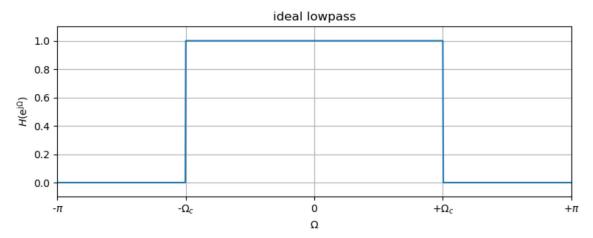
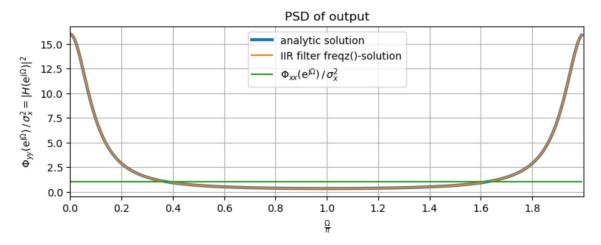
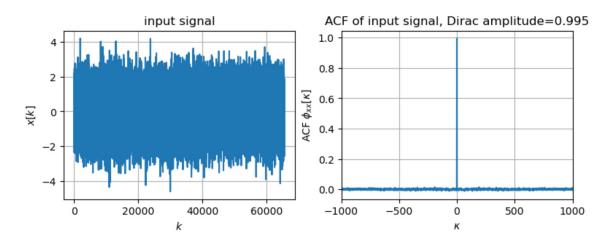
```
In [1]: import numpy as np
        import matplotlib as mpl
        import matplotlib.pyplot as plt
        from scipy import signal
        def my_xcorr2(x, y, scaleopt='none'):
            N = len(x)
            M = len(y)
            kappa = np.arange(0, N+M-1) - (M-1)
            ccf = signal.correlate(x, y, mode='full', method='auto')
            if N == M:
                if scaleopt == 'none' or scaleopt == 'raw':
                    ccf /= 1
                elif scaleopt == 'biased' or scaleopt == 'bias':
                    ccf /= N
                elif scaleopt == 'unbiased' or scaleopt == 'unbias':
                    ccf /= (N - np.abs(kappa))
                elif scaleopt == 'coeff' or scaleopt == 'normalized':
                    ccf /= np.sqrt(np.sum(x**2) * np.sum(y**2))
                else:
                     print('scaleopt unknown: we leave output unnormalized')
            return kappa, ccf
```



```
In [3]: N = 2**8
         Omega = np.arange(N) * 2*np.pi/N
         H2 = 2 / (25/8 - 3*np.cos(Omega)) # analytic
         Omega, H_{IIR} = signal.freqz(b=(1), a=(1, -3/4), worN=Omega) # numeric
         plt.figure(figsize=(9, 3))
         plt.plot(Omega/np.pi, H2, lw=3, label='analytic solution')
         plt.plot(Omega/np.pi, np.abs(H_IIR)**2, label='IIR filter freqz()-solution')
         plt.plot(Omega/np.pi, Omega*0+1,
                    label=r'\$\Phi_{xx}(\mathbb{e}^{\mathbf{j}}\Omega)^{,/}, sigma_x^2$')
         plt.xlabel(r'$\frac{\Omega}{\pi}$')
         plt.ylabel(
              r'$\Pi_{yy}(\mathbf{e}^{\mathbf{j}}\Omega_{y},\,\sigma_x^2 = \|H(\mathbf{e}^{\mathbf{e}^{\mathbf{d}}}),\,\,\sigma_x^2 = \|H(\mathbf{e}^{\mathbf{d}})\|_{y}
         plt.title('PSD of output')
         plt.xlim(0, 2)
         plt.xticks(np.arange(0, 20, 2)/10)
         plt.legend()
         plt.grid(True)
```

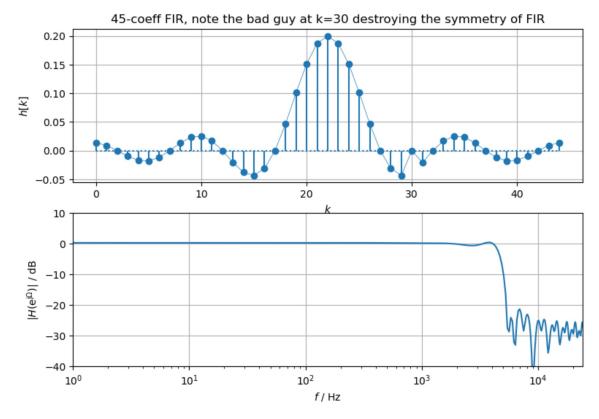


```
np.random.seed(4) # arbitrary choice
In [4]:
        Nx = 2**16
        k = np.arange(Nx)
        x = np.random.randn(Nx)
        kappa, phixx = my_xcorr2(x, x, 'biased') # we use biased here, i.e. 1/N normali
        idx = np.where(kappa==0)[0][0]
        plt.figure(figsize=(9, 3))
        plt.subplot(1, 2, 1)
        plt.plot(k, x)
        plt.xlabel('$k$')
        plt.ylabel('$x[k]$')
        plt.title('input signal')
        plt.grid(True)
        plt.subplot(1, 2, 2)
        plt.plot(kappa, phixx)
        plt.xlim(-1000, +1000)
        plt.xlabel('$\kappa$')
        plt.ylabel('ACF $\phi_{xx}[\kappa]$')
        plt.title('ACF of input signal, Dirac amplitude=%4.3f' % phixx[idx])
        plt.grid(True)
```

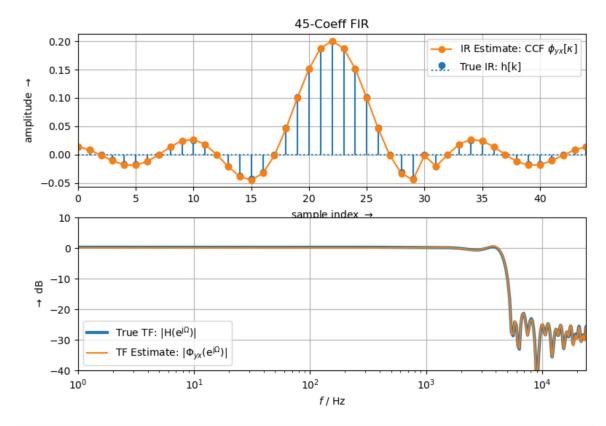


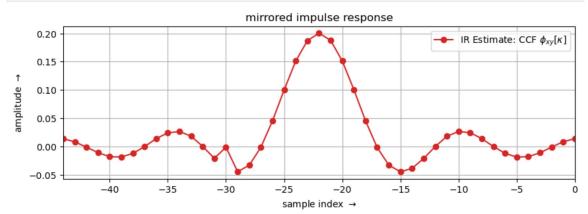
```
In [5]: fs = 48000 # sampling frequency in Hz
        fc = 4800 # cut frequency in Hz
        number_fir_coeff = 45 # FIR taps
        h = signal.firls(numtaps=number_fir_coeff, # example for demo
                         bands=(0, fc, fc+1, fs//2),
                         desired=(1, 1, 0, 0),
                         fs=fs)
        Nh = h.size
        k = np.arange(Nh)
        # make the IR unsymmetric by arbitray choice for demonstration purpose
        h[idx] = 0 # then FIR is not longer linear-phase, see the spike in the plot
        print('h[0]={0:4.3f}, DC={1:4.3f} dB'.format(h[0], 20*np.log10(np.sum(h))))
        N = 2**8
        Omega = np.arange(0, N) * 2*np.pi/N
        _, H = signal.freqz(b=h, a=1, worN=Omega)
        plt.figure(figsize=(9, 6))
        plt.subplot(2, 1, 1)
        plt.stem(k, h, basefmt='C0:')
        plt.plot(k, h, 'C0-', lw=0.5)
        plt.xlabel(r'$k$')
        plt.ylabel(r'$h[k]$')
        plt.title(str(Nh)+'-coeff FIR, note the bad guy at k=%d destroying the symmetry
        plt.grid(True)
        plt.subplot(2, 1, 2)
        plt.semilogx(Omega / (2*np.pi) * fs, 20*np.log10(np.abs(H)))
        plt.xlabel(r'$f$ / Hz')
        plt.ylabel(r'$|H(\mathrm{e}^{\mathrm{j}\Omega})|$ / dB')
        plt.xlim(1, fs//2)
        plt.ylim(-40, 10)
        plt.grid(True)
```

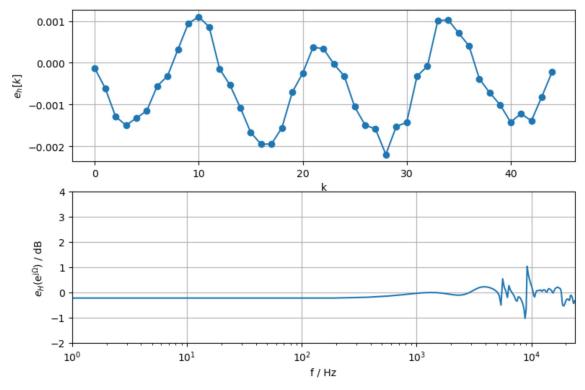
h[0]=0.014, DC=0.298 dB



```
In [6]:
        y = np.convolve(x, h, mode='full') # signal x through system h returns output y
In [7]: kappa, phiyx = my_xcorr2(y, x, 'biased') # get cross correlation in order y,x
        # find the index for kappa=0, the IR starts here
        idx = np.where(kappa == 0)[0][0]
        # cut out the IR, since we know the numtaps this is easy to decide here
        h_est = phiyx[idx:idx+Nh] / len(y)
        # get DTFT estimate of PSD
        _, Phiyx = signal.freqz(b=h_est, a=1, worN=Omega)
        plt.figure(figsize=(9, 6))
        plt.subplot(2, 1, 1)
        plt.stem(h, basefmt='C0:', label='True IR: h[k]')
        plt.plot(kappa, phiyx / len(y), 'C1o-',
                 label=r'IR Estimate: CCF $\phi_{yx}[\kappa]$')
        plt.xlim(0, Nh-1)
        plt.xlabel(r'sample index $\rightarrow$')
        plt.ylabel(r'amplitude $\rightarrow$')
        plt.title(str(Nh)+'-Coeff FIR')
        plt.legend()
        plt.grid(True)
        plt.subplot(2, 1, 2)
        plt.semilogx(Omega/2/np.pi*fs, 20*np.log10(np.abs(H)), lw=3,
                     label=r'True TF: $|\mathrm{H}(\mathrm{e}^{\mathrm{j}\Omega})|$')
        plt.semilogx(Omega/2/np.pi*fs, 20*np.log10(np.abs(Phiyx)),
                     label='TF Estimate: $|\Phi_{yx}(\mathrm{e}^{\mathrm{j}\Omega})|$')
        plt.xlabel(r'$f$ / Hz')
        plt.ylabel(r'$\rightarrow$ dB')
        plt.xlim(1, fs//2)
        plt.ylim(-40, 10)
        plt.legend()
        plt.grid(True)
```







In []: