

Write a function that calculates the values of MA(q) model. The function must have a parameter burnin that determines how many initial values are discarded.

```
In [2]: import numpy as np
import pandas as pd
import math
import matplotlib.pyplot as plt
from statsmodels.graphics.tsaplots import plot_acf, plot_pacf

def NextValue(p, prev_values):
    sum=0
    for i in np.arange(p):
        sum+=phis[i]*prev_values[len(prev_values)-p+i]
    noise=np.random.randn()
    return c+sum+noise, noise

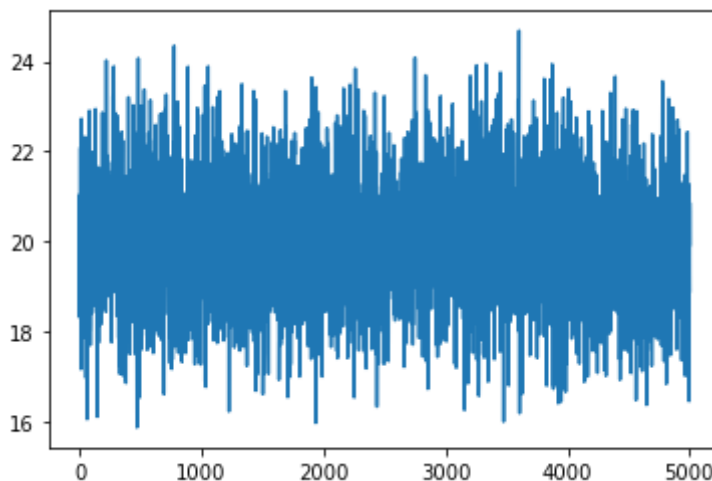
def MA(p,c,phis):
    MAvalues=start_numbers
    noises=start_noises
    for i in np.arange(simulation_length):
        res=NextValue(p,noises)
        MAvalues.append(res[0])
        noises.append(res[1])
    del MAvalues[0:burnin]
    return MAvalues
```

Calculate $n = 5000$ values of MA(1) model $y_t = 20 + \epsilon_t + 0.8\epsilon_{t-1}$.

```
In [3]: p=1
c=20
phis=[0.8]
burnin=300
start_numbers=[1,2,3]
start_noises=[np.random.randn() for i in range(3)]
simulation_length=5300

result=MA(p,c,phis)
plt.plot(pd.Series(result))
```

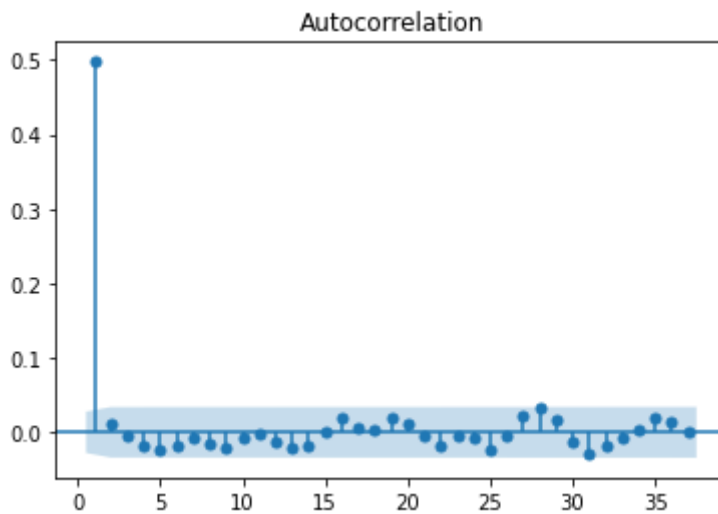
Out[3]: [<matplotlib.lines.Line2D at 0x1b1ef7bf1c0>]



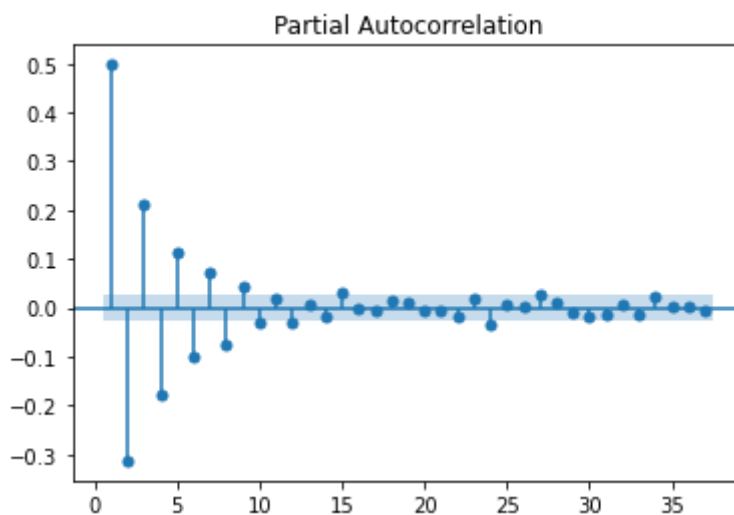
Calculate the autocorrelation (ACF) and partial autocorrelation (PACF) function for this time

series

```
In [4]: plot_acf(pd.Series(result), zero=False);
```



```
In [5]: plot_pacf(pd.Series(result), zero=False);
```

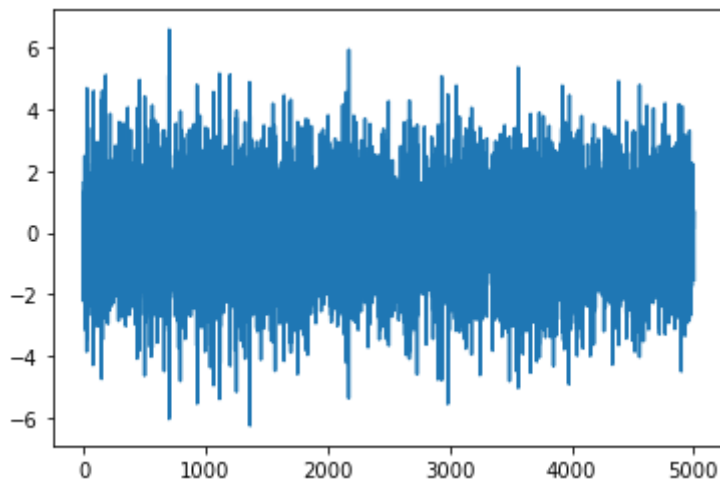


Repeat the calculations for MA(2) model $y_t = \epsilon_t - \epsilon_{t-1} + 0.8\epsilon_{t-2}$.

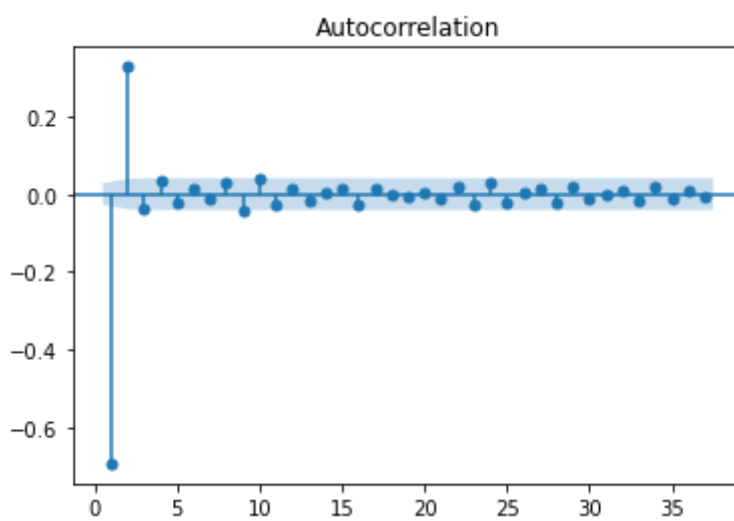
```
In [6]: p=2
c=0
phis=[0.8, -1]
burnin=300
start_numbers=[1,2,3]
start_noises=[np.random.randn() for i in range(3)]
simulation_length=5300
```

```
In [7]: result=MA(p,c,phis)
plt.plot(pd.Series(result))
```

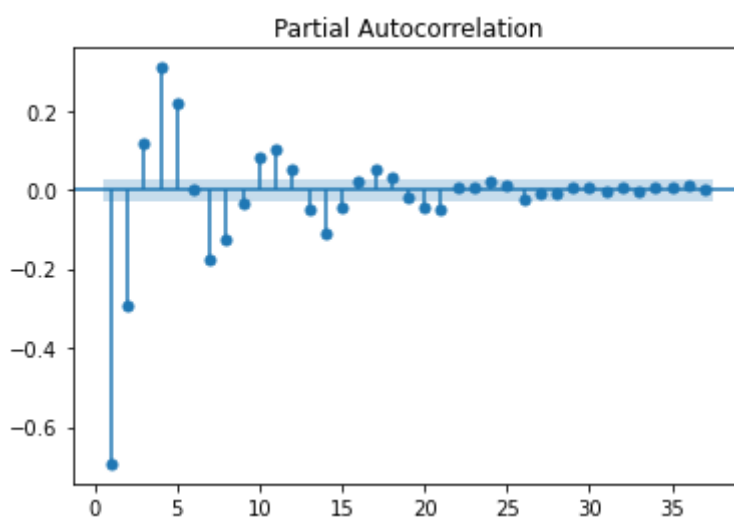
```
Out[7]: [<matplotlib.lines.Line2D at 0x1b1f070fd90>]
```



```
In [8]: plot_acf(pd.Series(result), zero=False);
```



```
In [9]: plot_pacf(pd.Series(result), zero=False);
```



We can see that comparing to AR models, this time autocorrelation values degrade much faster. High values are visible only for lag less or equal model parameter q .

```
In [ ]:
```