### DISCRETE MATHEMATICS

# DIRECTED GRAPH

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#### 1 Assignment

- 1. Specify a directed non-weighted graph.
- 2. Implement and test a directed non-weighted graph with an edges linked list. Calculate the order of each operation.
- 3. To test the correct functionality of the previous class:
  - (i) Implement a function to load data to a graph (for both vertices and edges).
  - (ii) Implement a function to generate a random graph.
  - (iii) Implement a function to show the graph on screen (either a list with vertices and edges or a graph drawing).
- 4. Implement all three traversal algorithms (Plain search, BFS and DFS)
- 5. Modifying previous functions, write and test algorithms that:
  - (i) Calculate the amount of sources and sinks.
  - (ii) Verify if the graph is weakly connected.
  - (iii) Given two vertices, verify if a path of length 2 exists between them.
  - (iv) Implement Warshall's algorithm.

## 2 Specification

#### 2.1 DirectedGraph

Description: Represents a directed non-weighted graph.

**DirectedGraph**: IdMaterial x Type x Title x Author x Year  $\rightarrow$  Material

**Description:** Creates a new Material with the given data.

Precondition:

o Type is either 1 or 2. o IdMAterial  $\geq 1$ 

Postcondition: A Material is created.

Classification: Constructor

 $\mathbf{destroyMaterial}: \mathbf{Material} \to \mathbf{void}$ 

**Description:** Deallocates all memory assigned to the Material.

Precondition: Material must exist.
Postcondition: Memory freed.
Classification: Destructor

#### 2.2 Graph Related Algorithms

Description: Algorithms related to graph theory

 $getSources: Graph \rightarrow Number$ 

**Description:** Given a graph returns the number of source vertices.

Precondition: Graph must exist

Postcondition: Return the amount of source vertices in the graph

Classification: Analyzer

 $\mathbf{getSinks}$ : Graph  $\rightarrow$  Number

**Description:** Given a graph returns the number of sink vertices.

Precondition: Graph must exist

Postcondition: Return the amount of sink vertices in the graph

Classification: Analyzer

 $\mathbf{isWeaklyConnected} \colon \mathsf{Graph} \to \mathsf{Boolean}$ 

**Description:** Given a graph, checks whether it is weakly connected.

**Precondition:** Graph must exist

Postcondition:

• True if the graph is weakly connected.

• False if the graph is not weakly connected.

Classification: Analyzer

 $\mathbf{pathOfLengthTwoExists}$ : Graph x Vertex x Vertex  $\rightarrow$  Boolean

Description: Given a graph and two vertices checks if a path of length 2 exists between

them in the graph.

Precondition: Graph and both vertices must exist

Postcondition:

• True if a path of length two between the two vertces exists.

• False if a path of length two between the two vertces does not exist.

Classification: Analyzer

warshall: Graph  $\rightarrow$  Transitive Closure

**Description:** Given a graph calculates its transitive closure using Warshall's.

**Precondition:** Graph must exist

Postcondition: The transitive closure must have the capability of calculating whether there

is a path between two vertices in O(1) time.

Classification: Analyzer