# ASTR 541 - Interstellar Medium

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# 1a. Hydrogen density

We can first calculate the density of the disc as

$$\rho = \frac{M}{\pi R_{\rm disc}^2 H} \tag{1}$$

$$= 1.9 \times 10^{-24} \,\mathrm{g \, cm^{-3}} \tag{2}$$

Now we need to convert the density to a number density as follows

$$\rho = m_{\rm H} n_{\rm H} + m_{\rm He} n_{\rm He} \tag{3}$$

$$= n_{\rm H} \left( m_{\rm H} + m_{\rm He} \frac{n_{\rm He}}{n_{\rm H}} \right) \tag{4}$$

$$= n_{\rm H}(m_{\rm H} + 0.1m_{\rm He}) \tag{5}$$

$$=1.4n_{\rm H}m_{\rm p}\tag{6}$$

$$n_{\rm H} = \frac{\rho}{1.4m_p} \tag{7}$$

This gives that the average number density of hydrogen is

$$n_{\rm H} = 0.8 \, \rm cm^{-3}$$
 (8)

### 1b. Dust grain density

The mass of each dust grain is given by

$$m_{\rm DG} = \frac{4}{3}\pi R_{\rm RG}^3 \cdot \rho_{\rm RG} \tag{9}$$

$$= 8.4 \times 10^{-15} \,\mathrm{g} \tag{10}$$

We are given the total dust mass and we already calculated the volume of the disc in part a so now the number density is just

$$n_{\rm DG} = \frac{M_{\rm dust}}{m_{\rm DG}} \cdot \frac{1}{V_{\rm disc}}$$

$$n_{\rm DG} = 1.6 \times 10^{-12} \,\rm cm^{-3}$$
(11)

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 (12)

### 1c. Molecular clouds - frequency and mass

The typical mass can be found by multiplying the number density, mass of particles and volume.

$$M_{\rm MC} = m_{\rm H_2} n_{H_2} V_{\rm MC} \tag{13}$$

$$= (2m_p) \cdot n_{H_2} \cdot \left(\frac{4}{3}\pi R_{\text{MC}}^3\right) \tag{14}$$

$$M_{\rm MC} = 7 \times 10^4 \,\mathrm{M}_{\odot} \tag{15}$$

The approximate number of clouds in the galaxy is then just

$$N_{\rm MC} = \frac{0.3 M_{\rm disc}}{M_{\rm MC}}$$

$$N_{\rm MC} = 1.7 \times 10^4$$

$$(16)$$

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 (17)

# 1d. Molecular clouds getting in the way

If the centre of a molecular cloud passes within a radius of the line of sight then it will obscure our view. This defines the volume within which a molecular cloud could block our sight as

$$V_{\rm LoS} = \pi R_{\rm MC}^2 \cdot 8.5 \,\text{kpc} = 6 \times 10^6 \,\text{pc}^3$$
 (18)

Given the total volume of the disc and the approximate number of molecular clouds in the disc, this implies that the expectation value of the number of clouds intersecting our line of sight is

$$N = \frac{V_{\text{LoS}}}{V_{\text{disc}}} N_{\text{MC}} = 0.73$$
(19)