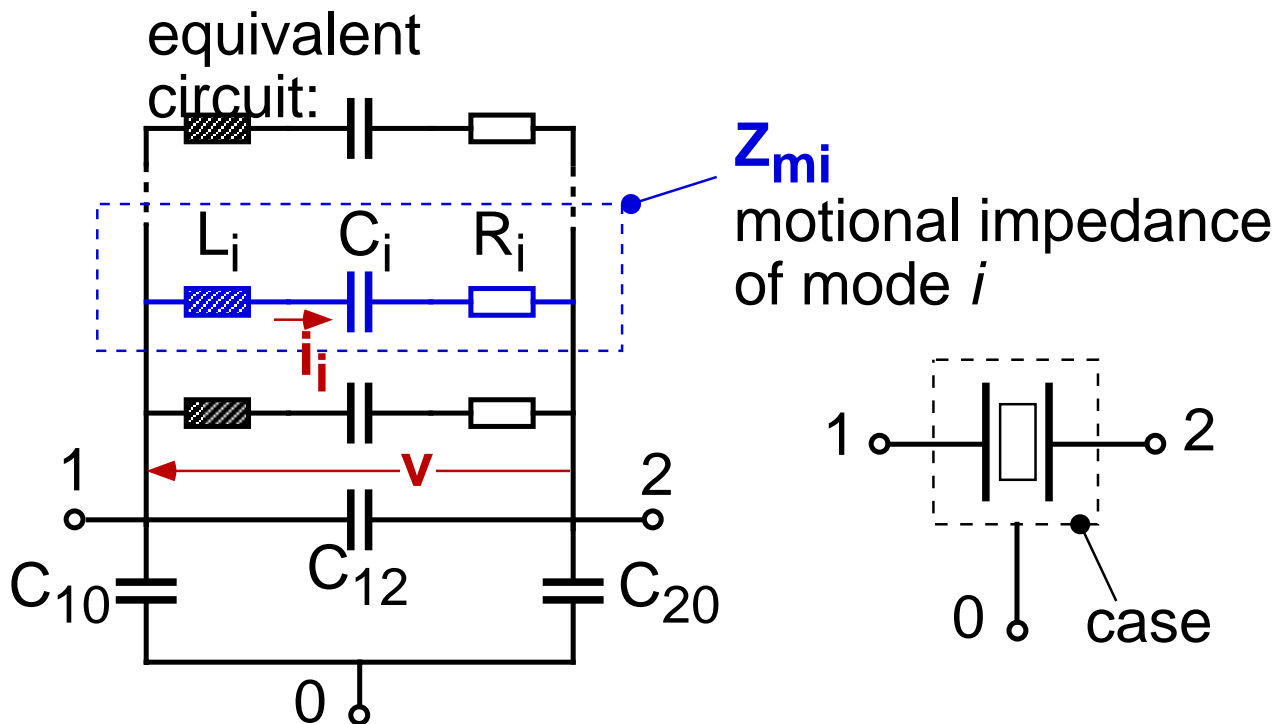
- Resonator and sustaining circuit



- Stable oscillation at frequency ω_0 :

$\mathbf{Z_r}(\omega_0, A_0) + \mathbf{Z_c}(\omega_0, A_0) = 0$

CRYSTAL RESONATOR



- Mechanical resonant frequency : $\omega_{mi} = \frac{1}{\sqrt{L_i C_i}}$
- Mechanical quality factor: $Q_i = \frac{1}{\omega_{mi} C_i R_i} \gg 1$
- $i_i \sim$ velocity \sim amplitude of mode i
- $C_i \sim$ electromech. coupling of mode i , $C_i \ll C_{12}$
- ω_{mi} of different modes are not exact multiples of each other, and $Q_i \gg 1$; therefore:

even if $v(t)$ is strongly distorted

all branches other than Z_{mi} are negligible

(for a single mode i of oscillation), and

the motional current i_i is always sinusoidal

MECHANICAL POWER AND ENERGY

- Mechanical energy of oscillation:

$$E_m = \frac{L\hat{I}^2}{2} = \frac{\hat{I}^2}{2\omega_m^2 C}$$

must be limited to avoid destruction, aging, and nonlinear effects.

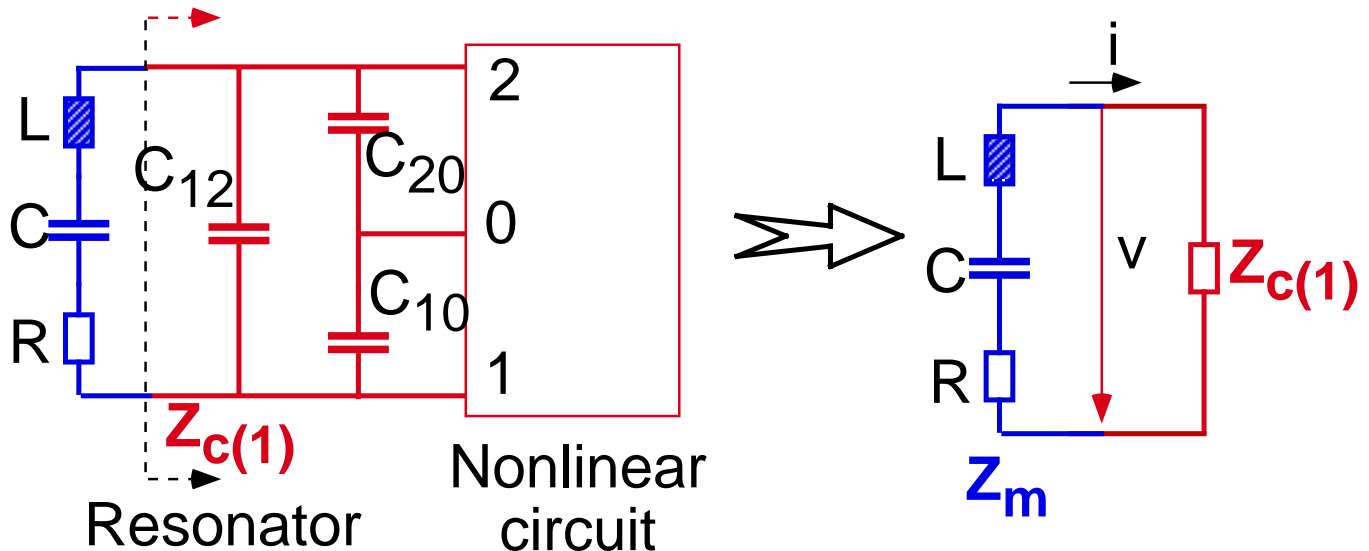
- Mechanical power dissipation:

$$P_m = \frac{R\hat{I}^2}{2} = \frac{\hat{I}^2}{2\omega_m Q C}$$

- Can be calculated as soon as the peak value \hat{I} of sinusoidal current $i(t)$ is known.

GENERAL FORM OF CRYSTAL OSCILLATOR

- The resonator is combined with an active circuit to sustain oscillation (compensate R)



- Frequency of oscillation ω slightly different of ω_m (effect of circuit)
- Frequency pulling $p = \frac{\omega - \omega_m}{\omega_m} \ll 1$
- The system must be conceptually split into:

Motional impedance $Z_m = R + j\frac{2p}{\omega C}$
(linear, strongly dependent on p)

Circuit impedance $Z_{c(1)}$, independent of p

Since no energy can be exchanged at harmonic frequencies (i sinusoidal), nonlinear effects are included by defining the circuit impedance at fundamental frequency:

$$Z_{c(1)} = \frac{V_{(1)}}{I}$$

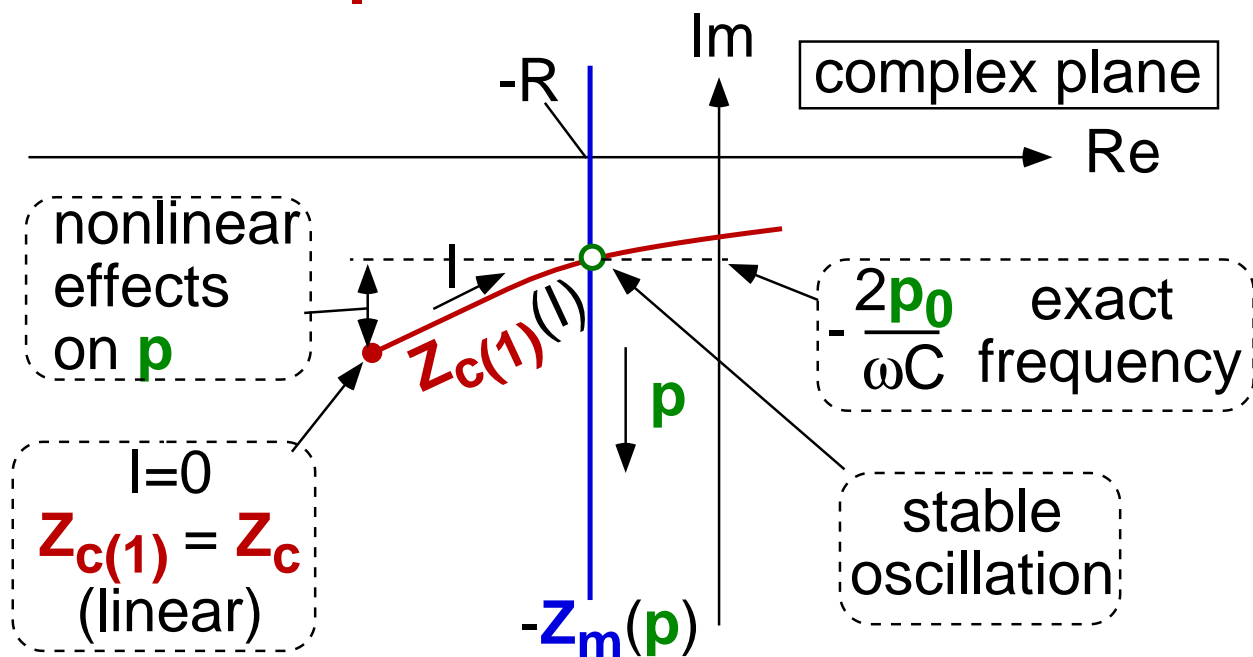
where $V_{(1)}$ is the complex value of the fundamental of v for complex value I of sinusoidal current i .

OSCILLATION

- Stable oscillation:

$$\boxed{Z_m + Z_{c(1)} = 0} \begin{cases} \text{Re}|Z_{c(1)}| = -R \\ \text{Im}|Z_{c(1)}| = -\frac{2p_0}{\omega C} \end{cases}$$

where $Z_{c(1)} = \frac{V_{(1)}}{I}$ circuit impeded. at fundam. frequency



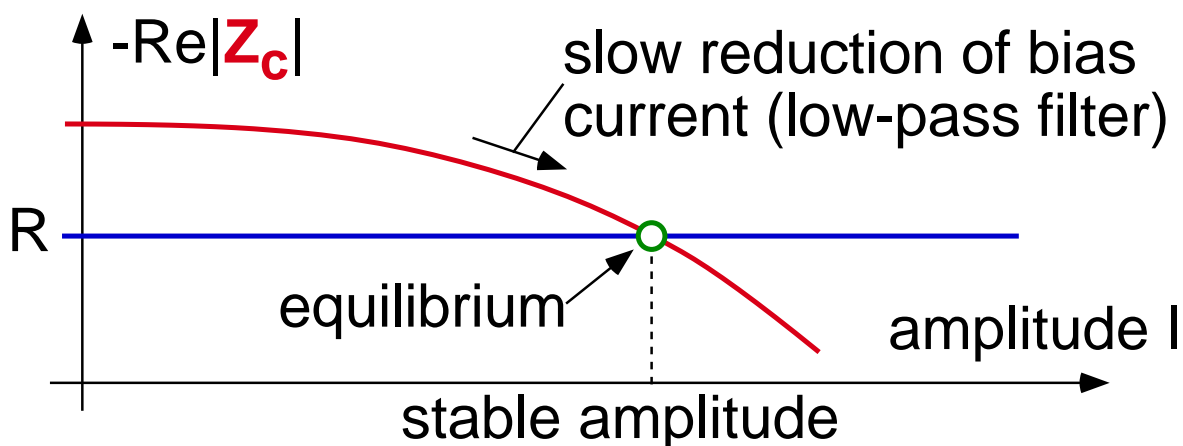
- Growth of oscillation:
exponential, with time constant $\tau = \frac{2L}{-\text{Re}|Z_{c(1)}| - R}$
- Critical condition for start-up of oscillation:

$$Z_m + Z_c = 0$$

(linear circuit)

AMPLITUDE LIMITATION

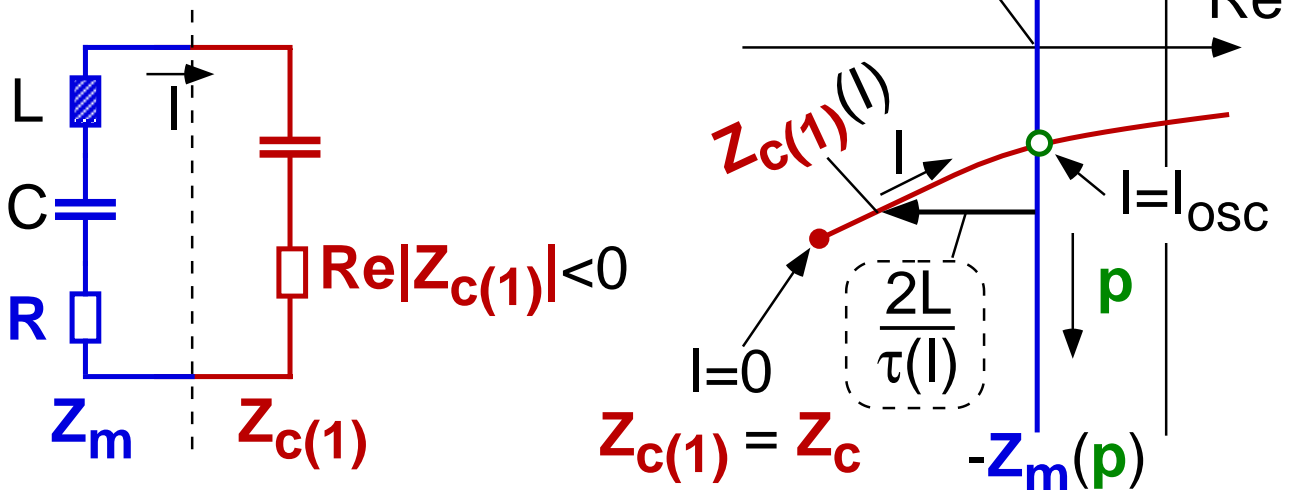
- Necessary to define amplitude
(an oscillator is always non linear)
- Instantaneous limitation by distortion:
 - creates harmonics
 - inter-modulation
 - addit. fundam. component of current
 - frequency change
 - poor stability
 - power dissipated in harmonics.
- Non-distorting amplitude limitation:
 - Z_c linear but slowly variable.



- + improved stability
- + reduced power dissipation in circuit
(just above critical condition).

START-UP TIME OF OSCILLATOR

- Equivalent circuit:

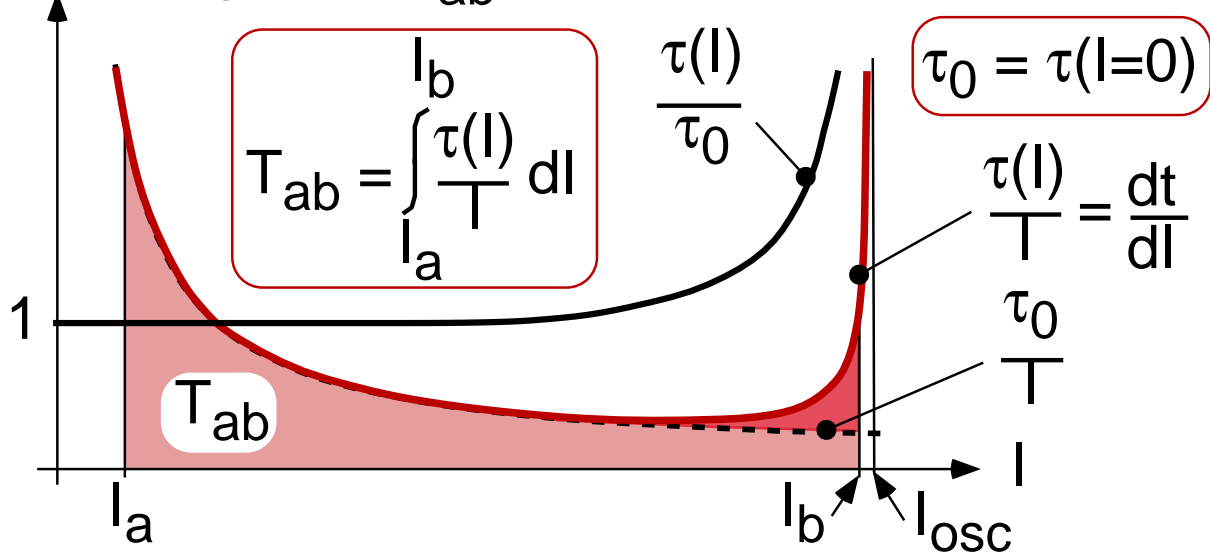


- Growth of oscillation:

$$I = I_0 e^{t/\tau(I)} \quad \text{with } \tau(I) = \frac{2L}{-\text{Re}|Z_{c(1)}| - R}$$

$$\frac{dI}{dt} = \frac{I}{\tau(I)} \rightarrow \boxed{\frac{dt}{dI} = \frac{\tau(I)}{I}}$$

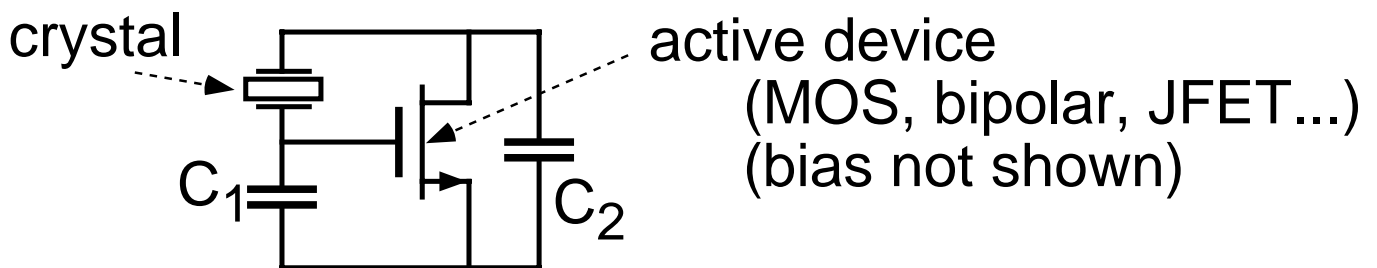
- Start-up time T_{ab} from $I_a(\text{noise})$ to I_b



- Approximation: $T_{ab} = \tau_0 \ln(I_b/I_a)$

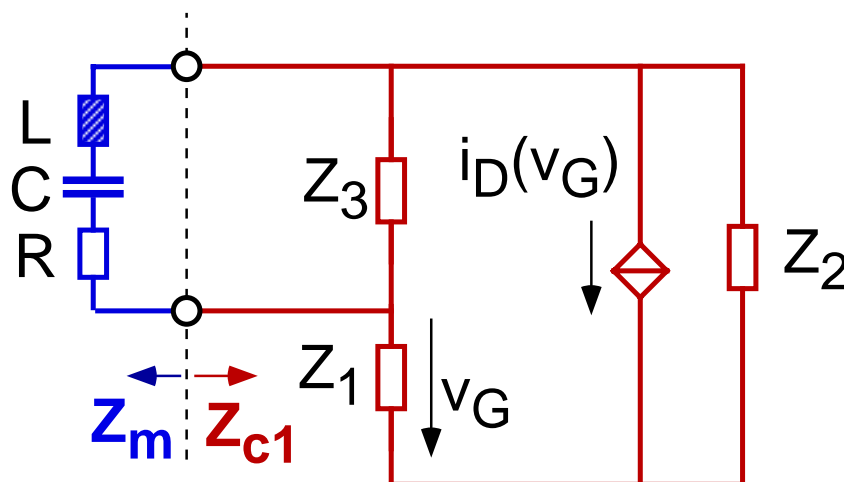
BASIC 3-POINT OSCILLATOR

- Only possibility to use a single active device when no inductance is available:



C_1, C_2 are necessary functional capacitors.

- General equivalent circuit:

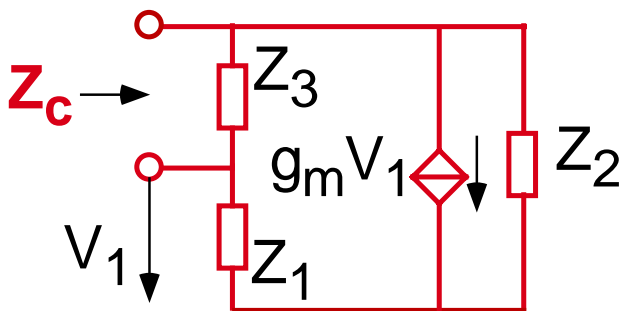


where $Z_i^{-1} = G_i + j\omega C_i$ (independent of p)

- include all circuit losses
- may be nonlinear.

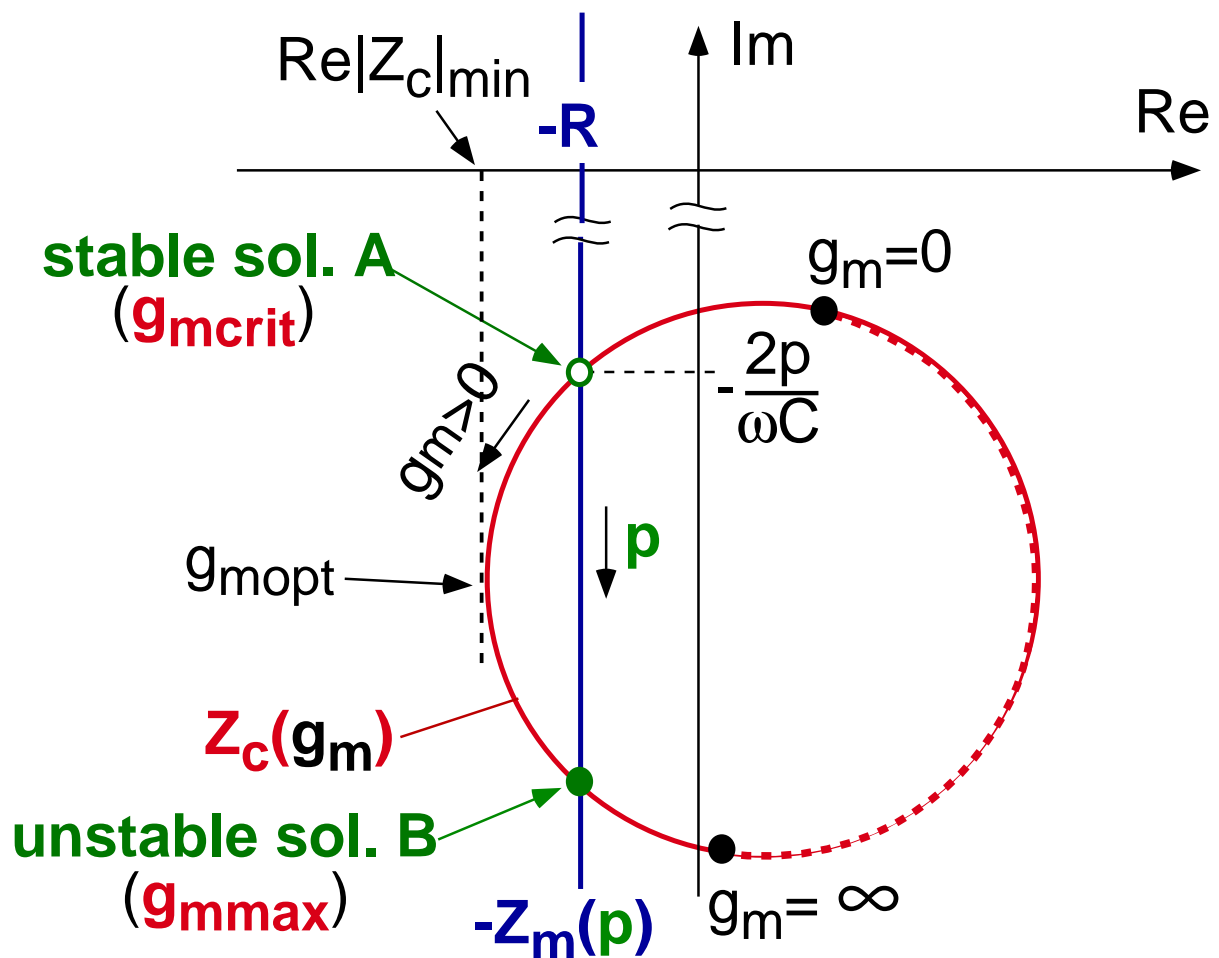
LINEAR ANALYSIS

- $Z_{c1} \rightarrow Z_c$ and $i_D(v_1) \rightarrow g_m V_1$
- General form of circuit (all losses included):



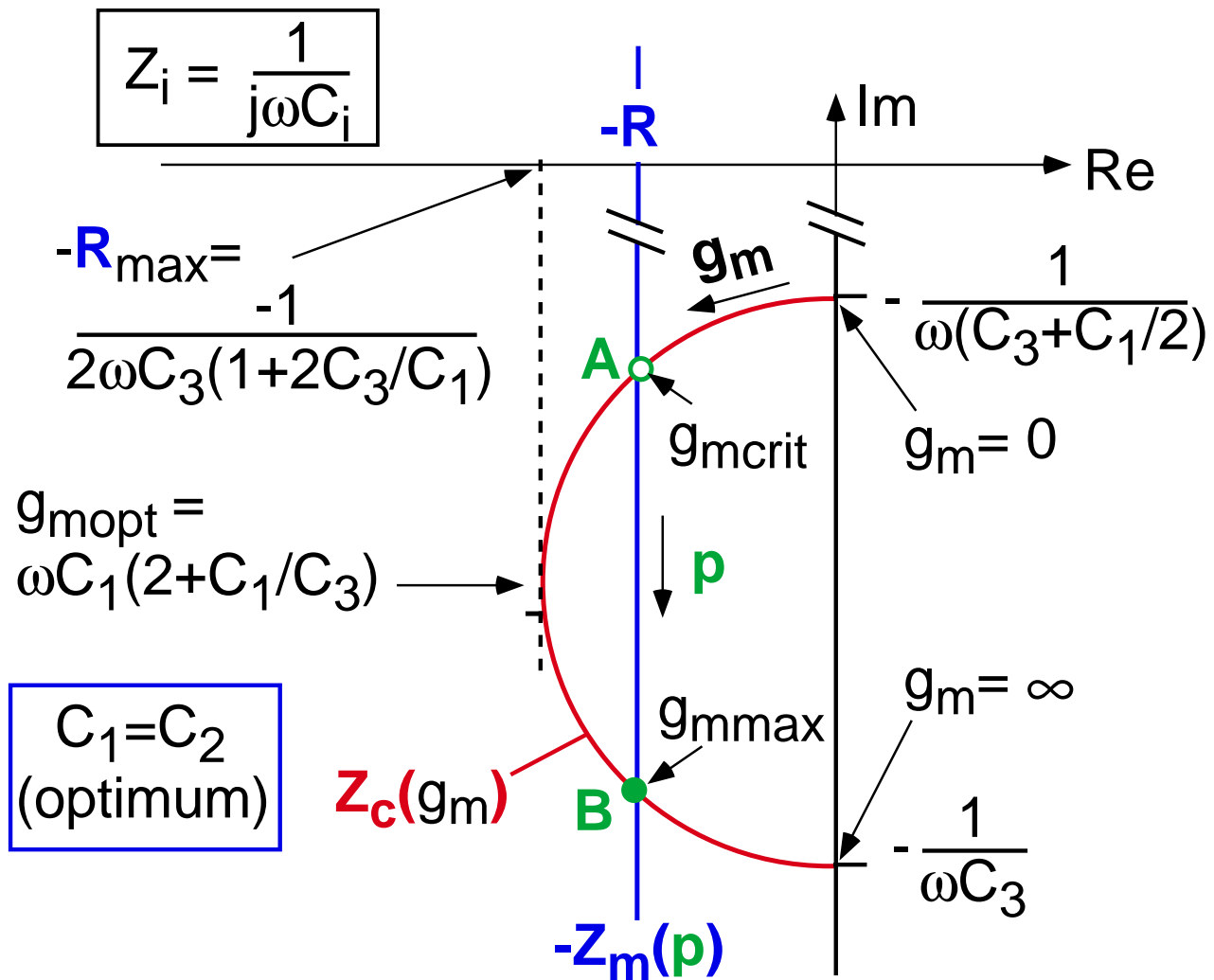
$$Z_c = \frac{Z_1 Z_3 + Z_2 Z_3 + g_m Z_1 Z_2 Z_3}{Z_1 + Z_2 + Z_3 + g_m Z_1 Z_2}$$

bilinear function of g_m



- No oscillation if g_m too small or **too large**.

LOSSLESS LINEAR ANALYSIS



- Oscillation **only possible** if: $\frac{QC}{C_3} > 2(1+2C_3/C_1)$

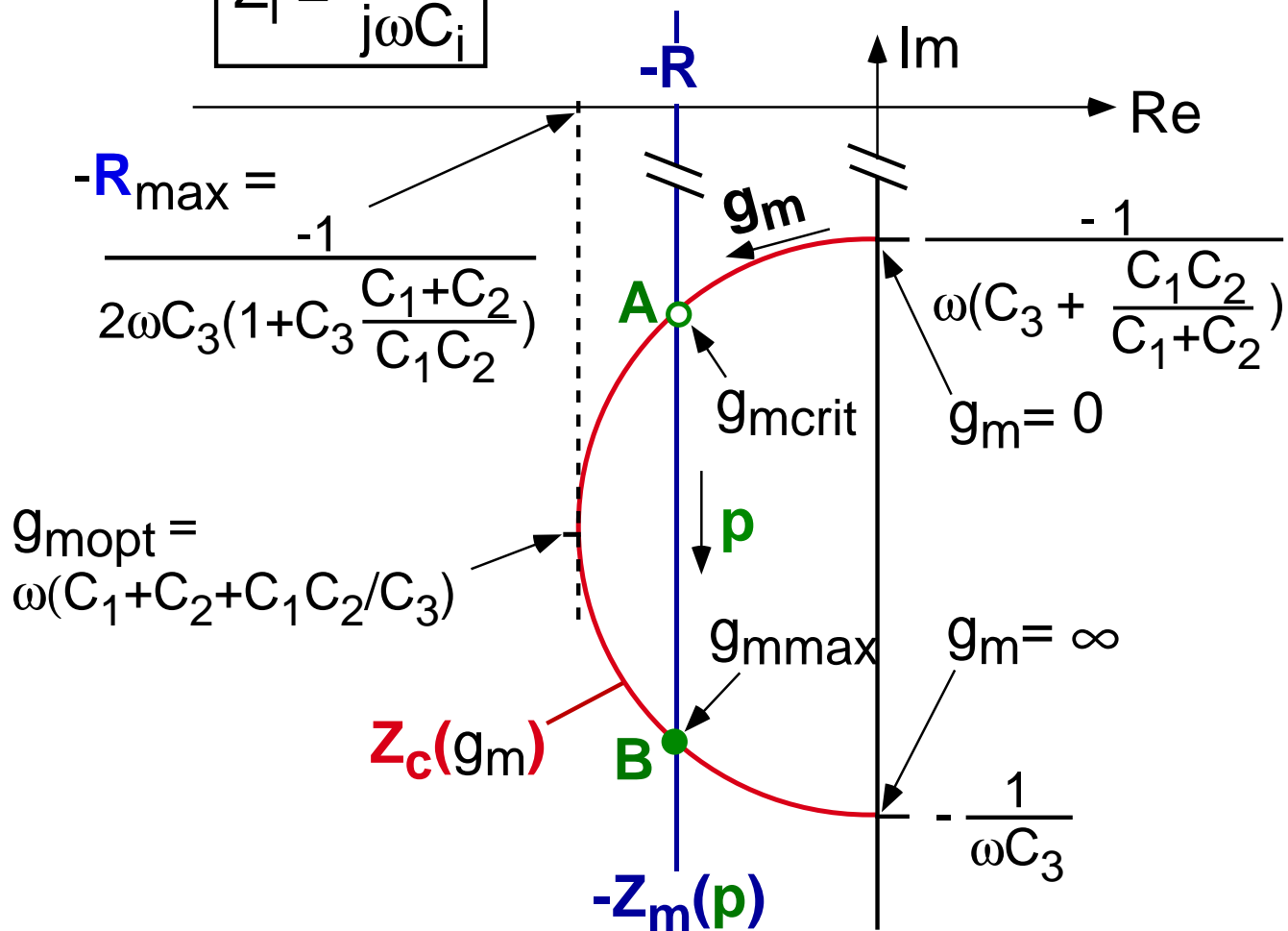
If large margin to minimize $d\mathbf{p}/dR$, then:

- $\mathbf{p}_0 = \frac{\omega_0 - \omega_m}{\omega_m} \cong \frac{C}{2C_3+C_1}$
 - $g_{m\text{crit}} \cong \frac{\omega}{QC} (C_1+2C_3)^2 = \frac{\omega C}{Q\mathbf{p}_0^2}$
 - $g_{m\text{max}} \cong \omega C C_1^2 Q / C_3^2$
- trade-off
- thus: $\frac{g_{m\text{max}}}{g_{m\text{crit}}} \cong \left[\frac{C C_1 Q}{C_3(C_1+2C_3)} \right]^2 \cong \left[\frac{QC}{C_3} \right]^2$ for $C_3 \ll C_1$

LOSSLESS LINEAR ANALYSIS

OSC-8a

$$Z_i = \frac{1}{j\omega C_i}$$



- Oscillation **only possible** if: $\frac{QC}{C_3} > 2(1 + C_3 \frac{C_1 + C_2}{C_1 C_2})$
If large margin to minimize dp/dR , then:

- $p_0 = \frac{\omega_0 - \omega_m}{\omega_m} \cong \frac{C}{2(C_3 + \frac{C_1 C_2}{C_1 + C_2})}$ **min.** for $C_1 = C_2$
- $g_{mcrit} \cong \frac{\omega}{QC} \frac{(C_1 C_2 + C_2 C_3 + C_3 C_1)^2}{C_1 C_2} = \frac{\omega C}{Q p_0^2} \frac{(C_1 + C_2)^2}{4 C_1 C_2}$ **trade-off**
- $g_{mmax} \cong \omega C C_1 C_2 Q / C_3^2$ for $C_3 \ll C_1$ and C_2

thus: $\frac{g_{mmax}}{g_{mcrit}} \cong \left[\frac{C C_1 C_2 Q}{C_3 (C_1 C_2 + C_2 C_3 + C_3 C_1)} \right]^2 \cong \left[\frac{QC}{C_3} \right]^2$

EFFECT OF LOSSES

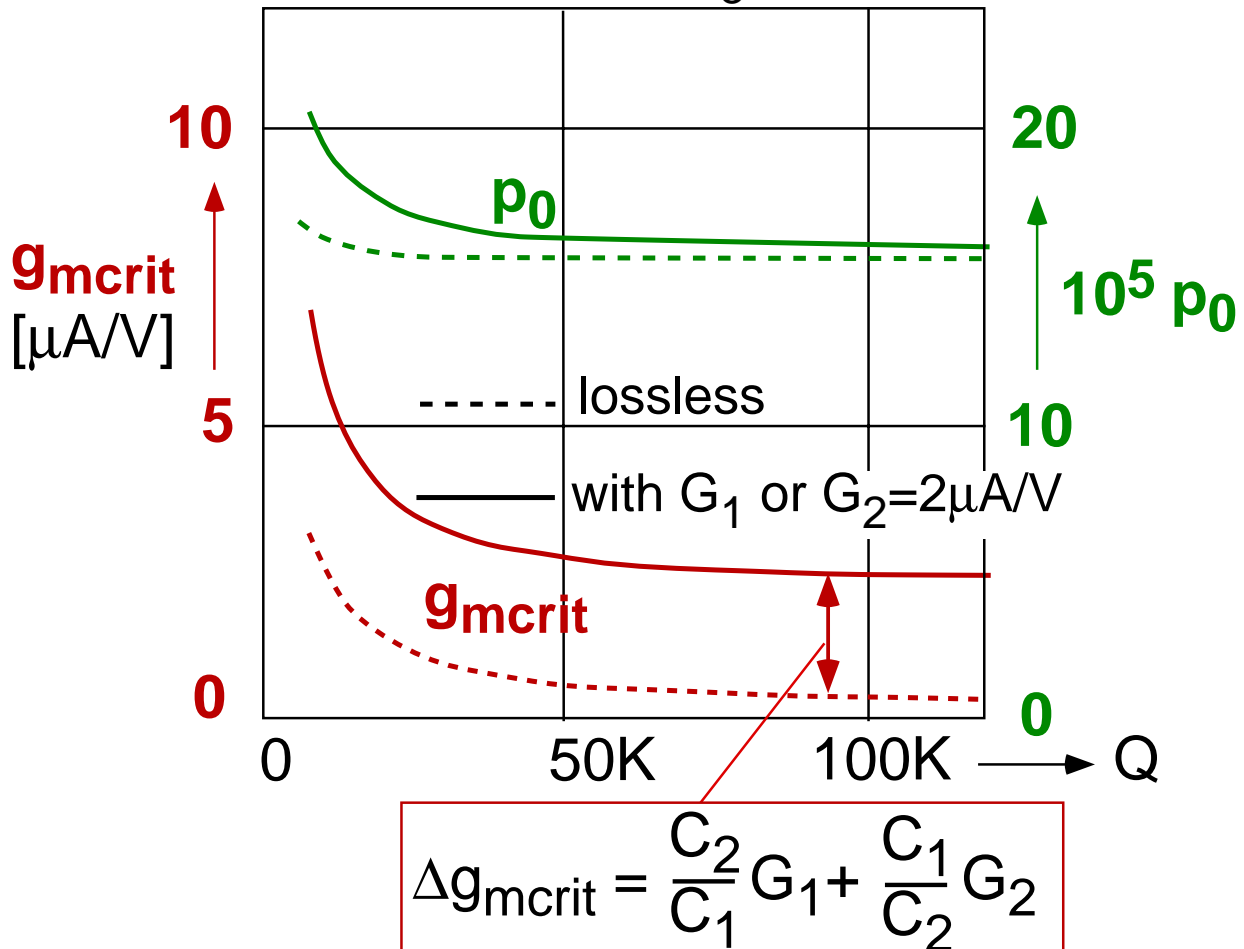
- Example of linear analysis with:

$$C = 3\text{fF}$$

$$C_1 = C_2 = 15\text{pF}$$

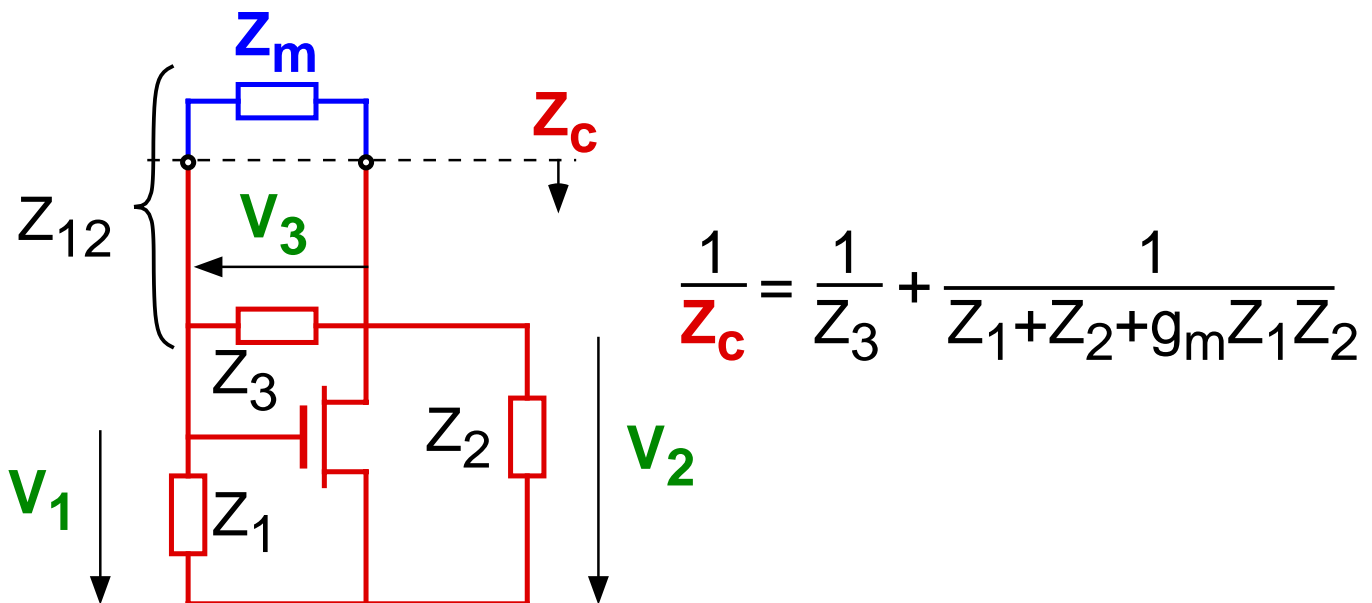
$$f = 32\text{KHz}$$

$$C_3 = 2\text{pF}$$



- Causes of losses:
 - biasing circuitry
 - loading by amplifier
 - series resistance of capacitors (HF)
 - output conductance of active device
 - input conductance of active device (bipolar)
 - external load (moisture)

RELATIVE VOLTAGE AMPLITUDES



$$\frac{1}{Z_c} = \frac{1}{Z_3} + \frac{1}{Z_1 + Z_2 + g_m Z_1 Z_2}$$

- Critical oscillation: $Z_m = -Z_c$
 thus: $1/Z_{12} = 1/Z_m + 1/Z_3 = -1/Z_c + 1/Z_3$
 yields: $Z_{12} = -(Z_1 + Z_2 + g_{mcrit} Z_1 Z_2)$

$$1 + Z_{12}/Z_1 = V_2/V_1 = -Z_2(1/Z_1 + g_{mcrit})$$

$$V_3/V_1 = V_2/V_1 - 1$$

- Lossless circuit ($Z_i = 1/j\omega C_i$) with $R \ll R_{max}$

$$g_{mcrit} = \frac{\omega}{QC} \frac{(C_1 C_2 + C_2 C_3 + C_3 C_1)^2}{C_1 C_2}$$

$$\text{yields: } \frac{V_2}{V_1} = -\frac{C_1}{C_2} + j \frac{C_1}{QC} \left(1 + \frac{C_3}{C_1} + \frac{C_3}{C_2}\right)^2$$

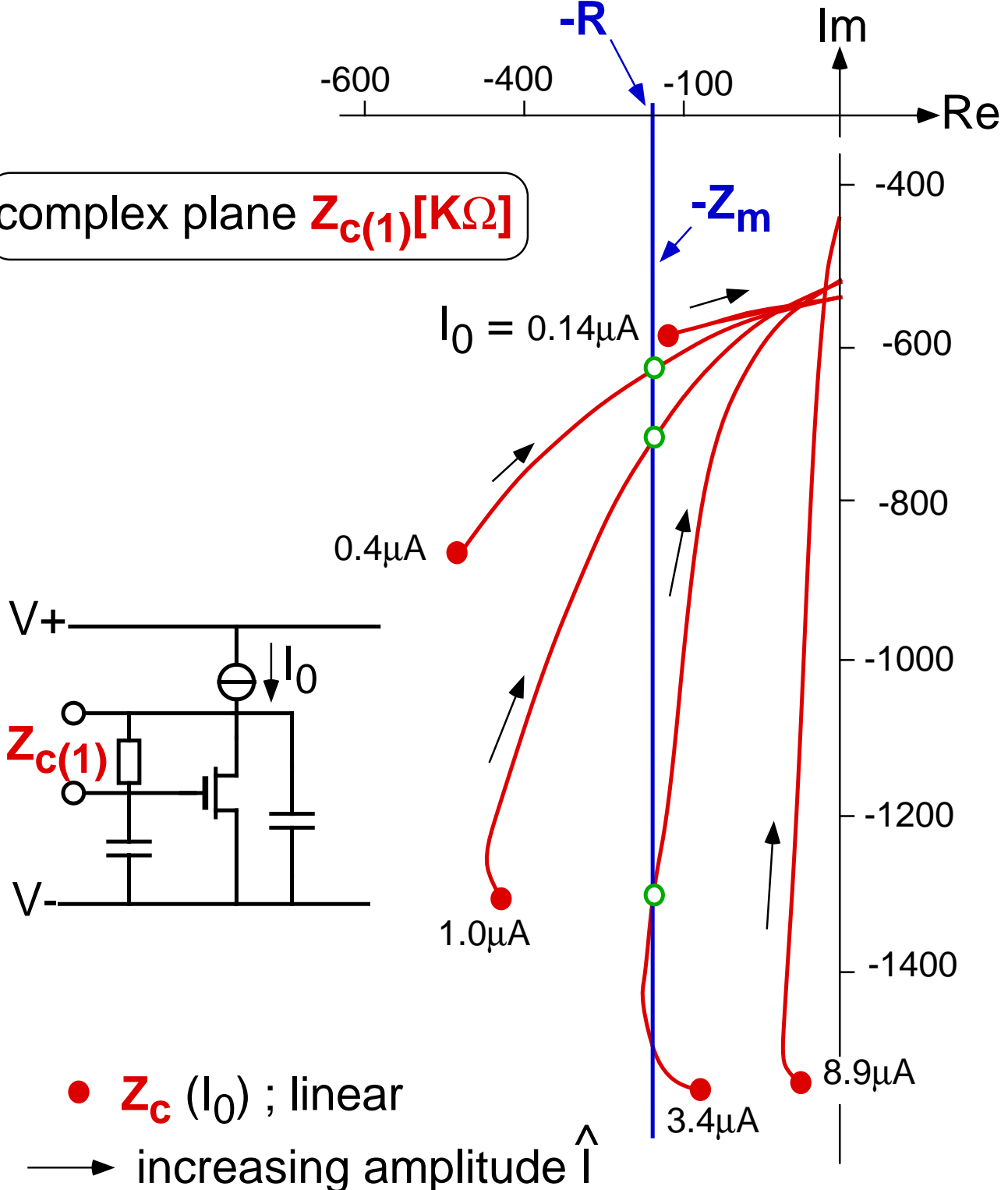
usually $<$ or $\ll 1$

$$\text{Then: } V_2/V_1 \cong -C_1/C_2 \quad \text{and} \quad V_3/V_1 \cong -(1 + C_1/C_2)$$

EXAMPLE OF NONLINEAR ANALYSIS

[L.Astier, 1987]

complex plane $Z_{c(1)}[K\Omega]$



• $Z_c(I_0)$; linear

→ increasing amplitude \hat{I}

○ stable oscillation for particular value of R

DISTORTION OF GATE SIGNAL

- Drain current is distorted

V_2 is distorted
- Drain to gate attenuation:
 - for fundamental frequency: $F = \frac{V_1}{V_2} \Big|_{\text{fund.}} \cong -\frac{C_2}{C_1}$
 (as shown before)
 - for harmonic components: $H = \frac{V_1}{V_2} \Big|_{\text{harm.}} \cong \frac{C_3}{C_1 + C_3}$
 ($Z_m = \infty$)
 - relative attenuation $\left| \frac{H}{F} \right| = \frac{C_3 C_1}{(C_1 + C_3) C_2}$
 usually $\ll 1$, thus V_1 approximately **sinusoidal**
- Effect of residual distortion of V_1 :
 - intermodulation of harmonics in transistor
 - creation of out-of-phase fund. in drain
 - current
- C_3 must therefore be **minimized** (change in p, \Rightarrow frequency instability) (Z_3 large)

AMPLITUDE LIMITATION BY $i_D(v_G)$

- Small effect on **p** (none if $Z_3 = \infty$).
- Assumption: AC signal at gate sinusoidal:

$$v_G = V_0 + V_1 \sin \omega t$$

Results in: $i_D = f(v_G) = I_0 + I_1 \sin \omega t + \text{harmonics}$

then: $I_1/V_1 = \mathbf{g_{m1}}(V_1) = g_{m\text{crit}}$

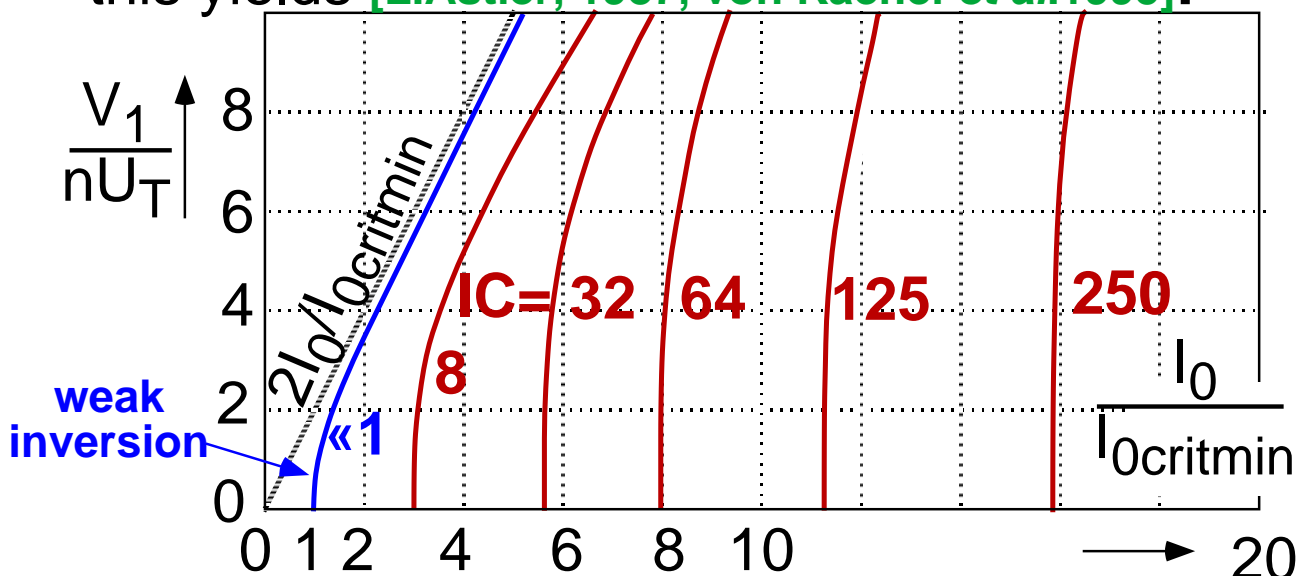
transconductance for
fundamental frequency

for **stable oscillation**

- Using continuous model for saturated MOS

$$i_D = I_S \ln^2(1 + e^{v/2}) \quad \begin{matrix} \text{[Vittoz, 1994]} \\ \text{[Enz et al., 1995]} \end{matrix}$$

where $v = (v_{GS} - V_T)/(nU_T)$ and $I_S = 2n\beta U_T^2$
this yields [L.Astier, 1987, von Kaenel et al.1995]:



V_1 = peak voltage amplitude at gate of transistor

I_0 = bias current of transistor

$I_{0\text{critmin}} = nU_T g_{m\text{crit}}$

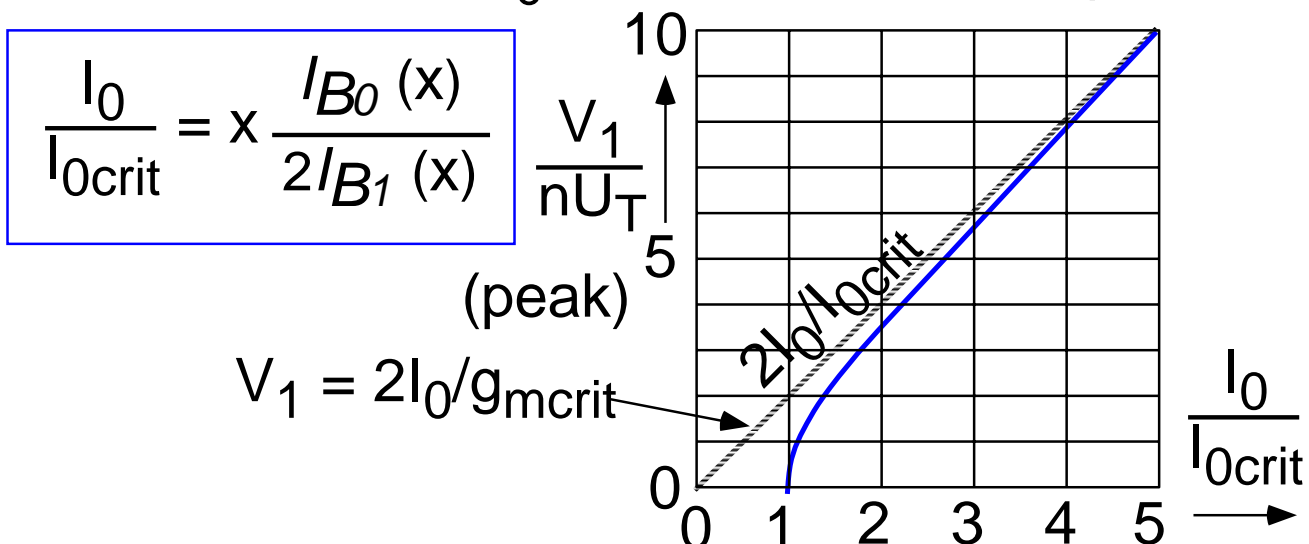
IC = $I_{0\text{crit}}/I_S$ = inversion coefficient at $I_{0\text{crit}}$

- $I_0(V_1)$ is minimum in weak inversion ($I_{0\text{critmin}}$).

AMPLITUDE OF OSCILLATION

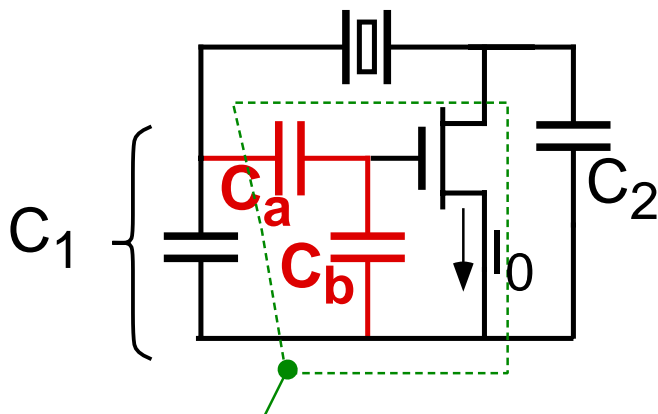
- Limitation by nonlinear $i_D(v_G)$ only
 → Very small effect on frequency pulling **p**
 (none if $Z_3 = \infty$).
- Goal: minimum current to produce $g_{m\text{crit}}$:
 → transistor operated in **weak inversion**:
 $i_D = A \exp(v_G/nU_T)$ (with $n=1.4...1.6$)
- Assumption: AC signal at gate sinusoidal:
 $v_G = V_0 + V_1 \sin(\omega t)$
 results in: $i_D = I_0 + I_1 \sin(\omega t) + \text{harmonics}$
 where: $I_1 = I_0 \frac{2I_{B1}(x)}{I_{B0}(x)}$ with $x=V_1/nU_T$
 and $I_{Bk}(x)$ are modified Bessel functions of order k
- Transconductance **g_{m1}** for the fundamental:
 $g_{m1} = I_1/V_1 = g_{m\text{crit}} = I_{0\text{crit}}/(nU_T)$
 stable oscillation

Yields bias current I_0 as a function of amplitude V_1 :



LARGER AMPLITUDES

- Limited overdrive to avoid excessive distortion
- Use capacitive input attenuator C_a - C_b :

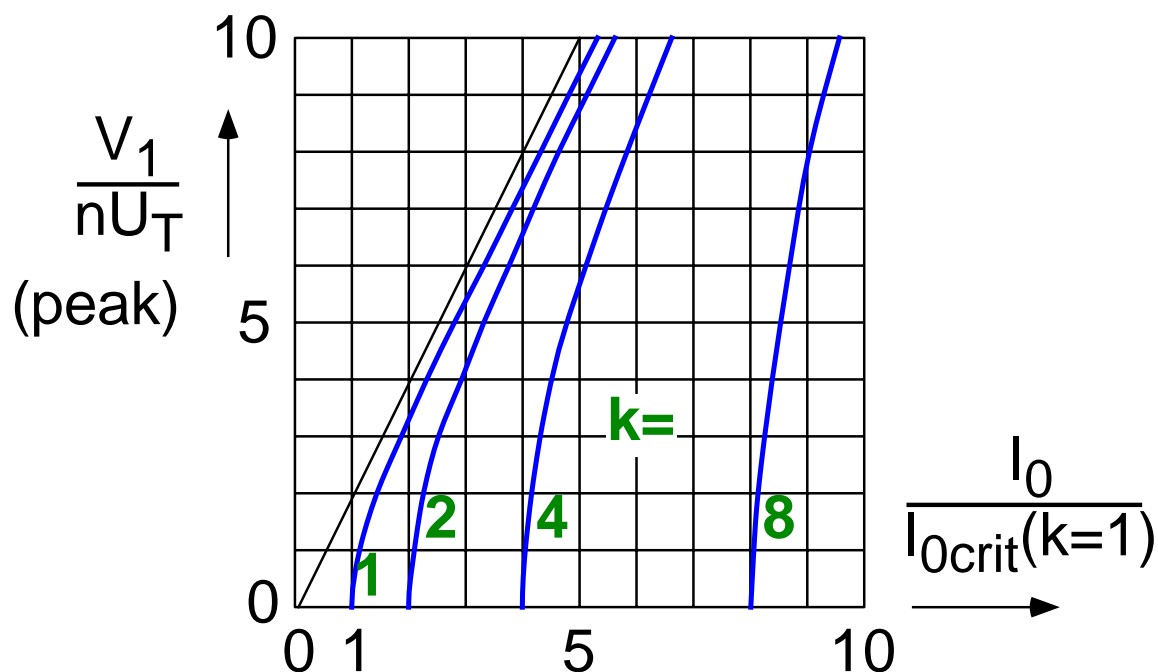


- Attenuation $1/k = \frac{C_a}{C_b + C_a}$
- C_b includes C_G
- In weak inversion:

$$C_G = C_{ox}(1 - 1/n)$$

equivalent to transistor with $U_T \Rightarrow kU_T$

- Result for transistor in **weak** inversion:
 $g_{mequ} = I_0 / (knU_T)$, thus V_1 and I_0 amplified by k .



- Alternative solution: **strong** inversion
 - might be necessary for $f \gg 10\text{MHz}$
 (large $W/L \rightarrow$ large C_1 and C_2)

AMPL. LIM. BY $i_D(v_G)$ IN STRONG INVERSION

- Assumption: AC signal at gate sinusoidal:

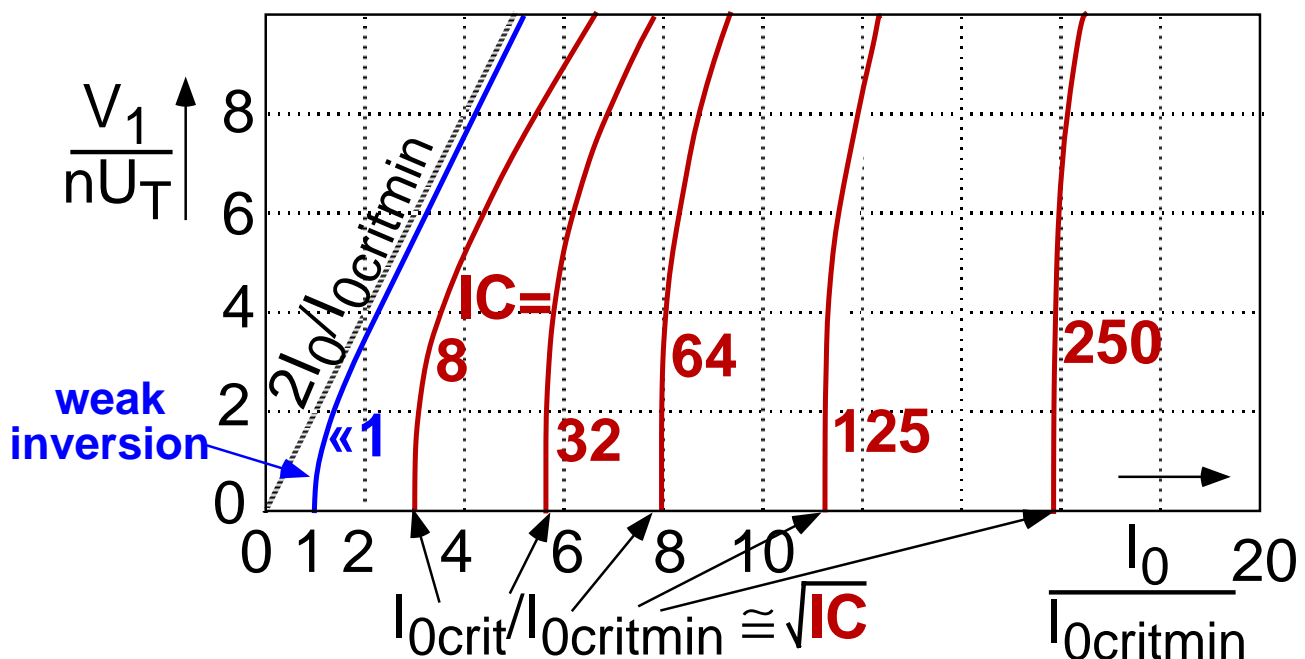
$$v_G = V_0 + V_1 \sin(\omega t)$$

results in: $i_D = I_0 + I_1 \sin(\omega t) + \text{harmonics}$

- $I_1/V_1 = g_{m1}(V_1) = g_{m\text{crit}}$ can be calculated numerically by using a continuous model for saturated MOS transistor :

$$i_D = I_S \ln^2(1 + e^{v/2})$$

where $v = (v_{GS} - V_T)/(nU_T)$ and $I_S = 2n\beta U_T^2$
this yields [L.Astier, 1987]:



V_1 = peak voltage amplitude at gate of transistor

I_0 = DC bias current of transistor

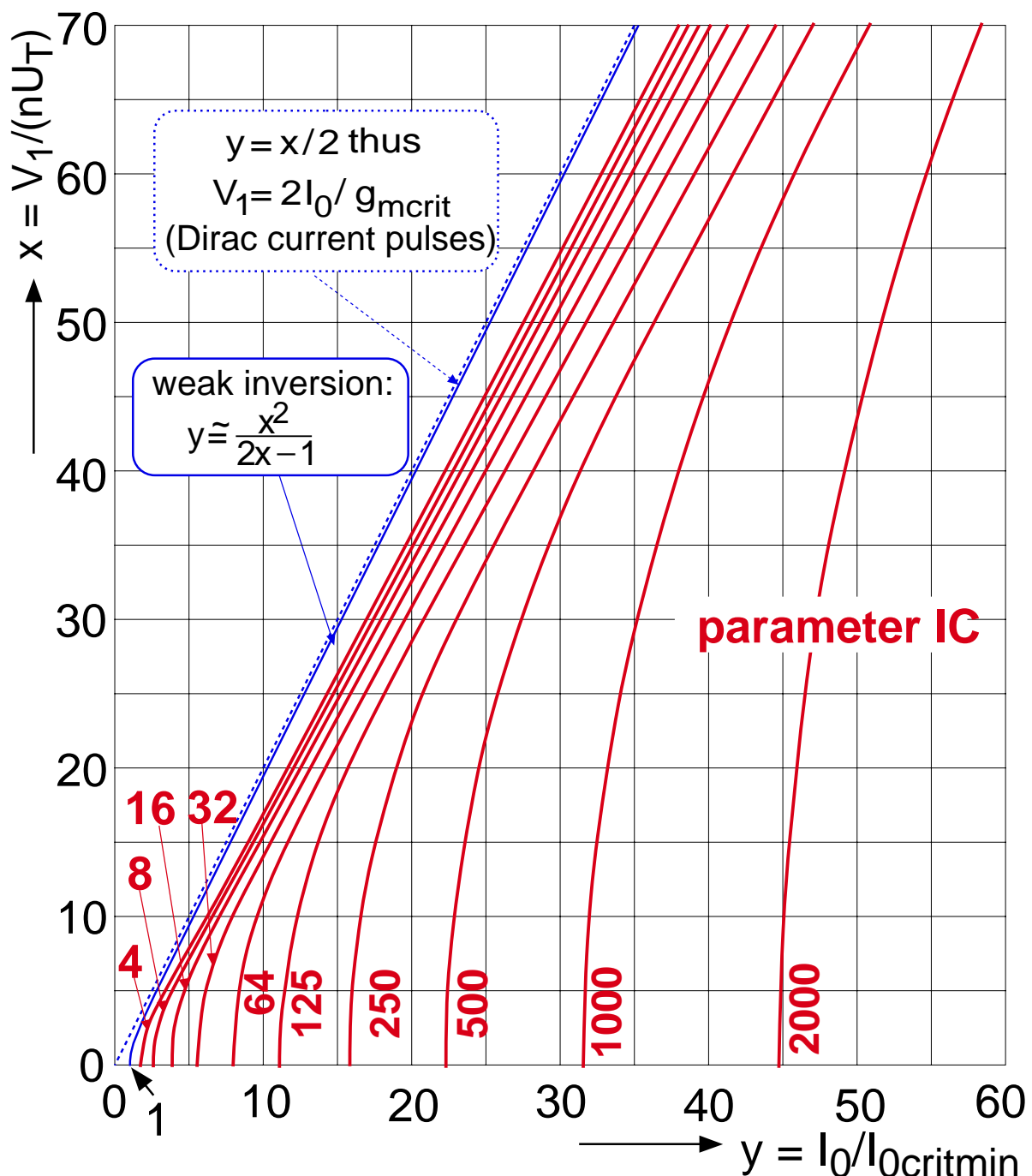
$I_{0\text{critmin}} = nU_T g_{m\text{crit}}$ (weak inversion)

$IC = I_{0\text{crit}}/I_S = \text{inversion coefficient at } I_{0\text{crit}}$

CHART FOR LARGE AMPLITUDES

[L.Astier, 1987]

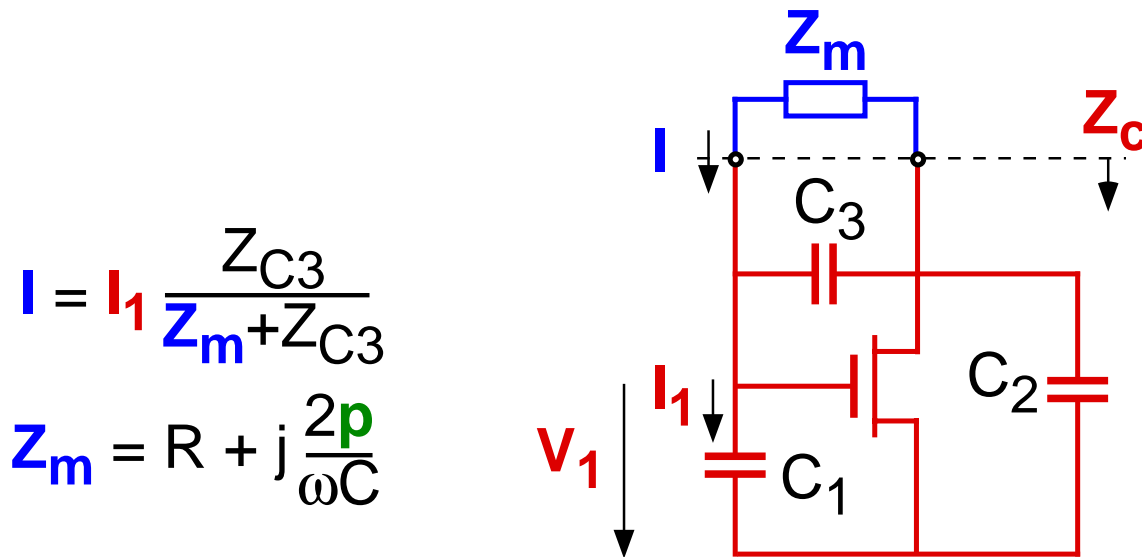
- Assumptions:
 - gate voltage sinusoidal (peak V_1)
 - transistor always saturated
 - constant mobility
 - constant Q , linear Z_1, Z_2 and Z_3
- Definitions:
 - $I_{0critmin} = I_{0crit}$ in weak inversion
 - IC** = I_{0crit}/I_S with $I_S = 2n\beta U_T^2$



BASIC DESIGN PROCEDURE

	main criteria	ref.OSC
1. Select crystal resonator frequency	frequency	
	temp. stability	
	cost, size	
2. Choose value of $C_1=C_2$	precision	12
	power	8a
	"circle"	8a
3. Calculate p_0 and $\omega_m=\omega_0(1-p_0)$		8a
4. Calculate g_{mcrit}		8a, 9
	$I_{0critmin}$	11c
5. Fix ampl. of oscill. V_1	too small:	
	- phase noise	13b
	- amplification	14a
	- jitter of amplif.	
	too large:	
	- power	
	- aging	
6. Fix amount of overdrive	too small:	11d
	- large I_0/V_1	
	too large:	
	- poor stability	12
	- risk of overtone	14
7. Select $IC=I_{0crit}/I_S$	from 5. and 6.	11d
8. Calculate I_{0crit} , I_0 , $I_S=2n\beta U_T^2$, β , W/L		11d
9. Calculate energy E_m and phase noise		13a,b
10. Return to 2, 5 or 6, or detailed design.		

ENERGY OF MECHANICAL OSCILLATION



$$I = I_1 \frac{Z_{C3}}{Z_m + Z_{C3}}$$

$$Z_m = R + j \frac{2p}{\omega C}$$

(I , I_1 and V_1 are complex **RMS** values)

Thus:

$$I = I_1 \frac{-j/\omega C_3}{R + 2pj/\omega C - j/\omega C_3}$$

Assumptions:

negligible $2p \gg \omega CR = 1/Q$ $p = \frac{C}{2(C_3 + C_1 C_2 / (C_1 + C_2))} \ll \frac{C}{2C_3}$ *dominate*

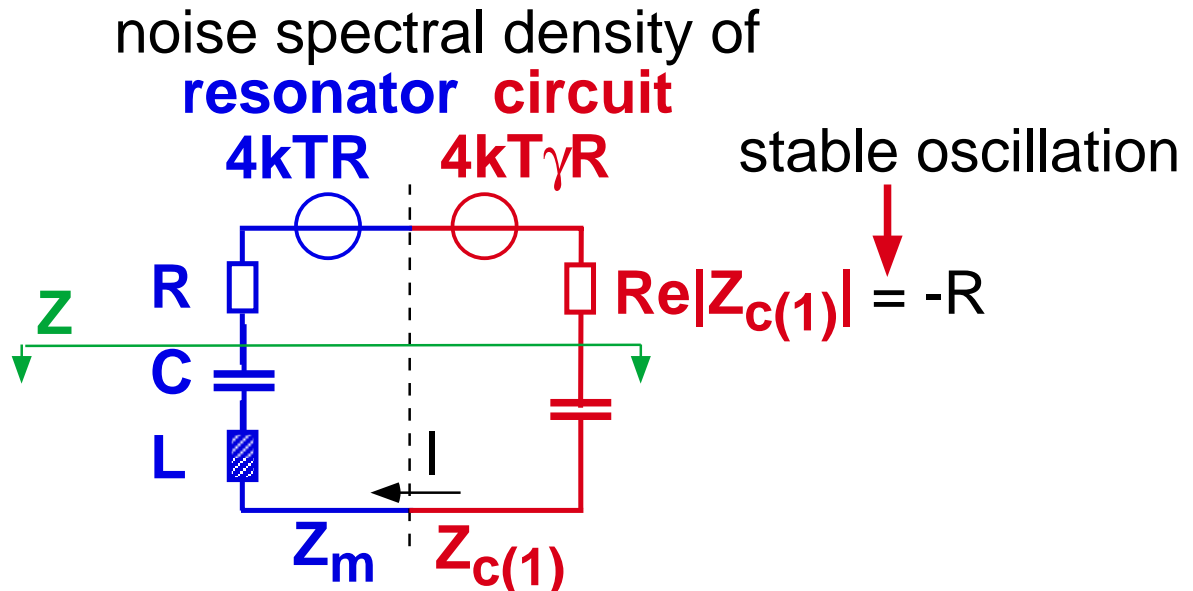
Then: $I \cong I_1 \left(1 + \frac{C_3}{C_s} \right)$ where $C_s = \frac{C_1 C_2}{C_1 + C_2}$

$I \cong j\omega C_1 V_1 \left(1 + \frac{C_3}{C_s} \right)$ current through motional impedance Z_m

- Mechanical energy: $E_m \cong \frac{I^2}{\omega^2 C} = \frac{C_1^2 |V_1|^2}{C} \left(1 + \frac{C_3}{C_s} \right)^2$

PHASE NOISE

- Simple model [Leeson, 1966] (linear, time invariant)
- Equivalent circuit at stable oscillation



- Impedance loading the noise sources:

$$Z = 2j\omega L \left(\frac{f - f_0}{f_0} \right) = 2jQR \left(\frac{f - f_0}{f_0} \right) \quad \text{for } |f - f_0| \ll f_0$$

where f_0 is the frequency of oscillation

- Noise current I_N circulating in the loop:

$$\frac{dI_N^2}{df} = \frac{4kT(1+\gamma)R}{|Z|^2} = \frac{(1+\gamma)kT}{Q^2R} \left(\frac{f_0}{f - f_0} \right)^2$$

- Phase noise spectral density:

$$\frac{d\phi_N^2}{df} = \frac{1}{2} \frac{dI_N^2/df}{I^2} \quad \text{(half phase noise, half amplitude noise)}$$

$$\frac{d\phi_N^2}{df} = \frac{(1+\gamma)kT}{2Q^2P_m} \left(\frac{f_0}{f - f_0} \right)^2 = \frac{(1+\gamma)kT}{2\omega QE_m} \left(\frac{f_0}{f - f_0} \right)^2$$

- Nonlinear, time-variant:

noise may added, including $1/f$ [Hajimiri-Lee, 1999]

FREQUENCY INSTABILITY

Cause

Remedy

a. Crystal resonator

- Aging
- Temperature

- Pre-aging.
- Better cut
- analog or digital compensation.

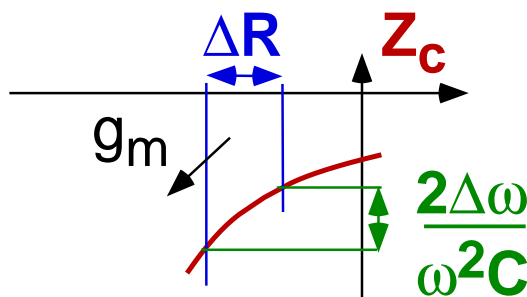
b. Nonlinear effects in circuit (variations with V_B , V_T , T)

- Nonlinear Z_1 , Z_2 or Z_3
- Nonlinear $I_D(V_G)$

- Keep trans.in saturation
- avoid $C(V)$ effects.
- Reduce overdrive
- stabilize amplitude
- increase $|Z_3|$.

c. Variation of linear effects

- Variation of $R \sim 1/Q$



- Variation of losses
- Variation of C_1 , C_2 , C_3

- Increase Q
- reduce losses in circuit.
- increase $\frac{C_1 C_2}{C_3 (C_1 + C_2)}$
- Reduce losses
- Decrease pulling p
- avoid $C(V)$ effects
- stabilize V_B .

FREQUENCY TUNING

- On the resonator:
precision limited to a few 10^{-5} .

- By C_1 and/or C_2 in the circuit:

tuning range:

$$\frac{f_{\max} - f_{\min}}{f} = \frac{p_{\max}}{p_{\min}}$$

C_1, C_2 small
large effect of circuit

g_m large

degrades stability

increases power
consumption

- Digital tuning:
 - adjust the ratio of subsequent counters
 - inhibit an adequate percentage of pulses
requires a few bits of memory:
pad bondings
RAM
E²PROM.

ELIMINATION OF UNWANTED MODES

- A resonator has always several mech. modes (parallel series resonator in model).
- One mode is wanted (**WM**)
- All other modes are unwanted (**UM**).

$$g_{m\text{crit}} = \sim \frac{\omega}{QC} \underbrace{(C_1 + 2C_3)^2}_{\text{same for all modes}} \quad (\text{for } C_2 = C_1)$$

$$\downarrow$$

$$= \omega^2 R$$

activity different for each mode

a. Non-distorting amplitude limitation

- No interaction between modes; g_m decreases until the most active reaches critical amplitude.
- **WM** ensured if $\omega^2 R|_{\text{WM}} < \omega^2 R|_{\text{UM}}$

b. Distorting amplitude limitation

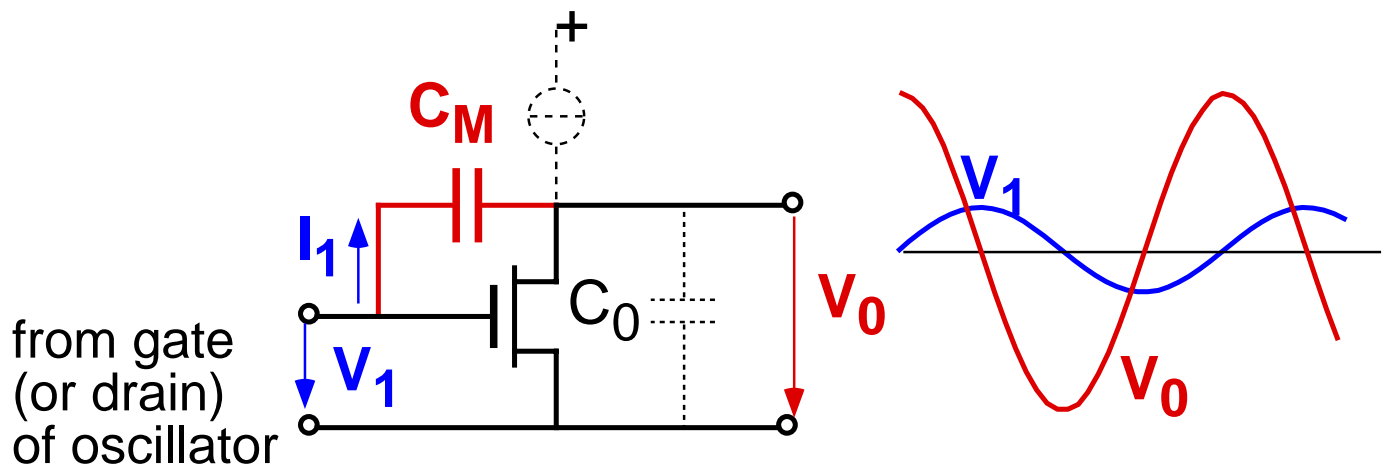
- Possible interaction between modes (very complicated).
- Safe solution: $g_{m\text{crit}}|_{\text{WM}} < g_m < g_{m\text{crit}}|_{\text{UM}}$
requires $\omega^2 R|_{\text{WM}} \ll \omega^2 R|_{\text{UM}}$

c. Selection of **WM** of lesser activity

- frequency selective $Z_c \rightarrow$ degrades stability.
 - low- or high-pass for large difference in ω_m
 - LC bandpass to select a particular overtone

LOADING BY OUTPUT AMPLIFIER

- Elementary voltage amplifier, gain $A = |V_0|/|V_1|$



- Capacitive load: $V_0 = j A V_1$ (complex gain)
- Miller capacitance C_M , thus, for $A \gg 1$

$$I_1 = -j\omega C_M V_0 = \omega A C_M V_1, \text{ in phase with } V_1$$

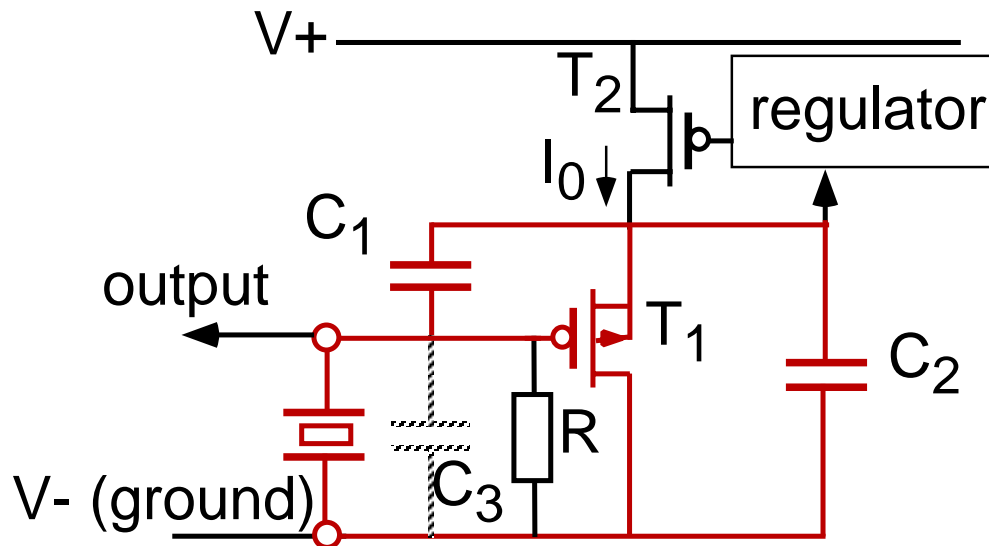
- Input **conductance** $G_1 = I_1/V_1 = \omega C_M A$
may be large if C_M and A large.

↓
significant loss in oscillator

- Increasing V_1 requires more current in lossless oscillator, but reduces loss due to G_1 : **trade-off**.

GROUND-ED-DRAIN OSCILLATOR

[Luescher, 1968, Santos-Meyer, 1984]

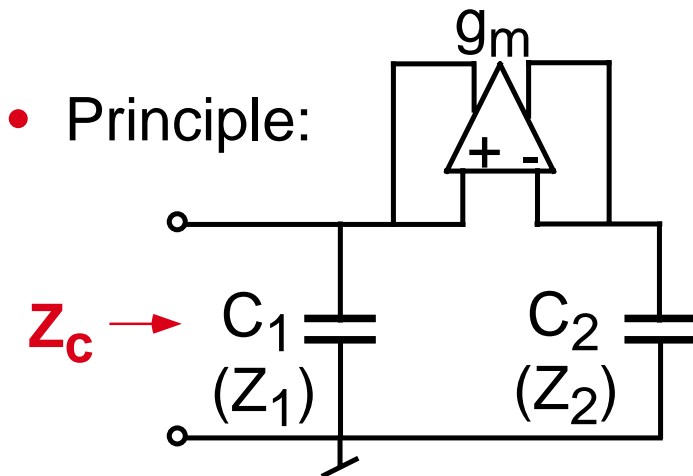


T_1 active, biased by R and current source T_2 .

- + One single pin for resonator ("1-pin oscillator").
- + Doubled output amplitude.
- Increased C_3 : decreases stability and/or increases power.
- T_1 must be put in a separate well connected to its source; otherwise an additional conductance $g_m(n-1)$ is added to G_2 (large increase of losses).

ONE-PIN OSCILLATOR WITH GROUNDED C's

[van den Homberg, 1998/99]



$$Z_c = \frac{Z_1 + g_m Z_1 Z_2}{1 + g_m (Z_1 - Z_2)}$$

bilinear function of g_m

- For $Z_i = \frac{1}{j\omega C_i}$:

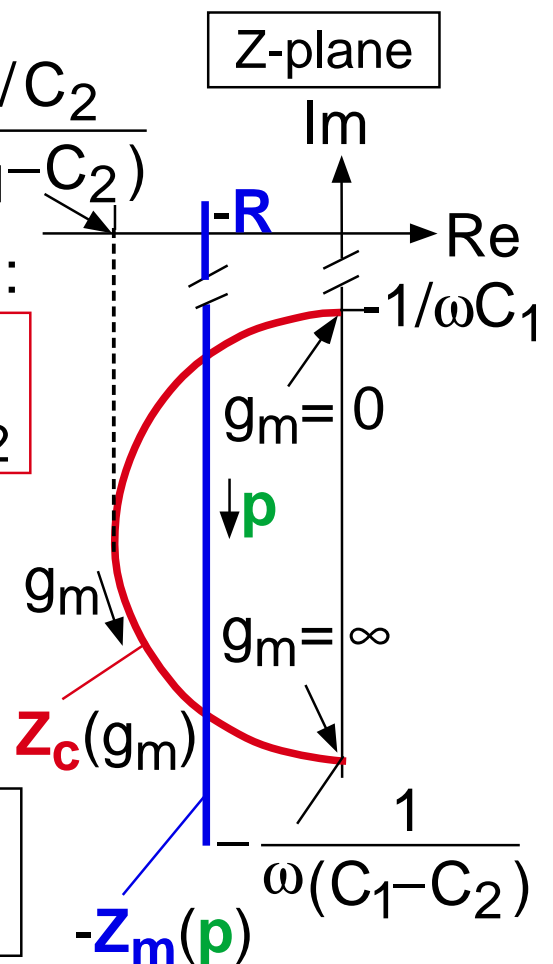
- Necessary condition for oscill.:

$$R < \frac{C_1/C_2}{\omega(C_1 - C_2)} \rightarrow Q > \frac{C_1 - C_2}{C \cdot C_1/C_2}$$

- If realized with large margin:

$$p_0 = \frac{C}{2C_1}$$

$$g_{m\text{crit}} = \frac{\omega}{Q C} C_1 C_2 = \frac{\omega C}{4Q p_0^2} \frac{C_2}{C_1}$$



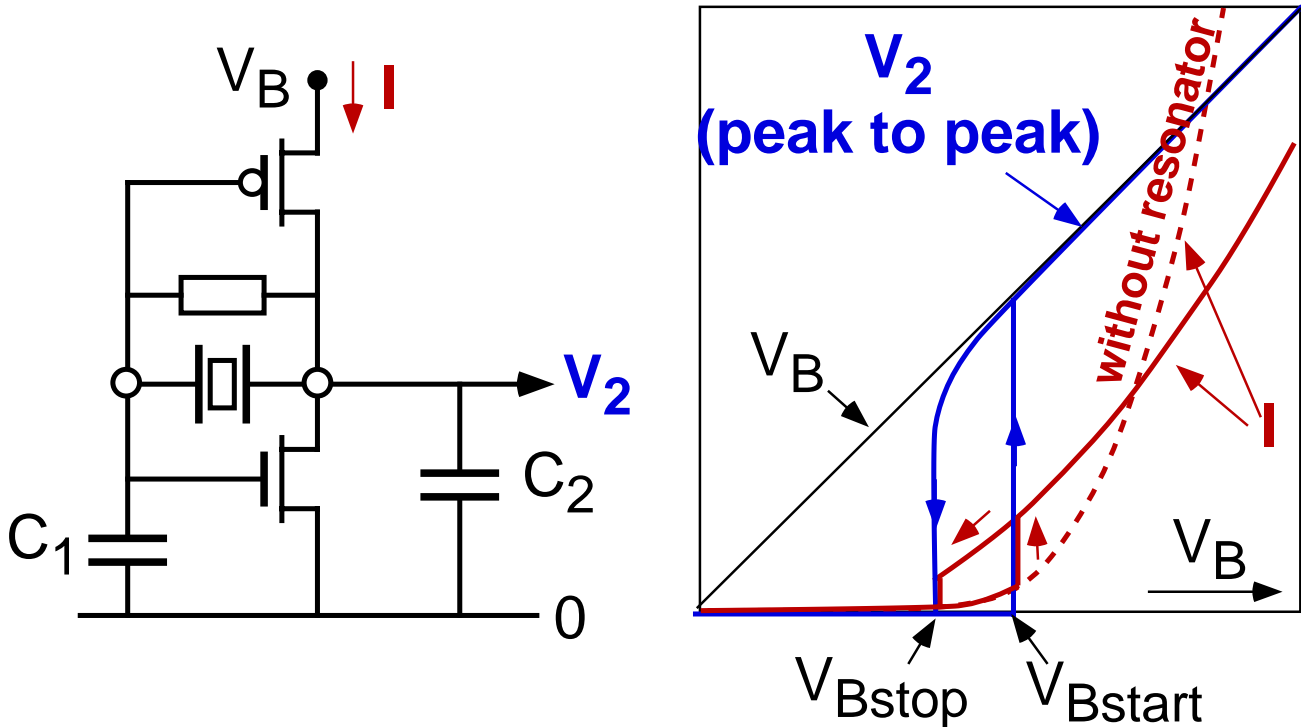
- Condition for stability:
(pole of Z_c with negative real part)

$$C_1 > C_2$$

radius of circle **reduced for**
increased **margin**

CMOS-INVERTER OSCILLATOR

- a simple but poor solution -

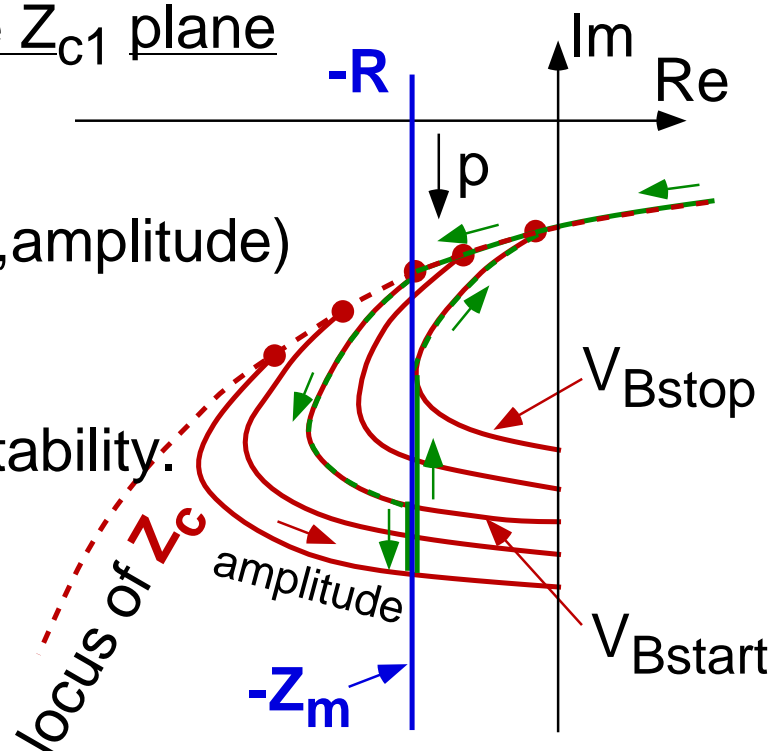


Putative Z_{c1} plane

• $Z_c(V_B)$

— $Z_{c1}(V_B, \text{amplitude})$

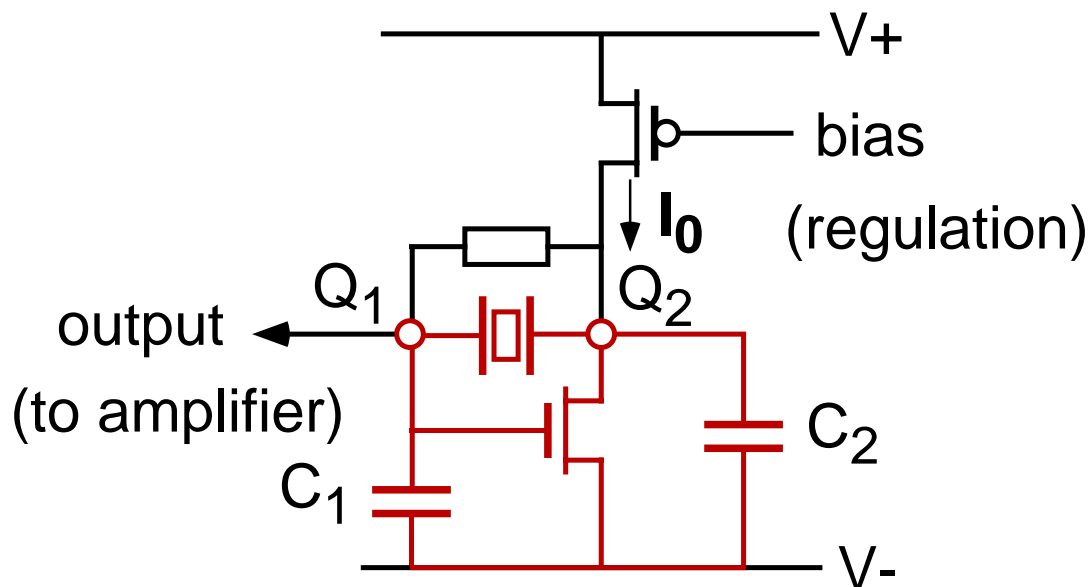
- Poor frequency stability.
- Waste of power.
- Risk of overtone.



- Possible improvement by resistors in the drains.

GROUNDED-SOURCE OSCILLATOR

(non-complementary)



- For fixed bias current I_0 :

Margin needed for variations of Q and process

possible overdrive

waste of power

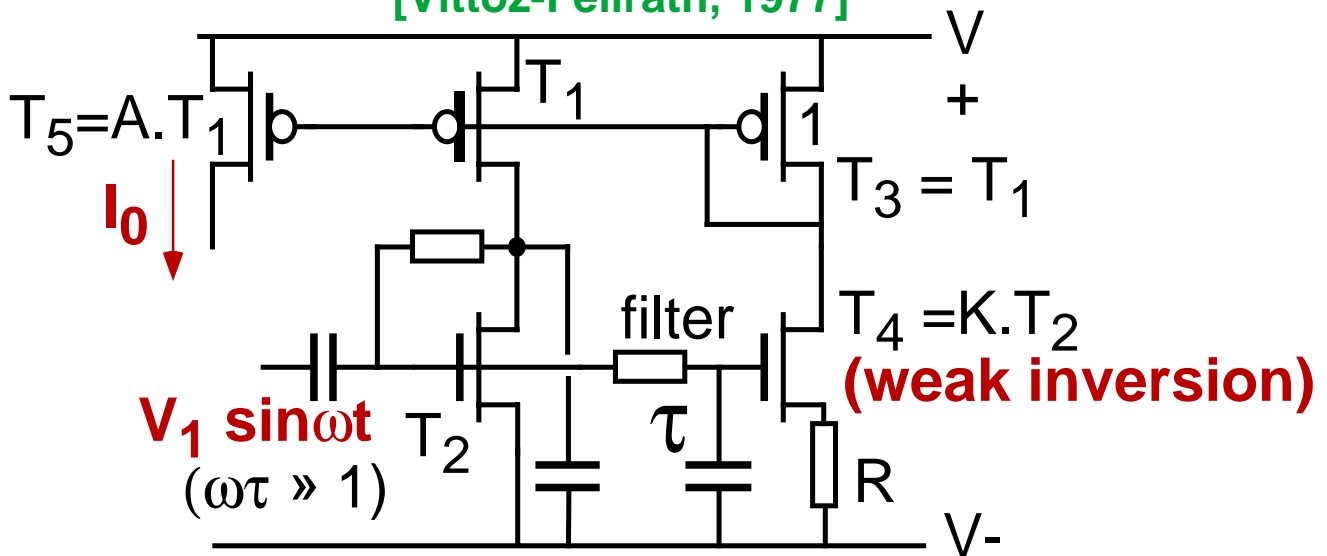
limitation by distortion

Best:

- Low-level **amplitude regulation**+ output amplifier

AMPLITUDE REGULATOR

[Vittoz-Fellrath, 1977]



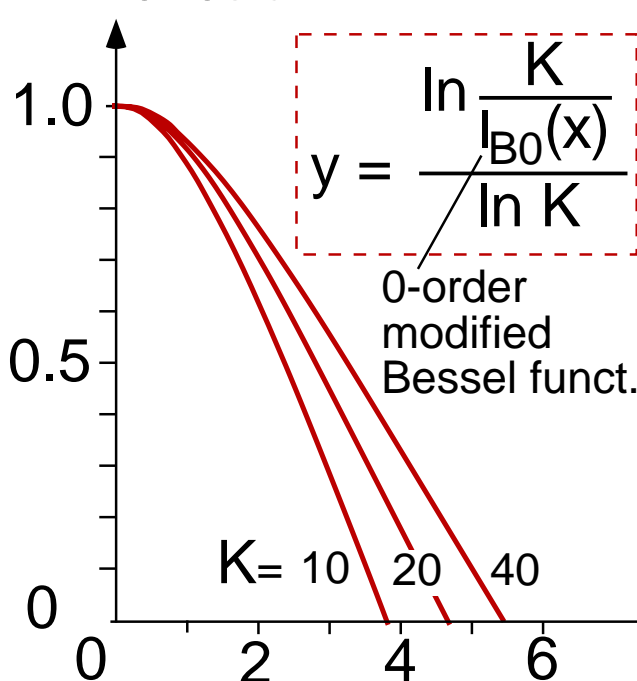
- No AC input voltage ($V_1=0$):

$$I_0 = I_{0\text{start}} = \frac{AU_T}{R} \ln K \quad (\text{start-up current})$$

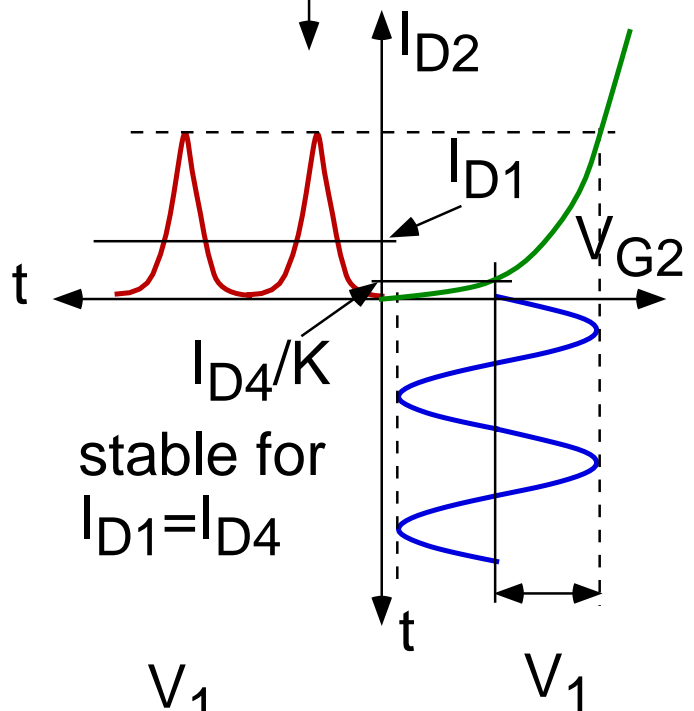
- For $V_1 > 0$:

General solution

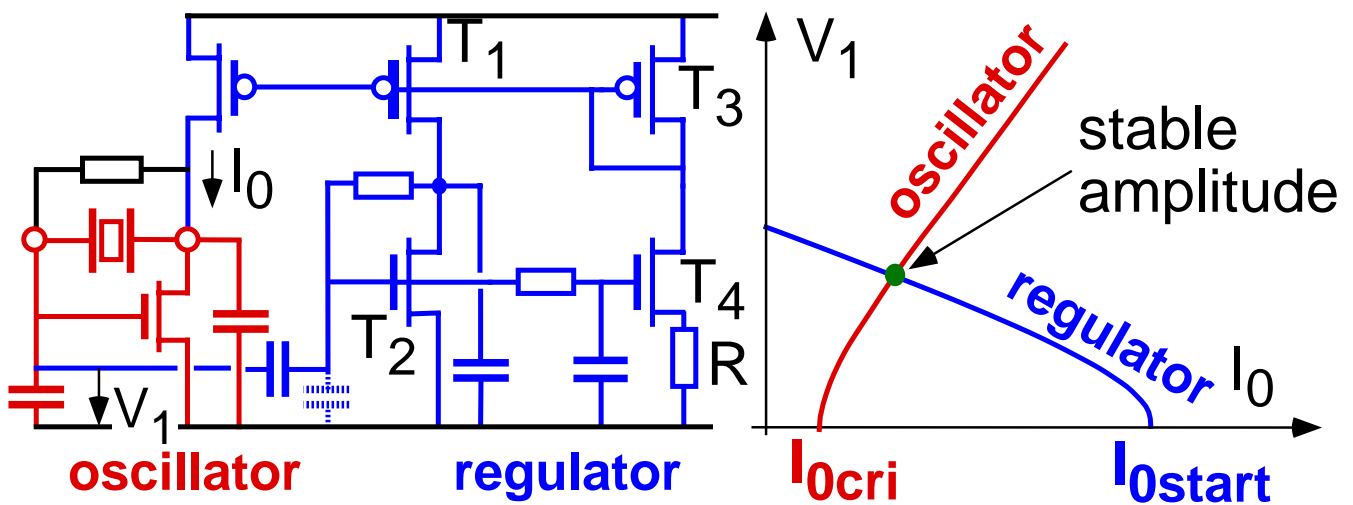
$$y = I_0 / I_{0\text{start}}$$



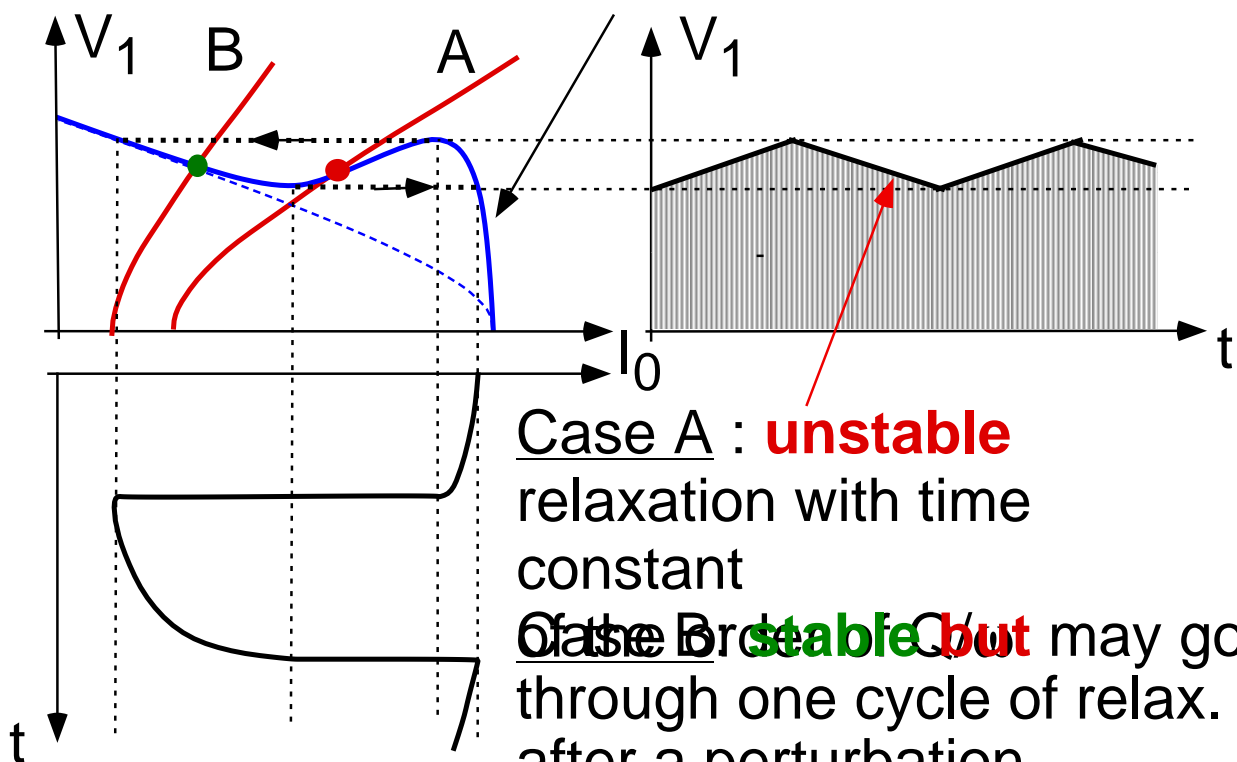
For R negligible



AMPLITUDE REGULATING LOOP



- Effect of T_2 - T_4 entering strong inversion: distortion of the regulator's characteristics



Case A : **unstable**
relaxation with time constant

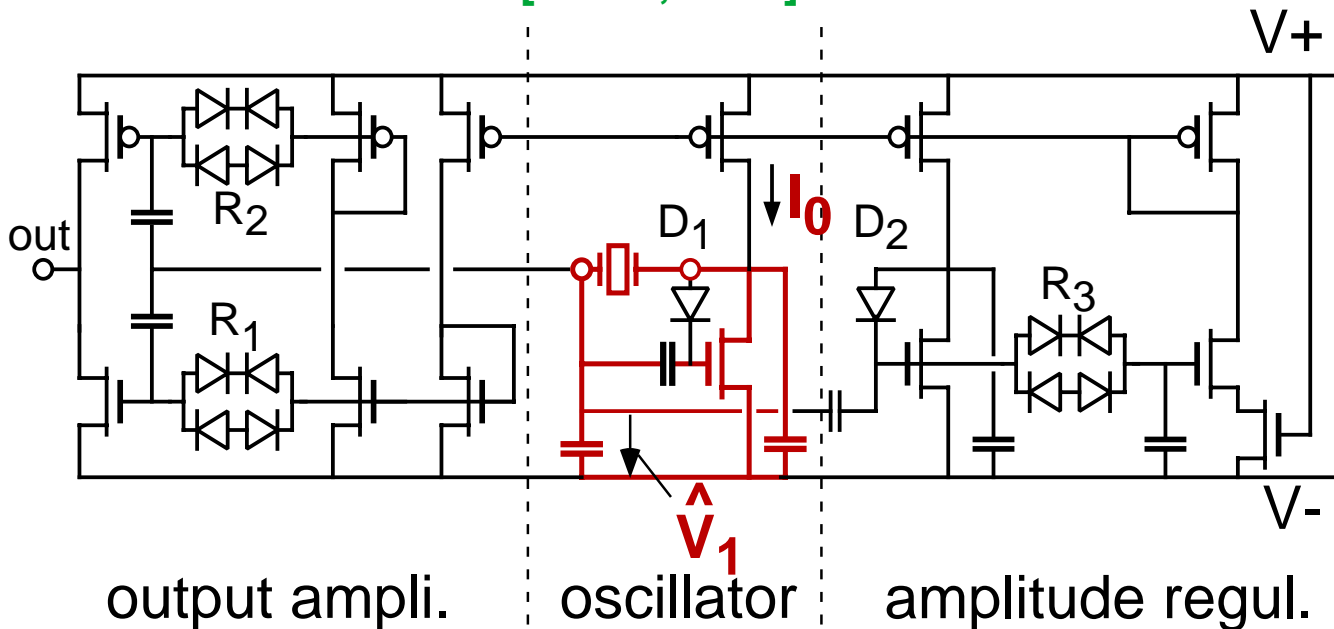
Case B : **stable** but may go through one cycle of relax. after a perturbation

- Design criterion: $i_{D2max} < I_{S2} = 2n\beta_2 U_T^2$ (too strict)

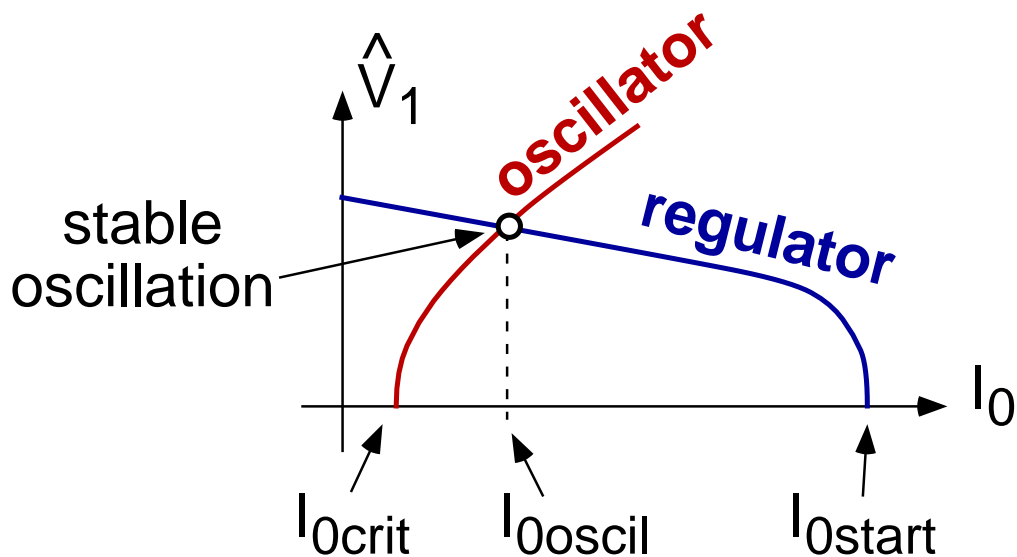
semi-empirical:
$$R > \frac{2\beta_1/\beta_3}{\beta_2 n U_T}$$

MICROPOWER CRYSTAL OSCILLATOR

[Vittoz, 1979]



R_1, R_2, R_3, D_1, D_2 : lateral diodes in poly layer



Example: $f=32\text{KHz}$

$V_B=1$ to 3 V

$I_{tot}= 20$ to 100nA (depends on C_1, C_2, Q)

no external component except crystal.

CURRENT DRAIN

of micropower crystal oscillator

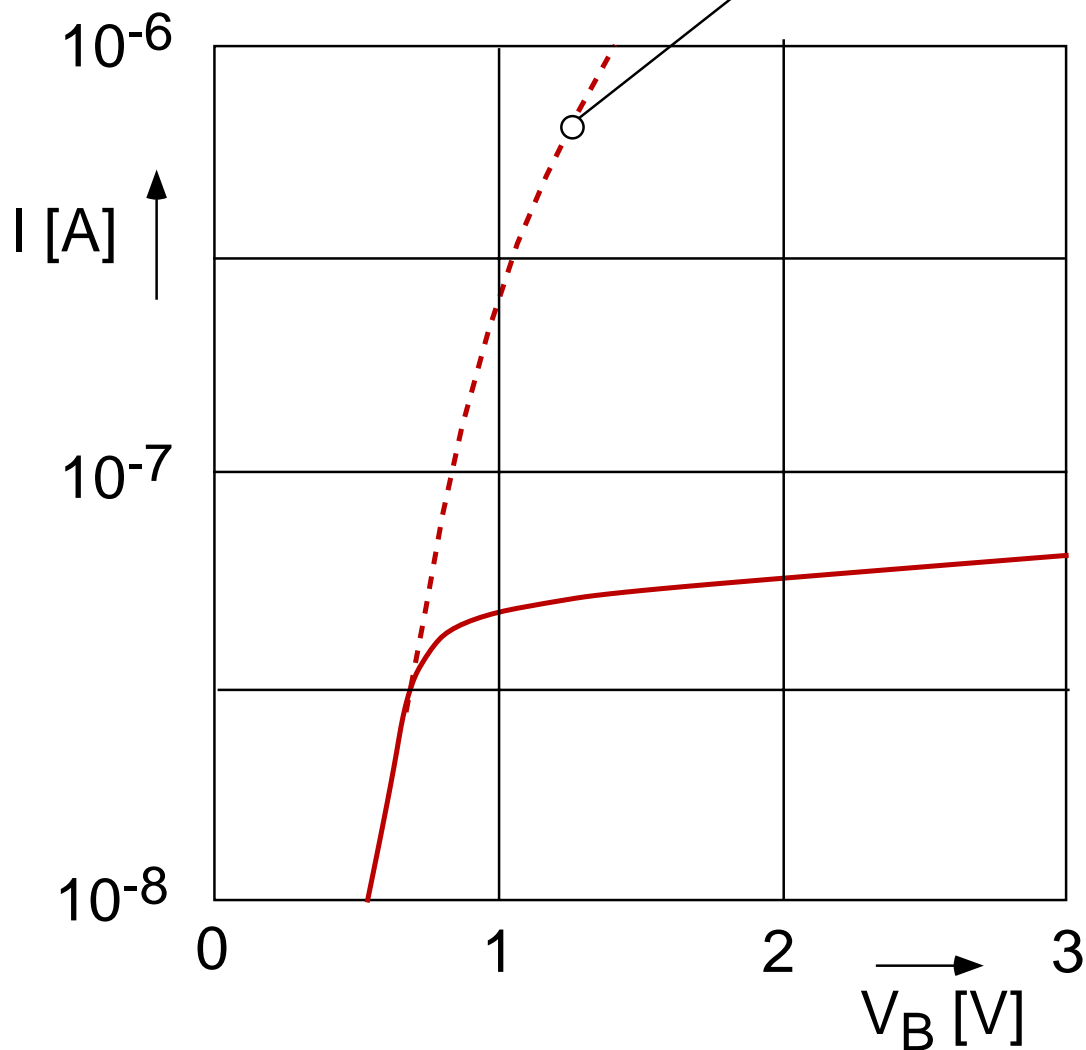
$$f = 32\text{KHz}$$

$$C = 2.9\text{fF}$$

$$Q = 80'000$$

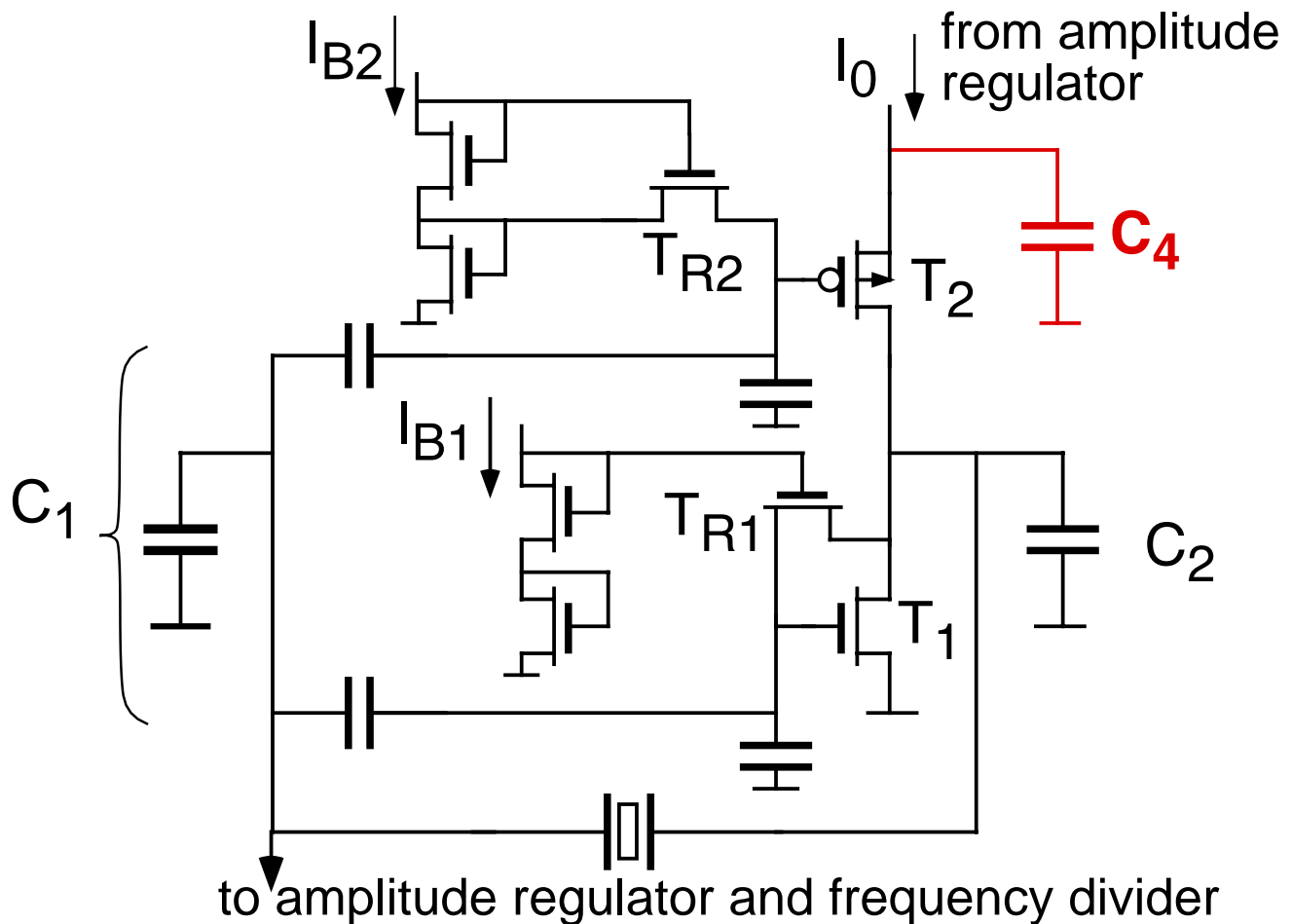
$$C_1 = C_2 = 10\text{pF}$$

$$C_3 = 3\text{pF}$$

Crystal resonator
removed

VERY LOW-POWER 2MHZ OSCILLATOR

[Aebischer et al, 1997]



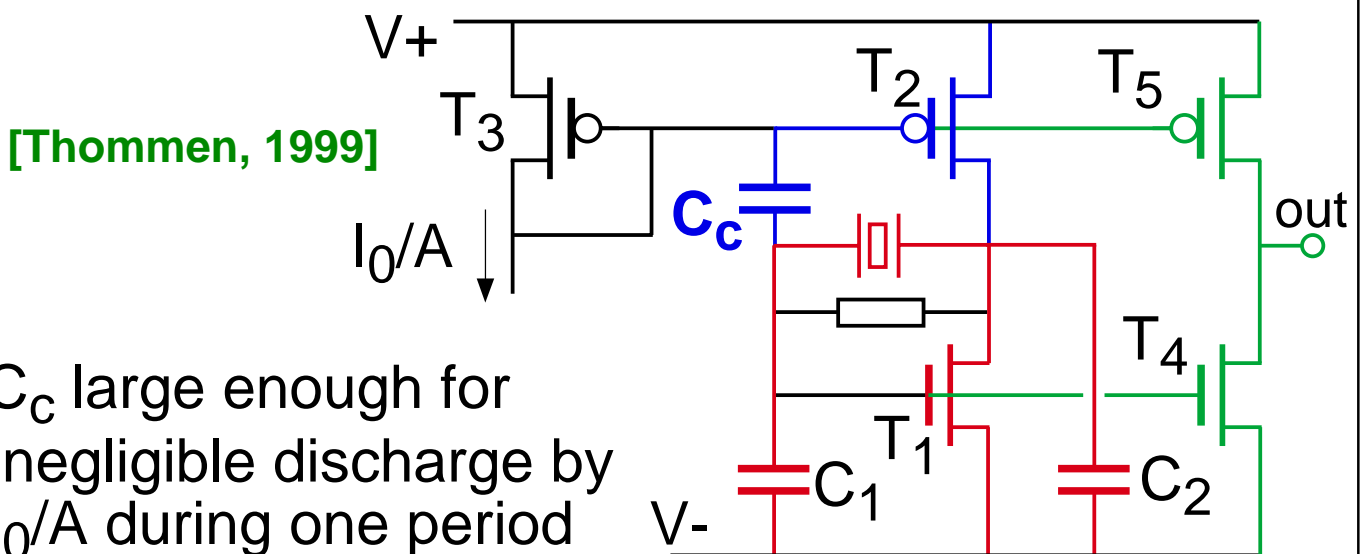
- Current controlled CMOS inverter T_1 - T_2
 - gates separately biased by T_{R1} - T_{R2}
 - controlled by bias I_{B1} - I_{B2}
 - source of T_2 AC grounded by C_4 , with $\omega C_4 \gg g_{m2}$
- 2.1 MHz ZT cut quartz, $C=0.5\text{fF}$, $Q=300\text{-}900\text{K}$
 $C_1=C_2=2.5\text{pF}$, $C_3=0.7\text{pF}$, $C_4=10\text{pF}$

$I = 60\text{-}180\text{nA}$
 $I < 500\text{nA}$
 @ 1.8 to 3.5V

(core oscillator only)

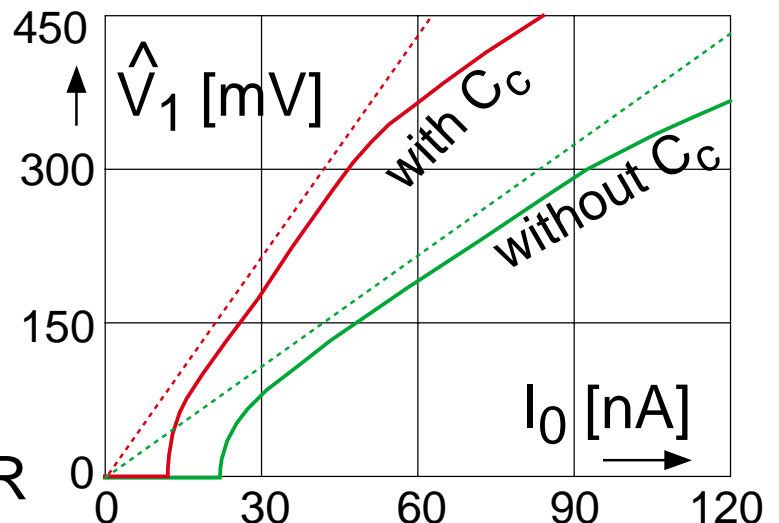
(oscill.+freq. divider+ dig. tuning)

COMPACT PUSH-PULL OSCILLATOR



- C_c large enough for negligible discharge by I_0/A during one period
- Average current I_0 through T_1 and T_3 :
 - imposed by T_3
 - from amplitude regulator
- Instantaneous current in T_3
 - proportional to that in T_2
 - creates a loss conductance, thus:
 - effect. trans. of T_2 for fundamental: $g_{m2(1)}(1-1/A)$
- Output amplifier T_4 - T_5 directly coupled to T_1 - T_2
- Experimental results:

f	$= 32 \text{ kHz}$
R	$= 35 \text{ k}\Omega$
A	$= 16$
C_1	$= 12.3 \text{ pF}$
C_2	$= 24.6 \text{ pF}$
C_3	$= 1 \text{ pF}$
V_{Bmin}	$= 0.7 \text{ V}$



- Drawback: poor PSRR

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