

CHARLES UNIVERSITY
FACULTY OF SOCIAL SCIENCES
Institute of Economic Studies



**Noise reduction and feature extraction
with principal component analysis for
cryptocurrency price modeling**

Bachelor's thesis

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Year of defense: 2024

Declaration of Authorship

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Prague, March 5, 2024

Tomas Barhon

Abstract

The abstract should concisely summarize the contents of a thesis. Since potential readers should be able to make their decision on the personal relevance based on the abstract, the abstract should clearly tell the reader what information he can expect to find in the thesis. The most essential issue is the problem statement and the actual contribution of described work. The authors should always keep in mind that the abstract is the most frequently read part of a thesis. It should contain at least 70 and at most 120 words (200 when you are writing a thesis). Do not cite anyone in the abstract.

JEL Classification	C01, G00, F23, H25, H71, H87
Keywords	Cryptocurrency, Bitcoin, Ethereum, Litecoin, Machine Learning, PCA, Noise Reduction
Title	Noise reduction and feature extraction with principal component analysis for cryptocurrency price modeling
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Abstrakt

Nutnou součástí práce je anotace, která shrnuje význam práce a výsledky v ní dosažené. Anotace práce by neměla být delší než 200 slov a píše se v jazyce práce (tj. česky, slovensky či anglicky) a v překladu (tj. u anglicky psané práce česky či slovensky, u česky či slovensky psané práce anglicky). Anotace práce by neměla být delší než 200 slov a píše se v jazyce práce (tj. česky, slovensky či anglicky) a v překladu (tj. u anglicky psané práce česky či slovensky, u česky či slovensky psané práce anglicky). V abstraktu by se nemělo citovat.

Klasifikace JEL	C01, G00, F23, H25, H71, H87
Klíčová slova	Kryptoměny, Bitcoin, Ethereum, Litecoin, Strojové učení, PCA, Redukce šumu
Název práce	Redukce šumu a extrakce rysů pomocí analýzy hlavních komponent pro modelování cen kryptoměn
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Acronyms

BTC	Bitcoin
ETH	Ethereum
LTC	Litecoin
ML	Machine Learning
DL	Deep Learning
ANN	Artificial Neural Network
LR	Linear Regression
SVM	Support Vector Machines
SVR	Support Vector Regression
RNN	Recurrent neural network
LSTM	Long Short-Term Memory
PCA	Principal Component Analysis
SVD	Support Vector Decomposition
ARIMA	Autoregressive Integrated Moving Average

Bachelor's Thesis Proposal

Author	Tomáš Barhoň
Supervisor	prof. PhDr. Ladislav Krištofuk Ph.D.
Proposed topic	Noise reduction and feature extraction with principal component analysis for cryptocurrency price modeling

Motivation Crypto assets have always been exceptionally volatile compared to traditional assets such as stocks or gold. The historical window is relatively short, thus modeling their price or volatility proposes quite a difficult challenge. It is generally believed that noise in any data decreases the precision of predictions. This effect might be reduced, which will improve the performance of traditional models that are used for cryptocurrency price modeling.

The main motivation for researching this topic is that there is still an ongoing discussion about the role of different features in crypto pricing dynamics. (Kukacka; Kristoufek 2023) have shown that a lot of the pricing dynamic emerges from complex interactions between fundamental and speculative components. They also show the different correlations between all of the explanatory variables which have a direct connection to principal component analysis. It is crucial to study the real impact of those variables in different models as many of them might turn out to be obsolete.

There is currently little use of this dimensionality reduction technique in the academic literature about cryptocurrencies. However, for more traditional financial series this technique is already quite established as a preprocessing technique to reduce noise and dimensionality from which financial data inherently suffer (Chowdhury, U. ; Chakravarty, S. and Hossain, M. 2018). Moreover (Bouri, E.; Kristoufek, L.; Ahmad, T. et al. 2022) studied the effect of microstructural noise on idiosyncratic volatility in cryptocurrencies which further supports the need for a technique that will mitigate this effect on the predictions.

The research will address the problem of variable selection for different types of predictive models with respect to the analysis of the principle components aiming to reduce the dimensionality and simultaneously increase precision. The second question is whether it is more appropriate to transform the high dimensionality with

PCA into lower dimensionality or simply omit the variables with high multicollinearity from the models. These approaches are fundamentally different and the answer is not clear.

Methodology The data will come from various sources because the aim is to look at all the possible variables even if they might not seem useful at first glance. As already mentioned the dynamic is driven by a lot of completely different effects. Most of it will be collected from: coinmetrics.io, studio.glassnode.com, and for macroeconomic indicators <https://fred.stlouisfed.org/>. Some of the data might need to be interpolated to daily observations. Lastly, the observations will need to be sliced to different window sizes and shifted by one so that the predictions can be made for the next day with the data available on that day.

Afterward, the multicollinearity in the data will be examined and different approaches to solve it will be used. The two main ones are using only a smaller set of uncorrelated variables (simple dimensionality reduction) and the second being employing PCA transformation to preserve a predefined threshold of variance or directly targeting the number of principal components.

All the different setups will be compared across three models: linear regression, SVM, and LSTM neural network. The hypothesis is that PCA transformation will substantially lower the measured errors for linear regression and SVM although for LSTM it will result in lower performance as it will only decrease the capacity of the model as the model is powerful enough to create such uncorrelated features without the PCA transformation.

Expected Contribution Existing research agrees that financial data and especially cryptocurrency data are significantly affected by noise. The main goal is to extend the research on the topic of variable selection for algorithmic trading models as there are still a lot of unanswered questions. It will most likely become clearer which approach to dimensionality reduction is the most efficient concerning cryptocurrencies.

Also, not only the underlying pricing dynamics will be detected but the results can be used for investors that are trying to lower their risk of loss which is relatively high in crypto markets. The effect of having a more stable and precise model might significantly cut the transaction costs that are associated with more frequent exchanges as the predictions will become less volatile. That is a desirable property needed to maximize profit and increase credibility towards its customers.

Core bibliography

Kukacka, J., & Kristoufek, L. (2023). Fundamental and speculative components of the cryptocurrency pricing dynamics (Vol. 9). Financial Innovation.

Kristjanpoller, W., & Minutolo, M. C. (2018). A hybrid volatility forecasting framework integrating GARCH, artificial neural network, technical analysis and principal components analysis (Vol. 109). Expert Systems with Applications.

Chowdhury, U. N., Chakravarty, S. K., & Hossain, M. T. (2018). Short-Term Financial Time Series Forecasting Integrating Principal Component Analysis and Independent Component Analysis with Support Vector Regression (Vol. 6).

Bouri, E., Kristoufek, L., , & Shahzad, S. J. H. (2022). Microstructure noise and idiosyncratic volatility anomalies in cryptocurrencies. Springer Link. <https://doi.org/10.1007/s10479-022-04568-9>

Rea, A., & Rea, W. (2016). How many components should be retained from a multivariate time series PCA?. arXiv preprint arXiv:1610.03588.

Chapter 1

Introduction

Since the introduction of the first cryptocurrency Bitcoin (BTC) associated with the unknown author Satoshi Nakamoto (2008) cryptocurrencies have become part of our everyday life. Their high volatility, futuristic name and alternative nature are of interest to the media and the general public. According to **coinmarketcap.com** the overall cryptocurrency market capitalization peaked at around 2.8 trillion \$USD in the year 2022 which makes them a substantial part of the financial sphere. The initial idea of BTC was to establish an alternative to traditional fiat currencies. The BTC whitepaper pointed out the weakness of the current trust-based model that relies on a third-party instance responsible for verifying transactions. A different approach was suggested to validate transactions known as the proof-of-work which utilizes the computational power of miners in the network. The fact that the power is distributed across the network ensures that it becomes exponentially harder with an increasing number of blocks to generate blocks faster than the rest of the miners (Nakamoto 2008, pg. 6). However, the mining process is interconnected with the creation of new BTCs which is a crucial parameter in all monetary systems. This fact gives researchers such as Kukacka & Kristoufek (2023) the possibility to use various attributes of the network to study the pricing dynamics of cryptocurrencies. On the other hand, there are a couple of substantial drawbacks that make price modeling relatively challenging. Those are non-stationarity of the target prices, relatively short historical window, the limited power of proxies for speculative components and as pointed out by many researchers such as Bouri *et al.* (2022), Dimpfl & Peter (2021), WÄ...torek *et al.* (2023) an idiosyncratic noise in volatility. Addressing these issues might potentially lead to better-performing models, especially with longer forecasting periods.

Likewise in other fields, the recent rise of machine learning has also affected the cryptocurrency area where various Machine Learning (ML) and Deep Learning (DL) models are often being used to model the price Khedr *et al.* (2021) or volatility Kristjanpoller & Minutolo (2018).

The main objective of this thesis is to try to tackle the problem of idiosyncratic noise in the high dimensional data used for price and returns modeling across three ML models: Ridge Linear Regression (LR), Support Vector Machines (SVM) and Long Short-Term Memory (LSTM) Recurrent neural network (RNN). We will examine the effect of a method known as Principal Component Analysis (PCA) which was according to Farebrother (2022) developed in 1933 by Harold Hotelling. However, others often refer to the fact that the idea was already introduced before by Karl Pearson in the article *On lines and planes of closest fit to systems of points in space* Pearson (1901). Nevertheless, despite the initial focus on dimensionality reduction different types of PCA are often being used as noise reduction techniques in signal or image processing. Interestingly many studies in recent years have incorporated PCA for time series data as a part of their preprocessing pipeline Chowdhury *et al.* (2018), Kristjanpoller & Minutolo (2018). The idea stems from the fact that removing the most idiosyncratic components might help with capturing clear dynamics that enter the price-making process. We perceive that there is currently a lack of literature that would examine the effect of noise reduction techniques on the performance of other ML based regression techniques for cryptocurrencies. We want to mitigate most of the mentioned challenges using the currently available academic knowledge and focus exclusively on the effect of noise in the data. Admittedly it is always intricate to establish a *ceteris paribus* relationship in such a scenario where a lot of variables change in the process.

Chapter 2

Literature Review

2.1 Formal requirements of master's thesis at the Faculty of Social Sciences

According to Dean's Provision no. 18/2017:

- The minimum extent of master's thesis is 60 standard pages (108 thousand characters including spaces) of the text itself, i.e. without an abstract and appendices and a list of literature. In case the master's thesis is written in English, its minimum extent is 50 standard pages (90 thousand characters including spaces) without an abstract and appendices and a list of literature. For bachelor's thesis, these requirements go down to 30 standard pages in any language. When writing a standard text document, the minimum requirement is 60 characters per line and 30 lines per page, i.e. 1,800 characters per page (the so-called standard page). Font size, page layout, margins, and line spacing need to be customized.
- Generally, a standard form of the page of the final thesis applies the fonts of 12 points, the gaps between the paragraphs are recommended to be of the size of 6 points. Notes and footnotes can be written in a 10-point font. The text is aligned on both sides (aligned to a block). Electronic version of the thesis will be entered by a student/applicant for a state doctoral examination through the SIS website interface in the archive format of PDF/A version 1.3 or higher. Further details are stipulated by the rector's provision.

Chapter 3

Data

3.1 Citations

Text text text text text text text text text text text text. Text text text text text text text text text. Text text text text text text text text text text text text text text. Text text ?.

Text text text text text text text text text text text text text. Text text text text text text text (see, *inter alia*, ?, pg. 10).

3.2 Acronyms

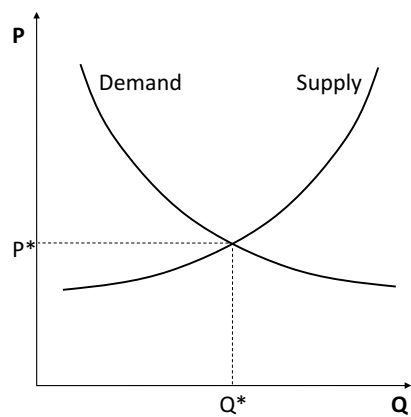
Text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text. Politicians usually like inward BTC and an **MNC!** (**MNC!**) appreciates **FDI!** (**FDI!**) subsidies. Are **MNC!**s greedy?

3.3 Figures

To achieve compatibility with PDF/A 2u, your file must not include links to external fonts, audio, video, or scripts. On the other hand, your file must declare each color environment you use, it must include all the pictures/figures either in jpeg or PDF/A 2u format, used fonts compliant under Unicode (your file cannot use any external fonts), and it must include meta-data in XMP format.

Most troubleshooting comes from the conversion of figures to compliant formats. You can convert from simple PDF using Adobe Acrobat:

Figure 3.1: Market equilibrium



Source: ?.

Look at the Figure 3.1. Text text text text text text text text text. Text text text text text text. Text text text text text text text text text. Text text text text text text text text text text.

3.4 Tables

If you use Stata, you might want to check the `sutex`, `outtable`, `outtex`, and `estout` tools, which help you with exporting Stata tables to L^AT_EX.

3.5 Table

	BTC-LR - 1 day	BTC-LR - 5 days	BTC-LR - 10 days	BTC-SVR
Full dimensionality	960.371278	2392.049220	3765.643891	973.251758
95% retained variance	6389.795421	7910.647028	7980.389921	7532.51343
98% retained variance	1330.381121	2103.339885	2951.848360	1042.12669
99% retained variance	978.447494	2153.450254	3124.302129	1078.08062

Table 3.1: Model’s predictions

<i>Case</i>	Y_1	Y_2	τ_1	τ_2	a	n
CR—Slovakia	10.9	10	0.24	0.19	1,000	2.16
CR—Poland	13.3	12	0.24	0.19	1,000	0.38
CR—Hungary	10.4	8	0.24	0.16	1,000	1.10

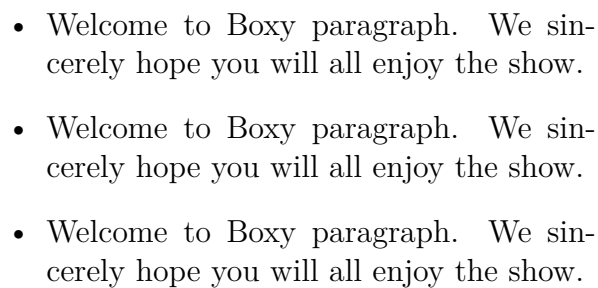
Source: If the source is author himself (like a calculation output), this line is redundant.

Text text text text text text text text text text text text.
 Text text text text text text text text text text. Text text text text text text.
 Text text text text text text text text text text. Text text text text text text
 text text text text.

3.6 Boxes

Text text text text text text text text text text text text. Text
 text text text text text text text text text. Text text text text text text. Text
 text text text text text text text text text text. Text text text text text text text
 text text text. Let us make a box:

Figure 3.2: Boxy’s example

- 
- Welcome to Boxy paragraph. We sincerely hope you will all enjoy the show.
 - Welcome to Boxy paragraph. We sincerely hope you will all enjoy the show.
 - Welcome to Boxy paragraph. We sincerely hope you will all enjoy the show.

Source: ?

Text text text text text text text text text text text text.
 Text text text text text text text text text text. Text text text text text text.
 Text text text text text text text text text text. Text text text text text text
 text text text text.

3.7 Theorems, Definitions, ...

Definition 3.1 (My original definition). This is a definition.

Assumption 3.1 (My realistic assumption). This is an assumption.

Proposition 3.1 (My clever proposition). *This is a proposition.*

Lemma 3.1 (My useful lemma). *This is a lemma.*

Example 3.1. This is an example.

Proof. This is a proof. □

3.8 Equations

3.8.1 Nonumbered Equations

Text text text text text text text text text text text text. Text text text text text text text text text. Text text text text text text. Text text text text text text text text text. Text text text text text text text text text text text text.

$$U = \underbrace{\int_0^\infty \frac{1}{1-\sigma} (C^{1-\sigma} - 1) e^{-\rho t} dt}_{\text{meaning of life}}$$

3.8.2 Numbered Equations

Text text text text text text text text text text text text. Text text text text text text text text text. Text text text text text text. Text text text text text text text text text. Text text text text text text text text text text text text.

$$U = \int_0^\infty \overbrace{\frac{1}{1-\sigma} (C^{1-\sigma} - 1)}^{\text{instantaneous utility}} e^{-\rho t} dt \quad (3.1)$$

3.8.3 Matrix Equations

Text text text text text text text text text text text text. Text text text text text text text text text. Text text text text text text. Text text text text text text text text text. Text text text text text text text text text text text text.

$$A = B + C \quad (3.2)$$

3.9 Cross-references

- to literature (?, pg. 10) or ?, pg. 10,
- to Figure 3.1,
- see Table 3.1,

- to Section 3.8,
- to Definition 3.1, to Proposition 3.1, Example 3.1,
- to equations like this: see (3.1).

3.10 Source codes

You can input a source code like this:

```
omega = 1;
syms zeta;
jmn = [1 2*zeta*omega omega^2];
figure(1);
    for zeta = 1E-5 : 0.2 : 1+1E-12
        G = tf(omega^2,subs([1 2*zeta*omega omega^2]));
        bode(G); hold on;
    end
legend('\zeta = 0', '\zeta = 0.2', '\zeta = 0.4', '\zeta = 0.6', '');
```

Should you prefer a different font size, redefine file `Styles/Mystyle.sty`.

3.11 Paragraphs

Usually you should not use the first person singular (I) in your text, write we instead. As a general recommendation, use the first person sparsely, sometimes it can be replaced by a phrase like “This work presents . . .”

Text text text text text text text text text text text. Text text text text text text text text. Text text text text text text. Text text text text text text text text. Text text text text text text text text text text. Text text text text text text (?). Let us make two paragraphs:

Proin Text text text text text text text text text text text text.
Text text text text text text text text text. Text text text text text text.
Text text text text text text text text text. Text text text text text text
text text text text. Text text text text text text text text text text text text
text text text. Text text text text text text text text text text. Text text text
text text text. And a subparagraph:

Velit Text text text text text text text text text text text text. Text text text text text text text text text. Text text text text text text. Text text text text text text text text text text text. Text text text text text text text text text text.

Chapter 4

Methodology

4.1 Title of Section One

Many people use simple n-dash in many occasions – like this –, where however typographic convention—it looks a bit strange at first sight—requires m-dash. Text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text ?.

Text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text. Text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text ?.

Let us describe the following animals:

Item 1 Text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text. Text text text text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text text.

Item 2 Text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text. Text text text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text text.

Text text text text text text text text text text text text text. Text text text text text text text text text text. Text text text text text text. Text text text text text text text text text text text text text. Text

Chapter 5

Results and Discussion

5.1 Results Intepretation

The following checklist should help in avoiding some frequently made mistakes, if any of the following propositions apply for your thesis, there is a problem:

- You have citations in your abstract.
- The introduction does not cover the three parts as described in Chapter 1.
- The introduction contains subheadings.
- You described different aspects than promised in the title.
- You copied some parts of the text from other work without proper referencing and citing.
- You used automatic translation tools to produce text by translating it from another language.
- Your thesis contains many typos and grammatical errors. (Use an electronic spell checker. Please!)
- You used color in your figures and refer to the “blue” line (assume that your readers use a monochrome printer).
- You mainly used websites and other unrefereed material as your sources or you used Wikipedia as your source.
- You refer to something in your conclusion which you have not mentioned before.

- Some forenames in the references are abbreviated, some not.
- Some references miss a publishing date.

5.2 Limitations

Chapter 6

Conclusion

If you write in English, you might find the following hint useful: The indefinite article *a* is used as an before a vowel sound—for example an apple, an hour, an unusual thing, an (because the acronym is pronounced Em-En-See). Before a consonant sound represented by a vowel letter *a* is usual—for example a one, a unique thing, a historic chance. Few more tips to follow:

- Don't give orders—don't write in the imperative mood—unless you are training to be a teacher.
- Avoid the use of questions. You may know the answer: does your reader? It's much safer to tell her, or him.
- Do not become entangled in the problems of 'sexist' language. It is much easier to write in the plural. "Students should check their work" is good English. "A student should check—" is also good English, but now the problems begin: "—her work?" "—his work?" Which? You can write "his or her," but that seems clumsy. Stick to the plural.
- If you must refer to yourself, use the third person such as "The present writer would recommend that . . ." may be useful.
- Use the full forms of words and phrases, not contractions like "he's," "don't," etc. Keep the apostrophe to indicate possession—and use it correctly. Academics really sneer at students who use the "Greengrocer's apostrophe."
- Do not despise short, workmanlike, and effective plain English words. If they mean what you want to say. Accurately.

- Avoid the use of humor in academic writing—unless you are very sure of yourself.
- Even when you are not being funny, avoid the use of irony or sarcasm.
- Paragraphs in academic English should contain more than one sentence. (Short paragraphs look as if you are writing for a tabloid newspaper—or a simple Template!) I guess that the average academic book runs to two or three paragraphs per page. Look at the books in your subject, and get a feel for how long your own paragraphs should be when you are imitating the academic style.
- Use the word that more in formal writing than most of us do in speech—particularly after such verbs of utterance as to say, to report, to think etc. It can help to make your writing much clearer.
- Develop an academic vocabulary. The ‘long words’ you learn in the course of your studies are long usually because they have more precise meanings than their less formal equivalents. They are therefore better when you want to be accurate. (Also they allow you to sound like someone who deserves a degree.)
- Use as few words as you can; but use enough words to express your meaning as fully as you can. Your judgment of what is appropriate here is part of what you should learn throughout your course.
- Avoid lazy words such as “nice”. It is usually better to say “acquire” or “obtain” than “get;” and it may be better, if you mean “through the use of money,” to say “purchase” or—better still—“buy.”
- A short word like “buy” is better than a long one like “purchase”—unless the long one is more accurate. A “statutory instrument” is better than a “rule”—to a lawyer, at any rate.
- Proof-read with care. Ask someone else to help—you may be too close to your work to be able to see your mistakes.
- If in doubt, choose the more formal, or possibly just the more old-fashioned, of two words. For example, say quotation rather than quote whenever you mean the use of somebody else’s words.

-
- You will often sound more academic if you include doubts in your work—and qualifications. Within the scope of this thesis, the current writer cannot hope to cover all the possible implications of the question.Ô
 - In this context, the use of litotes sounds very academic. This is the construction where a writer uses a negative with a negative adjective, e.g. it is not unlikely that ... This does not mean the same as it is probable that ... It has a shade of meaning and qualification that can be useful to academic writers.

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Appendix B

Additional Contents

All of the source codes and data to reproduce the results are available at <https://github.com/Tomas-Barhon/Noise-reduction-and-feature-extraction>. Including all the instruction on how to install the necessary dependencies.