# Halfmoon: Log-Optimal Fault-Tolerant Stateful Serverless Computing (Extended Version)

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### **Abstract**

Serverless computing separates function execution from state management. Simple retry-based fault tolerance might corrupt the shared state with duplicate updates. Existing solutions employ log-based fault tolerance to achieve exactly-once semantics, where every single read or write to the external state is associated with a log for deterministic replay. However, logging is not a free lunch, which introduces considerable overhead to stateful serverless applications.

We present Halfmoon, a serverless runtime system for fault-tolerant stateful serverless computing. Our key insight is that it is unnecessary to symmetrically log both reads and writes. Instead, it suffices to log either reads or writes, i.e., asymmetrically. We design two logging protocols that enforce exactly-once semantics while providing log-free reads and writes, which are suitable for read- and writeintensive workloads, respectively. We theoretically prove that the two protocols are log-optimal, i.e., no other protocols can achieve lower logging overhead than our protocols. We provide a criterion for choosing the right protocol for a given workload, and a pauseless switching mechanism to switch protocols for dynamic workloads. We implement a prototype of Halfmoon. Experiments show that Halfmoon achieves 20%-40% lower latency and 1.5-4.0× lower logging overhead than the state-of-the-art solution Boki.

#### 1 Introduction

Recent years have seen an increasing popularity of serverless computing [16, 32, 33, 36, 37, 53, 88, 91, 98, 112] in building cloud applications [51, 78, 85, 92, 104, 110]. It features the Function-as-a-Service (FaaS) paradigm [86, 99, 115], where developers break down an application into a set of functions and their dependencies, and the cloud automates the deployment. FaaS enjoys elastic scaling and pay-per-use billing, which dramatically reduces resource management overhead.

Serverless platforms enable autoscaling by disaggregating compute and storage [42, 65]. Function-local state is not guaranteed to persist across invocations due to load balancing and elastic scaling of resources. To share state across multiple functions, applications typically rely on external storage for state management [11].

Extracting the state from stateful serverless functions (SSFs) [50, 108] brings challenges to application-level consistency in the presence of failures. While SSFs are decomposed into stateless functions and the external state, achieving fault tolerance of SSFs is not as simple as achieving fault

tolerance for each component individually. Specifically, the fault tolerance of stateless functions can be achieved by retrying crashed functions, and that of the external state can be achieved by using a fault-tolerant external storage service. However, naively combining the two introduces anomalies upon failures. Consider an SSF that writes to the external state and then crashes. Retrying this function would duplicate the write that has already been applied.

Serverless runtimes should avoid such anomalies with exactly-once semantics [87, 108]. That is, no matter how many times an SSF crashes and gets re-executed, the effect on the external state should be equivalent to that produced by running the SSF exactly once, without crashing.

Log-based fault tolerance is a common approach to realizing exactly-once semantics [24, 87]. The idea is to enhance the retry-based at-least-once semantics with idempotence, i.e., at-most-once semantics. To achieve this, existing solutions associate every read or write to the external state with a log record. During re-execution, the SSF replays the log, recovering read results and skipping completed writes. Beldi proposes to atomically perform writing and logging in the external storage [108]. The state-of-the-art solution Boki decouples the log to a more efficient logging layer [50].

However, logging is not a free lunch. Beldi reports that reads and writes with logging are 2-4× more expensive than their raw counterparts. Even for Boki's optimized implementation, logging still accounts for 30%-50% overhead compared to raw operations (§2). Thus the primary goal of this paper is to provide idempotence while minimizing logging overhead.

We present Halfmoon, a serverless runtime system for fault-tolerant SSFs. Halfmoon provides two logging protocols that enforce exactly-once semantics while providing log-free reads and writes, respectively. Our intuition is that there is no need to symmetrically log *both* reads and writes. Instead, it suffices to log *either* reads *or* writes, i.e., asymmetrically. Consider the stream of events that take place in the system. Our key insight is that reads and writes are *parameterized* by their timestamps in the stream, and idempotence boils down to the stability of timestamps [48]. An idempotent write should always be applied at the same point in the stream, i.e., at the same timestamp. Similarly, an idempotent read should always seek backward from its timestamp and observe the latest preceding write in the stream.

The key challenge of Halfmoon's asymmetric design is persisting events without logging. While a logged event (and its timestamp) is persistent on its own, an unlogged

1

**Table 1.** Latency of log, read and write operations in Boki.

	Log	Read	Write
median	1.18ms	1.88ms	2.47ms
99%-tile	1.91ms	4.60ms	5.86ms

event must be recovered from other logged events after failure. The problem is that the assignment of timestamps is inherently non-deterministic. Halfmoon addresses this problem by leveraging the fact that many serverless applications do not require real-time consistency [89, 90, 100]. Instead of assigning the non-recoverable real time to log-free reads or writes, we generate their timestamps based on those of previous logged operations, in a *deterministic* and *recoverable* fashion. This allows us to eliminate the logging overhead for one type of operation, and rely on the log records of the other type to achieve both persistence and idempotence. We discuss Halfmoon's consistency guarantees in § 4.4.

We prove that the two logging protocols are *log-optimal* for exactly-once semantics, i.e., no other protocols can achieve exactly-once semantics with lower worst-case logging overhead than our protocols. Intuitively, the two protocols are suitable for read- and write-intensive workloads, respectively. We provide theoretical and empirical analysis of Halfmoon under different read/write intensities, and propose a criterion for choosing the right protocol for a given workload.

Halfmoon also supports dynamic workloads that change their read/write intensity over time. We design a switching mechanism that allows the runtime to change between Halfmoon's log-free read protocol and log-free write protocol. The switching is *pauseless*, i.e., the system remains operational and fault-tolerant during this process.

In summary, we make the following contributions.

- We design two logging protocols that enable exactly-once log-free reads and writes for SSFs, respectively.
- We theoretically prove that our protocols are log-optimal.
   Therefore, Halfmoon pushes the overhead of log-based fault tolerance to its lower bound.
- We provide a criterion for choosing the right protocol for a given workload, and a pauseless switching mechanism to switch protocols for dynamic workloads.
- We implement a prototype of Halfmoon. Our experiments show that Halfmoon achieves 20%-40% lower latency and 1.5-4.0× lower logging overhead than the state-of-the-art solution Boki.

## 2 Motivation

**Problem: logging overhead.** To achieve exactly-once semantics for SSFs, existing solutions [50, 108] require logging for *both* reads and writes to the external state. Note that reads should be idempotent because writes and the branching of SSF logic may arbitrarily depend on read results. We refer to these fault-tolerant logging protocols as *symmetric*. Boki [50] is the state-of-the-art symmetric approach that specifically optimizes its logging implementation. Nevertheless, logging

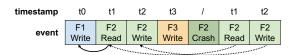


Figure 1. Parameterizing reads and writes with timestamps.

still incurs substantial overhead. We benchmark Boki's logging latency under the setup of §6, using Amazon DynamoDB as the external storage [34]. Table 1 shows that logging accounts for 63% (48%) overhead at the median and 42% (33%) at the 99%-tile for reads (writes). This motivates us to design minimally fault-tolerant protocols for SSFs that perform logging only if necessary.

Opportunity: parameterizing reads and writes. The event stream is the key enabler of Halfmoon's design. The ordering of events in the stream can be obtained through sequencers [17, 29, 50, 67], synchronized clocks [26, 57, 70], or state machine replication (SMR) [13, 27, 35, 59]. Without loss of generality, we assume for now that each operation is associated with a timestamp and the event stream follows the timestamp order. We further discuss the availability of the event stream in §7.

Our key insight is that reads and writes are *parameterized* by their timestamps in the event stream. To achieve idempotence, a read should consistently seek backward from the same timestamp. Figure 1 shows a real-time interleaving of SSFs and the event timestamps. The first time F2 executes read at  $t_1$ , it sees the latest write from F1 at  $t_0$ . During re-execution, instead of seeing F3's write at  $t_3$ , it should also seek backward from  $t_1$  and recover the previous result, i.e., the value written at  $t_0$ . Similarly, for a write to be idempotent, it should always take effect at the same point in the stream regardless of re-execution. As shown in Figure 1, when F2 recovers from failure, it should avoid overwriting F3's write because F2's write has been parameterized at  $t_2$ , i.e., it should take effect before F3's write.

By parameterizing reads and writes, idempotence boils down to the stability of read and write timestamps [48]. This motivates us to rethink the necessity of existing logging protocols. Our intuition is that there is no need to symmetrically log *both* reads and writes. Instead, by leveraging the inherent dependencies between events, it suffices to log *either* reads *or* writes, i.e., asymmetrically.

Challenge: persistence without logging. Parameterizing reads and writes does not provide fault tolerance on its own. The critical part is to persist the event stream in the first place, such that timestamps and the ordering of events remain stable across failures. This property is implicitly satisfied by symmetric logging protocols, as logged events are persistent by themselves. However, Halfmoon's design goal of being log-free presents a new challenge to persisting the event stream. For an unlogged event, the only way to persist it is to make sure that it can be recovered from other logged events. Consequently, the dependencies of this event must be

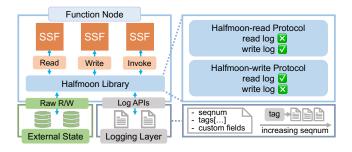


Figure 2. Halfmoon overview.

deterministic. By requiring that SSFs be deterministic [108], the input parameters to reads or writes can be stably inferred from function context. However, the assignment of event timestamps is inherently non-deterministic, which must be logged to rule out the uncertainty.

At first glance, this seems to be contradictory to our design goal. To address this problem, Halfmoon leverages the fact that many serverless applications function well under less stringent guarantees than real-time consistency, i.e., linearizability. For example, Cloudburst [90] provides *repeatable reads* or *causal consistency* for SSFs; AFT [89] provides *read atomicity*. Therefore, the read/write timestamps do not have to reflect the real time, which is non-deterministic and unrecoverable without logging. Instead, we can deterministically generate *logical* timestamps for log-free operations based on the SSF context, similar to the way we infer the input parameters for reads or writes. In other words, it is possible to infer all events from a skeleton of the event stream. Only the skeleton needs to be persisted, thereby saving the logging overhead for the rest.

### 3 Halfmoon Overview

Figure 2 shows the overall architecture of Halfmoon. SSFs interact with the external state through Halfmoon's client library. The library exposes similar APIs as existing solutions [50, 108], including data operations such as read/write, and control flow operations such as invoke to enable stateful workflows. The APIs have the same signature as their raw counterparts, but automatically performs logging behind the scene to ensure idempotence. To achieve exactly-once semantics, Halfmoon relies on the serverless runtime to detect and re-execute crashed SSFs. This feature is widely supported among existing platforms [1, 7, 87, 108].

Halfmoon applies log-based fault tolerance with novel logoptimal protocols. The Halfmoon-read protocol is log-free on reads, and the Halfmoon-write protocol is log-free on writes. In line with the state-of-the-art solution Boki [50], Halfmoon decouples the log from the external state into a separate logging layer. The logging layer implements the shared log abstraction [18, 29, 50], which enforces a global total order of log records and serves as the event stream of Halfmoon. We note that Halfmoon is not tied to Boki's logging layer (§7).

Figure 3. The log APIs in Halfmoon.

Our prototype uses Boki because it specifically optimizes logging for stateful serverless computing.

Figure 3 lists Halfmoon's log APIs. logAppend appends to the log and assigns a monotonically increasing sequence number (segnum) to the log record. Each log record has a number of tags as specified in logAppend. The main log is logically divided into sub-streams where log records have a common tag, and a record may appear in several sub-streams. Because the order of records is determined by their seqnums, the order within each sub-stream is consistent with that of the main log. Sub-streams reduce log replay overhead by enabling selective reads, a common approach in shared log systems [19, 50, 96]. logReadPrev (logReadNext) seeks backward (forward) on a sub-stream specified by the tag parameter. logTrim garbage collects a sub-stream. Besides the APIs of prior work [50], we introduce logCondAppend to resolve conflicts between concurrent SSF instances (§5). Because all log APIs target specific sub-streams, we abbreviate sub-streams as streams for the rest of this paper.

# 4 Halfmoon Design

This section presents the design of the Halfmoon-read and the Halfmoon-write protocol. We start by clarifying the concepts and assumptions.

Race conditions. We note that several *concurrent* function instances may correspond to the same SSF invocation. For example, if an instance times out (but is still live) due to a network error, the runtime may assume that this instance has crashed and launch another. We use *instances* specifically to denote such concurrent functions for a particular SSF invocation. Without loss of generality, instances should be assigned a common identifier (tag) so that they may refer to the same log stream containing the SSF's execution history. We use *instancesID* to denote this common identifier.

Consequently, there are two race conditions against the exactly-once semantics. First, a re-executed SSF may race with a previously failed invocation of the same SSF, at the risk of repeating a completed step. Second, an SSF may also race with its peer instances, both attempting to execute the same step. For the sake of presentation, this section focuses on addressing the first race condition. We extend the protocols to handle the second one in §5.

**Time-related concepts.** The logAppend API returns a monotonically increasing *seqnum* from the logging layer (Figure 3). Within each SSF, we use a variable *cursorTS* to record the function-local seqnum that advances after each logging operation. As per §2, *timestamp* is a general concept that parameterizes the position of the associated event in the event stream. Note that depending on the logging protocol, timestamps can be based on seqnums (i.e., logical) or the real time.

**Transactions.** In line with previous works, we assume that SSFs are non-transactional by default [50]; to execute several steps atomically, SSFs should explicitly use transactions. Halfmoon can reuse existing transactional APIs, and focuses on optimizing the logging overhead for normal operations.

# 4.1 Halfmoon-Read: the Log-Free Read Protocol

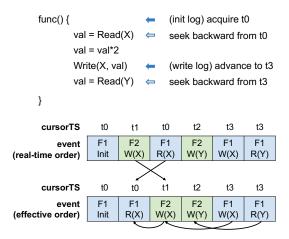
**Overview.** Under Halfmoon-Read, all reads are log-free and only writes perform logging. The persistent part of the event stream consists only of writes. Writes achieve idempotence by checking the write logs in advance. For reads, we take two steps to ensure idempotence. First, we assign timestamps to reads in a deterministic manner. Second, we use the timestamps to map reads to existing writes in the write log. In other words, reads are inserted into the event stream given their timestamps, and are idempotent because their positions are deterministic.

In step one, we must infer the read timestamps from the SSF context. Our solution is to use cursorTS, i.e., the sequum of the latest logged operation in the SSF; then the fault tolerance of the logging layer guarantees that read timestamps are deterministic.

In step two, we must ensure that writes are traceable. Our solution is to use multi-versioning to manage the external state. Each write creates a new version of the object and registers the version number in the logging layer; a read locates a specific object version by querying the write log (logReadPrev). Note that the version numbers are unordered by themselves; the write log defines the order. Therefore the external storage only needs to support plain key-value APIs; the version numbers serve as pointers to the actual object. Because the position of a write in the event stream is determined by the seqnum of the associated write log record, the write timestamp is set to that seqnum accordingly.

**Example.** Figure 4 shows an example of the Halfmoon-read protocol. F1's initial cursorTS is  $t_0$ . When reading object X, it does not see F2's write at  $t_1$  because the read uses an earlier timestamp. However, when reading object Y, it sees F2's write at  $t_2$  because it has advanced its cursorTS to  $t_3$  after its previous write. The effective order of events follows the order of the seqnum-based logical timestamps. We show in §4.4 that Halfmoon-read provides *sequential consistency* [62].

**Init.** Figure 5 shows the pseudocode of the Halfmoon-read protocol. At the start of execution, the SSF appends an *init* log record, and uses the seqnum of this record as the initial



**Figure 4.** Example of the Halfmoon-read protocol. F1 runs the pseudocode. F2 is another SSF. The top and bottom timeline show the real-time order and the effective order of events, respectively. The arrows below the bottom timeline show the dependencies between operations on object X and Y.

cursorTS (line 7). The cursorTS is recovered from the log record, if present (line 5). The SSF also retrieve all records from the log stream tagged by its instanceID (line 3), which contains the execution history of the SSF. We refer to this per-SSF log stream as the step log. The current records in the step log are stored in a local array env.stepLogs. Later the SSF may check this array for existing log records and skip finished operations.

Write first obtains a version number (line 20), performs multi-version DBWrite, and finishes by logging the version number (line 22). Specifically, Halfmoon-read first checks if the write log record exists. If so, the write has been applied. Otherwise, it means that either the write has not yet created a new version of the object, or it has created the new version but crashed before logging.

To be idempotent, the write needs to use a deterministic version number. For example, it can generate the version number by simply concatenating the unique and deterministic InstanceID (env. ID) and the current step number (to distinguish different operations in the same SSF). Alternatively, if the version number is to be randomly generated, the SSF should log and check the version number before DBWrite to transform it into a deterministic operation. Our current prototype adopts the latter approach such that Halfmoonread logs before and after DBWrite. This is because our primary baseline, Boki [50], also logs twice for each write. Our prototype aligns the logging overhead of writes such that our performance gains come solely from eliminating the logging of reads. Alternatively, if the external state exposes its internal logging and ordering of events, then DBWrite and logging can be merged into a single step, where it atomically creates a new object version and receives a timestamp.

4

```
1 def Init(env, input):
2
      # retrieve all log records of the SSF
      env.stepLogs = getStepLogs(env.ID)
      if env.stepLogs[0] is not None:
4
          env.cursorTS = env.stepLogs[0]["seqnum"]
          env.cursorTS = logAppend([env.ID], LogRecord{
               "step": 0, "op": "init",
8
               "data": input,
10
          })
11
      env.step = 0
12
  def Write(env, key, value):
      # check if write can be skipped
14
15
      env.step += 1
      if env.stepLogs[env.step] is not None:
16
          env.cursorTS = env.stepLogs[env.step]["seqnum"]
18
19
      # deterministically generate version number
      vNum = getVersionNumber(env)
20
      DBWrite(key, value, version=vNum)
22
      env.cursorTS = logAppend([env.ID, key], LogRecord{
          "step": env.step, "op": "write",
23
24
           "version": vNum,
      7)
25
26
27
  def Read(env, key):
      writeLog = logReadPrev(key, env.cursorTS)
28
      return DBRead(key, version=writeLog["version"])
29
30
31
  def Invoke(env, funcName, input):
      # check if invoke can be skipped
33
      env.step += 1
      if env.stepLogs[env.step] is not None:
34
35
          env.cursorTS = env.stepLogs[env.step]["seqnum"]
          return env.stepLogs[env.step]["result"]
36
37
      # deterministically generate ID
      ID = getUUID(env)
38
      # ID is passed into callee's env
39
      result = InvokeFunc(ID, funcName, input)
40
      env.cursorTS = logAppend([env.ID], LogRecord{
41
          "step": env.step, "op": "invoke",
42
           "result": result,
43
44
      })
```

**Figure 5.** Pseudocode of the Halfmoon-read protocol.

Read first queries the per-object write log tagged by key. It passes the cursorTS into logReadPrev to retrieve a particular write log record. The "version" attribute in the record points to the actual object the read should see (line 28). To facilitate this process, we pass two tags into logAppend when logging the write, namely the instanceID of the SSF (env.ID) and the key of the target object, such that the record is visible in two log streams, namely the SSF's step log and the object's write log. Therefore, a write log record serves a dual purpose. First, it checkpoints the progress of the initiating SSF, allowing the write to be skipped during re-execution by checking the step log. Second, it functions as the commit point of the write where it becomes visible to other SSFs in the write log. Because the logging layer assigns monotonically

increasing sequents, a read has full visibility of all writes with smaller logical timestamps, thereby allowing the read to seek backward in the event stream deterministically.

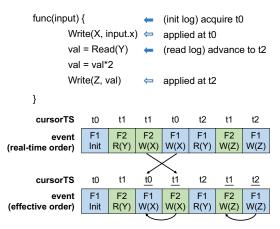
The second purpose requires that the logging be performed after <code>DBWrite</code>, as opposed to write-ahead logging. The reason is that the logging layer is decoupled from the external state. If the version number is made visible in advance, then reads could obtain version numbers with no matching objects in the external state. In contrast, Halfmoon-read ensures that the exposed object versions are always available.

In spite of being log-free, Read still needs to pay one round of logReadPrev. This overhead is implementation specific. Because Boki caches log records on function nodes, logReadPrev takes 0.12ms at the median and 0.72ms at the 99%-tile [50], which is negligible compared to DBRead (Table 1). Therefore our prototype of Halfmoon-read provides near-zero overhead for reads. Note that the critical data of a write log record consists only of its seqnum and version number, which can be covered in a few dozen of bytes. Therefore the cache size is not a concern here. Alternatively, if the logging layer is merged with the external state, a read can directly issue a query with a filter on object versions, instead of retrieving the version and the object separately.

Invoke first generates the callee's instanceID (line 38), calls the function, and finishes by logging the result (line 41). In case the log record already exists, the actual invocation can be skipped. The callee's instanceID must be deterministic to ensure idempotence. Similar to the version numbers in Write, the SSF can deterministically generate the instanceID from its context, or randomly generate it and perform additional logging and checking to turn it into a deterministic operation. In line with Boki, our prototype adopts the latter approach. Note that by logging the result, the SSF ensures that the cursorTS is monotonic even across invocations. Because each individual SSF is idempotent, by induction the entire workflow is also idempotent.

Remark. Halfmoon-read is primarily designed for key-value stores with read/write interfaces. To perform table-level queries, e.g., scan, join, and aggregation, one should first use logReadPrev to get a list of version numbers for all objects in the table. This list captures a snapshot of the table at a given timestamp. It is necessary because the ordering of individual writes is defined by the write log, and the version numbers are not ordered by themselves. As an optimization, it is possible to cache the database index in the logging layer to reduce the size of the returned list. Alternatively, the table should be read-only to bypass any logging or version lookup. Our prototype implementation of Halfmoon-read does not support queries over *mutable* tables.

As Halfmoon-read requires multi-versioning, an important concern is the garbage collection and the storage overhead. We address this problem in §4.5 and §4.6, respectively.



**Figure 6.** Example of the Halfmoon-write protocol. F1 runs the pseudocode. F2 is another SSF. The top and bottom timeline show the real-time order and the effective order of events, respectively. The arrows below the bottom timeline show the dependencies between operations on object X and Z.

### 4.2 Halfmoon-Write: the Log-Free Write Protocol

**Overview.** The Halfmoon-read protocol is ideal for readintensive workloads. We now present the Halfmoon-write protocol that supports log-free writes. Similar to Halfmoonread, the idea is to assign deterministic timestamps to logfree operations, but with roles reversed. Under Halfmoonwrite, all reads are logged, while writes use the cursorTS. Because reads directly log the real-time data they have seen from the external state, they are idempotent on their own. Moreover, there is no need to use multi-versioning to keep the history of writes. Instead, writes in Halfmoon-write perform conditional updates to the single-version external state. Specifically, a write deterministically generates a version number based on the cursorTS, and updates the object only if the stored version number is smaller. The monotonicity of version numbers and the determinism of the cursorTS ensures that a write is always applied at the same point in the event stream, thereby achieving idempotence.

For writes, version numbers serve as their logical timestamps. Read timestamps, in contrast, are based on real time because reads always target the latest data. Note that the read timestamp is *implicit* and unknown to Halfmoon; SSFs have no need to explicitly parameterize reads with timestamps given the already *materialized* read log records. We define the read timestamps only to help understand the ordering of events in Halfmoon-write.

**Example.** Figure 6 shows an example of the Halfmoon-write protocol. F1 initializes its cursorTS to  $t_0$ , and issues Write(X) using  $t_0$  as the version number. At this point, F2 has already applied Write(X) with version number  $t_1$ . Consequently, F1 does *not* overwrite F2's Write(X) because its version number is smaller. The effect on the external state is equivalent to a virtual interleaving where F1's Write(X) does "happen" before F2's Write(X), which adheres to the definition of

```
1 def Write(env, key, value):
      env.consecutiveW += 1
      vNum = (env.cursorTS, env.consecutiveW)
      DBWrite(key, cond="VERSION < {vNum}",
          update="VALUE={value}; VERSION={vNum}")
7 def Read(env, key):
      env.step += 1
8
      env.consecutiveW = 0
10
      if env.stepLogs[env.step] is not None:
          env.cursorTS = env.stepLogs[env.step]["seqnum"]
          return env.stepLogs[env.step]["data"]
13
      value = DBRead(key)
      env.cursorTS = logAppend([env.ID], LogRecord{
14
15
          "step": env.step, "op": "read",
           "data": value,
16
      })
18
      return value
```

**Figure 7.** Pseudocode of the Halfmoon-write protocol.

exactly-once semantics. In contrast, F1's later Write(Z) overwrites F2's Write(Z), in accordance with the real-time order. This is because F1 has advanced its cursorTS to  $t_2$  after reading the latest value of Y.

Note that there is a major difference between Halfmoon-read and Halfmoon-write in terms of the ordering of events. In Halfmoon-read, the effective order of events follows the order of logical timestamps. In Halfmoon-write, logical timestamps (version numbers) are only relevant for writes, while reads are based on real time<sup>1</sup>. Consequently, the effective order under Halfmoon-write combines the real-time and logical-timestamp order. We derive this order through the following steps. First, we order all events by real time. Second, for write events only, we reorder them according to their version numbers (§4.4).

For example, Figure 6 underlines the version numbers of writes. F1's Write(X) with version  $t_0$  is ordered immediately before F2's Write(X) with  $t_1$ , but still after F2's Read(Y). Formally, we show in §4.4 that the ordering under Halfmoonwrite enforces a sequential history for each SSF except that consecutive log-free writes to different objects may commute. For now, we give an intuitive interpretation of Halfmoonwrite's reordering of writes. Because the cursorTS is refreshed after logging each read, a higher cursorTS implies that the SSF has seen "fresher" data, which in turn gives a higher priority to the SSF's writes. In Figure 6, F1's Write(X) is reordered because F2 has seen a fresher value of Y. F1's later Write(Z) is not reordered because F1 is at least as fresh as F2.

Figure 7 shows the pseudocode of the Halfmoon-write protocol. It reuses the Init and Invoke functions from the Halfmoon-read protocol and differs only in Read and Write.

<sup>&</sup>lt;sup>1</sup>Realtime-ness applies to failure-free reads. Since exactly-once semantics ensures that operations appear exactly once in the event stream, regardless of failure and re-execution, we consider only the failure-free case when discussing the ordering of events.

Write performs *conditional* update by comparing the version numbers. It is applied to the object only if the stored version number is smaller (line 4) [50]. The version number is structured as a tuple (line 3). The first field is the cursorTS; the second is a counter that records the number of *consecutive* writes. For simplicity, we omit the counter in Figure 6. The counter is incremented upon writes and reset upon reads. The purpose of the second field is to break ties between consecutive writes to the *same* object. A version number V1 is smaller than V2 if V1's cursorTS is smaller, or if they have equal cursorTS but V1's counter is smaller.

**Read** first recovers the previous result from the step log if possible. Otherwise, it reads the current object and logs the result. The cursorTS is updated accordingly. CursorTS is only relevant to subsequent log-free writes. Reads always see the latest state regardless of the cursorTS. Note that there is no per-object read log in Halfmoon-write, as opposed to the write log in Halfmoon-read. This is because read log records are only checked by the initiating SSF, so there is no need to tag them with the object's key to make them publicly visible. Halfmoon-write only maintains the per-SSF step logs.

### 4.3 Log Optimality

Given the two logging protocols that enable log-free exactlyonce reads or writes, it is worth exploring whether there is still room for further optimization. We now prove that our protocols are log-optimal, i.e., no other log-based faulttolerant protocol can achieve lower worst-case logging overhead than our protocols. We start by formalizing the concepts and assumptions. For simplicity, we focus on accessing a single object in this section.

**Definition 4.1.** Write. Let S be the set of valid states. A write operation is a function  $w: S \to S$  that transforms the current state s to a new state w(s).

**Definition 4.2.** Read. A read is a function  $r: S \to V$  that maps the current state s to a value  $r(s) \in V$ . A read is logged if there is a fault-tolerant record containing the read result.

Without loss of generality, writes transform the current state while reads interpret it. Note that a read may not be defined over some states. For example, in Halfmoon-read, a read with cursorTS t is only valid if the latest seqnum in the logging layer is larger than t. A correct protocol must ensure at any time that any read allowed by the protocol is defined over the state at that time.

Next, we clarify the concept of logged and log-free writes. A write is logged if it is associated with a *standalone* record in fault-tolerant storage. Moreover, the record is either created by the write itself, e.g., in write-ahead logging, or it should be publicly visible, e.g. in Halfmoon-read. If there is no such record, the write is defined to be log-free. Consequently, in case a read is logged, we assume that the log record is private to the SSF; otherwise, it would be equivalent to associating

a publicly visible log record with the write that created the object, so this write is also considered logged. Formally, we have the following assumption for log-free writes.

**Assumption 4.3.** Log-free writes are memoryless. Let w be a log-free write over state  $s_1$  with visible external effect. Then there exist  $s_2 \in S$  and read r s.t.  $w(s_1) = w(s_2)$  and  $r(s_1) \neq r(s_2)$ .

Intuitively, a log-free write directly *overwrites* the object. It does not create a standalone record such that the old state is lost after the write. Consequently, there are multiple distinct old states that end with the same new state after the write. One cannot determine the actual old state from the new state alone. Note that the existence of r and  $s_2$  entails that r is defined over both  $s_1$  and  $s_2$  and thus allowed by the protocol. Moreover, because  $r(s_1) \neq r(s_2)$ , at least one of them is not equal to  $r(w(s_1))$ , the read result over the current state. This implies that the write has visible external effects.

**Assumption 4.4.** The SSF logic, i.e., how subsequent operations depend on a preceding event, is unknown to other SSFs.

Assumption 4.4 implies that SSFs are not aware of operations from other SSFs ahead of time. Therefore, there can be arbitrary interleaving of reads and writes.

Based on the definitions and assumptions, we have the following lemma that captures the relationship between the logging of reads and writes.

**Lemma 4.5.** If a fault-tolerant logging protocol allows an object to be updated with log-free writes (i.e., with visible external effect), then the protocol cannot be log-free on reads.

*Proof.* We prove by contradiction. We construct a counter-example that violates the idempotence of reads. Suppose an SSF performs a log-free read r over external state  $s_1$  and then crashes. During the crash failure,  $s_1$  is modified by a log-free write w. When the SSF re-executes the read, it cannot always recover the previous result based on the modified state. This is because given Assumption 4.3, we can choose  $s_2$  and r s.t.  $w(s_1) = w(s_2)$  and  $r(s_1) \neq r(s_2)$ . Moreover, given Assumption 4.4, the chosen  $s_2$  and r in the counter example is always possible to happen. Consequently, it is impossible for the read to choose between  $r(s_1)$  and  $r(s_2)$  as the previous read result, violating idempotence.

**Theorem 4.6.** In the worst case, a fault-tolerant logging protocol either logs all reads or all writes with visible external effects.

**Remark.** We can immediately derive Theorem 4.6 from Lemma 4.5. If there are writes that are log-free and have visible external effects, then in the worst case, every read may be interleaved with log-free writes in a similar fashion as the counterexample in Lemma 4.5. Note that by Assumption 4.4, the worst case is always possible to happen. Therefore all

reads should be logged. If there are no such writes, then by definition all writes with visible external effects are logged.

We only consider writes with visible external effects because a protocol may skip logging some writes by making sure that none can read them. For example, a protocol may handle log-free writes like Halfmoon-write do, occasionally take a snapshot of the object, and serve all reads using the snapshots like Halfmoon-read do. This implies that only the writes captured by the snapshots are visible and logged; the rest are effectively *stateless* operations with no visible effects.

We also note that the concept of logging in Lemma 4.5 and Theorem 4.6 is a general abstraction for installing a standalone record in fault-tolerant storage, independent of implementation. The actual cost of logging, however, is implementation-specific. For example, the write logging in Halfmoon-read can be overlapped with execution, or merged with DBWrite if the external state exposes its internal logging and ordering of events. Nonetheless, all writes in Halfmoonread are considered logged because they are all associated with persistent objects in the multi-version external storage at the least. In contrast, even if an SSF performs logging in Init under Halfmoon-read and then issues a log-free read, the preceding logging operation is not considered part of the read because the Init call is not even aware of such an operation. As we show in § 4.4, the logging in Init serves to bring the cursorTS up-to-date, and is not necessary for idempotence. The initial cursorTS is only required to be deterministic, which can be inherited from the parent SSF, or if there is no such SSF, be arbitrarily out-of-date.

Halfmoon measures the logging overhead as the number of *abstract* logging operations. Given any particular implementation, a fault-tolerant logging protocol either logs more reads than Halfmoon-read or logs more writes than Halfmoon-write in the worst case. Therefore our protocols identify two minimums in the design space. The actual choice between them depends on the implementation and the workload. We present an analysis in §4.6 to quantify this decision.

# 4.4 Consistency

The primary goal of this paper is to explore the minimal logging overhead required for idempotence. In doing so, Halfmoon relaxes the real-time guarantees of linearizability [45] such that events can be persisted without logging. Specifically, Halfmoon-read provides *sequential consistency* (SC), which guarantees that events are totally ordered, and the order adheres to the program order of each process in the system. The ordering under Halfmoon-write is semantically equivalent to SC as long as consecutive writes to different objects can commute. Formally, we have the following propositions. We provide TLA+ verification in the appendix.

**Proposition 4.7.** Halfmoon-read orders events according to their logical timestamps. This ordering provides sequential consistency.

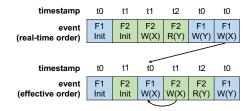
*Proof.* For simplicity, we consider only read and write events; nested SSFs can be flattened into a single SSF with auxiliary logging at the function boundaries. It follows that writes are already totally ordered by the logging layer according to the write timestamps, because the creation of a write log record serves as the commit point of the corresponding write where it becomes visible to other SSFs. Because log-free reads are mapped to writes by seeking backward on the write log, the effective interleaving of reads and writes is equivalent to the one produced by inserting the reads in the ordered sequence of writes based on read timestamps.

To see that the timestamp order provides sequential consistency, note that the cursorTS is monotonically increasing within each SSF. Suppose that there is a violation of program order, then there must be a timestamp inversion in the total order, contradicting the way it is constructed.

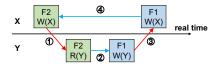
**Proposition 4.8.** Halfmoon-write orders events through the following steps. First, all events are ordered by real time. Second, write events are reordered according to their version numbers. Specifically, a write is not reordered if it succeeds in conditional update (§ 4.2); otherwrise, it is placed immediately before the next successful write to the same object with a higher version. This total ordering enforces a sequential history for each SSF except that consecutive log-free writes to different objects, i.e., those between two logged events, may commute.

*Proof.* In line with the proof of Proposition 4.7, we only consider read and write operations. For all reads and all successful writes, they are processed in real-time in the external state, which naturally adheres to the actual interleaving of reads and writes. Writes that get reordered do not change the external state and are not visible to any other SSFs. The placement of these writes in the event stream should maintain the monotonicity of version numbers for each object, as a result of conditional updates, and also respect the data dependencies of reads. Therefore we insert a reordered write immediately before the next successful write to the same object with a higher version.

Taking the sequential history of each SSF from the total ordering, we note that reads and successful writes adhere to the program order because they are ordered by real time. It remains to show that a reordered write w may never go backward across a preceding read r in the SSF. Suppose wis placed immediately before w', the next successful write. Then it suffices to show that w' happens later in real time than r. For w' to succeed in the conditional update, it must have acquired a higher cursorTS than that of w, which equals the one obtained after logging r. Because the logging layer issues monotonically increasing segnums respecting the monotonicity of the real time, w' indeed happens later than r in real time. Note that by combining cursorTS with a local counter, version numbers are always monotonic within each SSF. Therefore consecutive log-free writes to the same object are never reordered.



(a) Example of the ordering of events under Halfmoon-write.



**(b)** Enforcing program order among consecutive writes creates a dependency cycle in the example. Red edges (13) represent the program order; blue edges (24) represent the data dependencies. Note that the direction of edges indicates *precedence*, unlike the other figures in this paper.

**Figure 8.** Example of Halfmoon-write where consecutive log-free writes to different objects may commute.

**Example.** Figure 8a presents an example to illustrate the total ordering under Halfmoon-write. For simplicity, we consider only the cursorTS instead of the entire tuple for version numbers. F2's Write(X) with version  $t_1$  and F1's Write(Y) with version  $t_0$  succeed in conditional update and are not reordered. F1's Write(X) with version  $t_0$ , however, is reordered before F2's Write(X). Consequently, the program order of F1 is changed such Write(X) happens before Write(Y). However, although F1's Write(X) is reordered, it will never go past the preceding logged operation (Init in this case).

Ordering of consecutive writes. The example shows that Halfmoon-write may only change the program order of consecutive log-free writes to different objects. Consequently, the ordering of Halfmoon-write is exactly the same as SC when SSFs do not perform consecutive writes to different objects, and is semantically equivalent to SC when such writes can commute. In case the ordering of consecutive writes must be preserved, one can perform extra logging between the writes such that every dependent pair cannot be reordered. The best practice under Halfmoon-write is to make dependencies explicit through invocation or trigger edges in the SSF workflow, and utilize the logging in the init step of each SSF to prevent reordering. We observe this design pattern in a variety of workloads [3, 4, 9, 10, 30, 50, 108].

We also provide an extension of Halfmoon-write that eliminates possible reordering of consecutive writes. As a result, the extended protocol provides sequential consistency. It is also is log-free on writes in the best case. By best case, we mean that whether the protocol requires extra write logging depends only on the actual interleaving of operations, regardless of the dependencies in the SSF code. The key idea is to

utilize the pre-read cursorTS, i.e., the SSF's cursorTS before logging the read result, to detect and break possible dependency cycles in Figure 8b. By definition, the pre-read cursorTS represents the highest possible version number this SSF might have used in its writes (omitting the counter). This allows SSFs to check during writes if there exists a *timestamp inversion* edge, e.g., edge ② in Figure 8b, where a write has data dependency on a read with a higher cursorTS. If so, the write should perform extra logging to advance the cursorTS for subsequent writes, thereby inverting edge ④ in the dependency cycle. In the best case, e.g., under a write-intensive workload, there are no timestamp inversions and the protocol can be log-free on writes.

To check for timestamp inversion, we let reads maintain a monotonically increasing sequence of (version, pre-read cursorTS) pairs for each object. The version field equal the version of the object the read has seen. A read creates such a pair only if its cursorTS is higher than (i) the current object version, which indicates a potential timestamp inversion, and (ii) the largest pre-read cursorTS in the sequence of pairs, so as to ensure monotonicity. If several consecutive pairs have the same object version, they are merged by overwriting the tail of the sequence. Updating the sequence should be atomic with reading the object, which can be implemented using existing techniques such as DAAL [87, 108].

Upon visiting the object, a write atomically updates the object and searchs for a pair in the sequence that has the largest object version below the version of the write. If the cursorTS of this pair is higher than the write version, then there is a timestamp inversion. The subsequent extra logging step need not be atomic with the above step; the atomicity of reading the object and updating the sequence of pairs ensures idempotence in the detection of timestamp inversion. We provide a TLA+ verification of idempotence and sequential consistency of the extended protocol in the appendix.

**Remark.** One might wonder why the two protocols are dual to each other in terms of design but differ in the ordering of events. The reason is that writes have external effects while reads do not. Therefore, there is more freedom in placing logfree reads in the event stream than placing log-free writes. For a log-free read under Halfmoon-read, no matter when in real time the read is actually performed, we can always safely insert it in the event stream based on its assigned logical timestamp. In contrast, under Halfmoon-write, the placement of a log-free write not only depends on its version number (logical timestamp), but also on the real-time state of the object. If the conditional update succeeds, then the write must be placed precisely at this point in real time, since it would be immediately visible to reads after that point. This additional constraint leads to the permutation of program order in Figure 8.

Moreover, by advancing the cursorTS in Init, our protocols enforce a *rea-ltime* property at the *boundary* of SSFs: if

an operation finishes at t in real time, then all SSFs that starts after t are guaranteed to see the external effects of that operation. This property is well suited for a variety of serverless applications that use event triggers to invoke downstream tasks [5, 6, 8]. Optionally, an SSF can perform linearizable reads/writes by explicitly advancing the cursorTS beforehand. Similar to  ${\tt Init}$ , the SSF appends a special  ${\tt sync}$   ${\tt log}$  to acquire the up-to-date seqnum in the system. Halfmoon offers the flexibility for users to enforce linearizability if necessary, or achieve minimal logging overhead when our consistency guarantees suffice.

### 4.5 Garbage Collection

In line with previous work [50, 108], Halfmoon uses a garbage collector (GC) function to remove the log records of finished SSFs. The GC is periodically invoked by the runtime. For Halfmoon-write, the lifetime of a read log record is equal to that of the initiating SSF. For Halfmoon-read, the GC should delete both the write log records and the matching object versions in the external state. Because a write log record has a dual purpose (§4.1), its lifetime should be the maximum of the SSF's and the object version's lifetime. Finally, the object version should outlive all SSFs that might read it.

Consequently, to garbage collect an object version whose matching write log record has segnum t, the GC must wait until the following conditions are met: (a) there exists another record in the object's write log with seqnum t' > t, and (b) all SSFs that starts before t', i.e., with initial cursorTS less than t', finishes. Condition (b) entails the completion of the initiating SSF, so (a) and (b) also apply to garbage collecting the write log. Both conditions can be checked during the GC scan [50, 108]. Specifically, the GC tracks the latest segnum  $\bar{t}$ that satisfies (b). Upon advancing  $\bar{t}$ , for each per-object write log, the GC marks the latest log record whose seqnum falls below the new  $\bar{t}$ . These records point to the earliest object versions that might still be observed by current or future SSFs. Therefore, for each per-object write log, it deletes all records preceding the marked records, as well as the corresponding object versions in the external state.

### 4.6 Choosing the Right Protocol

So far, the protocols apply to accessing the entire external state. However, it is possible to use *independent* protocols per object. This is because the two protocols differ only in the handling of reads and writes, and both can reuse the cursorTS of the SSF. We therefore focus on choosing the protocol for a single object.

Qualitatively, we should use the Halfmoon-read/write protocol for read/write-intensive workloads, respectively. For simplicity, we consider only read and write operations. We now quantify the decision. Let  $P_r$ ,  $P_w$  as the probability that an SSF reads and writes the object, respectively. Let  $\lambda$  be the average arrival rate of SSFs. Then we can express the read/write intensity by multiplying  $P_r$  or  $P_w$  with  $\lambda$ .

**Storage overhead**. Let t be the average function lifetime (including re-execution in case of failures). The lifetime analysis in §4.5 assumes that GC is performed as soon as possible. To account for the periodicity of GC, we define  $T_{g\,c}$  as the average delay between the completion of an SSF and the next GC scan.

We start by deriving the storage overhead for Halfmoon-write, which consists of the read log records and a single version of the object. Let  $N_r$  be the average number of read log records across time. By Little's Law [71],  $N_r$  equals the effective arrival rate of reads, which is  $P_r\lambda$ , times the average lifetime of read log records. We therefore have  $N_r = P_r\lambda(t+T_{qc})$ , and the time-averaged storage overhead  $S_{read}$  is

$$S_{read} = S_{val} + N_r (S_{meta} + S_{val}) \tag{1}$$

$$= S_{val} + P_r \lambda (t + T_{gc}) (S_{meta} + S_{val})$$
 (2)

where  $S_{meta}$  and  $S_{val}$  denote the metadata size of a read log record and the object size, respectively. The full size of a read log record is  $S_{val} + S_{meta}$ .

For Halfmoon-read, the storage overhead consists of the write log and several versions of the object. Let  $N_w$  be the average number of write log records across time, which is also the average number of object versions. Let  $T_w$  be the average time gap between two consecutive writes to the object. According to §4.5, the average lifetime of a write log record and the corresponding object version is  $T_w + t$ , where  $T_w$  enforces condition (a), and t enforces (b). Considering  $T_{gc}$ , we have  $N_w = P_w \lambda (T_w + t + T_{gc})$ . Assuming a Poisson arrival of SSFs [64], we have  $T_w = 1/(P_w \lambda)$ . The average storage overhead  $S_{write}$  is

$$S_{write} = N_w (2S_{meta} + S_{val}) \tag{3}$$

$$= (1 + P_w \lambda (t + T_{ac}))(2S_{meta} + S_{val})$$
 (4)

Equation 3 assumes that the size of a write log is equal to  $S_{meta}$ . Note that there is a coefficient of two because our prototype of Halfmoon-read also logs *before* each write to align the write logging overhead with Boki (§ 4.1). We further assume that  $S_{meta}$  is negligible compared to  $S_{val}$ . Dividing both  $S_{read}$  and  $S_{write}$  with  $S_{val}$ , we derive the boundary condition as  $P_r = P_w$ . A higher read intensity means that Halfmoon-read has lower storage overhead, and vice versa.

Runtime overhead. Let  $C_w$  be the extra cost of a write in Halfmoon-read compared to that of Halfmoon-write. Similarly, let  $C_r$  be the extra cost of a read in Halfmoon-write over Halfmoon-read. The extra cost takes all relevant factors into account, including logging and multi-versioning. In a given time period T, the expected numbers of reads and writes to the object are  $P_r\lambda T$  and  $P_w\lambda T$ , respectively. Then the expected extra costs of the two protocols are  $P_w\lambda TC_w$  and  $P_r\lambda TC_r$  in total, respectively. For our system prototype, we have  $C_w\approx 2\,C_r$ , where the coefficient of two is due to the same reason as that of Equation 3 (aligning our write logging overhead with Boki). The boundary condition is then

 $P_r = 2P_w$ . A higher read intensity means that Halfmoonread has lower runtime overhead, and vice versa.

**Remark.** Note that the runtime analysis assumes that all SSFs have equal importance. To differentiate between SSFs, we can analyze the read and write activity of each SSF respectively, finally taking a weighted sum. We can also combine the runtime overhead with the storage overhead by taking another weighted sum, e.g., by their monetary cost, to facilitate the final decision.

### 4.7 Switching between Protocols

The intensity of read and write, namely  $P_r$  and  $P_w$ , may change over time for a particular object. We therefore present a switching mechanism between the two protocols. There are three major requirements. First, the switching must not violate Theorem 4.6. Second, SSFs must not be blocked during the switching. Third, the switching must be fault-tolerant, i.e., SSFs must consistently use the same protocol for each step during re-execution.

To satisfy the above requirements, we maintain a *transition log* to record the switching history. It is necessary because there can be an arbitrary delay between SSF failure and reexecution, possibly spanning several switching events. The runtime starts the switching by appending a "BEGIN" record to the transition log. It also scans the init log records (§4.1) to find all running SSFs that start before the switching. When all of these SSFs finish, the runtime completes the switching by appending an "END" record.

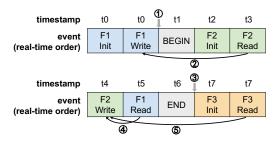
We now describe the switching from the perspective of an SSF. The first time an SSF reads or writes an object, it queries the transition log to determine which protocol to use, and consistently uses the same protocol for that object in subsequent operations. Specifically, it calls logReadPrev to retrieve a transition log record, using the initial cursorTS acquired in Init. This ensures that the switching is faulttolerant, since both the cursorTS and the transition log are persistent. If the log record is "END", the SSF should use the target protocol specified in the record as normal. However, if the record is "BEGIN", the SSF should use a special transitional protocol that logs all reads and writes. It cannot use the new protocol immediately; otherwise, SSFs using the old protocol will run concurrently with those using the new, violating Theorem 4.6. Once all SSFs using the old protocol finish, the runtime can safely switch to the new protocol.

## 5 Implementation

We implement the Halfmoon prototype on top of Boki. We modify 2300 lines of C++ in the logging layer. Halfmoon's client library consists of 1700 lines of Go.

# 5.1 Resolving Conflicts Among Peer Instances

We discuss in §4 that there are two race conditions against the exactly-once semantics. We handle the first one in §4.1–4.2. To address the second one (the race between peer instances),



 $\textcircled{1} \ \ \text{Halfmoon-write} \rightarrow \text{Transitional} \quad \textcircled{3} \ \ \text{Transitional} \rightarrow \text{Halfmoon-read}$ 

Figure 9. Example of the switching procedure.

We introduce logCondAppend (Figure 3). Compared with logAppend, it takes two additional parameters. condTag is the caller SSF's instanceID (env.ID); the log stream corresponding to this tag contains the log records created by the SSF. condPos is the current step number. logCondAppend first tries to append to the log normally as logAppend does. It then checks the offset of the log record in the caller's log stream specified by condTag. The conditional append succeeds if the offset is equal to condPos, i.e., the step number is as expected and the log record appears in the right position in the SSF's execution history. Otherwise, it undoes the log append and returns the seqnum of the log record at the expected offset, along with an error message.

logCondAppend is similar to the compare-and-swap operation in concurrent programming. It resolves conflicts in place to ensure that only a single instance succeeds in logging a certain operation. For symmetric protocols, logging and conflict resolution can be performed separately. For example, Boki immediately reads the caller's stream after appending to the log, and only honors the first log record of the current operation. This approach is practical because the sole purpose of logging in symmetric protocols is checkpointing SSF progress. Therefore the caller's log stream is visible to the peer instances but not to other SSFs. Conflict resolution, though as a separate step, naturally serves as a synchronization point among peers, i.e., it ensures that all instances have identical states after this step. However, Halfmoon's use of the write log (Figure 5), presents a new synchronization problem. Because the write log records also appear in the object's log stream specified by the key tag, they are visible to other SSFs as well. Suppose we resolve conflicts separately, then a concurrent log-free read might see an inconsistent state of the object's stream. In contrast, logCondAppend greatly simplifies the reasoning about concurrent instances.

We extend the implementation in §4 to handle the race condition among peers by simply replacing all logAppend with logCondAppend. If the conditional append fails, we let developers decide how to handle the error. For example, the SSF instance can use the returned seqnum to read the log records at the expected offset, and proceed with an identical state as its peers. Alternatively, it can quit the race by exiting.

### 5.2 Switching Between Protocols

To implement the switching procedure, we need to support both single- and multi-versioning in the external state. Our solution is to treat single-versioning as a special case of multiversioning. The former corresponds to a special LATEST version (managed by Halfmoon-write) among other versions (managed by Halfmoon-read). As per §4.1, multi-versioning can be implemented over plain key-value APIs where each version is represented by a separate key. Therefore the two versioning schemas can be seamlessly integrated. There is no intersection between them except during the switching. Figure 9 shows an example where the runtime switches from Halfmoon-write to Halfmoon-read. F1 (Halfmoon-write) and F3 (Halfmoon-read) perform single- and multi-version reads and writes, respectively. The handling of F2 is more complicated. F2's write should be visible to both F1 and F3 (4) and (5)), so it has to modify the LATEST version as well as create a separate version. F2's read should target both the LATEST version using Halfmoon-write (2) as well as some other version using Halfmoon-read (not shown in the figure), because its lifetime may overlap with both F1 and F3. F2 should compare the freshness of the data returned by the two protocols, namely the "version" attribute of the LATEST object version, and the sequum of the write log record matching the other version. The fresher one is chosen as the read result and logged for idempotence.

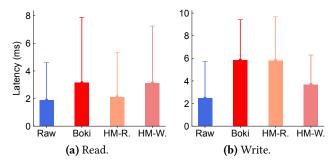
## 6 Evaluation

This section compares Halfmoon's performance with the state-of-the-art solution Boki [50], using microbenchmarks (§6.1) and realistic applications (§6.2). We also include an unsafe baseline with no logging. It does not offer exactly-once semantics and serves as the lower bound of Halfmoon. We evaluate Halfmoon's storage and runtime overhead under different read/write intensity in §6.3, and explores the switching delay between Halfmoon's protocols in §6.4.

**Experimental setup.** We conduct all our experiments on AWS EC2 c5d.2xlarge instances using the configuration reported in Boki [50]. Each instance has 8 vCPUs, 16GiB of DRAM, and 200GiB NVMe SSD. The runtime infrastructure consists of eight function nodes and one function gateway; the logging layer consists of three storage nodes and one sequencer node. Both Boki and Halfmoon use Amazon DynamoDB [34] as the external storage.

### 6.1 Microbenchmarks

We measure the median and 99%-tile tail latency of reads and writes over a period of 10 minutes. In line with previous works [50, 108], we use a synthetic SSF that issues one read and write per request. We populate the external state with 10K objects, each consisting of 8B key and 256B value. Figure 10 shows the results. Compared to Boki, Halfmoonread offers  $\sim$ 30% lower latency on reads and achieves similar



**Figure 10.** Latency of read and write. Halfmoon-read/write is abbreviated as HM-R/W. Main bars and error bars show median and 99%-tile tail latency, respectively.

performance on writes (as per § 4.1, we deliberately align Halfmoon-read's write logging overhead with Boki). It offers exactly-once reads with only  $\sim 15\%$  overhead over unsafe raw reads, which is  $4-5\times$  lower than Boki. Halfmoon-write also achieves  $\sim 30\%$  lower latency than Boki on writes, and has similar performance on reads. The latency of log-free writes is still higher than raw writes, because Halfmoon-write performs *conditional* updates (§4.2), which is more expensive than directly updating the object. However, the overhead is still  $2-6\times$  lower than Boki, of which writes are also conditional and require logging.

### 6.2 End-to-End Application Workloads

We evaluate Halfmoon over three realistic application workloads. The first two workloads, travel reservation and movie review, are adapted from DeathStarBench [3, 40] and are commonly used in Boki and Beldi. Travel reservation runs a workflow of 10 SSFs. Users search for nearby hotels based on distance and ratings, and then make reservations. This workload is read-intensive. Movie review runs a workflow of 13 SSFs. It is slightly skewed towards writes as posting user reviews makes up its core functionality. The third workload is Retwis, a simplified Twitter clone [12]. Retwis consists of several Twitter functions (e.g., post tweet, get timeline) that perform PUTs and GETs on a key-value store. This workload is also read-intensive. All three workloads store application data in DynamoDB. We evaluate both Halfmoon-read and Halfmoon-write to demonstrate the benefits of using the appropriate protocol, as well as the worst-case performance penalties when using the wrong protocol.

Figure 11 shows the results. Using the appropriate protocol, Halfmoon offers 20%-40% lower median latency for the three workloads, and achieves 1.5–4.0× lower overhead above the unsafe baseline. Logging is typically not the bottleneck of Boki, so it saturates at approximately the same load as Halfmoon. Halfmoon-read outperforms Halfmoon-write in read-intensive workloads (Figure 11a and 11c), and otherwise in write-intensive workload (Figure 11b). Halfmoon outperforms Boki even under the wrong protocol, because Boki either logs more reads than Halfmoon-read or logs more writes than Halfmoon-write.

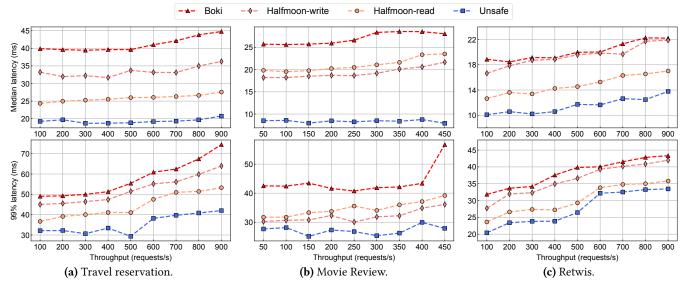


Figure 11. End-to-end performance of Boki and Halfmoon under three application workloads.

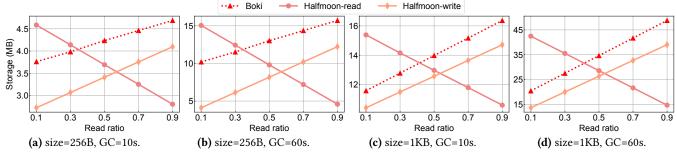


Figure 12. Storage overhead of Boki and Halfmoon under different object size and GC interval.

# 6.3 System Overhead

We use a synthetic SSF to validate the overhead analysis in §4.6. The SSF issues 10 operations to the database. We vary the read and write intensity of the workload by changing the ratio of reads among the operations. We populate 10K objects in the database. Each operation in the SSF targets a random object, such that the read ratio is representative of the read intensity over each object. We compare the two protocols to determine the boundary condition when they have equal overhead. For reference, we also measure the overhead of Boki.

**Storage overhead.** We measure the time-average storage usage over a period of 10 minutes. The overall usage consists of log and database storage. Halfmoon-write stores a single version of each object, while Halfmoon-read stores multiple versions. We vary the size of each object and the GC interval. Figure 12 shows the results. §4.6 predicts that the boundary condition is when the read and write intensity are equal, i.e., the read ratio is 0.5. The theoretical boundary is an asymptotic result when the log storage is negligible compared with database storage. The actual boundary is slightly higher, because Halfmoon-read logs twice for each write (§4.1), while

Halfmoon-write logs once for each read. As the object size increases, the boundary moves closer to 0.5 as the database storage becomes the decisive part. As per our analysis in §4.6, the boundary condition is not affected by the choice of GC interval in Figure 12. Halfmoon-read has a higher storage usage than Boki under low read ratio, i.e. high write intensity, because the overhead of multi-versioning outweighs that of the read log records, which are rather scarce. Compared with Boki, Halfmoon requires 1.2–3.4× less storage on average.

Runtime overhead. We measure the median latency under different request rates. The object size is set to 256B and the GC interval to 10s. Figure 13 shows the results. We predict in §4.6 that the boundary condition is when the read intensity is twice the write intensity, i.e., the read ratio is 2/3. The actual boundary is slightly higher, because  $C_w$  is more than twice  $C_r$  in practice (Figure 10). Figure 13 also confirms that the request rate has little impact on the boundary condition. Both of our protocols have lower latency than Boki, with an improvement factor of  $1.2-1.5\times$ . We empirically validate that Halfmoon's runtime performance is insensitive to the GC interval. This is because the overhead of querying the log or database index typically scales logarithmically with the number of log records or object versions.

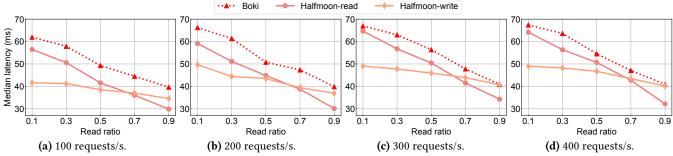
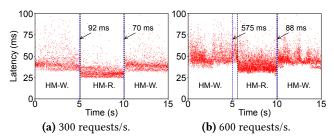


Figure 13. Runtime overhead of Boki and Halfmoon under different request rates.



**Figure 14.** The switching delay between Halfmoon's protocols (abbreviated as HM-R/W). The red dot shows SSF latency over time. The blue vertical line marks the beginning of switching. The black line marks its end.

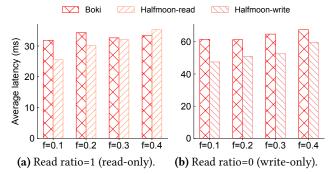
# 6.4 Switching Delay

We use the same SSF as §6.3 to evaluate the switching delay. The workload has two phases. The first phase runs Halfmoonwrite with a read ratio of 0.2. The second runs Halfmoonread with a read ratio of 0.8. We change the phase every five seconds. Figure 14 shows the dynamics of SSF latency over time. Under a moderate load of 300 requests/s, the switching takes less than 100 ms. Under 600 requests/s (the workload saturates at about 800 requests/s), it takes longer to switch from Halfmoon-write to Halfmoon-read than the other way around. This is because SSFs in the first phase have a longer completion time due to the higher write intensity, and Halfmoon needs to wait until all SSFs using the old protocol finish before switching to the new protocol (§4.7).

### 6.5 Recovery Cost

Halfmoon's asymmetric protocols are designed for the failure-free common case. During re-execution, Halfmoon always replays log-free operations. In contrast, symmetric logging protocols such as Boki may skip logged operations. The speedup is implementation-specific. For Boki, the overhead of reading a log record is negligible compared to database operations. Therefore Boki always checks the logs before performing the actual read or write. In the extreme case, its recovery cost consists only of log reads.

We now incorporate the recovery cost into the total latency. We model the execution of an SSF as a Bernoulli Process. Let f be the probability of SSF failure. In each round, the SSF finishes with probability 1 - f and crashes with probability



**Figure 15.** The total expected latency of Halfmoon and Boki under different failure rates.

f. Then the expected rounds of execution n before the SSF returns successfully is 1/(1-f). As an extreme case, we assume that the symmetric protocol has zero recovery cost, and the asymmetric protocol needs to replay every operation such that there is no speed up for recovery. Consequently, the total expected SSF latency under the symmetric protocols is simply the runtime cost of a single failure-free round. For our asymmetric protocols, the total expected latency consists of a single failure-free round and n-1 recovery rounds (with the same runtime cost as the failure-free round). Suppose that our protocols have x percent less runtime cost than the symmetric protocols in the failure-free case. Substituting xinto the total expected latency, we see that the boundary condition is when f equals x, and a lower f implies that our asymmetric protocols have lower latency. According to Figure 10, the boundary condition between Boki and Halfmoon is  $f \approx 30\%$ , which far exceeds the actual failure rate of real applications.

We use the synthetic SSF workload in §6.3 to evaluate the actual end-to-end latency in the presence of failures. To represent the extreme cases where Boki has zero recovery cost and Halfmoon replays every operation, we set the read ratio of the workload to 1 or 0, i.e., the workload is read-only or write-only, and use Halfmoon-read and Halfmoon-write for the two cases, respectively. We run the workload at 100 requests/s and set the object size to 256B. Figure 15 shows the average latency of Halfmoon and Boki under different failure rates. Halfmoon outperforms Boki when f is less than

**Table 2.** The 99%-tile latency of Halfmoon and Boki under f = 10%.

	Read-only	Write-only
Boki	52.06ms	92.97ms
Halfmoon	62.69ms	103.79ms

30% and 40% under the read-only and write-only workloads, respectively. We also measure the 99%-tile tail latency of Halfmoon and Boki under a failure rate of f=10%. As shown in Table 2, even if one out of every ten SSF fails, Halfmoon only incurs 10%-20% higher tail latency than Boki.

### 7 Discussion

Ordering and timestamps. State machine replication (SMR) [13, 27, 35, 56, 59, 82] and its equivalents [17, 20, 22, 25, 41, 52, 73, 95] are common ways of building fault-tolerant distributed services [14]. SMR ensures that each process replicating the service executes commands following a global total order. Timestamp-based ordering is widely adopted in SMR. Global ordering can be established using synchronized clocks [26, 57] or timestamp agreement mechanisms [29, 35, 50]. Halfmoon's event stream is built on top of SMR. It utilizes the event timestamps to deterministically parameterize log-free reads and writes. Halfmoon also requires that the event stream be traceable, which is naturally satisfied by existing SMR protocols that maintain a command log [17, 63, 81].

**Security and privacy.** The write log in Halfmoon-read serves a dual purpose (§4.6) and is visible to other SSFs. To avoid leaking private data, we can perform access control or encryption in the logging layer or the client library [111]. Only the shared fields should be exposed to other SSFs.

**Program analysis and verification.** Halfmoon takes no application-specific hints from SSF code. That is, it assumes the most pessimistic setup where all external operations are non-idempotent, which must be logged or deterministically parameterized. This is not necessarily true in practice. For example, if an object is read-only, then all reads to that object are inherently idempotent. Similarly, consider pushing to a message queue. If the receiver SSF can handle duplicate messages, then the push operation is also idempotent on its own. To avoid unnecessary logging, we can use existing tools [38, 39, 43, 47, 60, 66, 68, 75, 76, 79, 116] to analyze the SSF code beforehand to rule out such operations [66, 72, 74, 102, 103, 107]. Halfmoon is log-optimal in providing idempotent access to general mutable shared state.

### 8 Related Work

**Stateful serverless computing** on top of the stateless FaaS paradigm has been identified as a challenging task by many prior works [37, 44, 58, 90, 109]. A line of research optimizes the transfer of intermediate state across functions in analytic or stream processing workflows [58, 61, 69]. This paper targets a different scenario of sharing *mutable* state across

SSFs. In terms of accessing the shared state, some works [50, 89, 90, 100, 108] adopt a data-oriented approach using table or key-value APIs, while others [2, 21, 23, 24, 28] adopt an object-oriented approach by encapsulating the state and access methods. Another line of research focuses on the formal semantics [24, 49, 55] and verification of SSFs [15, 30]. Halfmoon studies the orthogonal problem of the minimally necessary logging overhead for idempotence. It is an interesting direction to integrate Halfmoon's idea with these works to automatically generate log-optimal SSF implementations.

Log-based replay is a well studied approach for fault tolerance [31, 46, 83, 87, 94] and troubleshooting [38, 54, 77, 84, 93, 105, 106, 113, 114, 117]. The idea has been broadly embraced by serverless computing [50, 55, 108]. Olive [87] proposes to use write-ahead redo logging to achieve exactly-once semantics. Beldi [108] extends Olive to the serverless environment and supports transactional workflows. Boki [50] implements Beldi's techniques using the shared log [17, 29, 96]. In terms of reducing logging overhead, DDOS [48] enforces determinism in distributed systems and only requires logging message arrival times. Halfmoon has similar inspirations in stabilizing timestamps, and moves further to eliminate the logging overhead for either reads or writes.

Multi-versioning has been widely adopted in ACID databases for concurrency control (MVCC) [80, 97, 101], where reads target old versions and writes install new versions. In the context of serverless computing, AFT [89] uses multi-versioning to provide read atomic isolation. The Halfmoon-read protocol applies the idea of existing works in a novel way to enable log-free exactly-once reads.

### 9 Conclusion

Halfmoon introduces novel optimizations to the log-based fault tolerance of SSFs. We design two logging protocols that enforce exactly-once semantics while providing log-free reads and writes, respectively. Instead of symmetrically logging every single read and write, our key insight is that it suffices to log *either* reads or writes, i.e., asymmetrically. We theoretically prove that our protocols are log-optimal. Therefore, Halfmoon pushes the overhead of log-based fault tolerance to its lower bound. We provide a criterion for choosing the right protocol for a given workload, and a pauseless switching mechanism to switch protocols for dynamic workloads. Experiments show that Halfmoon achieves 20%-40% lower latency and  $1.5-4.0\times$  lower logging overhead than the state-of-the-art solution.

Acknowledgements. We thank our shepherd, Ryan (Peng) Huang, and the anonymous reviewers for their insightful feedback. This work was supported in part by the National Key Research and Development Program of China under the grant number 2022YFB4500700, the National Natural Science Foundation of China under the grant numbers 62325201 and 62172008, the National Natural Science Fund for the

Excellent Young Scientists Fund Program (Overseas). Xin Jin and Xuanzhe Liu are the corresponding authors. Sheng Qi, Xuanzhe Liu, and Xin Jin are affiliated with Key Laboratory of High Confidence Software Technologies (Peking University), Ministry of Education, School of Computer Science at Peking University, and Center for Data Space Technology and System at Peking University.

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# Appendix A TLA+ Verfication

```
- module HMBase\ -
extends Naturals, Sequences
CONSTANTS
     SSFs,
     NumPeers,
     Objects,
     MaxOps
VARIABLES
    globalSeqnum,
     ssfCommand,
     ssfState,
     ssfHistory,
     objState,
     objHistory
EventIDs \stackrel{\triangle}{=} SSFs \times (1 ... MaxOps) (id, pc)
InstanceIDs \stackrel{\triangle}{=} SSFs \times (1..NumPeers) (id, pid)
Versions \stackrel{\triangle}{=} [ts:Nat, pc:0..MaxOps]
SSFRecords \triangleq [pc:0..MaxOps,
                     opName: {"read", "write", "init"},
                     key: \{```\} \cup Objects,
                     ts: Nat,
                     version
                                     : Versions]
SSFCommands \stackrel{\triangle}{=} [opName : \{\text{"read", "write"}\}, key : Objects]
SSFInternals \triangleq [cursorTS : Nat,
                       pc: 0 \dots MaxOps,
                       nextOp: \{\text{``init''}, \text{``all''}, \text{``readlog''}, \text{``writelog''}\},
                       tmp: [key: {""}] \cup Objects,
                               version: Versions]]
ObjRecords \stackrel{\triangle}{=} [eid : EventIDs,
                     version: Versions,
                     opName : {"read", "write"}]
 Type invariants
SSFTypeOK \triangleq
     \land ssfCommand \in [SSFs \rightarrow Seq(SSFCommands)]
     \land ssfState \in [InstanceIDs \rightarrow SSFInternals]
     \land ssfHistory \in [SSFs \rightarrow Seq(SSFRecords)]
ObjHistoryTypeOK \stackrel{\triangle}{=} objHistory \in [Objects \rightarrow Seq(ObjRecords)]
GlobalTypeOK \stackrel{\triangle}{=} NumPeers \ge 1 \land globalSeqnum \in Nat
```

```
SSF invariants SSFCursorTSUnique \stackrel{\triangle}{=} \\ \forall id1, id2 \in SSFs, pid1, pid2 \in 1... NumPeers:
```

```
Let ts1 \stackrel{\triangle}{=} ssfState[id1, pid1].cursorTS
ts2 \stackrel{\triangle}{=} ssfState[id2, pid2].cursorTS \text{ in}
id1 \neq id2 \implies ts1 \neq ts2 \lor ts1 = 0 \lor ts2 = 0
SSFCursorTSConsistent \stackrel{\triangle}{=}
\forall id \in SSFs, pid \in 1...NumPeers:
ssfState[id, pid].cursorTS \leq globalSeqnum
SSFHistoryMonotone \stackrel{\triangle}{=}
\forall id \in SSFs:
\text{Let }h \stackrel{\triangle}{=} ssfHistory[id] \text{ in}
\forall i, j \in 1...Len(h):
\land h[i].pc = i - 1
\land i < j \implies h[i].ts \leq h[j].ts
```

```
Object invariants
VersionHigher(left, right) \stackrel{\triangle}{=}
     \lor left.ts > right.ts
     \lor left.ts = right.ts \land left.pc > right.pc
VersionHigherOrEq(left, right) \stackrel{\triangle}{=}
     \lor left = right
     \lor VersionHigher(left, right)
ObjHistoryVersionMonotone \stackrel{\triangle}{=}
    \forall key \in Objects:
        LET objh \stackrel{\triangle}{=} objHistory[key] IN
        \forall i, j \in 1 ... Len(objh):
           i < j \implies VersionHigherOrEq(objh[j].version, objh[i].version)
BaseInvariants \triangleq
     \land SSFTypeOK
     \land ObjHistoryTypeOK
     \land GlobalTypeOK
     \land \ SSFCursorTSUnique
     \land \ SSFCursorTSConsistent
     \land \textit{SSFHistoryMonotone}
     \land ObjHistoryVersionMonotone
```

```
Init formula InitGlobalSeqnum \stackrel{\triangle}{=} globalSeqnum = 0 InitSSF \stackrel{\triangle}{=} \\ \land ssfCommand = [id \in SSFs \mapsto \langle \rangle] \\ \land ssfState = [id \in SSFs, pid \in 1 .. NumPeers \mapsto \\ [cursorTS \mapsto 0, \\ pc \mapsto 0, \\ nextOp \mapsto \text{``init''}, \\ tmp \mapsto [key \mapsto \text{``''}, \\ version \mapsto [ts \mapsto 0, \\ pc \mapsto 0]]]] \\ \land ssfHistory = [id \in SSFs \mapsto \langle \rangle]
```

```
let child modules specify object state InitObjectHistory \triangleq objHistory = [key \in Objects \mapsto \langle \rangle] BaseInit \triangleq \\ \land InitGlobalSeqnum \\ \land InitSSF \\ \land InitObjectHistory
```

```
Next formula
GetStepOffset(ssfh, pc, opName, key) \triangleq
      check that the step is unique and monotone instead
    LET offsets \stackrel{\triangle}{=} \{i \in 1 ... Len(ssfh) :
                               \wedge ssfh[i].pc = pc
                               \wedge ssfh[i].opName = opName
                               \wedge ssfh[i].key = key in
    if offsets = \{\} then 0
     ELSE CHOOSE i \in offsets: TRUE
GetOrLogInitTs(id, pid, deltaTS) \stackrel{\triangle}{=}
    LET step \stackrel{\triangle}{=} GetStepOffset(ssfHistory[id], 0, "init", "")
           initTS \stackrel{\triangle}{=} globalSeqnum + deltaTS in
    If step = 0 then
          \land ssfState' = [ssfState \ \texttt{EXCEPT} \ ! [id, pid] = [@ \ \texttt{EXCEPT} \ ! .nextOp = "all",
                                                                                     !.cursorTS = initTS]]
          \land ssfHistory' = [ssfHistory \ except \ ! [id] = Append(@, [pc \mapsto 0, ])
                                                                                       opName \mapsto "init",
                                                                                       key \mapsto "",
                                                                                       ts \mapsto initTS,
                                                                                       version \mapsto [ts \mapsto 0, pc \mapsto 0]])]
          \land qlobalSegnum' = initTS
     ELSE LET cursorTS \stackrel{\triangle}{=} ssfHistory[id][step].ts in
          \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                     !.cursorTS = cursorTS]]
          \land UNCHANGED \langle globalSeqnum, ssfHistory \rangle
EntryPoint(id, pid) \stackrel{\triangle}{=}
    LET ssf \stackrel{\triangle}{=} ssfState[id, pid]
           step \stackrel{\triangle}{=} GetStepOffset(id, 0, "init", "") in
     \wedge ssf.pc = 0
     \wedge ssf.nextOp = "init"
     \wedge \; ssf.cursorTS = 0
     \land \exists deltaTS \in 1 .. MaxOps : GetOrLogInitTs(id, pid, deltaTS)
     ∧ UNCHANGED ⟨objState, objHistory, ssfCommand⟩
ProposeCommand(id, opName, key) \stackrel{\triangle}{=}
    LET cmds \stackrel{\triangle}{=} ssfCommand[id] IN
     \land Len(cmds) < MaxOps
     \land ssfCommand' = [ssfCommand \ except \ ! [id] = Append(@, [opName \mapsto opName, ])
                                                                                        key \mapsto key])]
     \land unchanged \langle globalSeqnum, ssfState, ssfHistory, objState, objHistory <math>\rangle
BaseNext \stackrel{\triangle}{=}
     \vee \exists id \in SSFs, cmd \in SSFCommands : ProposeCommand(id, cmd.opName, cmd.key)
     \lor \exists \langle id, pid \rangle \in InstanceIDs : EntryPoint(id, pid)
```

```
Helper functions
Min(set) \stackrel{\triangle}{=} if set = \{\} THEN 0
                   ELSE CHOOSE x \in set : \forall y \in set : x \leq y
Max(set) \stackrel{\triangle}{=} if set = \{\} THEN 0
                   Else choose x \in set : \forall y \in set : x \ge y
 returns the index of the last element that satisfies the predicate
Partition(array, len, lhs, boolOp(\_, \_)) \stackrel{\triangle}{=}
    If len = 0 then 0
     ELSE Max(\{i \in 1 ... len : boolOp(lhs, array[i])\})
Insert(seq, prev, entry) \stackrel{\triangle}{=}
    LET left \stackrel{\triangle}{=} IF \ prev = 0 \ THEN \ \langle \rangle \ ELSE \ SubSeq(seq, 1, prev)
           right \stackrel{\triangle}{=} \text{ if } prev = Len(seq) \text{ THEN } \langle \rangle \text{ ELSE } SubSeq(seq, prev + 1, Len(seq)) \text{ in}
     Append(left, entry) \circ right
AppendToSSFHistory(id, record) \stackrel{\triangle}{=}
    Let ssfh \stackrel{\triangle}{=} ssfHistory[id]
           step \stackrel{\triangle}{=} GetStepOffset(ssfh, record.pc, record.OpName, record.key) in
    If step > 0 \land ssfh[step] = record then unchanged ssfHistory
     ELSE ssfHistory' = [ssfHistory \ EXCEPT \ ! [id] = Append(@, record)]
InsertReadToObjHistory(key, event) \stackrel{\triangle}{=}
    LET objh \stackrel{\triangle}{=} objHistory[key] IN
    If \exists i \in 1 ... Len(objh) : objh[i].eid = event.eid then unchanged objHistory
          vHistory \stackrel{\triangle}{=} [i \in 1 .. Len(objh) \mapsto objh[i].version]
          prev \stackrel{\triangle}{=} Partition(vHistory, Len(objh), event.version, VersionHigherOrEq) in
          objHistory' = [objHistory \ \texttt{EXCEPT} \ ! [key] = Insert(objh, prev, event)]
InsertWriteToObjHistory(key, event) \stackrel{\triangle}{=}
    Let objh \stackrel{\triangle}{=} objHistory[key]
           vHistory \stackrel{\triangle}{=} [i \in 1.. Len(objh) \mapsto objh[i].version]
           prev \stackrel{\triangle}{=} Partition(vHistory, Len(objh), event.version, VersionHigher) in
    If prev < Len(objh) \land objh[prev + 1].eid = event.eid then unchanged objHistory
     ELSE objHistory' = [objHistory \ except \ ! [key] = Insert(objh, prev, event)]
TopoCandidates(edges) \stackrel{\triangle}{=}
     \{e1 \in edges :
         \forall e2 \in edges:
             e2[2] \neq e1[1]
RECURSIVE TopoSort(_)
TopoSort(edges) \stackrel{\triangle}{=}
    If edges = \{\} then true
     ELSE LET candidates \stackrel{\triangle}{=} Topo Candidates (edges) in
          If candidates = \{\} then false
          ELSE TopoSort(edges \setminus candidates)
GlobalDepsAcyclic(programDeps(\_), dataDeps(\_)) \stackrel{\triangle}{=}
    LET pDeps \stackrel{\triangle}{=} \{edge \in EventIDs \times EventIDs : 
                              \exists id \in SSFs : edge \in programDeps(id)
           dDeps \stackrel{\triangle}{=} \{edge \in EventIDs \times EventIDs :
                              \exists key \in Objects : edge \in dataDeps(key) in
```

```
dataDeps(key) \stackrel{\triangle}{=}
     LET objh \stackrel{\triangle}{=} objHistory[key] in
     if Len(objh) \le 1 then \{\}
      ELSE \{\langle eid1, eid2 \rangle \in EventIDs \times EventIDs :
                   \exists i, j \in 1 .. Len(objh):
                       \wedge i < j
                       \land objh[i].eid = eid1
                       \land objh[j].eid = eid2
                       \land objh[i].opName = "write" \lor objh[j].opName = "write"}
                                                                    - module \mathit{HMRead} -
extends HMBase
 objState is an ordered sequence of object versions
 for the sake of reducing the state space, we reuse objHistory for objState
ObjVersionConsistent \stackrel{\Delta}{=}
     \forall key \in Objects:
         LET objh \stackrel{\triangle}{=} objHistory[key] IN
          \vee Len(objh) = 0
          \vee \exists id \in SSFs, pid \in 1...NumPeers:
              Let ssf \triangleq ssfState[id, pid]
                    version \triangleq objh[Len(objh)].version in
               \land version.ts \leq ssf.cursorTS
              \land version.pc \leq ssf.pc
 sequential consistency
programDeps(id) \stackrel{\triangle}{=}
     LET ssfh \stackrel{\triangle}{=} ssfHistory[id] IN
     if Len(ssfh) \le 1 then \{\}
      ELSE \{\langle \langle id, pc-1 \rangle, \langle id, pc \rangle \rangle : pc \in 2 ... Len(ssfh)\}
Invariants \stackrel{\triangle}{=}
      \land BaseInvariants
      \land ObjVersionConsistent
      \land GlobalDepsAcyclic(programDeps, dataDeps)
Init \stackrel{\triangle}{=} BaseInit \land objState = [key \in Objects \mapsto 0]
LookUpObjVersion(objh, version) \stackrel{\triangle}{=}
     LET vHistory \stackrel{\triangle}{=} [i \in 1 ... Len(objh) \mapsto objh[i].version]
            prev \stackrel{\triangle}{=} Partition(vHistory, Len(objh), version, VersionHigher) in
     If prev = 0 then [ts \mapsto 0, pc \mapsto 0]
      ELSE objh[prev].version
Read(id, pid, key) \stackrel{\triangle}{=}
       LET
       ssf \triangleq ssfState[id, pid]
       cmd \stackrel{\triangle}{=} ssfCommand[id]
       pcNext \stackrel{\triangle}{=} ssf.pc + 1
```

 $TopoSort(pDeps \cup dDeps)$ 

```
version \stackrel{\triangle}{=} Look Up Obj Version (obj History [key],
                                                   [ts \mapsto ssf.cursorTS, pc \mapsto pcNext])
       \land pcNext \leq Len(cmd)
       \land cmd[pcNext].opName = "read"
       \land cmd[pcNext].key = key
       \wedge ssf.nextOp = "all"
       \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid].pc = pcNext]
       \wedge LET record \stackrel{\triangle}{=} [pc \mapsto pcNext,
                                opName \mapsto "read",
                                key \mapsto key,
                                ts \mapsto ssf.cursorTS,
                                version \mapsto version] in
            AppendToSSFHistory(id, record)
       \land LET event \stackrel{\triangle}{=} [eid \mapsto \langle id, pcNext \rangle, version \mapsto version, opName \mapsto "read"] IN
            InsertRead To ObjHistory (key, event)
       \land UNCHANGED \langle globalSeqnum, ssfCommand, objState \rangle
Write(id, pid, key) \stackrel{\triangle}{=}
     LET
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
     cmd \stackrel{\triangle}{=} ssfCommand[id]
     pcNext \stackrel{\triangle}{=} ssf.pc + 1
      \land pcNext \leq Len(cmd)
      ∧ cmd[pcNext].opName = "write"
      \land cmd[pcNext].key = key
      \wedge ssf.nextOp = "all"
      \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "writelog",
                                                                                    !.pc = pcNext,
                                                                                    !.tmp.key = key]]
      ssf and obj history is updated in the logging step
      \land unchanged \langle globalSeqnum, ssfCommand, ssfHistory, objState, objHistory <math>\rangle
GetOrLogWrite(id, pid) \stackrel{\triangle}{=}
     LET
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
     key \stackrel{\triangle}{=} ssf.tmp.key
     version \stackrel{\triangle}{=} [ts \mapsto globalSeqnum + 1, pc \mapsto ssf.pc]
     step \stackrel{\triangle}{=} GetStepOffset(ssfHistory[id], ssf.pc, "write", key)
     If step = 0 then let
          wlog \stackrel{\triangle}{=} [pc \mapsto ssf.pc,
                        opName \mapsto "write",
                       key \mapsto key,
                       ts \mapsto globalSeqnum + 1,
                       version \mapsto version] in
           \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                         !.cursorTS = globalSegnum + 1]]
           \land ssfHistory' = [ssfHistory \ \texttt{EXCEPT} \ ! [id] = Append(@, wlog)]
           \land globalSeqnum' = globalSeqnum + 1
           \land LET event \stackrel{\triangle}{=} [eid \mapsto \langle id, ssf.pc \rangle, version \mapsto version, opName \mapsto "write"] IN
               objHistory' = [objHistory \ \texttt{except} \ ! [key] = Append(@, event)]
      ELSE LET wlog \stackrel{\triangle}{=} ssfHistory[id][step] in
```

```
\land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                    !.cursorTS = wlog.ts]]
          \land UNCHANGED \langle globalSegnum, ssfHistory, objHistory \rangle
WriteLog(id, pid) \triangleq
     \land ssfState[id, pid].nextOp = "writelog"
     \land GetOrLogWrite(id, pid)
     \land unchanged \langle objState, ssfCommand \rangle
Next \triangleq
     \vee BaseNext
     \vee \exists id \in SSFs, pid \in 1.. NumPeers : WriteLog(id, pid)
     \vee \exists id \in SSFs, pid \in 1...NumPeers, key \in Objects : \vee Read(id, pid, key)
                                                                             \vee Write(id, pid, key)
Spec \triangleq Init \land
                        \Box[Next]\langle globalSeqnum, ssfCommand,
                                    ssfState, ssfHistory,
                                    objState, objHistory⟩
Theorem Spec \implies \Box Invariants
                                                             - модиле \mathit{HMWrite} --
EXTENDS HMBase
ObjectStateTypeOK \triangleq
     objState \in [Objects \rightarrow [version : Versions]]
ObjVersionConsistent \triangleq
     \forall key \in Objects:
        LET obj \stackrel{\triangle}{=} objState[key] IN
        \exists id \in SSFs, pid \in 1... NumPeers:
           LET ssf \stackrel{\triangle}{=} ssfState[id, pid] IN
            \land obj.version.ts \leq ssf.cursorTS
            \land obj.version.pc \leq ssf.pc
 sequential consistency except that consecutive writes may commute
programDeps(id) \stackrel{\Delta}{=}
     Let ssfh \triangleq ssfHistory[id]
           eids \stackrel{\triangle}{=} \{id\} \times (1 ... MaxOps) in
     if Len(ssfh) \leq 1 then \{\}
     ELSE \{\langle eid1, eid2 \rangle \in eids \times eids :
                 \exists i, j \in 1 \dots Len(ssfh):
                     \wedge i < j
                     \wedge ssfh[i].pc = eid1[2]
                     \wedge ssfh[j].pc = eid2[2]
                     \land ssfh[i].opName = "read" \lor ssfh[j].opName = "read"}
Invariants \triangleq
     \land BaseInvariants
     \land ObjVersionConsistent
     \land GlobalDepsAcyclic(programDeps, dataDeps)
InitObjectState \triangleq
     objState = [key \in Objects \mapsto [version \mapsto [ts \mapsto 0,
```

```
Read(id, pid, key) \stackrel{\triangle}{=}
       LET
       cmd \stackrel{\triangle}{=} ssfCommand[id]
       ssf \stackrel{\triangle}{=} ssfState[id, pid]
       pcNext \stackrel{\triangle}{=} ssf.pc + 1
       ts \stackrel{\triangle}{=} ssf.cursorTS
       version \stackrel{\triangle}{=} objState[key].version
       \land pcNext \leq Len(cmd)
       \land cmd[pcNext].opName = "read"
       \land cmd[pcNext].key = key
       \land ssf.nextOp = "all"
        \land ssfState' = [ssfState \ \texttt{EXCEPT} \ ! \ [id, \ pid] = [@\ \texttt{EXCEPT} \ ! .nextOp = "readlog",
                                                                                       !.pc = pcNext,
                                                                                       !.tmp = [key \mapsto key, version \mapsto version]]]
        ssf and obj history is updated in the logging step
       \land unchanged \langle globalSeqnum, ssfCommand, ssfHistory, objState, objHistory <math>\rangle
GetOrLogRead(id, pid) \stackrel{\triangle}{=}
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
     key \stackrel{\triangle}{=} ssf.tmp.key
     version \stackrel{\triangle}{=} ssf.tmp.version
     step \stackrel{\triangle}{=} GetStepOffset(ssfHistory[id], ssf.pc, "read", key)
     If step = 0 then let
          rlog \stackrel{\triangle}{=} [pc \mapsto ssf.pc,
                       opName \mapsto "read",
                       key \mapsto key,
                       ts \mapsto globalSeqnum + 1,
                       version \mapsto version] in
           \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                           !.cursorTS = globalSegnum + 1]]
           \land ssfHistory' = [ssfHistory \ \texttt{EXCEPT} \ ! [id] = Append(@, rlog)]
           \land globalSegnum' = globalSegnum + 1
           \land LET event \stackrel{\triangle}{=} [eid \mapsto \langle id, ssf.pc \rangle, version \mapsto version, opName \mapsto "read"] IN
               InsertReadToObjHistory(key, event)
      ELSE LET rloq \stackrel{\triangle}{=} ssfHistory[id][step] IN
           \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                           !.cursorTS = rlog.ts]
           \land UNCHANGED \langle globalSeqnum, ssfHistory, objHistory \rangle
ReadLog(id, pid) \triangleq
      \land ssfState[id, pid].nextOp = "readlog"
          GetOrLogRead(id, pid)
      \land UNCHANGED \langle objState, ssfCommand \rangle
UpdateObj(id, pid, key) \stackrel{\triangle}{=}
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
```

```
pcNext \stackrel{\triangle}{=} ssf.pc + 1
     version \stackrel{\triangle}{=} [ts \mapsto ssf.cursorTS, pc \mapsto pcNext]
     event \stackrel{\triangle}{=} [eid \mapsto \langle id, pcNext \rangle, version \mapsto version, opName \mapsto "write"]
     obj \stackrel{\triangle}{=} objState[key]
     IF VersionHigher(version, obj.version) THEN
          \land objState' = [objState \ \texttt{EXCEPT} \ ! [key].version = version]
          \land objHistory' = [objHistory \ \texttt{EXCEPT} \ ! \ [key] = Append(@, event)]
     ELSE IF VersionHigher (obj.version, version) THEN
          \land Insert Write ToObjHistory (key, event)
          \land unchanged objState
     ELSE UNCHANGED \langle objState, objHistory \rangle
Write(id, pid, key) \stackrel{\triangle}{=}
     LET
     cmd \stackrel{\triangle}{=} ssfCommand[id]
     ssf \triangleq ssfState[id, pid]
     pcNext \stackrel{\triangle}{=} ssf.pc + 1
     version \stackrel{\triangle}{=} [ts \mapsto ssf.cursorTS, pc \mapsto pcNext]
     record \stackrel{\triangle}{=} [pc \mapsto pcNext,
                    opName \mapsto "write",
                    key \mapsto key,
                    ts \mapsto ssf.cursorTS,
                    version \mapsto version
     IN
     \land pcNext \leq Len(cmd)
     \land cmd[pcNext].opName = "write"
     \land cmd[pcNext].key = key
     \wedge ssf.nextOp = "all"
     \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid].pc = pcNext]
     \land Append To SSFHistory(id, record)
     \land UpdateObj(id, pid, key)
     \land unchanged \langle globalSeqnum, ssfCommand \rangle
Next \triangleq
     \vee BaseNext
     \vee \exists id \in SSFs, pid \in 1...NumPeers : ReadLog(id, pid)
     \vee \exists id \in SSFs, pid \in 1...NumPeers, key \in Objects : \vee Read(id, pid, key)
                                                                             \vee Write(id, pid, key)
Spec \stackrel{\triangle}{=} Init \wedge
                        \Box[Next]\langle globalSeqnum, ssfCommand,
                                    ssfState, ssfHistory,
                                     objState, objHistory)
Theorem Spec \implies \Box Invariants
                                                            -- морије HMWriteExt --
EXTENDS HMWrite
ReadTSs \triangleq [ts:Nat, version: Versions]
ReadTSHigher(left, right) \triangleq
     \lor VersionHigher(left.version, right.version)
     \lor left.version = right.version \land left.ts > right.ts
```

```
ExtObjectStateTypeOK \stackrel{\Delta}{=}
     objState \in [Objects \rightarrow [readTS : Seq(ReadTSs),
                                      version: Versions]]
ExtObjVersionConsistent \triangleq
      \land ObiVersionConsistent
      \land \forall key \in Objects:
          Let obj \stackrel{\triangle}{=} objState[key] in
          \forall i \in 1 .. Len(obj.readTS):
              LET rts \stackrel{\triangle}{=} obj.readTS[i] IN
              \land VersionHigherOrEq(obj.version, rts.version)
              \land rts.ts > rts.version.ts
              \land \exists id \in SSFs, pid \in 1...NumPeers:
                  Let ssf \stackrel{\triangle}{=} ssfState[id, pid] in
                  rts.ts \leq ssf.cursorTS
ExtObjReadTSMonotone \stackrel{\Delta}{=}
     \forall key \in Objects:
         LET readTS \stackrel{\triangle}{=} objState[key].readTS in
         \forall i, j \in 1 \dots Len(readTS):
            i < j \implies \land VersionHigherOrEq(readTS[j].version, readTS[i].version)
                         \land ReadTSHigher(readTS[j], readTS[i])
 sequential consistency
extProgramDeps(id) \stackrel{\triangle}{=}
     LET ssfh \stackrel{\triangle}{=} ssfHistory[id] IN
     If Len(ssfh) \leq 1 Then \{\}
      ELSE \{\langle \langle id, pc-1 \rangle, \langle id, pc \rangle \rangle : pc \in 2 ... Len(ssfh)\}
ExtInvariants \triangleq 
      \land BaseInvariants
      \land ExtObjectStateTypeOK
      \land ExtObjVersionConsistent
      \land \ ExtObjRead\,TSMonotone
      \land GlobalDepsAcyclic(extProgramDeps, dataDeps)
ExtInitObjectState \triangleq
     objState = [key \in Objects \mapsto [readTS \mapsto \langle \rangle,
                                               version \mapsto [ts \mapsto 0,
                                                               pc \mapsto 0]]]
ExtInit \stackrel{\triangle}{=} BaseInit \land ExtInitObjectState
ExtRead(id, pid, key) \stackrel{\triangle}{=}
     LET
     cmd \stackrel{\triangle}{=} ssfCommand[id]
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
     pcNext \stackrel{\triangle}{=} ssf.pc + 1
     ts \triangleq ssf.cursorTS
     obj \stackrel{\triangle}{=} objState[key]
     version \triangleq obj.version
     readTS \triangleq obj.readTS
```

```
\land pcNext \leq Len(cmd)
     \land cmd[pcNext].opName = "read"
     \wedge cmd[pcNext].key = key
     \land ssf.nextOp = "all"
     \land ssfState' = [ssfState \ except \ ![id, pid] = [@ \ except \ !.nextOp = "readlog",
                                                                               !.pc = pcNext,
                                                                               !.tmp = [key \mapsto key, version \mapsto version]]]
     \wedge IF \wedge ts > version.ts
             the second condition is just an optimization
            \wedge Len(readTS) = 0 \lor ts > readTS[Len(readTS)].ts then let
              myReadTS \stackrel{\triangle}{=} [ts \mapsto ssf.cursorTS, version \mapsto version]
              prev \stackrel{\triangle}{=} Partition(readTS, Len(readTS), myReadTS, ReadTSHigher) in
              objState' = [objState \ except \ ! [key].readTS = Insert(readTS, prev, myReadTS)]
         ELSE UNCHANGED objState
      ssf and obj history is updated in the logging step
     \land UNCHANGED \langle globalSeqnum, ssfCommand, ssfHistory, objHistory <math>\rangle
CheckTSInversion(readTS, version) \stackrel{\triangle}{=}
     versions \stackrel{\triangle}{=} [i \in 1 .. Len(readTS) \mapsto readTS[i].version]
    prev \stackrel{\triangle}{=} Partition(versions, Len(readTS), version, VersionHigher) in
    prev \neq 0 \land readTS[prev].ts > version.ts
ExtWrite(id, pid, key) \stackrel{\triangle}{=}
    LET
     cmd \stackrel{\triangle}{=} ssfCommand[id]
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
    pcNext \stackrel{\triangle}{=} ssf.pc + 1
     version \stackrel{\triangle}{=} [ts \mapsto ssf.cursorTS, pc \mapsto pcNext]
     record \stackrel{\triangle}{=} [pc \mapsto pcNext,
                   opName \mapsto "write",
                   key \mapsto key,
                   ts \mapsto ssf.cursorTS,
                   version \mapsto version
     \land pcNext \leq Len(cmd)
     \land cmd[pcNext].opName = "write"
     \land cmd[pcNext].key = key
     \wedge ssf.nextOp = "all"
     ∧ if CheckTSInversion(objState[key].readTS, version) then
          \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "writelog",
                                                                                   !.pc = pcNext,
                                                                                   !.tmp = [key \mapsto key, version \mapsto version]]]
          ∧ UNCHANGED ssfHistory
         ELSE
          \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid].pc = pcNext]
          \land AppendToSSFHistory(id, record)
     \land UpdateObj(id, pid, key)
     \land unchanged \langle globalSegnum, ssfCommand \rangle
GetOrLogWrite(id, pid) \stackrel{\triangle}{=}
    LET
     ssf \stackrel{\triangle}{=} ssfState[id, pid]
     key \stackrel{\triangle}{=} ssf.tmp.key
     version \triangleq ssf.tmp.version
```

```
step \stackrel{\triangle}{=} GetStepOffset(ssfHistory[id], ssf.pc, "write", key)
              If step = 0 then let
                             wlog \stackrel{\triangle}{=} [pc \mapsto ssf.pc,
                                                                    opName \mapsto "write",
                                                                    key \mapsto key,
                                                                  ts \mapsto globalSegnum + 1,
                                                                   version \mapsto version] in
                               \land ssfState' = [ssfState \ \texttt{except} \ ! [id, pid] = [@ \ \texttt{except} \ ! .nextOp = "all",
                                                                                                                                                                                                                                                           !.cursorTS = globalSeqnum + 1]]
                               \land ssfHistory' = [ssfHistory \ \texttt{except} \ ! [id] = Append(@, wlog)]
                               \land globalSeqnum' = globalSeqnum + 1
                ELSE LET wlog \stackrel{\triangle}{=} ssfHistory[id][step] in
                               \land \mathit{ssfState'} = [\mathit{ssfState} \ \mathtt{except} \ ! [\mathit{id}, \mathit{pid}] = [@ \ \mathtt{except} \ ! . \mathit{nextOp} = ``all",
                                                                                                                                                                                                                                                           !.cursorTS = wlog.ts]
                               \land unchanged \langle ssfHistory, globalSeqnum \rangle
WriteLog(id, pid) \stackrel{\triangle}{=}
                 \land ssfState[id, pid].nextOp = "writelog"
                \land \ GetOrLogWrite(id, \ pid)
                \land unchanged \langle objState, objHistory, ssfCommand <math>\rangle
ExtNext \stackrel{\triangle}{=}
                \vee BaseNext
                \lor \exists id \in SSFs, pid \in 1..NumPeers : \lor ReadLog(id, pid)
                                                                                                                                                                          \vee WriteLog(id, pid)
                \vee \exists id \in SSFs, pid \in 1...NumPeers, key \in Objects : \vee ExtRead(id, pid, key)
                                                                                                                                                                                                                                     \vee ExtWrite(id, pid, key)
ExtSpec \stackrel{\triangle}{=} ExtInit \land \Box [ExtNext] \land [Specification] \land [ExtNext] \land [ExtNe
                                                                                                                                      ssfState, ssfHistory,
                                                                                                                                      objState, objHistory⟩
Theorem ExtSpec \implies \Box ExtInvariants
```