

Giant Planet Formation

ASTR558 Final Project

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ABSTRACT

There are currently two main theories for the formation of giant planets, core accretion and direct collapse. Core accretion can explain the formation of most planets but for those far from their host star, direct collapse is needed to explain their existence on the timescale of the age of the Universe. In this paper we explain the processes involved in each theory as well as their relative merits and limitations. We additionally discuss recent work in the field and highlight some major unsolved questions. Lorem ipsum dolor sit amet, consectetur adipiscing elit. Ut purus elit, vestibulum ut, placerat ac, adipiscing vitae, felis. Curabitur dictum gravida mauris. Nam arcu libero, nonummy eget, consectetur id, vulputate a, magna. Donec vehicula augue eu neque. Pellentesque habitant morbi tristique senectus et netus et malesuada fames ac turpis egestas. Mauris ut leo. Cras viverra metus rhoncus sem. Nulla et lectus vestibulum urna fringilla ultrices. Phasellus eu tellus sit amet tortor gravida placerat. Integer sapien est, iaculis in, pretium quis, viverra ac, nunc. Praesent eget sem vel leo ultrices bibendum. Aenean faucibus. Morbi dolor nulla, malesuada eu, pulvinar at, mollis ac, nulla. Curabitur auctor semper nulla. Donec varius orci eget risus. Duis nibh mi, congue eu, accumsan eleifend, sagittis quis, diam. Duis eget orci sit amet orci dignissim rutrum.

1. KEY CONCEPTS

In this section, we explain the key concepts behind the two main theories of giant planet formation. Figure 2 provides a schematic illustration of the two formation channels that we discuss.

1.1. Core Accretion

1.1.1. How does it work?

At its simplest level, core accretion is where a central rocky core is formed and then accretes gas until it reaches a critical core mass and forms a giant planet (Pollack et al. 1996). This general process is illustrated in the left planet of Figure 2.

The formation occurs in three phases, which can be seen in Figure 1. In the first phase, the planet is formed primarily of solid material and continuously accretes planetesimals at a higher rate than gas until the planet clears its “feeding zone”, marking the end of the first

phase. At this point the core of the planet has formed and now the planet slowly accretes gas in an envelope. This gas is accreted from a sphere of radius (Bodenheimer et al. 2013)

$$R = \min\{R_{\text{Bondi}}, R_{\text{Hill}}\} \quad (1)$$

where R_{Bondi} is the Bondi radius, defining the maximum distance inside which gas can be bound to the core and R_{Hill} is the Hill radius, defining the radius in which the main gravitational influence is the planet. See Appendix A for a derivation of these radii.

The third phase of core accretion begins as the planetary core exceeds the critical core mass, resulting in rapid envelope contraction that leads to fast accretion of gas and thus planet mass growth. This finally results in a giant planet.

1.1.2. Critical core mass

During Phase 2 of formation via core accretion, slow accretion of gas and solids onto the core increases the core mass over time. For a given core mass, there exists an envelope mass above which hydrostatic equilibrium cannot be satisfied, which triggers the collapse of the envelope onto the core and the beginning of Phase 3.

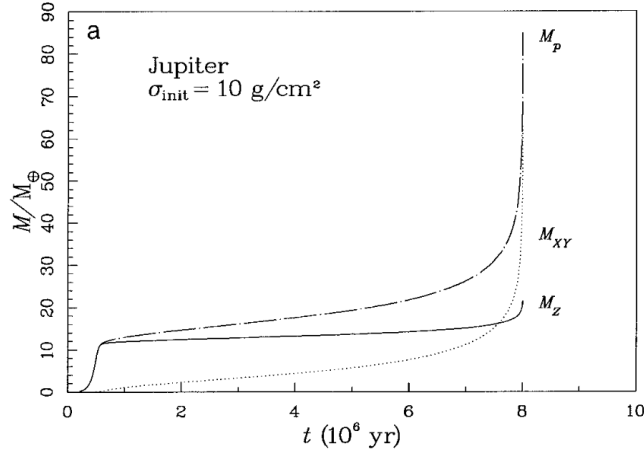


Figure 1. Figure 1 of Pollack et al. (1996). Planet mass as a function of time in which the three phases of core accretion are evident. Phase 1 is rapid early accretion of solids ($\sim 0\text{--}0.4$ Myr), Phase 2 is slow accretion onto the core ($\sim 0.4\text{--}7.5$ Myr) and Phase 3 is rapid final accretion once the critical core mass is exceeded ($\sim 7.5\text{--}8$ Myr). The different curves show the masses of different compositions.

This critical core mass can be derived using some basic assumptions about the locations of convective and radiative zones (Stevenson 1982; Lissauer et al. 2009). Previous work assumed that the envelope was fully radiative but a more accurate assumption is that there is an innermost convective zone and outermost radiative zone. The combination of these zones gives that the critical core mass is simply

$$M_c = \frac{1}{2}M \quad (2)$$

implying that once the core mass accounts for half of the overall planet mass, rapid contraction will occur and Phase 3 of formation begins.

1.1.3. The end of accretion

A giant planet formed via core accretion will finish its formation once there is no gas left for accretion. This termination occurs once the gas in the surrounding protoplanetary disc is dispersed (mainly by photoevaporation). Prior to this dispersal, the accretion of a planet can also stall once it forms a gap in the protoplanetary disc after the end of Phase 3. This means that you can form different sorts of planets depending on what phase of formation they were in once the gas in the disc is dispersed.

Lissauer et al. (2009) showed that Saturn’s mass is around the maximum for disc-limited accretion, whereas

Neptune and Uranus were slower to form and would still have been on Phase 2 when the gas in the disc dispersed.



Figure 2. An illustration of different giant planet formation channels. (Credit: NASA and A. Feild (STScI))

1.1.4. Timescale limits

1.2. Direct Collapse

1.2.1. How does it work?

1.2.2. Migration

2. RECENT RESEARCH

3. UNSOLVED QUESTIONS

- Challenges with direct collapse (Forgan & Rice 2013)
- Core accretion doesn’t account for compositional gradients (D’Angelo & Lissauer 2018)

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APPENDIX

A. DERIVATION OF BONDI AND HILL RADII

A.1. *Bondi Radius*

The Bondi radius is the maximum distance inside which gas can be bound to the core of the planet. The gas will be bound to the core if, in the frame of the core, its total energy becomes negative. This means that the gravitational potential energy needs to be greater than the total thermal energy and so we can write

$$\frac{GM_c}{R} \geq \frac{1}{2}(v_{\text{rel}}^2 + v_{\text{th}}^2), \quad (\text{A1})$$

where M_c is the core mass, R is the radius, v_{rel} is the relative velocity of the gas and the core and v_{th} is the thermal velocity of the gas. If we assume that the relative velocity is dominated by Keplerian shear (D'Angelo & Lissauer 2018) then

$$|v_{\text{rel}}| = R\Omega, \quad (\text{A2})$$

where $\Omega = \sqrt{GM_*/a^3}$ is the angular orbital velocity. And the thermal velocity is given by

$$v_{\text{th}} = c_g \sqrt{8/\pi} \quad (\text{A3})$$

where c_g is the speed of sound in the gas. The sound speed is often expressed as $c_g = H_g \Omega$, where H_g is the pressure scale height of the disc. We can now plug this all into the original inequality (and make it an inequality to solve for the Bondi radius)

$$\frac{GM_c}{R_B} = \frac{1}{2}(R^2\Omega^2 + \frac{8}{\pi}H_g^2\Omega^2) \quad (\text{A4})$$

$$\frac{GM_c}{R_B} = \frac{GM_*}{2a^3}(R^2 + \frac{8}{\pi}H_g^2) \quad (\text{A5})$$

$$R_B = \frac{M_c}{M_*} \frac{2a^3}{R^2 + \frac{8}{\pi}H_g^2} \quad (\text{A6})$$

$$R_B = a \left(\frac{M_c}{M_*} \right) \left(\frac{a}{2H_g} \right)^2 \quad (\text{A7})$$

A.2. *Hill Radius*

The Hill radius is a similar quantity but it is due to forces rather than energy. The radius is the maximum distance within which the main gravitational influence is the core of the planet. Therefore, the radius is found by equating the gravitational and centrifugal forces